



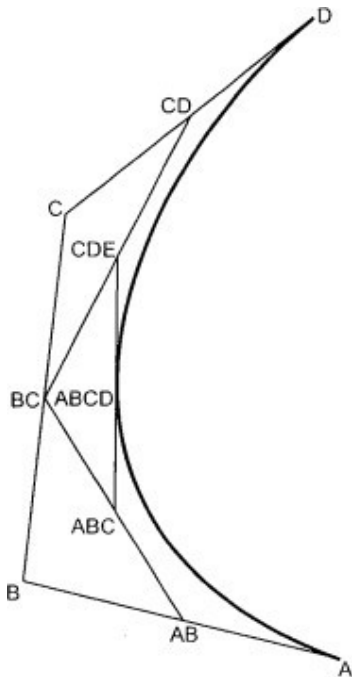
Aim: To implement Bezier curve for n control points. (Midpoint approach)

Objective:

Draw a Bezier curves and surfaces written in Bernstein basis form. The goal of interpolation is to create a smooth curve that passes through an ordered group of points. When used in this fashion, these points are called the control points.

Theory:

In midpoint approach Bezier curve can be constructed simply by taking the midpoints. In this approach midpoints of the line connecting four control points (A, B, C, D) are determined (AB, BC, CD, DA). These midpoints are connected by line segment and their midpoints are ABC and BCD are determined. Finally, these midpoints are connected by line segments and its midpoint ABCD is determined as shown in the figure –



The point ABCD on the Bezier curve divides the original curve in two sections. The original curve gets divided in four different curves. This process can be repeated to split the curve into smaller sections until we have sections so short that they can be replaced by straight lines.

Algorithm:



1) Get four control points say A(xa, ya), B(xb, yb), C(xc, yc), D(xd, yd).

2) Divide the curve represented by points A, B, C, and D in two sections.

$$x_{ab} = (x_a + x_b) / 2$$

$$y_{ab} = (y_a + y_b) / 2$$

$$x_{bc} = (x_b + x_c) / 2$$

$$y_{bc} = (y_b + y_c) / 2$$

$$x_{cd} = (x_c + x_d) / 2$$

$$y_{cd} = (y_c + y_d) / 2$$

$$x_{abc} = (x_{ab} + x_{bc}) / 2$$

$$y_{abc} = (y_{ab} + y_{bc}) / 2$$

$$x_{bcd} = (x_{bc} + x_{cd}) / 2$$

$$y_{bcd} = (y_{bc} + y_{cd}) / 2$$

$$x_{abcd} = (x_{abc} + x_{bcd}) / 2$$

$$y_{abcd} = (y_{abc} + y_{bcd}) / 2$$

3) Repeat the step 2 for section A, AB, ABC, ABCD and section ABCD, BCD, CD, D.

4) Repeat step 3 until we have sections so that they can be replaced by straight lines.

5) Repeat small sections by straight lines.

6) Stop.

Program:

```
#include<graphics.h>
```

```
#include<math.h>
```

```
#include<conio.h>
```

```
#include<stdio.h>
```

```
void main()
```

```
{
```

```
int x[4],y[4],i,n;
```



```
double put_x,put_y,t;
int gr=DETECT,gm;
initgraph(&gr,&gm,"C:\\TURBOC3\\BGI");
printf("\n Please enter x and y coordinates ");
for(i=0;i<4;i++)
{
scanf("%d%d",&x[i],&y[i]);
putpixel(x[i],y[i],3);
}
for(t=0.0;t<=1.0;t=t+0.001)
{
put_x = pow(1-t,3)*x[0] + 3*t*pow(1-t,2)*x[1] + 3*t*t*(1-t)*x[2] + pow(t,3)*x[3];
put_y = pow(1-t,3)*y[0] + 3*t*pow(1-t,2)*y[1] + 3*t*t*(1-t)*y[2] + pow(t,3)*y[3];
putpixel(put_x,put_y, WHITE);
}
getch();
closegraph();
}
```

Output:





Conclusion – Comment on

1. **Difference from arc and line:**
In graphics, a line can be described as a single point that continues for a distance, or as the connection between two points. While, the arc is defined as the smooth curve formed by joining two or more points.
2. **Importance of control point:**
In computer-aided geometric design a control point is a member of a set of points used to determine the shape of a spline curve or, more generally, a surface or higher-dimensional object. are nonnegative and sum to one. This property implies that the curve lies within the convex hull of its control points.
3. **Applications:**
Bezier curves have a lot of applications in the areas of science, engineering, and technology such as: railway route or highway modeling, networks, animation, computer-aided design system, robotics, environment design, communications, and many other fields due to their computational simplicity and stability