# abaisero.sty

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#### 1 Options

Options are processes left-to-right. If no options are provided, or none are enabled by the end of the processing, then by default they are all considered to be enabled.

| Option       | Description  |
|--------------|--|
| all          | Enable all commands  |
| (no-)math    | Disable/enable mathematical commands                       |
| (no-)linalg  | Disable/enable linear algebra commands                     |
| (no-)optim   | Disable/enable optimization commands                       |
| (no-)stats   | Disable/enable statistics commands                         |
| (no-)dists   | Disable/enable distributions commands                      |
| (no-)ml      | Disable/enable machine learning commands                   |
| (no-)rl      | Disable/enable reinforcement learning commands             |
| (no-)marl    | Disable/enable multi-agent reinforcement learning commands |
| (no-)theorem | Disable/enable theorem commands                            |
| (no-)misc    | Disable/enable miscellanea commands                        |

#### 2 Commands

#### Option [math]

| Symbol                      | Command                          | Description                                | Example  |
|-----------------------------|----------------------------------|--|--|
| $\mathbb{N}$                | \naturalset                      | the set of natural numbers                 | $\mathbb{N} \doteq \{1, 2, 3, \ldots\}$  |
| $\mathbb Z$                 | ackslashintegerset               | the set of integer numbers                 | $\mathbb{Z} \doteq \{0, 1, -1, 2, -3, \ldots\}$  |
| $\mathbb{R}$                | $\backslash {	t realset}$        | the set of real numbers                    | $\sqrt{2}\in\mathbb{R}$  |
| *                           | kstar                            | the Kleene star operator                   | $\mathcal{X}^* \doteq igcup_{k=0}^\infty \mathcal{X}^k$                                  |
| +                           | $\setminus$ kplus                | the Kleene plus operator                   | $\mathcal{X}^+ \doteq \bigcup_{k=1}^{\kappa-0} \mathcal{X}^k$                            |
| $\operatorname{softmax}$    | $\setminus \mathtt{softmax}$     | a.k.a. logsumexp, realsoftmax <sup>1</sup> | $\operatorname{softmax}(x_1, \dots, x_n) \doteq \log \sum_i \exp(x_i)$                   |
| $\operatorname{softmin}$    | $\setminus \mathtt{softmin}$     |  | $\operatorname{softmin}(x_1, \dots, x_n) \doteq -\log \sum_i \exp(-x_i)$                 |
| $\operatorname{softargmax}$ | $\backslash \mathtt{softargmax}$ | $a.k.a. softmax^1$                         | $\operatorname{softargmax}(x_1, \dots, x_n)_i \doteq \frac{\exp(x_i)}{\sum_k \exp(x_k)}$ |
| sign                        | \sign                            |  | $x = \operatorname{sign} x \cdot  x $  |

<sup>&</sup>lt;sup>1</sup>The functions that in this document are called "softmax" and "softargmax" are poorly and inaccurately named in the broader math and ML fields (see https://en.wikipedia.org/wiki/Softmax\_function and https://en.wikipedia.org/wiki/LogSumExp). Rather than stick to the more common naming conventions, I opt to rename the functions more accurately to appropriately reflect their actual properties. In any document where I would use these functions, I would need to define them anyway, so the risk of misunderstandings are minimal.

# Option [linalg]

| Symbol                | Command                    | Description                                  | Example   |
|-----------------------|----------------------------|--|---|
| diag                  | \diag                      |  |   |
| $\operatorname{rank}$ | $\backslash \mathtt{rank}$ |  |   |
| $\operatorname{tr}$   | $ackslash 	ag{trace}$      |  | $\operatorname{tr}(M) \doteq \sum_{i=1}^{n} M_{ii}$ |
| col                   | ackslashcolspace           |  |   |
| ker                   | $\null$ space              | Nullspace (a.k.a kernel) of a linear mapping |   |
| span                  | $\setminus$ spanspace      |  |   |
| Т                     | $\backslash \mathtt{T}$    | Transpose superscript                        | symmetric $M \implies M = M^{\top}$                 |
| -1                    | \I                         | Inverse superscript                          | invertible $M \implies MM^{-1} = I$                 |
| +                     | \PI                        | Pseudo-inverse superscript                   | $MM^+M=M$   |
| <b>−</b> T            | \IT                        | Inverse transpose superscript                | $M^{-\top} = (M^{-1})^{\top} = (M^{\top})^{-1}$     |
| <b>+</b> T            | \PIT                       | Pseudo-inverse transpose superscript         | $M^{+\top} = (M^+)^{\top} = (M^{\top})^{+}$         |

# Option [optim]

| Symbol                | Command                    | Description            | Example   |
|-----------------------|----------------------------|------------------------|---|
| argmax<br>argmin<br>* | \argmax<br>\argmin<br>\opt | Optimality superscript | $\begin{aligned} & \operatorname{argmax}_{a} Q^{\pi}(s, a) \\ & \theta^{*} \doteq \operatorname{argmin}_{\theta} \mathcal{L}(\theta) \\ & \pi^{*}(s) = \operatorname{argmax}_{a} Q^{*}(s, a) \end{aligned}$ |

# Option [stats]

| Symbol            | Command                   | Description                 | Example   |
|-------------------|---------------------------|-----------------------------|---|
| $\mathbb{C}$      | \Cov                      | Covariance                  | $\mathbb{C}(x,y) = \mathbb{E}[xy] - \mathbb{E}[x]\mathbb{E}[y]$                                     |
| $\mathbb{H}$      | Ent                       | Entropy                     | $\mathbb{H}[x] = -\mathbb{E}\left[\log \Pr(x)\right]$   |
| $\mathbb E$       | \Exp                      | Expectation                 | $\mathbb{E}\left[f(x)\right] = \sum_{x} \Pr(x) f(x)$  |
| ${\mathbb I}$     | $\setminus \mathtt{Ind}$  | Indicator function          | $\Pr(x=0) = \mathbb{E}\left[\mathbb{I}\left[x=0\right]\right]$                                      |
| $_{ m KL}$        | $\backslash \mathtt{KL}$  | KL-divergence               | $\mathrm{KL}\left(p\mid\mid q\right) \doteq \mathbb{E}_{x\sim p}\left[\log p(x) - \log q(x)\right]$ |
| $\mathrm{D_{KL}}$ | $\backslash \mathtt{DKL}$ | KL-divergence (alternative) | -   |
| $\mathbb{I}$      | \MI                       | Mutual Information          |   |
| $\mathbb{V}$      | $ackslash 	exttt{Var}$    | Variance                    | $\mathbb{V}\left[x\right] = \mathbb{E}\left[x^{2}\right] - \mathbb{E}\left[x\right]^{2}$            |

# Option [dists]

| Symbol                               | Command   | Description                                   |
|--------------------------------------|---|---|
| Categorical Dirichlet Normal Uniform | \Categorical<br>\Dirichlet<br>\Normal<br>\Uniform | Categorical<br>Dirichlet<br>Normal<br>Uniform |

# Option [ml]

| Symbol                      | Command        | Description                              | Example   |
|-----------------------------|----------------|--|---|
| $\mathcal{D}$ $\mathcal{L}$ | \data<br>\loss | Data set<br>Loss function                | $\mathcal{D} \doteq \{(x_i, y_i)\}_{i=1}^{N} \\ \mathcal{L}(\theta; x, y) = \frac{1}{2}   y - f(x; \theta)  ^2$ |
| $_{ m nll}^{\sim}$ MSE      | \nll<br>\mse   | Neg-log-likelihood<br>Mean-squared-error | $\operatorname{nll}(x) \doteq -\log \Pr(x)$   |

# Option [rl]

| Symbol         | Command                      | Description          |
|----------------|------------------------------|----------------------|
| $\mathcal{A}$  | \aset                        | Action set           |
| ${\cal B}$     | bset                         | Belief set           |
| ${\cal H}$     | hset                         | History set          |
| $\mathcal O$   | oset                         | Observation set      |
| ${\cal R}$     | $ackslash 	ext{rset}$        | Reward set           |
| ${\mathcal S}$ | $\setminus \mathtt{sset}$    | State set            |
| D              | \dfn                         | Dynamics function    |
| G              | \gfn                         | Generative function  |
| O              | $\backslash \mathtt{ofn}$    | Observation function |
| $\mathbf{R}$   | $\backslash \mathtt{rfn}$    | Reward function      |
| ${ m T}$       | $\backslash 	exttt{tfn}$     | Transition function  |
| ε              | $\verb \nohistory $          | Empty history        |
| $\pi$          | $\backslash {	t policy}$     | policy               |
| $Q^{\pi}$      | \qpolicy                     | Q policy values      |
| $\hat{Q}$      | \qmodel                      | Parametric model     |
| $V^{\pi}$      | \vpolicy                     | V policy values      |
| $\hat{V}$      | \vmodel                      | Parametric model     |
| $A^{\pi}$      | \apolicy                     | A policy values      |
| $\hat{A}$      | amodel                       | Parametric model     |
| $U^{\pi}$      | \upolicy                     | U policy values      |
| $\hat{U}$      | $\backslash \mathtt{umodel}$ | Parametric model     |

# Option [marl]

| Symbol              | Command                     | Description           |
|---------------------|-----------------------------|-----------------------|
| $ar{\mathcal{H}}$   | \hsset                      | Joint history set     |
| $ar{\mathcal{A}}$   | $\setminus \mathtt{asset}$  | Joint action set      |
| $\bar{\mathcal{O}}$ | $\setminus \mathtt{osset}$  | Joint observation set |
| $ar{h}$             | \hs                         | Joint history         |
| $\bar{a}$           | \as                         | Joint action          |
| $\bar{o}$           | \os                         | Joint observation     |
| $\bar{\pi}$         | $\backslash {\tt policies}$ | Joint policy          |
| $Q^{\bar{\pi}}$     | \qpolicies                  | Q joint-policy values |
| $V^{ar{\pi}}$       | \vpolicies                  | V joint-policy values |
| $A^{ar{\pi}}$       | \apolicies                  | A joint-policy values |
| $U^{\bar{\pi}}$     | \upolicies                  | U joint-policy values |

# Option [theorem]

| Symbol | Command  | Description |
|--------|--|-------------|
|        | \begin{definition} \begin{example}   |             |
|        | <pre>\begin{axiom} \begin{conjecture} \begin{proposition} \begin{lemma} \begin{theorem} \begin{corollary} \begin{generalization}</pre> |             |

# Option [misc]

| Symbol | Command  | Description  |
|--------|--|--|
| † (k)  | $\begin{tabular}{ll} $\backslash D$ \\ $\backslash iter\{k\}$ \end{tabular}$ | Dagger superscript<br>Superscript indicating iteration |