

Definition 0.0.1 (almost sure equality of two r.v.s). Two random variables X and Y are said to be **equal almost surely**, written $X \overset{\text{a.s.}}{=} Y$ if the set $\{\omega : X(\omega) \neq Y(\omega)\}$ is of probability zero.