

Corollary 0.0.1. (from Theorem 1.3.1) Two random variables X and Y are independent iff $\mathbb{P}(X \leq a, Y \leq b) = \mathbb{P}(X \leq a)\mathbb{P}(Y \leq b)$ for all $a, b \in \mathbb{Q}$.