

Definition 0.0.1 (measurability of a function). A function $X : \Omega \rightarrow \Psi$ is said to be **measurable** with respect to \mathcal{A} and \mathcal{G} if the pre-image $X^{-1}(G) = \{\omega : X(\omega) \in G\} \in \mathcal{A}$ for all $G \in \mathcal{G}$, or equivalently,

$$X^{-1}(\mathcal{G}) \subseteq \mathcal{A}.$$