

M3 Challenge 2025

Hot Button Issue: *Staying Cool as the World Heats Up*

Executive Summary

This report presents an in-depth analysis of energy consumption trends, heatwave vulnerability, and temperature in a non-air-conditioned dwelling in Memphis, Tennessee, using advanced statistical modeling techniques. The study is divided into three primary components: the temperature in buildings without AC, forecasting future energy consumption trends, and developing a vulnerability index for neighborhoods in the event of extreme heat waves or power outages. Each section applies quantitative methods to guide decision-making for policymakers and utility companies, ensuring efficient resource allocation and proactive infrastructure planning.

The model predicts indoor temperatures in a non-air-conditioned Memphis home during a 24-hour heatwave, accounting for heat transfer from insulation, windows, and inhabitants. It shows that indoor temperatures are typically higher than outdoor temperatures due to heat retention. Sensitivity analysis on parameters like window count and floor area showed moderate variability. The model works well but is limited by assumptions on room dimensions and lacks consideration for factors like ventilation.

Next, the study looks at historical energy consumption data, extrapolating trends and data from Shelby County and East South Central USA to predict future energy demands in Memphis. Utilizing an additive triple exponential smoothing model in excel by using the `forecast.ets` function, the analysis identifies seasonal variations and long-term trends in electricity usage. The model projects peak demand to occur in June 2025, with an estimated maximum consumption of 640,184,128.96 kWh. Over the next 20 years, energy consumption is expected to gradually decline due to technological advancements and efficiency improvements, with an estimated decrease of 147,948,413.90 kWh by 2045. While this trend suggests progress in energy conservation, the summer months continue to pose challenges with heightened demand, necessitating preparedness from energy providers. Additionally, this model suggests a constant trend which may not be applicable in all cases and over longer periods of years it becomes less accurate.

The next part of the study focuses on assessing neighborhood vulnerability to extreme heat events. The Analytic Hierarchy Process (AHP) was employed to weigh multiple socio-economic and infrastructure factors, including population size, age distribution, housing conditions, and transportation methods. Positive weights were assigned to characteristics indicating higher vulnerability, such as large populations of elderly and young residents, reliance on walking for transportation, and older housing structures with poor ventilation. Conversely, factors such as high median income, newer homes, and automobile dependence reduced vulnerability scores. The dispersion analysis yielded Q1 as -0.891 and Q3 as 0.624, giving an interquartile range (IQR) of 1.51 ($IQR = Q3 - Q1 = 0.624 - (-0.891)$). This suggests that neighborhoods with an AHP value (vulnerability score) below -0.891, such as Uptown / Pinch District, fall in the top quartile for heatwave preparedness. In contrast, neighborhoods with an AHP of 0.624 or higher, including Collierville / Piperton, are in the bottom quartile and are less prepared for heatwaves.

These findings offer valuable insights for policymakers and utility companies. Our results demonstrate the hazardous conditions created by abnormal high temperatures during a heat wave. Additionally, the predicted energy trends allow for utility companies to be prepared in high demand months, and more effectively plan for capacity needs. Finally, the neighborhood vulnerability assessment provides data for targeted interventions and resource allocations.

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Q1: Hot To Go

1.1 Defining the Problem

The first problem asked us to develop a model to predict the indoor temperature of any non-air-conditioned dwelling during a heatwave any time during a 24-hour period in one of the provided cities. We chose to find the indoor temperature of a non-air conditioned building in Memphis, Tennessee.

1.2 Assumptions

1.2-1 Adults who do not work stay in the dwellings for 16 hours per day relaxing/sitting

- **Justification:** It's difficult to predict where people who are unemployed or not working spend their time so they are expected to stay home for the purposes of finding the heat they emanate to predict indoor temperature.

1.2-2 Observations are independent and identically distributed

- **Justification:** For the purposes of the random forest regression we must assume that the data points we are analyzing are not reliant upon each other (meaning no time based dependencies).

1.2-3 Inside walls do not significantly contribute to the inside temperature

- **Justification:** While external walls usually contain insulation, thus hindering heat expansion, internal walls contain drywall, which is not a good insulator [1]. Thus the observer frame of reference can either be adjacent to an external wall or an internal wall.

1.2-4 All external walls are insulated with fiberglass

- **Justification:** Most houses in the U.S. are insulated with fiberglass [2]. Thus it is reasonable to assume that all houses are insulated with fiberglass.

1.2-5 There are no other methods in the house to lower room temperature, besides the impact of humans, windows, and fiberglass emitting heat.

- **Justification:** It is difficult to predict the impact of these methods, such as: opening a window, using a fan, using ventilation, etc. [4]

1.2-6 Each house is rectangular, with a width to length ratio of 5:7 and a floor area of around $2,469 \text{ ft}^2$.

- **Justification:** It is difficult to predict the size of a house. To simplify this, it was assumed that each house was a rectangle and took the dimensions width:length as 5:7, in lieu with the average size of a townhouse, as the authors were not knowledgeable of any other sources that provided house dimensions [3].

Additionally, the average floor area of a new home was around $2,469 \text{ ft}^2$ [5].

1.2-7 Heat transfer only occurs between the roof, walls, and the environment, not from the ground

- **Justification:** Because the ground has a high heat capacity, even when compared to fiberglass, this means that the floor will not contribute significantly to heat transfer from the environment into the house [6].

1.2-8 There are an average number of 8 windows in an American home, and each window is 24 in wide x 36 in long.

- **Justification:** Windows have a significantly larger thermal conductivity than fiberglass (1.05 and 0.04 respectively) and the heat transfer into the home. However it is difficult to assume the relative amount or size of windows on the walls of a house in Memphis, so as a result we decided on using the average number and size of windows in the U.S. (8 and 24 in x 36 in, respectively) [8, 9].

1.2-9 The initial inside temperature is assumed to be the same as the initial outside temperature.

- **Justification:** For ease of calculations, the initial inside temperature is equal to the outside temperature. Additionally, the problem implies that the 24-hour heat wave begins around the same time that air conditioning is lost, meaning that both external and internal temperatures were about the same.

1.3 The Model

1.3.1 Developing the Model

When choosing a model for this situation, we decided to use the equation $q = mc\Delta T$, where q is the amount of heat (J), m is the amount of substance (m), and ΔT is the change in temperature, or $T_i - T_0$, where T_i is the inside temperature and T_0 is the outside temperature. We utilized this equation because through some rearranging, it was possible to solve in terms of ΔT :

$$\Delta T = \frac{q}{mc_p}$$

Note that because $m = \rho V$, we can substitute this into our equation above.

Converting both sides to a differential form, we can get:

$$\frac{dT_i}{dt} = \frac{q}{\rho c_p V}$$

This equation is useful because it included time (t), which we could use. However, we still needed T_0 . To do this, we integrated both sides over time:

$$\int_{T_i(0)}^{T_i(t)} dT_i = \int_0^{\Delta t} \frac{q_{in}}{\rho c_p V} dt$$

$$T_i(t) - T_i(0) = \frac{q_{in}}{\rho c_p V} \cdot \Delta t$$

However, if we assume that $T_i(0)$ is equal to T_0 (see assumption 1.2-9), one can see that:

$$T_i(t) = T_0 + \frac{q_{in}}{\rho c_p V} \cdot \Delta t$$

We will use the variables q_f (amount of heat transferred into house from the fiberglass insulation), q_h (amount of heat transferred into house from the fiberglass insulation), and q_g (amount of heat transferred into the house from the glass). Additionally, because Δt is in seconds but the data was given in hours [10], $\Delta t = 3600t$, where t is in hours.

It is also important to include $\rho = \frac{P}{RT}$, where $R=287.05$ (J/kg), T is temperature (K), and P is pressure (Pa). P can depend on the temperature (in this case, temperature outside, or T_0), the molar mass of air (M) and height above sea level of the environment (h), and $P = P_0 \cdot e^{\frac{-Mgh}{R \cdot T_0}}$, where $R=8.314 \text{ J} \cdot \text{mol}^{-1} \text{ K}^{-1}$. It is also important to not that each

$q = -\frac{kA(T_i(t)-T_0)}{d}$, where d is the thickness of the material, A is the surface area of the surface that heat transfers through, and k is the thermal permittivity¹. Finally, V (volume) is equal to Putting all these variables together, we can get:

$$T_i(t) = T_0 + \frac{(q_f + q_h + q_g) \cdot 3600t}{\frac{c_p V P_0 \cdot e^{-\frac{Mgh}{R1 \cdot T_0}}}{RT}}$$

However, it is required to use an approximation of T_0 ' on the right hand side of the equation in order to solve the equation without rewriting to solve for T_i , and allows the formula to be calculated in a spreadsheet without returning a circular reference error. This approximation was optimized, and as a result, we estimated that T_0 ' was indeed 85°F, or 302.5944 K.

We then used the provided data on temperatures recorded during a heat wave during the 24-hour period.

1.4 Results

The model is as follows:

$$T_i(t) = T_0 + \frac{(q_f + q_h + q_g) \cdot 3600t}{\frac{c_p V P_0 \cdot e^{-\frac{Mgh}{R1 \cdot T_0}}}{R2To}}$$

Where

- T_i represents the outside temperature in *Kelvin*
- T_0 and To represent the outside temperature in *Kelvin*
- q_f represents the heat transfer rate of fiberglass in $\frac{\text{Watts}}{\text{Meter kelvin}}$
- q_h represents the heat transfer rate of the building's inhabitants in $\frac{\text{Watts}}{\text{Meter kelvin}}$
- q_g represents the heat transfer rate of glass in $\frac{\text{Watts}}{\text{Meter kelvin}}$
- c_p represents the specific heat capacity of air in $\frac{\text{Joules}}{\text{Kilogram}}$
- V represents the Volume of the building in *meters*³
- P_0 represents atmospheric pressure in *Pascals*
- M represents the molar mass of air in $\frac{\text{Kilograms}}{\text{Mole}}$
- g represents the acceleration due to gravity in $\frac{\text{meters}}{\text{seconds}^2}$
- h represents the elevation of Memphis in *meters*
- $R1$ represents the universal gas constant in $\frac{\text{Joules}}{\text{Mole} * \text{Kelvin}}$

¹ Specifically, $q_{\text{sub } h}$ was calculated through the following: employed people (47.05%) had an estimated 8 hours of leisure time (that they spent in the house), unemployed people (52.95%) had an estimated 16 hours of leisure time (that they spent in the house). For both individuals, 70 watts of energy was assumed to emit from these individuals during sleeping, and 100 watts of energy was assumed to emit from these individuals during leisure time. Using the k value for humans, $q_{\text{sub } h}$ was obtained [6.5].

- T'_0 represents the approximated inside temperature in *Kelvin*
- $R2$ represents the specific gas constant of air in $\frac{\text{Joules}}{\text{Kilogram} * \text{Kelvin}}$

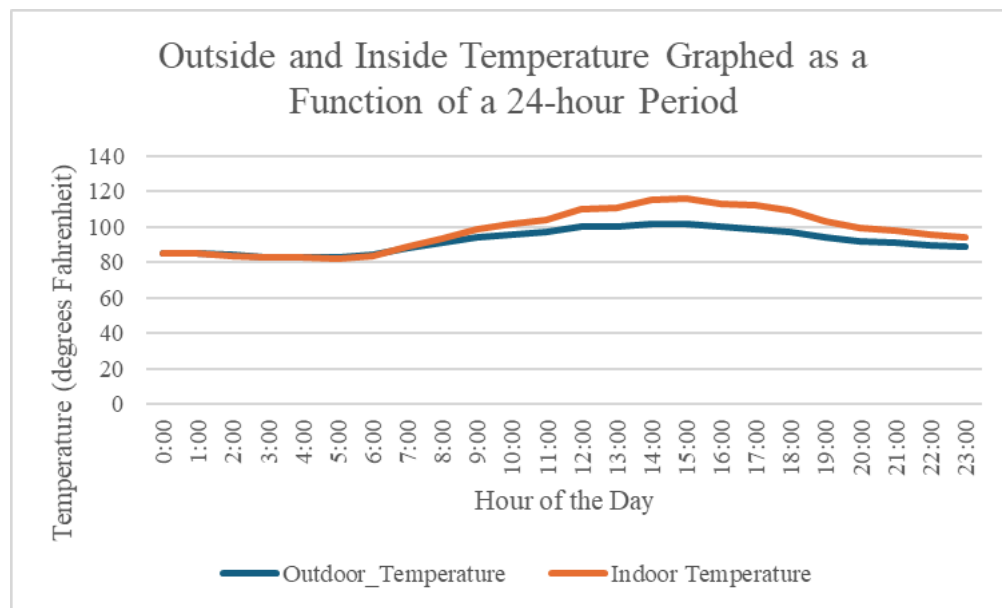
And for q_f and q_g

$$q = \frac{kA(T_i - T_o)}{d}$$

Where

- q represents heat transfer rate in *Watts*
- k represents the thermal conductivity of a material in $\frac{\text{Watts}}{\text{Meter kelvin}}$
- A represents the surface area being heated in meters^2
- T_i represents the approximated inside temperature in *Kelvin*
- T_o represents the outside temperature in *Kelvin*
- d represents the thickness of the surface being heated in *meters*

Figure 1:



This graph demonstrates the outside and inside temperature as a function of a 24 hour period.

1.5 Discussion

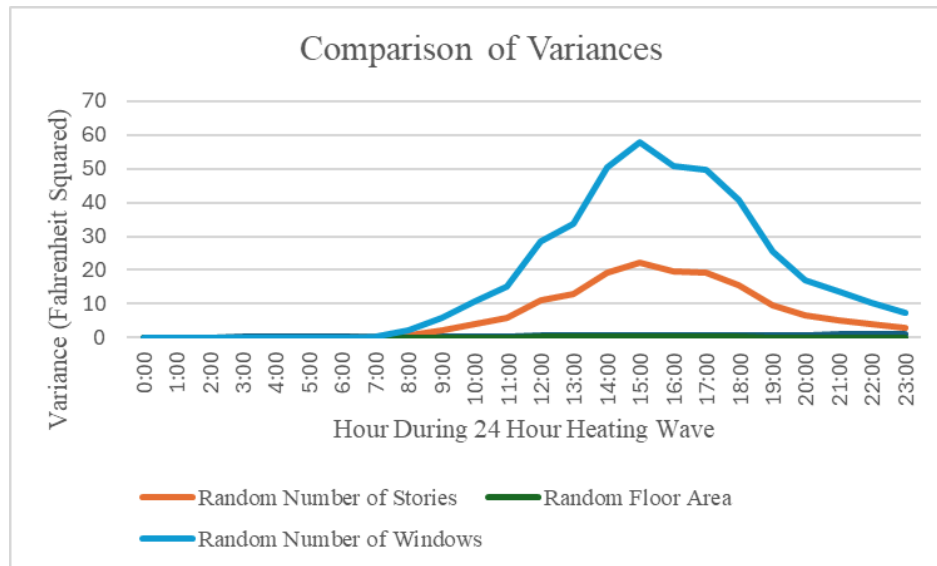
For a suburban house in Memphis, our model will predict a higher inside than outside temperature most of the time during a 24-hour heating wave, from 0:00-1:00 and from 7:00-23:00, which highlights the utility of proper insulating material in its goal of diminishing rises in temperature in the building. The trends in indoor temperatures follow that of outdoor temperatures; for example, the highest separation between the inside and outside temperature, at 14.16052°F, occurred at 15:00, yet the indoor temperatures do not seem to subside at the same rate as the outside temperatures. Rather, the model suggests that buildings seem to accumulate heat which they radiate into their

interior over time; despite losing heat through means such as windows, a majority of the heat gained is trapped inside by the insulating material, keeping temperatures higher than that outside.

1.6 Sensitivity Analysis

To determine the accuracy of our predicted model, sensitivity analysis was conducted on it. We changed the parameters, and the jittered variance was calculated. Three parameters were selected: the number of stories, the number of windows, and the floor surface area, as these parameters were most likely to vary between house to house.

Figure 2: Comparison of Variances for Certain Parameters



This graph demonstrates the variance, in $^{\circ}\text{F}^2$, when the number of floors, the floor area, and the number of windows is altered.

1. Because the tallest apartment in Memphis is 25 floors tall [8.5], a number of floors was randomly chosen between 1 and 25, and inside temperatures were calculated over the hypothetical 24 hour heat wave period. This was repeated 10 times. As seen in the graph, the highest variance observed was around 20°F^2 (24%), meaning that the model was relatively moderately prone to error.
2. Because house floor plan can vary drastically, we randomly offset the “ideal” floor plan area ($2,469\text{ ft}^2$) by 5% either way, and inside temperatures were calculated over the hypothetical 24 hour heat wave period. This was repeated 5 times. As seen in the graph, the highest variance was around $0.209559055^{\circ}\text{F}^2$ (0.24654%), that the model was relatively unlikely prone to error.
3. Because the number of windows can vary drastically from house to house, such as an average of 22 windows found by the EPA [7], a number of windows was randomly chosen between 1 and 22, and inside temperatures were calculated over the hypothetical 24 hour heat wave period. This was repeated 10 times. As seen in the graph, the highest variance observed was around 50°F^2 (59%), meaning that the model was relatively extremely prone to error.

1.7 Strengths and Weaknesses

The model worked very well in accounting for multiple variables and using them adequately, and can be changed to model buildings of different square footage and number of stories. However, the model is held back by the availability of data relating to room dimensions. The model assumes that each room is a rectangle with one window for every two walls, very much standardizing the nuanced architecture of Memphis. Additionally, the model fails to consider the effects of ventilation, which can circulate outside and inside air together, thus decreasing the interior temperature had there not been any ventilation, and solar gain, where sunlight entering through the windows can bring in warmth and increase the internal temperature significantly.

When discussing the importance of these findings, it is important to note from the graph that while lower outside temperatures (e.g. 80-85°F) do not result in vastly different interior temperatures, as the temperature rises in a heat wave (e.g. 100-120°F), do result in vastly different interior and exterior temperatures. This demonstrates that heat waves are extremely dangerous, as it can lead to unbearable and potentially hazardous temperatures to human life. However, the analysis of variance also demonstrates the high dependency of interior temperature on the number of windows and the number of stories to the building. Further research with lesser time constraints could investigate stronger models that could be less sensitive to parameter changes, as mentioned previously.

Q2: Power Hungry

2.1 Defining the Problem

The second question asks us to predict the peak demand that the city's power grid needs to be able to handle during summer months as well as changes in maximum demand 20 years from now. We looked at various trends in data to extrapolate an estimate for monthly energy consumption in the city of Memphis, Tennessee, as well as how the demand would change.

2.2 Assumptions

2.2-1 The per-capita energy usage in Shelby County is equal to the per-capita energy usage in Memphis, with negligible difference.

- **Justification:** Data for energy usage for specific cities is extremely limited, and therefore isn't sufficient to be able to come up with accurate predictions. Moreover, Memphis accounts for the majority of the Shelby County population, and therefore any differences in per-capita energy usage between Memphis and Shelby County are likely negligible. Since Memphis constitutes the majority of the county's population, its energy consumption patterns dominate the overall county's trends. As a result, even if there are slight variations in energy usage between Memphis and other parts of Shelby County, these differences are unlikely to significantly affect the overall per-capita average.

2.2-2 Examined monthly trends in energy consumption in Shelby County are similar to trends in the East South Central US region (encompassing Alabama, Mississippi, Tennessee, and Kentucky.)

- **Justification:** Month by month data for Shelby County is not easily accessible, making it difficult to determine monthly trends in Shelby County. Moreover, weather patterns in Shelby County can be assumed to be similar to those of the East South Central U.S. region, as both share similar geographical conditions

such as humidity, sunlight exposure, and proximity to large bodies of water. Due to this proximity, Shelby County experiences comparable seasonal energy demands, leading to similar energy consumption trends. The ratio for the change in months for energy consumption should therefore be constant across all regions included in the east south central US.

2.2-3 There will be no major innovative changes affecting energy consumption.

- **Justification:** Major inventions in energy use would significantly impact overall energy consumption. However, it is practically impossible to predict when these innovations will occur or how they will affect energy usage. Additionally, since our model is based on trends from 2012-2022, it accounts for gradual improvements in energy efficiency.

2.2-4 Consumer energy use trends will remain consistent in the future

- **Justification:** There was not enough time to accurately identify the effect of campaigns and movements on climate change on energy consumption. The model predicts future data off of historical data, so it is assumed that the data will follow the general trend over 2012-2022 and that no new social movements will massively change the energy consumption of citizens in Memphis, Tennessee, Shelby County, or the east south central US region.

2.2-5 Population trends of Shelby County and Memphis, Tennessee will not drastically change in the future

- Our model works off the assumption that the population of these two areas will not be drastically reduced or increased for any reason and continues to follow the general trends from 2012-2022. Population of these two regions should not drastically change unless events such as natural disasters or major diseases take place, which we consider too random to consider.

2.2-6 Current temperature trends and weather patterns will not significantly vary from the past, and people will react to these trends in similar ways

- Predicting future climate changes is challenging, as the effects of climate change movements are difficult to anticipate. Temperature fluctuations will impact energy use, such as increased reliance on air conditioning as temperatures rise. Since our model is based on existing energy consumption data, we assume that climate patterns will remain relatively consistent and that people will adjust their energy use in ways similar to the past. Climate change has driven rising temperatures for many years, leading the model to predict that this trend will continue. However, this assumption has limitations.

2.3 The Model

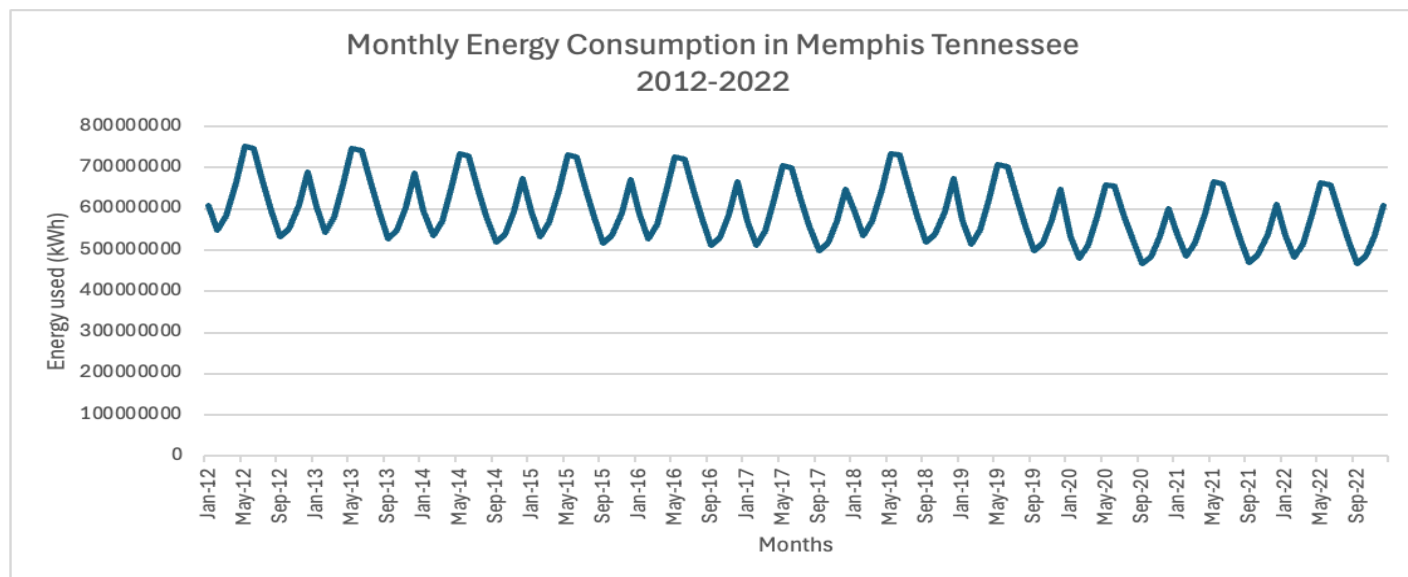
2.3.1 Developing the model

For this dataset, we chose an additive triple exponential smoothing forecasting model in Excel spreadsheets. Triple exponential smoothing is particularly useful for time series data that exhibit both trends and seasonality, making it ideal for our dataset, as energy consumption typically follows long-term and seasonal trends. Other models such as a linear regression or logistic curves would not be able to show seasonality and cannot give us the full trend data.

To generate our dataset, we first obtained total monthly energy consumption data for the East South Central U.S. states [10] and calculated the month-to-total ratio for 2024 by dividing each month's consumption by the total annual consumption (Appendix F). We assumed this ratio remained constant over time and applied it to Shelby County, considering its monthly energy consumption patterns to be identical to the regional trends. Next, we multiplied Shelby County's yearly energy consumption from 2012 to 2022 [10] by each month-to-total ratio to estimate monthly energy consumption values for those years (Appendix F). These monthly energy values were then divided by Shelby County's population [12] for each respective year to determine the per capita energy consumption (Appendix G). Assuming that Memphis, Tennessee, has the same per capita energy consumption as Shelby County, we multiplied these values by Memphis's population [12] to estimate monthly energy consumption in Memphis from 2012 to 2022 (Appendix E).

We then graphed this data, allowing us to analyze trends and justify our choice of forecasting model.

Figure 3: Graph of monthly energy consumption in kWh in Memphis, Tennessee, vs the various months (Month-20XX) with extrapolated data.



Shows trends in monthly energy consumption from 2012-2022, by plotting the extrapolated data points on a graph

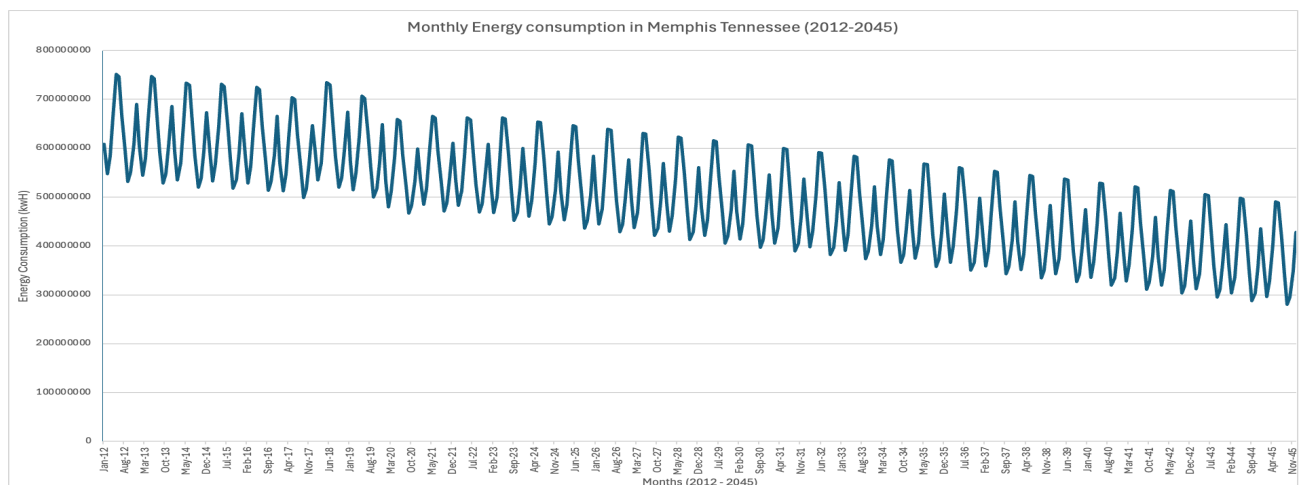
From the graph, we observe a clear seasonal trend. There are energy consumption peaks in the summer months (around June) and declines during moderately cool months, like February and September. Additionally, overall energy consumption appears to be gradually decreasing over time.

Given these patterns, we used triple exponential smoothing, which accounts for both seasonality and trends, to produce accurate future predictions. Furthermore, we employ the additive version of the triple exponential smoothing model because the seasonal variations remain relatively constant rather than fluctuating in magnitude over time.

2.3.2 Executing the model

Excel spreadsheets provides a function called “forecast.ets” which predicts future values off of historical values by using the additive version of the exponential smoothing algorithm. This is Excel's function for triple exponential smoothing. The function is additive because seasonality is constant and so are trends, which is seen in Figure 3. Using the Excel forecast functions, there are 5 parameters which we need to enter: The target date, the list of energy consumptions by month for all known values, the corresponding dates of the energy consumption, the seasonality, data completion, and aggregation. The seasonality is 12 because repetition of the peaks and troughs happens yearly. The historical data is fully complete as there are no missing values, so we can enter a 1, and the type of aggregation is an average, so that value is also a 1. We can input the values for our monthly energy consumption by month found in the earlier development to this forecast, using the known values of energy consumption corresponding to their specific month, the target date for our prediction, the seasonality, the data completion, and the data aggregation values. Using the same data for every date and only changing the target date in the forecast.ets formula until we reach December 2045 gives us our predicted values for every month between December 2022 and December 2045. Plotting a graph of these values vs the given months will give us the expected trend for energy consumption by month in Memphis, Tennessee:

Figure 4: graph of energy consumption in kWh by month in Memphis, Tennessee.



The graph shows increasing and decreasing trends throughout the year as well as a decreasing overall energy consumption over the next 20 years.

Our model equation for this situation will have two variables: the amount of time after the initial set of data in months and the seasonal factors. There are various other equations that have to be calculated but because of the complexity we were not able to get a specific value.

Figure 5:

Symbol	Variable	Unit
m	Seasonal smoothing coefficient	N/A
S	Seasonal factors	N/A
α	level smoothing coefficient	N/A

β	Trend smoothing coefficient	N/A
γ	Seasonal smoothing coefficient	N/A

Table of variables used in our model development

To derive an equation for our model and analyze sensitivity on this test we ran the original data set through a series of codes to determine the optimal alpha, beta, and gamma values. The equation for exponential smoothing is complex, consisting of multiple parts that are eventually combined together to create a final formula.

$$\text{(Level)} L_t = \alpha * (Y_t - S_{t-s}) + (1 - \alpha) * (L_{t-1} + b_{t-1})$$

$$\text{(Trend)} b_t = \beta * (L_t - L_{t-1}) + (1 - \beta) * b_{t-1}$$

$$\text{(Seasonal)} S_t = \gamma * (Y_t - L_t) + (1 - \gamma) * S_{t-s}$$

$$\text{(Forecast for period } m) F_{t+m} = L_t + m * b_t + S_{t+m-s}$$

These are the 4 parts of the triple exponential smoothing equation, where alpha is the coefficient for level smoothing, beta is the coefficient for trend smoothing, and gamma is the coefficient of seasonal smoothing. Running our original data set through a series of code in google co-lab calculates the optimized coefficients for the equation and fits them into the final equation. This optimization method chooses the best parameters for our model to assure accurate results and calculations (Appendix F). The finalized equation for our model is:

Figure 6: Forecast Equation

$$F_m = (547682731.9 + (m * -616451.7246)) + S_T$$

Equation, which finds the forecasted energy consumption in a certain month based on seasonality and months since December 2022.

Where F_m is the forecasted value, m is the amount of months after December 2022. Seasonal factors compare the specific data value with the forecasted data value. Seasonal factors are constant for every month because we are using triple exponential smoothing and seasonal trends should be constant. To calculate seasonal factors, a code script was run to calculate the trend by using a moving average to estimate the trend and then subtract the trend from the observed values to isolate seasonality. It then averaged the seasonal values for each month over all years and normalized the seasonal components so they sum to zero to give us our values for the seasonal factors.

Table 7: table of calculated seasonal values for our model

Month	Seasonal Factors
January	-22178994.82
February	-79081952.41
March	-45083242.81
April	30163132.82
May	115135446
June	110994948.8

July	38977596.92
August	-30176925.26
September	-90304856.17
October	-71618126.19
November	-17668884.14
December	60841857.28

2.4 Results

Running the data through the Forecast equation (Figure 6) gives us several data points as well as giving us an equation for forecasted values based on months. To find the maximum demand of energy consumption that the Memphis power grid would be required to handle, we can look at the highest peak in Figure 4 past the current date. As such, we conclude the highest energy consumption for the future is in June 2025 (Figure 4). To find the specific energy consumption, we use the Forecast equation $F_m = (547682731.9 + (m * -616451.7246)) + S_T$. Using June's seasonality factor and the month of June 2025, we find $F_m = (547682731.9 + (30 * -616451.7246)) + 110994948.8 = 640,184,128.962$. As such, in preparation for the summer months, the power grid should be able to handle 640,184,128.962kWh. Next, we can use Figure 4 to conclude how the max demand will change over the next 20 years. Observing the general trend, we can conclude that the max demand will decline over the years, with an estimated decrease of 147,948,413.904 by 2045 (485,955,292.5258 in March 2025 to 338,006,878.622 in March 2045), as per the Forecast equation.

2.5 Discussion

Our model indicates that energy consumption hits its peak during the summer months around May and June, and hits its lowest values in fall and winter months such as February and September, and predicts a general decrease in energy consumption as the years go on. Based on the past trends of the data, the energy consumption is decreasing. Our model accounts for variables such as innovation and temperature on a small scale by assuming they follow the same trends as historical values, meaning that as long as temperature and innovations follow similar trends as historical data and do not change drastically our data will be valid.

Our results provide valuable insight for policymakers and utility companies. Providing the maximum energy demand allows for utility companies in Memphis to be prepared for energy demands without being overwhelmed. Furthermore, by showing that over time, energy consumption is seen to decrease, policymakers and utility companies can shift focus to other infrastructure over time, and invest in other industries. Furthermore, the seasonal trends give utility companies ideas about how energy consumption changes throughout the year, allowing them to be prepared for increases or decreases in energy consumption throughout the year. The specific results provide deeper insight into specific predicted energy usage. According to our model, as long as there are no unexpected increases in temperature, energy consumption should continuously decrease over time. As such, it seems to show that while temperatures have been steadily increasing with climate change, factors, such as steady improvements in technology, have been decreasing energy consumption. Therefore, it appears that the issue about

energy consumption will, by itself, face improvements. However, summer months still show high energy consumption values, even in later years, showing a need for preparation from utility companies for these months.

2.6 Strengths and Weaknesses

Since our data is a time series with consistent trends throughout the years, an additive triple exponential smoothing model fits the requirements to accurately show the results and trends throughout the separate years and show a trend overall. This model effectively shows the trends in the months by using different values for seasonal factors and months as well as showing a decreasing overall trend for the energy consumption in total, allowing us to observe and analyze data across the years and throughout the years. One of the main things that can weaken exponential smoothing is the selection of the alpha, beta, and gamma parameters, since using the wrong ones will cause different results. Using a code script to optimize the results to give us the smallest amount of error helps us get the best values for our parameters to insert into our equation.

However, exponential smoothing cannot predict accurately very far into the future. The optimal range for exponential smoothing would be about 5-10 years, which we went far past. Additionally, we did not have enough time to account for additional variables that could have affected energy output, like views on energy consumption or temperature trends. Additionally, exponential smoothing cannot handle sudden disruptions in the data. This model works off the assumption that future data will proceed similarly to historical values in the same trend and assumes constant seasonality, though for this situation, seasonality should change very slightly. A better model, if we had more time, could be to do an exponential smoothing equation with multiple independent variables to account for temperature, cost, and populations that could affect the variables. Other models such as a Seasonal ARIMA that is adjusted for multiple independent variables would have been more accurate and offered a better scope for the data. However, we were not able to implement these methods because of the complexity and time constraints.

Q3: Beat the Heat

3.1 Defining the Problem

The third problem asked our team to develop a vulnerability score for each neighborhood with the goal of equitably allocating resources especially to those in need. These scores would come into play in the event of an extreme heat wave or power grid outage. In addition, we were asked to present an approach to how Memphis can incorporate the vulnerability scores into their heat wave management strategies.

3.2 Assumptions

3.2-1 The criteria being judged are independent from one another.

- **Justification:** In accordance with the Analytic Hierarchy Process we must assume that none of the variables are dependent on one another so the results from the model can be valid.

3.2-2 The criteria weighting reflects the relative importance of each factor on the need during a heatwave.

- **Justification:** In reality needs can be based on a case-by-case basis, but by generalizing each potential need and ranking it by its perceived relative importance we can estimate the total need of a neighborhood without having to individually analyze each case.

3.2-3 The scores are linearly scalable and meaningful and do not distort the real world significance.

- **Justification:** We are assuming that by scaling and normalizing the values linearly it doesn't distort the real world effect of the needs during a heatwave. For example, having a very low income is significantly worse than having a slightly below average income, but this could not be recognized by this particular model.

3.2-4 The combined effects of the model are additive.

- **Justification:** We assume by using this model that the individual effects contributing to need in a heatwave are still relevant when added because this model calculates the vulnerability score by adding the weighted needs of all the values.

3.2-5 Analytic Hierarchy Process Captures All Relevant Factors

- **Justification:** This model assumes that all the major relevant factors in determining need in the event of a severe heat wave are included in the model. If a factor is missing it's possible that the model may be incomplete.

3.3 The Model

3.3.1 Model Development

To best answer this question, we used the Analytic Hierarchy Process (AHP), a structured decision-making framework used to determine the relative importance (weights) of multiple factors when making complex decisions, to create the vulnerability scores for each neighborhood [13]. Factors are identified as a value between -1 and 1 based on their relative importance or unimportance to the vulnerability index at hand and combined they must add to 1. A score of 1 meaning significant importance to needing funds and a score of -1 meaning significant unimportance to needing extra funding. The scores given to a given factor are indicated by the number in parenthesis.

First, we determined which factors affected the need of a neighborhood in the event of a heatwave and weighed them based on their relative importance or unimportance to promote equity in fund allocation. For factors we thought would need extra fund allocation we weighted positively and higher on the scale. We said that Population, Households with one or more people 65 years and over, Households with one or more people under 18 years, Primary mode of transportation to work (persons aged 16 years+) walking, Homes built 1970 to 1989, Homes built 1950 to 1969, Homes built 1950 or earlier, and Detached whole house as indicators that these neighborhoods needed extra funding allocation due to their susceptibility to heat. A neighborhood with more people (0.40) overall means there are more potential victims and therefore a greater necessity of funds. Elderly (0.30) and younger people (0.25) are more vulnerable to heatwaves so having a greater population of these people increased a neighborhood's vulnerability score. Having walking as the main way of transportation (0.10) means more pedestrians which in turn indicates more heat exposure. Finally, older homes (0.10, 0.15, 0.20, 0.25) and detached homes have worse ventilation meaning that they need more support in the event of a heatwave. We used the data provided in the MathWorks Math Modeling Challenge 2025, curated data [10].

Then, we selected the factors that indicated a lack of need including: Population with Bachelor's degree or higher (-0.15), Median household income (in US dollars), Primary mode of transportation to work (persons aged 16 years+): driving, and Homes built 2010 or later. Having a bachelor's degree correlates with having more knowledge and resources to deal with a heatwave. Having a higher median household income means having greater access to

resources during such an event. Then, driving (-0.15) was an advantage in a heatwave because it kept one out of the sun. Finally, we listed Homes built in 2010 or after because these houses have improved insulation which is better for keeping cool and avoiding heat stroke.

Neighborhoods included in the model: Coro Lake / White Haven, East Memphis – Colonial Yorkshire, Frayser, Egypt / Raleigh, South Memphis, Bartlett, Zipcode 2, Collierville / Piperton, East Midtown / Central Gardens / Cooper Young, Cordova, Zipcode 1, Lakeland / Arlington / Brunswick, Hollywood / Hyde Park / Nutbush, Windyke / Southwind, Cordova, Zipcode 2, East Memphis, North Memphis / Snowden /New Chicago, Midtown / Evergreen / Overton Square, Bartlett, Zipcode 3, South Riverdale, Germantown, Zipcode 1, Bartlett, Zipcode 1, Uptown / Pinch District, South Forum / Washington Heights, Oakland, Downtown / South Main Arts District / South Bluffs, Germantown, Zipcode 2, Rossville, Hickory Withe.

Final Equation for AHP [14]:

$$S_j = \sum_{i=1}^n w_i x_{ij}$$

- S_j is the final score for alternative j
- w_i is the weight of criterion i
- x_{ij} is the performance of alternative j in criterion i

3.3.2 Model Execution

To execute this model we utilized the python code listed in Appendix B to generate the raw data listed in Appendix A. We used the data provided in the MathWorks Math Modeling Challenge 2025, curated data to create the raw data [10]. To utilize the AHP model in the most effective way we utilized the dependencies pandas, numpy, os, and zscore. We ran models with multiple different weights for different factors (Including: Population, Median income, Mode of transport, and Age of House), but we settled on these values because we thought the APH scores more accurately represented the neighborhood's actual need in the event of a heatwave.

The method of finding the dispersion of the model is Interquartile Range (IQR) which measures the bottom and top quarter of the data (as Q1 and Q3) to find the spread in the middle of the data. In this instance the Q3 would need the most help during a heatwave and Q1 would need the least help in terms of funding. This is an important step because it could help a local legislature differentiate between who's well off and who's not with a very clear and concise metric to help allocate resources more effectively. $IQR=Q3-Q1$.

3.4 Results

Figure 7: AHP (vulnerability) scores and neighborhoods

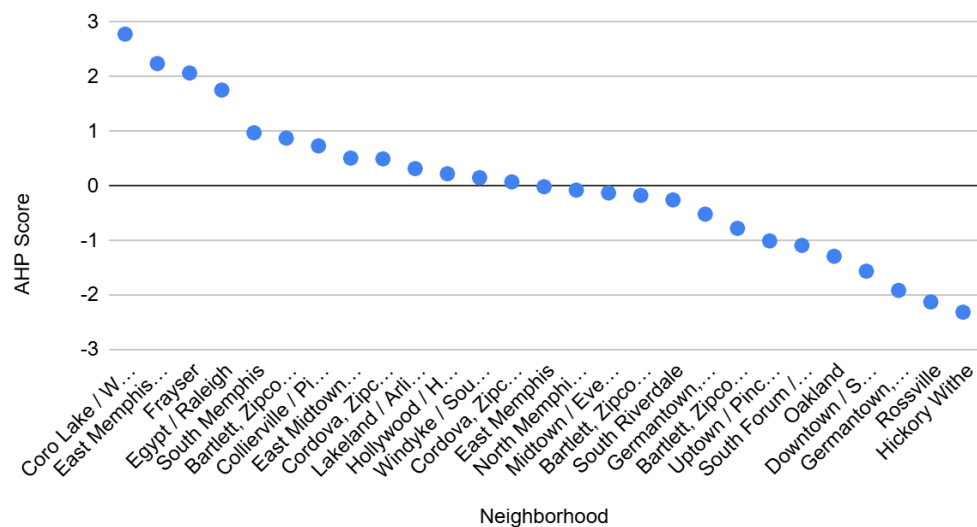
Neighborhood	AHP Score (Vulnerability Score)	Neighborhood Cont,	AHP Score Cont.
Coro Lake / White Haven	2.782739055	North Memphis / Snowden / New	-0.07527081364

		Chicago	
East Memphis – Colonial Yorkshire	2.242995109	Midtown / Evergreen / Overton Square	-0.1266843305
Frayser	2.070867369	Bartlett, Zipcode 3	-0.1721028342
Egypt / Raleigh	1.757415879	South Riverdale	-0.2544263029
South Memphis	0.9756716795	Germantown, Zipcode 1	-0.5155874691
Bartlett, Zipcode 2	0.8767937271	Bartlett, Zipcode 1	-0.7757207563
Collierville / Piperton	0.7355064008	Uptown / Pinch District	-1.005888846
East Midtown / Central Gardens / Cooper Young	0.511622048	South Forum / Washington Heights	-1.088127741
Cordova, Zipcode 1	0.4970329017	Oakland	-1.286871555
Lakeland / Arlington / Brunswick	0.3180753143	Downtown / South Main Arts District / South Bluffs	-1.56032771
Hollywood / Hyde Park / Nutbush	0.2245697538	Germantown, Zipcode 2	-1.912157699
Windyke / Southwind	0.1527953237	Rossville	-2.124292456
Cordova, Zipcode 2	0.0753290764	Hickory Withe	-2.310858494
East Memphis	-0.01309662882		

The table lists the AHP (neighborhood vulnerability score) of all the neighborhoods in Memphis, Tennessee.

Figure 8: AHP Score vs. Neighborhood

AHP Score vs. Neighborhood

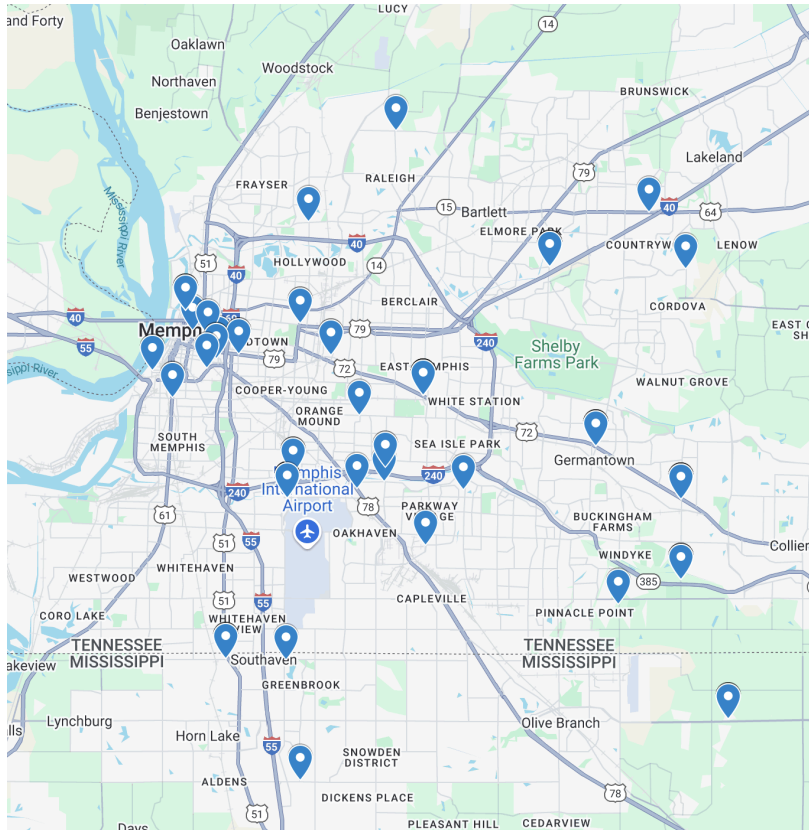


This figure shows the AHP scores in different neighborhoods, showing the distribution for the included neighborhoods

3.5 Discussion

This data suggests that Hickory Withe is the best off in the event where there is in the event of a heatwave in Memphis, Tennessee and Coro Lake / White Haven would need the most additional allocative funding. Based on our model, the city of Memphis should take action to address the differences in AHP scores and balance them. The AHP scores correlate with a neighborhood's vulnerability during a heat wave, with high scores representing a drastic need for intervention and low scores presenting an opportunity to scale back relief efforts. Specifically, city officials should direct large scale investment into heat wave-alleviation efforts, given their need and the city's surplus budget from power infrastructure. We propose that the city of Memphis facilitate citywide oases, locations where citizens can find shelter from the sun and get hydrated. This can be accomplished through partnerships and subsidy agreements with existing gas stations, like Shell and Marathon. Leveraging connections between these existing and well-established locations, the city can provide an effective number of easy to access oases. Given the gas stations' frequency and the large number of drivers in Memphis, subsidizing gas stations to hand out free and cheap beverages while allowing residents to enjoy the comfort of their air conditioning could prove an effective measure to combat the aggressive heat of the area. Additionally, giving gas stations tax breaks on AC bills would incentivize and allow more gas stations to help residents passing by.

Figure 9: Gas stations in the Memphis area



Gas stations in the Memphis, Tennessee area.

The dispersion analysis resulted in Q1 being -0.891 and Q3 being 0.624. This means that the IRQ is $IQR = Q3 - Q1 = 0.624 - (-0.891) = 1.51$. This means that the most well off neighborhoods are those with an AHP value (vulnerability score) of over -0.891 which indicates that Uptown / Pinch District and below (< -0.891) are in the top quarter of neighborhoods in terms of heat wave preparedness. And on the other hand, neighborhoods with an AHP of 0.624 or higher are in the bottom quarter of neighborhoods in preparedness; this indicates that Collierville / Piperton and above on Table 6 are not prepared.

3.6 Advantages and Disadvantages

This model has many advantages considering it's analytical and multivaried. The model incorporates multiple socio-economic and infrastructural factors (e.g., population demographics, housing conditions, transportation methods), allowing for a more holistic assessment of neighborhood vulnerability. By using the Analytic Hierarchy Process (AHP), the model provides a systematic and quantitative approach to determining vulnerability, reducing bias in decision-making. The model prioritizes neighborhoods with the highest vulnerability scores, ensuring that resources are directed where they are most needed during a heatwave or power grid failure.

This model isn't perfect either with some real-world inaccuracies. The weighting system may not capture nuances in how different factors interact or the varying degrees of vulnerability within neighborhoods. Plus, the

² Each pin represents a distinct gas station in Memphis which could potentially become an oasis

model assumes that all criteria are independent of each other, which may not fully reflect real-world interactions (e.g., income and housing quality are often correlated). Finally, Even with well-calculated vulnerability scores, practical constraints such as funding availability, political will, and logistical challenges could hinder the effective allocation of resources as recommended by the model.

If we had more time to work on this project we could find more data on more local neighborhoods to expand on the AHP values and find more neighborhoods in need and more funds that may not be necessary to allocate in the event of a heatwave

4 Conclusion

Our analysis provides a data-driven approach to understanding energy demand trends and heatwave vulnerability in Memphis. First, our results demonstrate the threatening interior temperatures created by abnormal high temperatures during a heat wave. The findings suggest that while overall energy consumption is decreasing due to technological advancements, peak summer demand remains high, requiring continued infrastructure preparedness. The vulnerability model highlights significant disparities in neighborhood resilience, emphasizing the need for equitable resource distribution to mitigate heat-related risks. Moving forward, policymakers should consider refining these models by incorporating additional variables such as climate projections, economic shifts, and evolving energy consumption behaviors to enhance long-term planning and decision-making.

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- [2] Energy.Gov. (2023). Insulation Materials. Energy.gov. <https://www.energy.gov/energysaver/insulation-materials>
- [3] <https://missingmiddlehousing.com/types/townhouse>
- [4] https://www.energy.gov/energysaver/passive-solar-homes?utm_source=chatgpt.com
- [5] <https://eyeonhousing.org/2023/05/new-single-family-home-size-trending-lower-3/>
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- [10] <https://mym3challenge.siam.org/>
- [11] https://en.wikipedia.org/wiki/List_of_tallest_buildings_in_Memphis?
- [12]: <https://worldpopulationreview.com>
- [13]: Gartner.com. (n.d.). *Definition of Analytical Hierarchy Process (AHP) - gartner information technology glossary*. Gartner. <https://www.gartner.com/en/information-technology/glossary/ahp-analytical-hierarchy-process>
- [14]: Saaty, T. L. (1980). *The analytic hierarchy process: Planning, priority setting, resource allocation*. McGraw-Hill.

[illegible]

Appendix B: AHP Python

```

import pandas as pd
import numpy as np
import os
from scipy.stats import zscore

# === CONFIGURATION ===
csv_file = "your_data.csv" # Ensure this file exists

columns = [
    "Neighborhood", "ZIP code", "Number of households", "Population",
    "Households with one or more people 65 years and over",
    "Households with one or more people under 18 years",
    "Population with Bachelor's degree or higher",
    "Median household income (in US dollars)",
    "Population age 16+ years old who work",
    "Primary mode of transportation to work (persons aged 16 years+): driving",
    "Primary mode of transportation to work (persons aged 16 years+): walking or public transit",
    "Primary mode of transportation to work (persons aged 16 years+): other and work from home",
    "Homes built 2010 or later", "Homes built 1990 to 2009", "Homes built 1970 to 1989",
    "Homes built 1950 to 1969", "Homes built 1950 or earlier", "Detached whole house",
    "Townhouse", "Apartments", "Mobile Homes/Other",
    "Maximum annual recorded temperature"
]

weights = {
    "Population": 0.40,
    "Households with one or more people 65 years and over": 0.30,
    "Households with one or more people under 18 years": 0.25,
    "Population with Bachelor's degree or higher": -0.15,
    "Median household income (in US dollars)": -0.40,
    "Primary mode of transportation to work (persons aged 16 years+): driving": -0.15,
    "Primary mode of transportation to work (persons aged 16 years+): walking or public transit": 0.10,
    "Homes built 2010 or later": -0.05,
    "Homes built 1970 to 1989": 0.10,
    "Homes built 1950 to 1969": 0.15,
    "Homes built 1950 or earlier": 0.20,
    "Detached whole house": 0.25,
} # Adjust weights based on importance

# === STEP 1: VERIFY CSV FILE EXISTS ===
if not os.path.exists(csv_file):
    print(f"Error: File not found at {os.path.abspath(csv_file)}")
    exit()

# === STEP 2: LOAD DATA ===
df = pd.read_csv(csv_file)

# === STEP 3: CLEAN COLUMN NAMES ===
df.columns = df.columns.str.strip()
df.columns = df.columns.str.replace("\\s+", " ", regex=True)

# === STEP 4: CHECK MISSING COLUMNS ===
missing_cols = [col for col in weights.keys() if col not in df.columns]
if missing_cols:
    print(f"Error: These columns are missing from the dataset: {missing_cols}")
    exit()

# === STEP 5: NORMALIZE DATA (ONLY NUMERICAL COLUMNS) ===
numerical_columns = list(weights.keys())
df[numerical_columns] = df[numerical_columns].apply(zscore)

# === STEP 6: APPLY WEIGHTS & COMPUTE SCORES ===
df["AHP Score"] = df[numerical_columns].mul(weights.values(), axis=1).sum(axis=1)

# === STEP 7: RANK NEIGHBORHOODS ===
df = df.sort_values(by="AHP Score", ascending=False)

# === STEP 8: OUTPUT RESULTS ===
output_file = "ranked_neighborhoods.csv"
df.to_csv(output_file, index=False)
print(f"Ranking complete! Results saved in {output_file}")

```

Appendix C

Q1: Power Hungry

Script to code for the triple exponential smoothing equation in google co-lab

```

import numpy as np
import pandas as pd

```

```
from statsmodels.tsa.holtwinters import ExponentialSmoothing
from statsmodels.tsa.stattools import adfuller

def load_dataset():
    data = [
        608410498.4, 547209444.3, 582730053.8, 662171421.7, 751932974.9, 746892885.5,
        669371546.2,
        595690279.3, 531609170.8, 550809502.7, 607210473.9, 690011909, 604644382.1,
        543822168,
        579122901.7, 658072520.4, 747278441.3, 742269550.6, 665228075.4, 592002902.2,
        528318461.6,
        547399941.7, 603451785.8, 685740672.5, 594136434.9, 534371233.3, 569058485.3,
        646636060.4,
        734291696.4, 729369853.8, 653667261.1, 581714647.9, 519136961.5, 537886829.9,
        592964564.5,
        673823375.4, 591953222.8, 532407634.2, 566967424.5, 644259933.3, 731593470.2,
        726689713.3,
        651265297.1, 579577080.8, 517229342.3, 535910312.4, 590785658.5, 671347345.9,
        586765962.8,
        527742169.6, 561999114, 638614311.9, 725182548.9, 720321763.4, 645558288,
        574498272.4,
        512696884.4, 531214154, 585608629.8, 665464358.7, 569940824.2, 512609500.5,
        545884148.9,
        620302455.1, 704388403.2, 699666997.6, 627047317.1, 558024902, 497995629.2,
        515981927.9,
        568816677, 646382593.9, 594712778.6, 534889601.5, 569610502, 647263331.5,
        735003998.1,
        730077381, 654301352.8, 582278941.8, 519640551.8, 538408608.5, 593539771.4,
        674477019.6,
        571947963.2, 514414737.9, 547806568.4, 622486950.7, 706869021.1, 702130988.4,
        629255565.9,
        559990077.1, 499749401.5, 517799041.9, 570819857.1, 648658935, 533416309.2,
        479759049,
        510901299.9, 580550527.6, 659247848.7, 654829013.3, 586863146.8, 522264015.9,
        466081704,
        482915355.3, 532364202.7, 599530693.5, 538816255.7, 484615805.6, 516073319.7,
        586427629.1,
```



```
665921628.8, 661458060, 592804153, 527551064.1, 470800000.4, 487804064.3,
537753498.4,
611083527, 536254849, 482312053.5, 513620028.9, 583639892.8, 662755992.8,
658313644.9,
589986104, 525043209.1, 468561929.2, 485485159.1, 535197147.1, 608178576.2
]
return np.array(data)
def check_stationarity(data):
result = adfuller(data)
print("ADF Statistic:", result[0])
print("p-value:", result[1])
if result[1] > 0.05:
print("Data is likely non-stationary.")
else:
print("Data is likely stationary.")

def triple_exponential_smoothing(data, season_length, forecast_periods):
model = ExponentialSmoothing(
data,
trend='add',
seasonal='mul',
seasonal_periods=season_length
)
fit = model.fit(optimized=True)
level = fit.level
trend = fit.trend
seasonal = fit.season
print("\nEquation for Triple Exponential Smoothing:")
print(f"y_t = ({level[-1]:.4f}) + t * {trend[-1]:.4f}) * S_{season_length}(t)")
forecast = fit.forecast(forecast_periods)
return fit.fittedvalues, forecast

def main():
season_length = 12
forecast_periods = 120
data = load_dataset()
check_stationarity(data)
```

```
fitted_values, forecast = triple_exponential_smoothing(data, season_length,
forecast_periods)
print("\nFitted Values (Original Scale):")
print(fitted_values)
print("\nForecast (Original Scale):")
print(forecast)
if __name__ == "__main__":
    main()
```

Appendix D

Q2: Power Hungry

Script to code for seasonal factors in google co-lab

```
import pandas as pd
import numpy as np
from statsmodels.tsa.seasonal import seasonal_decompose

dates = pd.date_range(start="2012-01", periods=132, freq='ME')
values = [
608410498.4, 547209444.3, 582730053.8, 662171421.7, 751932974.9, 746892885.5,
669371546.2, 595690279.3, 531609170.8, 550809502.7, 607210473.9, 690011909,
604644382.1, 543822168, 579122901.7, 658072520.4, 747278441.3, 742269550.6,
665228075.4, 592002902.2, 528318461.6, 547399941.7, 603451785.8, 685740672.5,
594136434.9, 534371233.3, 569058485.3, 646636060.4, 734291696.4, 729369853.8,
653667261.1, 581714647.9, 519136961.5, 537886829.9, 592964564.5, 673823375.4,
591953222.8, 532407634.2, 566967424.5, 644259933.3, 731593470.2, 726689713.3,
651265297.1, 579577080.8, 517229342.3, 535910312.4, 590785658.5, 671347345.9,
586765962.8, 527742169.6, 561999114, 638614311.9, 725182548.9, 720321763.4,
645558288, 574498272.4, 512696884.4, 531214154, 585608629.8, 665464358.7,
569940824.2, 512609500.5, 545884148.9, 620302455.1, 704388403.2, 699666997.6,
627047317.1, 558024902, 497995629.2, 515981927.9, 568816677, 646382593.9,
594712778.6, 534889601.5, 569610502, 647263331.5, 735003998.1, 730077381,
654301352.8, 582278941.8, 519640551.8, 538408608.5, 593539771.4, 674477019.6,
571947963.2, 514414737.9, 547806568.4, 622486950.7, 706869021.1, 702130988.4,
629255565.9, 559990077.1, 499749401.5, 517799041.9, 570819857.1, 648658935,
533416309.2, 479759049, 510901299.9, 580550527.6, 659247848.7, 654829013.3,
586863146.8, 522264015.9, 466081704, 482915355.3, 532364202.7, 599530693.5,
538816255.7, 484615805.6, 516073319.7, 586427629.1, 665921628.8, 661458060,
592804153, 527551064.1, 470800000.4, 487804064.3, 537753498.4, 611083527,
```

```

536254849, 482312053.5, 513620028.9, 583639892.8, 662755992.8, 658313644.9,
589986104, 525043209.1, 468561929.2, 485485159.1, 535197147.1, 608178576.2
]

assert len(dates) == len(values),
df = pd.DataFrame({"Date": dates, "Value": values}).set_index("Date")

decomposition = seasonal_decompose(df["Value"], model="additive", period=12)
seasonal_values = decomposition.seasonal[:12]

seasonal_values_rounded = [f"{val:.10g}" for val in seasonal_values]

seasonality_dict = dict(zip(dates[:12].strftime("%b"),
seasonal_values_rounded))
print(seasonality_dict)

```

Appendix E - data for monthly Energy use in memphis and calculations

	A	B	C	D	E	F	G	H
46	year	E use year shelyby	month to total ratio	E use month shelyby	month	Population	E use/capita shelyby	Month E use memphis
47		2022.00	0.091464361	83451181.9	Jan		974.9576406	608178576.2
48			0.080488658	786237040.1	feb	shelby2022	857.9627238	535197147.1
49			0.072012439	713207117.4	march	916400.00	778.270534	485485159.1
50			0.070467343	688345867.1	april		751.1412779	468561929.2
51			0.070861901	71320268.6	may	memphis 2022	841.6551701	525043209.1
52			0.068728406	866725337.8	june	623800	945.7936903	589986104
53			0.090004231	967102635.8	july		1055.328062	658313644.9
54			0.098672119	973628714	august		1062.449492	662755992.8
55			0.087773895	857402369	september		935.6202193	583639892.8
56			0.077343661	754538945.9	october		823.3729222	513620028.9
57			0.072536234	708545632.9	november		773.1837985	482312053.5
58			0.080647727	787790868.2	december		859.6583023	536254849
59			0.091464361	896385272.1	Jan		970.7422843	611083527
60		2021	0.080488658	788819031.6	feb	shelby21	854.2548617	537753498.4
61			0.072012439	715549281.9	march	923400.00	774.9071712	487804064.3
62			0.070467343	690606386.7	april		747.8951556	470800000.4
63			0.070861901	738553300.4	may	memphis 21	838.0477587	527551064.1
64			0.068728406	869571652	june	629500	941.7065891	592804153
65			0.090004231	970278590.4	july		1050.767371	661458060
66			0.098672119	976826103.3	august		1057.858028	665921628.8
67			0.087773895	860218066.2	september		931.5786532	586427629.1
68			0.077343661	757018944.2	october		819.8146461	516073319.7
69			0.072536234	710872493.9	november		769.8424236	484615805.6
70			0.080647727	790377967.5	december		855.943218	538816255.7
71			0.091464361	804670824.8	Jan		952.391888	599530693.5
72		2020	0.080488658	778515598	feb	shelby20	838.1048531	532384202.7
73			0.072012439	706202886.5	march	920800.00	760.2571714	482913555.3
74			0.070467343	681585791.6	april		733.7558312	466081704
75			0.070861901	763745346.9	may	memphis 20	822.2040552	522264015.9
76			0.068728406	852213440	june	635200	923.9029389	586863146.8
77			0.090004231	957604959.8	july		1030.902099	654829013.3
78			0.098672119	964066950.1	august		1037.858704	659247848.7
79			0.087773895	849820209.4	september		913.9648363	580550527.6
80			0.077343661	747128805.9	october		804.3156485	510901299.9
81			0.072536234	701587186.1	november		755.2881753	479759049
82			0.080647727	780054171.3	december		839.7611921	533416309.2
83		2019	0.091464361	933730089.1	Jan		996.403894	648658935
84			0.080488658	821682470.2	feb	shelby19	876.835418	570819857.1
85			0.072012439	745360187.7	march	937100	786.9802334	517799041.9
86			0.070467343	719378132.3	april		767.8642112	499748401.5
87			0.070861901	806093243.1	may	memphis 19	860.1988113	559990077.1
88			0.068728406	805798371.4	june	651000	966.984115	629255565.9
89			0.090004231	1010701919	july		1078.542225	702130968.4
90			0.098672119	1017522211	august		1085.820309	706869021.1
91			0.087773895	896056100.6	september		956.2011532	622486950.7
92			0.077343661	78855353.7	october		841.4847441	547806588.4
93			0.072536234	740488557.4	november		790.1916097	514414737.9
94			0.080647727	823306353.8	december		878.568298	571947963.2
95		2018	0.091464361	969955290.5	Jan		1034.950161	674477019.6
96			0.080488658	855560647.1	feb	shelby18	910.7561322	593539771.4
97			0.072012439	774217346.3	march	937200.00	826.1602094	538408688.6
98			0.070467343	747287287.3	april		797.3615955	519640551.8

	A	B	C	D	E	F	G	H
100			0.080728406	10409096.4 june		651700	1003.991842	654301352.8
101			0.08004231	1049913337 july			1120.266044	730077381
102			0.080672319	1056998231 august			1127.825684	735003998.1
103			0.08773995	930819693.5 september			993.1921613	647263331.5
104			0.077243661	819148323.6 october			874.037954	569610502
105			0.072535234	769516717.1 november			820.760475	534889601.5
106			0.080647727	855247531.2 december			912.5560513	594712778.6
107		2017	0.091464385	928790463.5 jan	shelby17		992.2975037	648382593.9
108		10154668000.00	0.080486958	817335599.8 feb		986000.00	873.2217946	568616677
109			0.073012439	741417077.9 march			792.1122627	515081927.9
110			0.070467343	715572473 april	memphis 17		764.5005053	497995629.2
111			0.07891601	801828842.9 may		651400	856.6547467	558024902
112			0.080728406	901007505.1 june			962.6146559	627047517.1
113			0.08004231	1005355096 july			1074.097325	699666997.6
114			0.08672319	1012139308 august			1081.345415	704388403.2
115			0.08773995	891315778.3 september			952.2604469	620302455.1
116			0.077243661	764363732.6 october			838.0168083	545884148.9
117			0.072535234	736571219.6 november			786.9350636	512609500.5
118			0.080647727	818950892.6 december			874.9475349	569940824.2
119		2016	0.091464385	954579678.6 jan	shelby16		1019.087839	665464358.7
120		10436620000.00	0.080486958	84003020.9 feb		936700.00	896.7972892	585608629.8
121			0.073012439	762003519.2 march			813.4979387	531214154
122			0.070467343	735441304.1 april			785.1407111	512696884.4
123			0.07891601	824092698 may	memphis 16		879.7829593	574498272.4
124			0.080728406	926025189 june		653000	968.6038102	645553288
125			0.08004231	1033270131 july			1103.096115	720321763.4
126			0.08672319	1040242716 august			1110.539891	725182548.9
127			0.08773995	916054358.3 september			977.9686498	638614311.9
128			0.077243661	806163200.7 october			860.6418285	561899114
129			0.072535234	757023109.1 november			808.1809641	527742169.6
130			0.080647727	841690164.4 december			898.5696215	586765962.8
131		2015	0.091464385	961734953 jan	shelby15		1025.740788	671347345.9
132		10514893000.00	0.080486958	846326407 feb		937600.00	902.6518846	590789558.5
133			0.073012439	767715063.3 march			818.8087279	535910312.4
134			0.070467343	740955752.9 april			790.2663747	517229342.3
135			0.07891601	830209627.2 may	memphis 15		885.524795	579577080.8
136			0.080728406	932965146 june		654500	955.6577496	651265297.1
137			0.08004231	1041014935 july			1110.297499	726689713.3
138			0.08672319	1048039782 august			1117.78987	731593470.2
139			0.08773995	92230554.8 september			984.3543672	644259933.3
140			0.077243661	812205740.6 october			866.2603889	56967424.5
141			0.072535234	762697322.8 november			813.4570423	532407634.2
142			0.080647727	84799894.2 december			904.4357873	591953222.8
143		2014	0.091464385	964411534.1 jan			1028.267016	673823375.4
144		10541220000.00	0.080486958	846862229.6 feb	shelby14		904.8749649	502964564.5
145			0.073012439	769852064.3 march		937900.00	820.8253165	537886829.9
146			0.070467343	743016261.6 april			792.2126983	519136961.5
147			0.07891601	832680754.3 may	memphis 14		887.7073827	581714647.9
148			0.080728406	935563137.7 june		655300	997.50841	653667261.1
149			0.08004231	1043912690 july			1113.031976	729369853.8
150			0.08672319	1050957092 august			1120.542799	734291696.4
151			0.08773995	925499711.7 september			986.7766669	646363060.4
152			0.077243661	814466585.3 october			868.333543	569055485.3

	A	B	C	D	E	F	G	H
153			0.072535234	764820356.6 november			815.4604506	534371233.3
154			0.080647727	850359472.5 december			906.663261	594136434.9
155		2013	0.091464385	979167583.3 jan			1043.110241	685740672.5
156		10705452000.00	0.080486958	861667464.8 feb	shelby13		917.9370031	603451785.8
157			0.073012439	781631161.1 march		938700.00	832.6740824	547399941.7
158			0.070467343	754384758.1 april			803.6484053	528318461.6
159			0.07891601	845319629.3 may	memphis 13		900.5216037	592002902.2
160			0.088728406	949877691.5 june		657400	1011.907629	665228075.4
161			0.099004231	1059885043 july			1129.098799	742269550.6
162			0.099672319	1067037227 august			1136.718043	747278441.3
163			0.08773995	939660290.3 september			1001.023	658072520.4
164			0.077243661	826928305.1 october			880.9292694	579122901.7
165			0.072535234	776522465.9 november			827.2317736	543822168
166			0.080647727	863370370.3 december			919.751136	60464382.1
167		2012	0.091464385	983607264.6 jan	shelby12		1047.059043	690011909
168		10753992000.00	0.080486958	865574384.2 feb			921.4119483	607210473.9
169			0.073012439	785175184.9 march		939400	835.826256	550809502.7
170			0.070467343	757805242.9 april			806.6906993	531609170.8
171			0.07891601	849152425.5 may	memphis 12		903.9306211	595690279.3
172			0.088728406	954184568.3 june		659000	1015.73831	669371546.2
173			0.099004231	1064690708 july			1133.373119	746892885.5
174			0.099672319	1071875321 august			1141.021206	751932974.9
175			0.08773995	943920840 september			1004.812476	662171421.7
176			0.077243661	830677712.4 october			884.264118	582730053.8
177			0.072535234	780043326.2 november			830.3633449	547209444.3
178			0.080647727	867285011 december			923.2329263	608410498.4

Appendix F - calculations for ratio of month per year

32	energy consumption SEUs a	total per year	Month	consumption per month	ratio of month per year
33	28750000000.00	314330000000.00	January	28750000000.00	0.091464385
34	25300000000.00		February	25300000000.00	0.080488658
35	22950000000.00		March	22950000000.00	0.073012439
36	22150000000.00		April	22150000000.00	0.070467343
37	24820000000.00		May	24820000000.00	0.07891601
38	27890000000.00		June	27890000000.00	0.088728406
39	31120000000.00		July	31120000000.00	0.099004231
40	31330000000.00		August	31330000000.00	0.099672319
41	27590000000.00		September	27590000000.00	0.08773995
42	24280000000.00		October	24280000000.00	0.077243661
43	22800000000.00		November	22800000000.00	0.072535234
44	25350000000.00		December	25350000000.00	0.080647727

Appendix G - calculations for per month capita in shelby county

	South East USA			
Month	Consumption (kWh)			
January	28750000000.00			
February	25300000000.00			
March	22950000000.00			
April	22150000000.00			
May	24820000000.00			
June	27890000000.00			
July	31120000000.00			
August	31330000000.00			
September	27590000000.00			
October	24280000000.00			
November	22800000000.00			
December	25350000000.00			
	Consumption shelby county			
	(kWh)	average per month	average per month per capita	population of shelby
2022.00	9768296000.00	814024666.7	888.2853194	916400.00
2021.00	9800375000.00	816697916.7	884.4465201	923400.00
2020.00	9672364000.00	806030333.3	867.7256253	928900.00
2019.00	10208674000.00	850722833.3	907.8250276	937100.00
2018.00	10604732000.00	883727666.7	942.9445867	937200.00
2017.00	10154668000.00	846222333.3	904.0836895	936000.00
2016.00	10436626000.00	869718833.3	928.4924024	936700.00
2015.00	10514853000.00	876237750	934.5539142	937600.00
2014.00	10544122000.00	878676833.3	936.8555638	937900.00
2013.00	10705452000.00	892121000	950.3792479	938700.00
2012.00	10753992000.00	896166000	953.9770066	939400.00