

**Definition 0.0.1** (Ito's integral for general integrands). For any process  $\gamma \in L^2_{\mathbb{P}}(W)$ , the random variable  $I_T(\gamma)$  is called Ito's integral of  $\gamma$  with respect to  $W$  over  $[0, T]$ . We write (notation only, not a formal definition):

$$I_T(\gamma) = \int_0^T \gamma_u \cdot dW_u$$

$$I_t(\gamma) = I_T(\gamma \mathbf{1}_{[0,t]}) = \int_0^t \gamma_u \cdot dW_u$$