

Proposition 0.0.1. Suppose that γ is an \mathbb{R}^d -valued \mathcal{F} -progressively measurable process such that $\mathbb{E}^{\mathbb{P}}[\mathcal{E}_T(U)] = 1$. Define a probability measure $\widetilde{\mathbb{P}}$ on (Ω, \mathcal{F}_T) equivalent to \mathbb{P} by means of the Radon–Nikodym derivative

$$\eta_T = \frac{d\widetilde{\mathbb{P}}}{d\mathbb{P}} = \mathcal{E}_T\left(\int_0^\cdot \gamma_u \cdot d\mathbf{W}_u\right) = \mathcal{E}_T(U).$$

Then the process $\widetilde{\mathbf{W}}$ given by the formula

$$\widetilde{\mathbf{W}}_t = \mathbf{W}_t - \int_0^t \gamma_u \, du, \quad \forall t \in [0, T]$$

follows a standard d -dimensional Brownian motion on the space $(\Omega, \mathcal{F}, \widetilde{\mathbb{P}})$.