

Proposition 0.0.1. Suppose that γ is an \mathbb{R}^d -valued \mathcal{F} -progressively measurable process such that $\mathbb{E}^\mathbb{P}[\mathcal{E}_T(U)] = 1$. Define a probability measure $\tilde{\mathbb{P}}$ on (Ω, \mathcal{F}_T) equivalent to \mathbb{P} by means of the Radon-Nikodym derivative

$$\eta_T = \frac{d\tilde{\mathbb{P}}}{d\mathbb{P}} = \mathcal{E}_T \left(\int_0^T \gamma_u \cdot dW_u \right) = \mathcal{E}_T(U).$$

Then the process \tilde{W} given by the formula

$$\tilde{W}_t = W_t - \int_0^t \gamma_u du, \quad \forall t \in [0, T]$$

follows a standard d -dimensional Brownian motion on the space $(\Omega, \mathcal{F}, \tilde{\mathbb{P}})$.