

(from Lemma 3.3.3) If the quadratic variation of a continuous stochastic process is a.s. strictly positive, then the total variation of the process is almost surely infinity. In particular, sample paths of a Brownian motion are a.s. functions of infinite variation on any interval.

Theorem 0.0.1.