

**Theorem 0.0.1.** *The Borel  $\sigma$ -algebra  $\mathcal{B}(\mathbb{R})$  is generated by intervals of the form  $(-\infty, a]$  where  $a \in \mathbb{Q}$  is a rational number.*