#### Содержание Strategy.txt Проверить руками сэмплы Подумать как дебагать после написания $flows/dinic.cpp \dots \dots \dots \dots \dots \dots \dots$ Выписать сложные формулы и все +-1 Проверить имена файлов Прогнать сэмплы Переполнения int, переполнения long long Выход за границу массива: \_GLIBCXX\_DEBUG Переполнения по модулю: в псевдо-онлайн-генераторе, в функциях-обертках Проверить мультитест на разных тестах Прогнать минимальный по каждому параметру тест Прогнать псевдо-максимальный тест (немного чисел, geometry/halfplanes.cpp ....... но очень большие или очень маленькие) Представить что не зайдет и заранее написать assert'ы, прогнать слегка модифицированные тесты cout.precision: в том числе в интерактивных задачах Удалить debug-output, отсечения для тестов, вернуть оригинальный тахп, удалить \_GLIBCXX\_DEBUG Вердикт может врать Если много тестов (>3), дописать в конец каждого теста ответ, чтобы не забыть (WA) Потестить не только ответ, но и содержимое значимых массивов, переменных (WA) Изменить тест так, чтобы ответ не менялся: поменять координаты местами, сжать/растянуть координаты, поменять ROOT дерева (WA) Подвигать размер блока в корневой или битсете (WA) Поставить assert'ы, возможно написать чекер c assert'om (WA) Проверить, что программа не печатает что-либо неожиданное, что должно попадать под PE: inf - 2, не лекс. мин. решение, одинаковые числа вместо разных, неправильное количество чисел, пустой ответ, перечитать output format (TL) cin -> scanf -> getchar (TL) Упихать в кэш большие массивы, поменять местами for'ы или измерения массива (RE) Проверить формулы на деление на 0, выход за область определения(sqrt(-eps), acos(1 + eps)) (WA) Проверить, что ответ влезает в int 29 structures/convex hull trick.cpp . . . . . . . . . . . . . . 18 $30\ structures/heavy\_light.cpp\dots\dots\dots\dots 19$

#### 2 flows/dinic.cpp

```
1namespace Dinic {
2const int maxn = 10010;
 4struct Edge {
        int to, c, f;
 6 } es[maxn*2];
 7 int ne = 0:
 9 int n;
10 vector<int> e[maxn];
11 int q[maxn], d[maxn], pos[maxn];
12 int S, T;
14 void addEdge(int u, int v, int c) {
        assert(c <= 1000000000);
es[ne] = {v, c, 0};
15
16
        e[u].push_back(ne++);
17
18
        es[ne] = \{u, 0, 0\};
19
        e[v].push_back(ne++);
20}
21
22bool bfs() {
        forn(i, n) d[i] = maxn;
d[S] = 0, q[0] = S;
23
24
        int lq = 0, rq = 1;
while (lq != rq) {
25
26
27
              int v = q[1q++];
              for (int id: e[v]) if (es[id].f < es[id].c) {
   int to = es[id].to;</pre>
28
29
30
                   if (d[to] == maxn)
31
                         d[to] = d[v] + 1, q[rq++] = to;
32
33
34
        return d[T] != maxn;
35 }
37int dfs(int v, int curf) {
38    if (v == T || curf == 0) return curf;
        for (int &i = pos[v]; i < (int)e[v].size(); ++i) {</pre>
              int id = e[v][i];
int to = es[id].to;
42
              if (es[id].f < es[id].c \&\& d[v] + 1 == d[to]) {
                    if (int ret = dfs(to, min(curf, es[id].c-es[id].f)))
44
                         es[id].f += ret;
es[id^1].f -= ret;
45
46
47
                         return ret:
48
49
             }
50
        return 0;
51
52}
53
54i64 dinic(int S, int T) {
        Dinic::S = S, Dinic::T = T; i64 res = 0;
55
56
        while (bfs()) {
57
             forn(i, n) pos[i] = 0;
while (int f = dfs(S, 1e9)) {
   assert(f <= 1000000000);</pre>
58
59
60
61
                   res += f:
62
63
64
        return res;
65 }
     // namespace Dinic
67}
68
69 void test() {
        Dinic::n = 4;
70
        Dinic::addEdge(0, 1, 1);
71
72
        Dinic::addEdge(0, 2, 2);
73
        Dinic::addEdge(2, 1, 1);
        Dinic::addEdge(1, 3, 2);
Dinic::addEdge(2, 3, 1);
74
75
76
        cout << Dinic::dinic(0, 3) << endl; // 3</pre>
77
78}
79
81\,\mathit{LR}-поток находит не максимальный поток.
82 Добавим новый сток S' и исток T'. Заменим ребро (u, v, l, r) 83 LR-сети на ребра (u, T', l), (S', v, l), (u, v, r - l). 84 Добавим ребро (T, S, k). Ставим значение k=inf, пускаем поток. 85 Проверяем, что все ребра из S' насыщены (иначе ответ не
86 существует). Бинпоиском находим наименьшее к, что величина
87 потока не изменится. Это k - величина МИНИМАЛЬНОГО потока,
88 удовлетворяющего ограничениям. */
```

# 3 flows/globalcut.cpp

```
1 #include <bits/stdc++.h>
 2using namespace std;
 3 \# define \ forn(i,n) \ for \ (int \ i = 0; \ i < int(n); ++i) 4 const int inf = 1e9 + 1e5; 5 \# define \ all(x) \ (x).begin(), \ (x).end()
 7const int maxn = 505;
 8namespace StoerWagner {
 9int g[maxn] [maxn];
10 int dist[maxn];
11bool used[maxn];
12 int n;
13
14void addEdge(int u, int v, int c) {
15    g[u][v] += c;
       g[v][u] += c;
17}
19 int run() {
       vector<int> vertices;
20
21
       forn (i, n)
           vertices.push_back(i);
        int mincut = inf;
        while (vertices.size() > 1) {
25
            int u = vertices[0];
            for (auto v: vertices) {
   used[v] = false;
   dist[v] = g[u][v];
26
27
28
29
30
            used[u] = true;
            forn (ii, vertices.size() - 2) {
31
                 for (auto v: vertices)
32
33
                      if (!used[v])
                           if (used[u] || dist[v] > dist[u])
34
35
                                u = v;
36
                 used[u] = true;
                 for (auto v: vertices)
  if (!used[v])
37
38
39
                           dist[v] += g[u][v];
40
            int t = -1;
41
            for (auto v: vertices)
42
                 if (!used[v])
43
            t = v;
assert(t != -1);
45
            mincut = min(mincut, dist[t]);
46
47
            vertices.erase(find(all(vertices), t));
48
            for (auto v: vertices)
                 addEdge(u, v, g[v][t]);
49
50
51
       return mincut;
52}
53} // namespace StoerWagner
55 int main() {
56
       StoerWagner::n = 4;
57
       StoerWagner::addEdge(0, 1, 5);
       StoerWagner::addEdge(2, 3, 5);
       StoerWagner::addEdge(1, 2, 4);
cerr << StoerWagner::run() << '\n'; // 4</pre>
60
```

## 4 flows/hungary.cpp

```
1// left half is the smaller one
 2namespace Hungary {
3const int maxn = 505;
 4int a[maxn][maxn];
 5int p[2][maxn];
 6int match[maxn];
 7bool used[maxn];
 8int from[maxn];
 9int mind[maxn];
10 int n, m;
11
12 int hungary(int v) {
13  used[v] = true;
       int u = match[v];
       int best = -1;
forn (i, m + 1) {
15
17
           if (used[i])
                continue
           int nw = a[u][i] - p[0][u] - p[1][i];
if (nw <= mind[i]) {</pre>
21
                mind[i] = nw;
                from[i] = v;
23
24
            if (best == -1 || mind[best] > mind[i])
25
                best = i;
26
27
       v = best;
       int delta = mind[best];
28
29
       forn (i, m + 1) \{
           if (used[i]) {
	p[1][i] -= delta;
30
31
32
                p[0][match[i]] += delta;
33
           } else
34
                mind[i] -= delta;
35
       if (match[v] == -1)
36
37
           return v:
38
       return hungary(v);
39 }
40
41 void check() {
       int edges = 0, res = 0;
42
43
       forn (i, m)
           if (match[i] != -1) {
44
45
                ++edges;
                assert(p[0][match[i]] + p[1][i] == a[match[i]][i]);
46
47
                res += a[match[i]][i];
48
           } else
       assert(p[1][i] == 0);
assert(res == -p[1][m]);
49
50
       forn (i, n) forn (j, m)
51
            assert(p[0][i] + p[1][j] <= a[i][j]);
52
53}
54
55 int run() {
       forn (i, n)
56
57
          p[0][i] = 0;
       forn (i, m + 1) {
   p[1][i] = 0;
58
59
60
           match[i] = -1;
61
62
       forn (i, n) {
63
           match[m] = i;
64
            fill(used, used + m + 1, false);
            fill(mind, mind + m + 1, inf);
65
66
            fill(from, from + m + 1, -1);
67
            int v = hungary(m);
            while (v != m) {
    int w = from[v];
68
70
                match[v] = match[w];
71
72
           }
73
74
       check();
75
       return -p[1][m];
    // namespace Hungary
```

# flows/mincost.cpp

```
1namespace MinCost {
2const ll infc = 1e12;
 4struct Edge {
 5
       int to;
 6
       ll c, f, cost;
 8
       Edge(int to, 11 c, 11 cost): to(to), c(c), f(0), cost(cost)
10};
11
12 int N, S, T;
13 int totalFlow;
1411 totalCost;
15 const int maxn = 505;
16 vector < Edge > edge;
17 vector<int> g[maxn];
19 void addEdge(int u, int v, ll c, ll cost) {
       g[u].push_back(edge.size());
20
       edge.emplace_back(v, c, cost);
22
       g[v].push_back(edge.size());
       edge.emplace_back(u, 0, -cost);
24}
25
2611 dist[maxn];
27int fromEdge[maxn];
29bool inQueue[maxn];
30bool fordBellman() {
      forn (i, N)
           dist[i] = infc;
32
       dist[S] = 0;
inQueue[S] = true;
33
       vector<int> q;
35
36
       q.push_back(S);
       for (int ii = 0; ii < int(q.size()); ++ii) {</pre>
37
           int u = q[ii];
38
           inQueue[u] = false;
39
           for (int e: g[u]) {
    if (edge[e].f == edge[e].c)
40
41
42
                    continue:
                int v = edge[e].to;
43
                ll nw = edge[e].cost + dist[u];
if (nw >= dist[v])
44
45
                     continue:
46
                dist[v] = nw;
47
                fromEdge[v] = e;
48
                if (!inQueue[v]) {
49
50
                     inQueue[v] = true;
                     q.push_back(v);
51
                }
52
           }
53
54
       return dist[T] != infc;
55
56 }
57
5811 pot[maxn];
59bool dikstra() {
       typedef pair<11, int> Pair;
61
       priority_queue<Pair, vector<Pair>, greater<Pair>> q;
62
       forn (i, N)
63
           dist[i] = infc;
       dist[S] = 0;
65
       q.emplace(dist[S], S);
66
       while (!q.empty()) {
           int u = q.top().second;
11 cdist = q.top().first;
67
68
           q.pop();
69
70
           if (cdist != dist[u])
71
                continue;
           for (int e: g[u]) {
   int v = edge[e].to;
72
73
                if (edge[e].c == edge[e].f)
75
                    continue;
                11 w = edge[e].cost + pot[u] - pot[v];
                assert(w >= 0);
ll ndist = w + dist[u];
77
                if (ndist >= dist[v])
79
                     continue;
                dist[v] = ndist;
                fromEdge[v] = e;
                q.emplace(dist[v], v);
           }
       if (dist[T] == infc)
86
87
           return false;
       forn (i, N) \{
           if (dist[i] == infc)
                continue;
           pot[i] += dist[i];
```

#### 93 return true; 94} 95 96bool push() { //2 variants 97 //if (!fordBellman()) 99 if (!dikstra()) 100 return false; 101 ++totalFlow; 102 int u = T; while (u != S) { 103 int e = fromEdge[u]; 104 105 totalCost += edge[e].cost; edge[e].f++; edge[e ^ 1].f--; 106 107 u = edge[e ^ 1].to; 108 109 110 return true; 111 } 112 113 //min-cost-circulation 114ll d[maxn][maxn]; 115 int dfrom[maxn][maxn]: 116 int level[maxn]; 117 void circulation() { while (true) { 118 int q = 0; fill(d[0], d[0] + N, 0); 119 120 121 forn (iter, N) { fill(d[iter + 1], d[iter + 1] + N, infc); 122 forn (u, N) for (int e: g[u]) { if (edge[e].c == edge[e].f) 123 124 125 126 continue; int v = edge[e].to; ll ndist = d[iter][u] + edge[e].cost; if (ndist >= d[iter + 1][v]) 127 128 129 130 continue; d[iter + 1][v] = ndist; 131 132 dfrom[iter + 1][v] = e;} 133 q ^= 1; 134 135 136 int w = -1; 137 ld mindmax = 1e18; forn (u, N) { 138 ld dmax = -1e18; 139 140 forn (iter, N) 141 dmax = max(dmax,142 (d[N][u] - d[iter][u]) / ld(N - iter)); 143 if (mindmax > dmax) mindmax = dmax, w = u; 144 145 146 if (mindmax >= 0)147 148 fill(level, level + N, -1); int k = N; 149 150 while (level[w] == -1) { level[w] = k; 151 $w = edge[dfrom[k--][w] ^ 1].to;$ 152 153 154 int k2 = level[w]; ll delta = infc; 155 while (k2 > k) { 156 int e = dfrom[k2--][w];157 delta = min(delta, edge[e].c - edge[e].f); 158 159 $w = edge[e ^1].to;$ 160 161 k2 = level[w];while (k2 > k) { 162 int e = dfrom[k2--][w];163 totalCost += edge[e].cost \* delta; edge[e].f += delta; edge[e ^ 1].f -= delta; 164 165 166 w = edge[e ^ 1].to; 167 } 168 169 170} 171} // namespace MinCost 172 173 int main() { MinCost::N = 3, MinCost::S = 1, MinCost::T = 2; MinCost::addEdge(1, 0, 3, 5); MinCost::addEdge(0, 2, 4, 6); 174 175 176 while (MinCost::push()); 177 cout << MinCost::totalFlow << ' '</pre> 178 << MinCost::totalCost << '\n'; //3 33</pre> 179 180 }

# geometry/chan.cpp

```
1 #include <bits/stdc++.h>
 2using namespace std;
 3 \# define \ forn(i,n) \ for \ (int \ i = 0; \ i < int(n); ++i)
 4typedef long double ld;
 6 const int maxn = 100100;
 7 const ld eps = 1e-9;
 9mt19937 rr(111);
10ld rndEps() {
11
       return (ld(rr()) / rr.max() - 0.5) / 1e5;
12}
13
14bool gt(1d a, 1d b) { return a - b > eps; }
15bool lt(1d a, 1d b) { return b - a > eps; }
16bool eq(ld a, ld b) { return fabsl(a - b) < eps; }
18struct pt {
        ld x, y, z;
19
        ld ox, oy, oz;
20
        int pr, nx;
22
        bool inHull;
        static pt *NIL;
26
       pt() {}
        pt(1d x, 1d y, 1d z): x(x), y(y), z(z) {}
30
        pt operator-(const pt &p) const {
31
            return pt(x - p.x, y - p.y, z - p.z);
32
33
34
        ld operator*(const pt &p) const {
            return x * p.x + y * p.y + z * p.z;
35
36
37
38
        pt operator%(const pt &p) const {
            return pt(y * p.z - z * p.y,
z * p.x - x * p.z,
39
40
41
                         x * p.y - y * p.x);
        }
42
43
        bool operator==(const pt &a) {
   return eq(x, a.x) && eq(y, a.y) && eq(z, a.z);
44
45
46
47
        void transform(bool rev) {
48
            if (rev) {
49
50
                 x = ox, y = oy, z = oz;
             } else {
51
                  ox = x, oy = y, oz = z;
52
                  x += rndEps(), y += rndEps(), z += rndEps();
53
54
55
       }
56};
57
58 ostream & operator << (ostream & out, pt & p) {
59    return out << p.x << ' ' << p.y << ' ' << p.z;
60 }
61
62istream &operator>>(istream &in, pt &p) {
63
       return in >> p.x >> p.y >> p.z;
64}
65
66 typedef tuple < int, int, int > Facet;
68 namespace Chan {
69 int n;
70pt p[maxn];
71
72ld turn(int p1, int p2, int p3) {
73    assert(p1 != -1 && p2 != -1 && p3 != -1);
74    return (p[p2].x - p[p1].x) * (p[p3].y - p[p1].y) -
             (p[p3].x - p[p1].x) * (p[p2].y - p[p1].y);
76}
78//replace\ y\ with\ z
791d turnz(int p1, int p2, int p3) {
80    assert(p1 != -1 && p2 != -1 && p3 != -1);
81    return (p[p2].x - p[p1].x) * (p[p3].z - p[p1].z) -
82    (p[p3].x - p[p1].x) * (p[p2].z - p[p1].z);
83 }
85ld gett(int p1, int p2, int p3) {
       return turnz(p1, p2, p3) / turn(p1, p2, p3);
87}
89 void act(int i) {
      if (p[i].inHull) {
            p[p[i].nx].pr = p[i].pr;
```

```
p[p[i].pr].nx = p[i].nx;
 93
 94
            p[p[i].nx].pr = p[p[i].pr].nx = i;
 95
        p[i].inHull ^= 1;
 97}
 99vector<int> buildHull(int 1, int r, bool upper) {
        if (1 + 1 >= r) {
100
            p[1].pr = p[1].nx = -1;
101
            p[l].inHull = true;
102
103
            return {};
104
105
        int mid = (1 + r) / 2;
        auto L = buildHull(1, mid, upper);
106
        auto R = buildHull(mid, r, upper);
107
        reverse(L.begin(), L.end());
reverse(R.begin(), R.end());
108
109
        int u = mid - 1, v = mid;
while (true) {
110
111
             if (p[u].pr != -1 &&
112
113
                     ((turn(p[u].pr, u, v) < 0) ^ upper))
                 u = p[u].pr;
114
             else if (p[v].nx != -1 && ((turn(u, v, p[v].nx) < 0) ^ upper))
115
116
117
                 v = p[v].nx;
118
             else
119
                 break:
        }
120
121
        1d T = -1e100;
122
123
        ld t[6];
        vector<int> A;
124
        while (true) {
125
            forn (i, 6)
126
127
                 t[i] = 1e100:
128
             if (!L.empty()) {
                 int id = L.back();
129
130
                 t[0] = gett(p[id].pr, id, p[id].nx);
131
132
             if (!R.empty()) {
                 int id = R.back();
133
134
                 t[1] = gett(p[id].pr, id, p[id].nx);
135
136
             if (p[u].pr != -1)
             t[2] = gett(p[u].pr, u, v);
if (p[u].nx != -1)
137
138
139
                 t[3] = gett(u, p[u].nx, v);
140
             if (p[v].pr != -1)
141
                 t[4] = gett(u, p[v].pr, v);
142
             if (p[v].nx != -1)
143
                 t[5] = gett(u, v, p[v].nx);
144
             ld nt = 1e100;
145
             int type = -1;
146
             forn (i, 6)
147
                 if ((t[i] - T \ge 1e-15) \&\& t[i] < nt)
148
                     nt = t[i], type = i;
             if (type == -1)
149
150
                 break;
151
             if (type == 0) {
152
                 act(L.back());
153
154
                 if (L.back() < u)
                      A.push_back(L.back());
155
            L.pop_back();
} else if (type =
156
157
                 act(R.back());
158
                 if (R.back() > v)
159
                      A.push_back(R.back());
160
            R.pop_back();
} else if (type ==
161
162
                 A.push_back(u);
163
             u = p[u].pr;
} else if (type == 3) {
164
165
166
                 u = p[u].nx;
167
                 A.push_back(u);
            } else if (type == 4) {
    v = p[v].pr;
168
169
170
                 A.push_back(v);
             } else if (type == 5) {
171
                 A.push_back(v);
172
                 v = p[v].nx;
173
174
             } else
                 assert(false);
175
            T = nt;
176
177
        assert(L.empty() && R.empty());
178
179
        p[u].nx = v, p[v].pr = u;
for (int i = u + 1; i < v; ++i)
    p[i].inHull = false;</pre>
180
181
182
        for (int i = int(A.size()) - 1; i >= 0; --i) {
183
             int id = A[i];
184
```

```
if (id <= u \mid \mid id >= v) {
                if (u == id)
186
                     u = p[u].pr;
187
                 if (v == id)
188
                     v = p[v].nx;
                 act(id);
190
191
            } else {
                p[id].pr = u, p[id].nx = v;
192
193
                act(id);
                 if (id >= mid)
194
                     v = id;
195
196
                 else
197
                     u = id;
198
            }
199
       }
200
201
       return A;
202}
203
204//facets are oriented ccw if look from the outside
205 vector < Facet > getFacets() {
       forn (i, n)
    p[i].transform(false);
206
207
       //WARNING: original order of points is changed sort(p, p + n, [](const pt &a, const pt &b) {
208
209
210
                     return a.x < b.x;
211
212
        vector<Facet> facets;
213
       forn (q, 2) {
214
            auto movie = buildHull(0, n, q);
215
            for (auto x: movie) {
216
                if (!p[x].inHull)
217
                     facets.emplace_back(p[x].pr, x, p[x].nx);
218
219
                 else
220
                     facets.emplace_back(p[x].pr, p[x].nx, x);
221
                 act(x);
            }
222
223
       forn (i, n)
224
225
           p[i].transform(true);
226
       return facets;
227 }
228} //namespace Chan
229
230 int main() {
231
       int n;
232
        cin >> n;
233
        Chan::n = n;
234
        forn (i, n)
235
           cin >> Chan::p[i];
236
        auto facets = Chan::getFacets();
237
        set<int> nodes;
        for (auto f: facets) {
238
239
            nodes.insert(get<0>(f));
240
            nodes.insert(get<1>(f));
241
            nodes.insert(get<2>(f));
242
        assert(nodes.size() * 2 == facets.size() + 4);
243
        ld V = 0, S = 0;
244
        for (auto f: facets) {
245
            pt v1 = Chan::p[get<1>(f)] - Chan::p[get<0>(f)];
246
247
            pt v2 = Chan::p[get<2>(f)] - Chan::p[get<0>(f)];
            pt v3 = Chan::p[get<0>(f)];
248
            pt vv = v1 % v2;
249
            forn (i, n) {
250
                pt v4 = Chan::p[i] - Chan::p[get<0>(f)];
251
                 assert(v4 * vv < 0.1);
253
254
            S += sqrtl(vv.x * vv.x + vv.y * vv.y + vv.z * vv.z) / 2;
255
            V += vv * v3 / 6;
256
257
       cout.precision(10);
       cout << fixed;
cout << S << ' ' << V << '\n';</pre>
259
260}
```

#### 7 geometry/convex hull.cpp

```
1 #include <bits/stdc++.h>
 2using namespace std;
 3 \# define forn(i, n) for (int i = 0; i < int(n); ++i)
 4 #define sz(x) ((int) (x).size())
 6 #include "primitives.cpp"
 8bool cmpAngle(const pt &a, const pt &b) {
      bool ar = a.right(), br = b.right(); if (ar ^ br)
11
           return ar;
12
      return gt(a % b, 0);
13}
14
15struct Hull {
16
      vector<pt> top, bot;
17
       void append(pt p) {
18
           while (bot.size() > 1 && ge((p - bot.back())
19
                    % (bot.back() - *next(bot.rbegin())), 0))
20
21
               bot.pop_back();
           22
23
24
25
               top.pop_back();
26
           top.push_back(p);
27
      }
28
      void build(vector<pt> h) {
   sort(h.begin(), h.end());
   h.erase(unique(h.begin(), h.end()), h.end());
29
30
31
           top.clear(), bot.clear();
32
           for (pt p: h)
33
34
               append(p);
35
      }
36
      pt kth(int k) {
   if (k < sz(bot))</pre>
37
38
39
               return bot[k];
40
           else
41
               return top[sz(top) - (k - sz(bot)) - 2];
      }
42
43
44
      pt mostDistant(pt dir) {
45
           if (bot.empty()) {
46
                //empty hull
47
               return pt{1e18, 1e18};
48
49
           if (bot.size() == 1)
50
               return bot.back();
           dir = dir.rot();
52
           int n = sz(top) + sz(bot) - 2;
           int L = -1, R = n;
while (L + 1 < R) {</pre>
53
54
               int C = (L + R) / 2;
pt v = kth((C + 1) % n) - kth(C);
55
56
57
                if (cmpAngle(dir, v)) //finds upper bound
58
                    R = C;
60
                    L = C;
61
           return kth(R % n);
64 }:
```

## 3 geometry/halfplanes.cpp

```
1 #include <bits/stdc++.h>
 2using namespace std;
  3 \textit{ #define forn}(i, n) \textit{ for (int } i = 0; i < int(n); ++i) \\ 4 \textit{ #define forab(i, a, b) for (int } i = int(a); i < int(b); ++i) 
 5 #include "primitives.cpp"
7ld det3x3(line &11, line &12, line &13) {
       return 11.a * (12.b * 13.c - 12.c * 13.b) +
11.b * (12.c * 13.a - 12.a * 13.c) +
8
9
               11.c * (12.a * 13.b - 12.b * 13.a);
10
11 }
12
13vector<pt> halfplanesIntersecion(vector<line> lines) {
       sort(lines.begin(), lines.end(),
            [](const line &a, const line &b) {
   bool ar = a.right(), br = b.right();
   if (ar ^ br)
15
17
                          return ar;
                     ld prod = (pt{a.a, a.b} % pt{b.a, b.b});
19
                      if (!eq(prod, 0))
20
                          return prod > 0;
                      return a.c < b.c;
                 }):
24
       vector<line> lines2;
25
       pt pr;
       forn (i, lines.size()) {
26
           pt cur{lines[i].a, lines[i].b};
if (i == 0 || cur != pr)
27
28
29
                lines2.push_back(lines[i]);
            pr = cur;
30
31
       lines = lines2;
32
       int n = lines.size();
33
       forn (i, n)
34
35
           lines[i].id = i;
       vector<line> hull;
36
       forn (i, 2 * n) {
    line l = lines[i % n];
37
38
            while ((int) hull.size() >= 2) {
39
                ld D = det3x3(*next(hull.rbegin()), hull.back(), 1);
40
                 if (ge(D, 0))
41
42
                      break:
                 hull.pop_back();
43
44
            hull.push_back(1);
45
46
47
       vector<int> firstTime(n, -1);
48
       vector<line> v;
       form (i, hull.size()) {
   int cid = hull[i].id;
49
50
            if (firstTime[cid] == -1) {
51
                 firstTime[cid] = i;
52
53
                 continue:
54
55
            forab(j, firstTime[cid], i)
56
                v.push_back(hull[j]);
57
            break;
58
       }
59
       n = v.size();
       if (v.empty()) {
60
61
            //empty intersection
62
            return {};
63
       v.push_back(v[0]);
65
       vector<pt> res;
       pt center{0, 0};
66
67
       forn (i, n) {
            res.push_back(linesIntersection(v[i], v[i + 1]));
68
            center = center + res.back();
70
71
       center = center / n;
       for (auto 1: lines)
            if (gt(0, 1.signedDist(center))) {
                 //empty intersection
                 return {};
76
       return res;
```

### 9 geometry/planar faces.cpp

# 10 geometry/polygon.cpp

```
lint m, n; // segs, points
2pair pt, pt> segs[maxn];
 3pt p[maxn], from, to;
 4map<pt, int> shr;
5vi e[maxn]; // points adjacent to point
 6int getPoint(pt x) {
       if (shr.count(x)) return shr[x];
       p[n] = x;
       return shr[x] = n++;
10}
11// segIntersection: {bool, point}, true iff exactly one point
12 void genIntersections() {
13
       forn(i, m) {
14
            getPoint(segs[i].fi);
15
             getPoint(segs[i].se);
16
             forn(j, i) {
17
                 auto t = segmentsIntersection(
18
                      segs[i].fi, segs[i].se, segs[j].fi, segs[j].se);
19
                  if (t.fi) getPoint(t.se);
20
21
22}
23
24 void genGraph() {
25
       forn(i, m) {
26
             vi pts;
27
             forn(j, n) if (pointInsideSegment(
                           p[j], segs[i].fi, segs[i].se)) {
28
                 pts.push_back(j);
30
            sort(all(pts), [](int i, int j) {
    return p[i] < p[j]; });
forn(j, pts.size() - 1) {
    int u = pts[j], v = pts[j+1];</pre>
31
32
33
34
                  e[u].push_back(v);
35
36
                 e[v].push_back(u);
37
38
39
       forn(i, n) {
            sort(all(e[i]), [i](int x, int y) {
   pt a = p[x] - p[i];
   pt b = p[y] - p[i];
   if (a.right() != b.right()) return a.right();
40
41
42
43
                 return a \% b > 0;
44
45
             }):
       }
46
47 }
48
49 vector < pt > faces [maxn];
50 bool inner [maxn];
51 int nf;
52 map<pii, int> faceForEdge;
53 vi ef[maxn]; // graph on faces
55 void genFaces() {
       forn(i, n) for (int to: e[i]) {
    if (faceForEdge.count({i, to})) continue;
56
57
            int f = nf++;
int v = i, u = to;
58
59
60
61
                 faces[f].push_back(p[v]);
62
                 faceForEdge[{v, u}] = f;
63
                  auto it = lower_bound(all(e[u]), v,
                       [u] (int x, int y) {
64
                           pt a = p[x] - p[u];
pt b = p[y] - p[u];
65
66
67
                            if (a.right()!=b.right()) return a.right();
68
                            return a % b > 0;
69
                 });
70
                 assert(*it == v);
71
                 if (it == e[u].begin()) it = e[u].end();
                 v = u;
u = *--it;
72
73
74
             } while (v != i || u != to);
75
76
       forn(i, nf) {
77
78
             forn(j, faces[i].size()) {
79
                  s += faces[i][j] % faces[i][(j+1)%faces[i].size()];
81
             inner[i] = gt(s, 0);
82
       forn(v, n) for (int to: e[v]) {
83
84
            int f1 = faceForEdge[{v, to}];
             int f2 = faceForEdge[{to, v}];
             if (f1 != f2) {
86
                 ef[f1].push_back(f2);
87
                  ef[f2].push_back(f1);
89
90
91 }
```

```
1bool pointInsidePolygon(pt a, pt *p, int n) {
        double sumAng = 0;
        forn (i, n) {
             pt A = p[i], B = p[(i + 1) \% n];
 5
             if (pointInsideSegment(a, A, B))
                   return true;
 7
             sumAng += atan2((A - a) \% (B - a), (A - a) * (B - a));
 8
 9
        return fabs(sumAng) > 1;
10}
12//p must be oriented counterclockwise
13bool segmentInsidePolygon(pt a, pt b, pt *p, int n) {
14   if (!pointInsidePolygon((a + b) / 2, p, n))
        if (a == b)
17
            return true;
        forn (i, n) {
   pt c = p[i];
             if (eq((a - c) % (b - c), 0) &&
gt(0, (a - c) * (b - c))) {
20
                   //point on segment
                  pt pr = p[(i + n - 1) % n];
pt nx = p[(i + 1) % n];
if (gt((c - pr) % (nx - c), 0))
24
25
                        return false;
26
                  ld s1 = (pr - a) % (b - a);
ld s2 = (nx - a) % (b - a);
27
28
                  if ((gt(s1, 0) || gt(s2, 0)) && (gt(0, s1) || gt(0, s2)))
29
30
31
                        return false;
32
             //interval intersection
33
             pt d = p[(i + 1) % n];
ld s1 = (a - c) % (d - c);
ld s2 = (b - c) % (d - c);
34
35
36
             if (ge(s1, 0) && ge(s2, 0))
37
38
                   continue;
             if (ge(0, s1) && ge(0, s2))
39
40
                   continue:
41
             s1 = (c - a) \% (b - a):
42
             s2 = (d - a) \% (b - a);
43
             if (ge(s1, 0) && ge(s2, 0))
44
             continue;
if (ge(0, s1) && ge(0, s2))
45
46
47
                   continue;
48
49
             return false;
        }
50
51
        return true;
52 }
```

### 11 geometry/primitives.cpp

```
1//\mathit{WARNING!} do not forget to normalize vector (a,b)
 2struct line {
       ld a, b, c;
 4
       int id;
 5
       line(pt p1, pt p2) {
   gassert(p1 != p2);
   pt n = (p2 - p1).rot();
 6
 7
 8
 9
            n /= n.abs();
10
            a = n.x, b = n.y;
11
            c = -(n * p1);
12
13
       bool right() const {
14
           return gt(a, 0) || (eq(a, 0) && gt(b, 0));
15
16
17
18
       line(ld _a, ld _b, ld _c): a(_a), b(_b), c(_c) {
19
            ld d = pt{a, b}.abs();
20
            gassert(!eq(d, 0));
21
            a /= d, b /= d, c /= d;
22
23
24
       ld signedDist(pt p) {
25
            return p * pt{a, b} + c;
26
27};
28
291d pointSegmentDist(pt p, pt a, pt b) {
30    ld res = min((p - a).abs(), (p - b).abs());
31    if (a != b && ge((p - a) * (b - a), 0) &&
32         ge((p - b) * (a - b), 0))
            res = min(res,
33
34
                fabsl((p - a) % (b - a)) / (b - a).abs());
35
       return res;
36}
37
38pt linesIntersection(line 11, line 12) {
       1d D = 11.a * 12.b - 11.b * 12.a;
39
       if (eq(D, 0)) {
40
            if (eq(11.c, 12.c)) {
41
42
                //equal lines
            } else {
43
                //no intersection
44
45
46
       47
48
49
       //gassert(eq(l1.signedDist(res), 0));
//gassert(eq(l2.signedDist(res), 0));
50
51
52
       return res:
53}
54
55bool pointInsideSegment(pt p, pt a, pt b) {
       if (!eq((p - a) % (p - b), 0))
56
            return false;
57
       return ge(0, (a - p) * (b - p));
58
59 }
60
61bool checkSegmentIntersection(pt a, pt b, pt c, pt d) {
       if (eq((a - b) \% (c - d), 0)) {
62
            if (pointInsideSegment(a, c, d) \mid \mid
63
64
                 pointInsideSegment(b, c, d) ||
65
                 pointInsideSegment(c, a, b) ||
66
                 pointInsideSegment(d, a, b)) {
67
                 //intersection of parallel segments
68
                 return true;
69
70
            return false;
71
72
73
       ld s1, s2;
74
       s1 = (c - a) \% (b - a);

s2 = (d - a) \% (b - a);
75
76
77
       if (gt(s1, 0) && gt(s2, 0))
78
            return false;
       if (gt(0, s1) && gt(0, s2))
79
            return false;
82
       swap(a, c), swap(b, d);
83
       s1 = (c - a) \% (b - a);

s2 = (d - a) \% (b - a);
       if (gt(s1, 0) && gt(s2, 0))
86
87
            return false;
       if (gt(0, s1) && gt(0, s2))
89
            return false;
       return true;
```

```
92}
 94// WARNING! run checkSegmentIntersecion before and process
 95 // parallel case manually
 96pt segmentsIntersection(pt a, pt b, pt c, pt d) {
97    ld S = (b - a) % (d - c);
98    ld s1 = (c - a) % (d - a);
         return a + (b - a) / S * s1;
100}
101
102vector<pt> circlesIntersction(pt a, ld r1, pt b, ld r2) {
103
         1d d2 = (a - b).abs2();
         1d d = (a - b).abs();
104
105
         if (a == b \&\& eq(r1, r2)) {
107
              //equal circles
108
109
         if (gt(d2, sqr(r1 + r2)) || gt(sqr(r1 - r2), d2)) {
110
              //empty intersection
              return {};
111
112
         int num = 2;
113
         if (eq(sqr(r1 + r2), d2) \mid \mid eq(sqr(r1 - r2), d2))
114
115
         ld cosa = (sqr(r1) + d2 - sqr(r2)) / ld(2 * r1 * d);
116
         ld oh = cosa * r1;
117
         pt h = a + ((b - a) / d * oh);
if (num == 1)
118
119
             return {h}:
120
         ld hp = sqrtl(max(0.L, 1 - cosa * cosa)) * r1;
121
122
         pt w = ((b - a) / d * hp).rot();
return {h + w, h - w};
123
124
125 }
126
127 //a is circle center, p is point
128 vector < pt > circleTangents (pt a, ld r, pt p) {
129    ld d2 = (a - p).abs2();
         ld d = (a - p).abs();
130
131
132
         if (gt(sqr(r), d2)) {
133
              //no tangents
              return {};
134
135
136
         if (eq(sqr(r), d2)) {
137
              //point lies on circle - one tangent
138
              return {p};
139
         }
140
        pt B = p - a;
pt H = B * sqr(r) / d2;
141
142
143
         ld h = sqrtl(d2 - sqr(r)) * ld(r) / d;
         pt w = (B / d * h).rot();
144
         H = H + a;
145
         return \{H + w, H - w\};
146
147}
148
149vector<pt> lineCircleIntersection(line 1, pt a, ld r) {
150    ld d = 1.signedDist(a);
         if (gt(fabsl(d), r))
152
             return {};
         pt h = a - pt{l.a, l.b} * d;
         if (eq(fabsl(d), r))
             return {h};
         pt w(pt{l.a, l.b}.rot() * sqrtl(max<ld>(0, sqr(r)-sqr(d))));
156
         return \{h + w, h - w\};
157
158}
160 //modified magic from e-maxx
161vector<line> commonTangents(pt a, ld r1, pt b, ld r2) {
         if (a == b \&\& eq(r1, r2)) {
162
             //equal circles
163
             return {};
164
165
166
         vector<line> res;
        pt c = b - a;
ld z = c.abs2();
167
168
        for (int i = -1; i <= 1; i += 2)

for (int j = -1; j <= 1; j += 2) {

    ld r = r2 * j - r1 * i;

    ld d = z - sqr(r);
169
170
171
172
                   if (gt(0, d))
173
174
                       continue;
                   d = sqrtl(max<ld>(0, d));
pt magic = pt{r, d} / z;
line l(magic * c, magic % c, r1 * i);
l.c -= pt{l.a, l.b} * a;
175
176
177
178
                   res.push_back(1);
179
             }
180
181
         return res;
182 }
```

## 12 geometry/svg.cpp

```
1struct SVG {
2
      FILE *out;
3
      ld sc = 50;
5
           out = fopen("image.svg", "w");
6
           fprintf(out, "<svg xmlns='http://www.w3.org/2000/svg'

→ viewBox='-1000 -1000 2000 2000'>\n");
7
8
10
      void line(pt a, pt b) {
           11
12
13
14
      void circle(pt a, ld r = -1, string col = "red") {
   r = (r == -1 ? 10 : sc * r);
15
16
           a = a * sc;
17
           fprintf(out, "<circle cx='%Lf' cy='%Lf' r='%Lf'</pre>
18
            \hookrightarrow fill='%s'/>\n", a.x, -a.y, r, col.c_str());
19
20
21
      void text(pt a, string s) {
22
           a = a * sc;
           fprintf(out, "<text x='%Lf' y='%Lf'</pre>
            \rightarrow font-size='10px'>%s</text>\n", a.x, -a.y,

    s.c_str());

24
25
26
      void close() {
27
           fprintf(out, "</svg>\n");
28
           fclose(out):
29
           out = 0;
30
31
       ~SVG() {
32
          if (out)
33
               close();
34
35
36} svg;
```

### 13 graphs/2sat.cpp

```
1 const int maxn = 200100; //2 x number of variables
 3namespace TwoSAT {
       int n; //number of variables
       bool used[maxn];
       vector<int> g[maxn];
vector<int> gr[maxn];
       int comp[maxn];
       int res[maxn];
10
11
       void addEdge(int u, int v) { //u or v
            g[u].push_back(v ^ 1);
g[v].push_back(u ^ 1);
13
            gr[u ^ 1].push_back(v);
gr[v ^ 1].push_back(u);
15
17
       vector<int> ord;
       void dfs1(int u) {
19
            used[u] = true;
20
            for (int v: g[u]) {
                if (used[v])
                      continue;
                 dfs1(v);
25
            }
26
            ord.push_back(u);
27
28
       int COL = 0;
29
       void dfs2(int u) {
30
            used[u] = true;
comp[u] = COL;
31
32
            for (int v: gr[u]) {
    if (used[v])
33
34
35
                      continue;
36
                 dfs2(v);
            }
37
       }
38
39
       void mark(int u) {
40
            res[u / 2] = u % 2;
used[u] = true;
41
42
            for (int v: g[u]) {
43
                 if (used[v])
44
45
                      continue;
                 mark(v);
46
            }
47
       }
48
49
       bool run() {
50
            fill(res, res + 2 * n, -1);
51
            fill(used, used + 2 * n, false);
52
            forn (i, 2 * n)
if (!used[i])
53
54
55
                      dfs1(i);
56
            reverse(ord.begin(), ord.end());
57
            assert((int) ord.size() == (2 * n));
58
            fill(used, used + 2 * n, false);
59
            for (int u: ord) if (!used[u]) {
60
                 dfs2(u);
61
                 ++COL;
62
            7
63
            forn (i, n)
                 if (comp[i * 2] == comp[i * 2 + 1])
65
                      return false;
66
67
            reverse(ord.begin(), ord.end());
68
            fill(used, used + 2 * n, false);
            for (int u: ord) {
70
                 if (res[u / 2] != -1) {
71
                      continue;
72
                 mark(u);
73
            }
74
75
            return true;
       }
76
77};
78
79int main() {
       TwoSAT::n = 2;
80
       TwoSAT::addEdge(0, 2); //x or y
TwoSAT::addEdge(0, 3); //x or !y
TwoSAT::addEdge(3, 3); //!y or !y
assert(TwoSAT::run());
81
83
       cout << TwoSAT::res[0] << ' ' << TwoSAT::res[1] << '\n';</pre>
85
86
87}
```

```
graphs/directed mst.cpp
14
```

```
vector<Edge> firstResult = bfs(e, {root}, {});
                                                                                   if ((int)firstResult.size() + 1 == n) {
                                                                                       return firstResult;
                                                                            94
 1// WARNING: this code wasn't submitted anywhere
                                                                            95
 3namespace TwoChinese {
                                                                            97
                                                                                   // find stongly connected comp-s and build compressed graph
                                                                                   vector<int> comp(n);
 5struct Edge {
                                                                                   forn(i, n) b[i] = 0;
                                                                            99
 6
      int to, w, id;
                                                                           100
                                                                                   nc = 0;
      bool operator<(const Edge& other) const {</pre>
                                                                                   dtime = 0;
           return to < other.to || (to == other.to && w < other.w); 102
 8
                                                                                   forn(i, n) if (!b[i]) tarjan(i, e, comp);
 9
                                                                           103
10 };
                                                                           104
                                                                                   // multiple edges may be removed here if needed
11typedef vector<vector<Edge>> Graph;
                                                                           105
                                                                                   Graph ne(nc);
12
                                                                                   forn(v, n) for (Edge t: e[v]) {
    if (comp[v] != comp[t.to]) ...
                                                                           106
13 const int maxn = 2050;
                                                                           107
                                                                                           ne[comp[v]].push_back({comp[t.to], t.w, t.id});
                                                                           108
15// global, for supplementary algorithms
                                                                           109
16 int b[maxn];
                                                                           110
17int tin[maxn], tup[maxn];
                                                                                   int oldnc = nc;
                                                                           111
18 int dtime; // counter for tin, tout
                                                                           112
19 vector<int> st;
                                                                                   // run recursively on compressed graph
vector<Edge> subres = run(ne, comp[root]);
                                                                           113
20 int nc; // number of strongly connected components
                                                                           114
21int q[maxn];
                                                                           115
                                                                                     find incoming edge id for each component, init queue
                                                                           116
                                                                                   // if there is an edge (u, v) between different components
                                                                           117
                                                                                   // than v is added to queue
                                                                           118
25 void tarjan(int v, const Graph& e, vector<int>& comp) {
                                                                           119
                                                                                   nc = oldnc:
      b[v] = 1;
                                                                                   vector<int> incomingId(nc);
                                                                           120
27
       st.push_back(v);
                                                                                   for (Edge e: subres) {
                                                                           121
       tin[v] = tup[v] = dtime++;
28
                                                                                       incomingId[e.to] = e.id;
                                                                           122
                                                                           123
30
       for (Edge t: e[v]) if (t.w == 0) {
                                                                           124
           int to = t.to;
if (b[to] == 0) {
31
                                                                                   vector<Edge> result;
vector<int> init;
                                                                           125
32
                                                                           126
           tarjan(to, e, comp);
  tup[v] = min(tup[v], tup[to]);
} else if (b[to] == 1) {
33
                                                                           127
                                                                                   init.push_back(root);
34
                                                                                   forn(v, n) for (Edge t: e[v]) {
                                                                           128
35
                                                                                       if (incomingId[comp[t.to]] == t.id) {
                                                                           129
36
               tup[v] = min(tup[v], tin[to]);
                                                                           130
                                                                                            result.push_back(t);
37
                                                                           131
                                                                                            init.push_back(t.to);
38
      }
                                                                           132
                                                                                       }
39
                                                                                   }
                                                                           133
       if (tin[v] == tup[v]) {
40
                                                                           134
41
           while (true) {
                                                                           135
                                                                                   // run bfs to add edges inside components and return answer
               int t = st.back();
42
                                                                                   vector<Edge> innerEdges = bfs(e, init, comp);
                                                                           136
               st.pop_back();
comp[t] = nc;
43
                                                                                   result.insert(result.end(), all(innerEdges));
                                                                           137
44
                                                                           138
               b[t] = 2;
45
                                                                          139
                                                                                   assert((int)result.size() + 1 == n);
               if (t == v) break;
46
                                                                           140
                                                                                   return result;
47
           }
                                                                           141}
48
           ++nc:
                                                                           142
49
      }
                                                                           143} // namespace TwoChinese
50 }
                                                                           144
51
                                                                           145\, {	t void} test () {
52 vector < Edge > bfs(
                                                                                   auto res = TwoChinese::run({
                                                                           146
53
       const Graph& e,const vi& init, const vi& comp)
                                                                           147
                                                                                       {{1,5,0},{2,5,1}},
54 €
                                                                                       {{3,1,2}},
                                                                           148
55
       int n = e.size():
                                                                                       {{1,2,3},{4,1,4}},
{{1,1,5},{4,2,6}},
                                                                           149
      forn(i, n) b[i] = 0;
int lq = 0, rq = 0;
56
                                                                           150
57
                                                                                       {{2,1,7}}},
                                                                           151
      for (int v: init) b[v] = 1, q[rq++] = v;
58
                                                                           152
59
                                                                                   cout << TwoChinese::answer << endl;</pre>
                                                                           153
60
       vector<Edge> result;
                                                                           154
                                                                                   for (auto e: res) cout << e.id << " ";
61
                                                                                   cout << endl;</pre>
                                                                           155
62
      while (lq != rq) {
                                                                                             0 6 2 7
                                                                           156
                                                                                   // 9
           int \bar{v} = q[lq++];
63
                                                                           157}
           for (Edge t: e[v]) if (t.w == 0) {
   int to = t.to;
64
65
66
                if (b[to]) continue;
67
                if (!comp.empty() && comp[v] != comp[to]) continue;
               b[to] = 1;
q[rq++] = to;
68
69
70
                result.push_back(t);
71
72
      }
73
74
       return result;
75}
77// warning: check that each vertex is reachable from root
78vector<Edge> run(Graph e, int root) {
79
       int n = e.size();
       // find minimum incoming weight for each vertex
       vector<int> minw(n, inf);
82
       forn(v, n) for (Edge t: e[v]) {
83
84
           minw[t.to] = min(minw[t.to], t.w);
85
86
       forn(v, n) for (Edge &t: e[v]) if (t.to != root) {
87
           t.w -= minw[t.to];
88
89
       forn(i, n) if (i != root) answer += minw[i];
       // check if each vertex is reachable from root by zero edges
```

#### 15 graphs/edmonds matching.cpp

# 16 graphs/euler\_cycle.cpp

```
1int n;
                                                                                        1struct Edge {
 2vi e[maxn];
                                                                                              int to, id;
 3 int mt[maxn], p[maxn], base[maxn], b[maxn], blos[maxn];
                                                                                       3};
 4int q[maxn];
 5int blca[maxn]; // used for lca
                                                                                       5bool usedEdge[maxm];
                                                                                       6vector<Edge> g[maxn];
 7 int lca(int u, int v) {
8  forn(i, n) blca[i] = 0;
                                                                                       7int ptr[maxn];
        while (true) {
                                                                                       9vector<int> cycle;
            u = base[u];
                                                                                       10 void eulerCycle(int u) {
            blca[u] = 1;
if (mt[u] == -1) break;
                                                                                              while (ptr[u] < sz(g[u]) && usedEdge[g[u][ptr[u]].id])
11
                                                                                      11
                                                                                              ++ptr[u];
if (ptr[u] == sz(g[u]))
12
13
            u = p[mt[u]];
                                                                                      13
                                                                                                  return;
14
                                                                                      14
                                                                                              const Edge &e = g[u][ptr[u]];
usedEdge[e.id] = true;
15
       while (!blca[base[v]]) {
                                                                                       15
16
             v = p[mt[base[v]]];
                                                                                      16
17
                                                                                              eulerCycle(e.to);
                                                                                      17
                                                                                              cycle.push_back(e.id);
18
       return base[v];
                                                                                      18
                                                                                              eulerCycle(u);
19 }
                                                                                      19
20
                                                                                      20}
21void mark_path(int v, int b, int ch) {
22 while (base[v] != b) {
                                                                                      21
                                                                                      22 int edges = 0;
                                                                                      23 void addEdge(int u, int v) {
23
             blos[base[v]] = blos[base[mt[v]]] = 1;
            p[v] = ch;
                                                                                              g[u].push_back(Edge{v, edges});
24
25
             ch = mt[v];
                                                                                      25
                                                                                              g[v].push_back(Edge{u, edges++});
             v = p[mt[v]];
26
                                                                                      26 }
27
28 }
29
30int find_path(int root) {
       forn(i, n) {
   base[i] = i;
   p[i] = -1;
   b[i] = 0;
31
32
33
34
35
36
37
       b[root] = 1:
38
       q[0] = root;
       int lq = 0, rq = 1;
while (lq != rq) {
39
40
             int v = q[lq++];
41
             for (int to: e[v]) {
   if (base[v] == base[to] || mt[v] == to) continue;
   if (to==root || (mt[to] != -1 && p[mt[to]] != -1)) {
42
43
44
                       int curbase = lca(v, to);
forn(i, n) blos[i] = 0;
45
46
47
                       mark_path(v, curbase, to);
48
                       mark_path(to, curbase, v);
                       forn(i, n) if (blos[base[i]]) {
   base[i] = curbase;
49
50
51
                            if (!b[i]) b[i] = 1, q[rq++] = i;
52
                  } else if (p[to] == -1) {
   p[to] = v;
53
54
                       if (mt[to] == -1) {
55
56
                            return to;
57
58
                       to = mt[to];
                       b[to] = 1;
q[rq++] = to;
60
61
62
            }
63
64
65
       return -1;
66}
67
68int matching() {
        forn(i, n) mt[i] = -1;
69
        int res = 0;
70
       forn(i, n) if (mt[i] == -1) {
   int v = find_path(i);
   if (v != -1) {
71
72
73
74
                  ++res;
75
                  while (v != -1) {
                       int pv = p[v], ppv = mt[p[v]];
mt[v] = pv, mt[pv] = v;
76
77
78
                       v = ppv;
79
80
            }
81
82
       return res:
```

#### 17 math/factor.cpp

```
1//WARNING: only mod <= 1e18
 5
          res += mod;
       while (res >= mod)
          res -= mod;
 8
      return res;
 9}
10
11bool millerRabinTest(ll n, ll a) {
      if (\gcd(n, a) > 1)
13
           return false;
14
       11 x = n - 1;
      int 1 = 0;
while (x % 2 == 0) {
15
16
17
           x /= 2;
19
      11 c = binpow(a, x, n);
for (int i = 0; i < 1; ++i) {</pre>
20
21
          ll nx = mul(c, c, n);
22
           if (nx == 1) {
   if (c != 1 && c != n - 1)
23
24
25
                    return false;
26
27
                    return true;
           }
28
29
           c = nx;
30
31
      return c == 1;
32 }
33
34bool isPrime(ll n) {
      if (n == 1)
35
           return false;
36
      if (n % 2 == 0)
37
      return n == 2;
for (ll a = 2; a < min<ll>(8, n); ++a)
38
39
          if (!millerRabinTest(n, a))
40
41
               return false;
42
      return true:
43 }
44
45 // \mathit{WARNING}: p is not sorted
46 void factorize(ll x, vector<ll> &p) {
47
      if (x == 1)
48
           return;
       if (isPrime(x)) {
49
50
           p.push_back(x);
51
           return;
52
      for (11 d: {2, 3, 5})
if (x % d == 0) {
53
54
               p.push_back(d);
55
56
                factorize(x / d, p);
57
58
           7
59
      while (true) {
           11 \times 1 = rr() \% (x - 1) + 1;
60
           11 x2 = (mul(x1, x1, x) + 1) % x;
int i1 = 1, i2 = 2;
61
62
63
           while (true) {
               11 c = (x1 + x - x2) \% x;
if (c == 0)
64
65
66
                    break;
                11 g = gcd(c, x);
if (g > 1) {
67
68
                    factorize(g, p);
factorize(x / g, p);
70
71
                     return;
72
73
                if (i1 * 2 == i2) {
74
                    i1 *= 2;
75
                    x1 = x2;
76
77
                x2 = (mul(x2, x2, x) + 1) \% x;
79
           }
```

## 18 math/fft.cpp

```
1const int maxlg = 20;
 3vector<base> ang[maxlg + 5];
 5void init_fft() {
       int n = 1 << maxlg;</pre>
 6
       ld e = acosl(-1) * 2 / n;
 7
        ang[maxlg].resize(n);
 8
 9
       forn(i, n) {
10
            ang[maxlg][i] = { cos(e * i), sin(e * i) };
11
12
       for (int k = maxlg - 1; k >= 0; --k) {
   ang[k].resize(1 << k);
   forn(i, 1<<k) {</pre>
13
15
                  ang[k][i] = ang[k+1][i*2];
17
       }
18
19}
20
21 void fft_rec(base *a, int lg, bool rev) {
       if (lg == 0) {
            return;
24
25
        int len = 1 << (lg - 1);</pre>
26
       fft_rec(a, lg-1, rev);
       fft_rec(a+len, lg-1, rev);
27
28
       forn(i, len) {
29
            base w = ang[lg][i];
30
            if (rev) {
31
                 w.im *= -1:
32
33
            base u = a[i];
34
            base v = a[i+len] * w;
a[i] = u + v;
35
36
            a[i+len] = u - v;
37
       }
38
39 }
40
41//n must be power of 2
42 void fft(base *a, int n, bool rev) {
       int lg = 0;
while ((1<<lg) != n) {
    ++lg;
43
44
45
       }
46
       int j = 0, bit;
for (int i = 1; i < n; ++i) {</pre>
47
48
            for (bit = n >> 1; bit & j; bit >>= 1)
49
            j ^= bit;
j ^= bit;
50
51
52
            if (i < j) swap(a[i], a[j]);</pre>
53
       fft_rec(a, lg, rev);
if (rev) forn(i, n) {
   a[i] = a[i] * (1.0 / n);
54
55
56
57
58}
59
60 \operatorname{const} \operatorname{int} \operatorname{maxn} = 1050000;
61
62 int n;
63base a[maxn];
64 base b[maxn];
65
66 void test() {
67
       int n = 8;
       init_fft();
68
       base a[8] = \{1,3,5,2,4,6,7,1\};
       base b[16];
70
       fft(b, 16, 0);
       fft(a, n, 0);
       forn(i, n) cout << a[i].re << " "; cout << endl;
       forn(i, n) cout << a[i].im << " "; cout << endl; // 29 -5.82843 -7 -0.171573 5 -0.171573 -7 -5.82843
        // 0 -3.41421 6 0.585786 0 -0.585786 -6 3.41421
```

#### 19 math/fft inv.cpp

```
1vector <int> mul(vector <int> a, vector <int> b,
            bool carry = true) {
 3
       int n = sz(a);
       if (carry) {
 5
            a.resize(n * 2);
            b.resize(n * 2);
       fft(a.data(), a.size(), false);
fft(b.data(), b.size(), false);
for (int i = 0; i < sz(a); ++i)</pre>
            a[i] = mul(a[i], b[i]);
11
       fft(a.data(), a.size(), true);
12
13
       a.resize(n);
14
       return a;
15}
16
17 vector <int> inv(vector <int> v) {
       int n = 1;
while (n < sz(v))</pre>
18
19
         n <<= 1;
20
21
       v.resize(n, 0);
      22
23
24
25
26
27
28
29
30
           A[0] = sum(A[0], 1);

for (int i = 0; i < k; ++i)

    assert(A[i] == 0);

copy(A.begin() + k, A.end(), A.begin());
31
32
33
34
35
            A.resize(k);
36
            vector <int> B(k);
            copy(v.begin() + k, v.begin() + 2 * k, B.begin());
37
38
            C.resize(k);
39
            B = mul(B, C);
            for (int i = 0; i < k; ++i)
40
            A[i] = sub(A[i], B[i]);
A = mul(A, C);
41
42
            res.resize(k * 2);
43
            copy(A.begin(), A.end(), res.begin() + k);
44
45
46
       return res;
```

## 20 math/golden search.cpp

```
return 5 * x * x + 100 * x + 1; //-10 is minimum
 3}
 51d goldenSearch(ld 1, ld r) {
      ld phi = (1 + sqrtl(5)) / 2;
ld resphi = 2 - phi;
      ld x1 = 1 + resphi * (r - 1);
ld x2 = r - resphi * (r - 1);
       ld f1 = f(x1);
10
       1d f2 = f(x2);
11
      forn (iter, 60) {
12
13
           if (f1 < f2) {
               r = x2;
14
                x2 = x1;
15
               f2 = f1;
16
               x1 = 1 + resphi * (r - 1);
17
                f1 = f(x1);
18
           } else {
19
                1 = x1;
20
                x1 = x2;
21
               f1 = f2;
22
                x2 = r - resphi * (r - 1);
23
24
                f2 = f(x2);
25
           }
      }
26
      return (x1 + x2) / 2;
27
28 }
29
30 int main() {
       std::cout << goldenSearch(-100, 100) << '\n';
31
32 }
```

#### 21 math/numbers.tex

#### • Simpson and Gauss numerical integration:

```
\int_{a}^{b} f(x) dx = (b - a)/6 \cdot (f(a) + 4(f(a + b)/2) + f(b))\int_{-1}^{1}, x_{1,3} = \pm \sqrt{0.6}, x_2 = 0; a_{1,3} = 5/9, a_2 = 8/9
```

- Large primes:  $10^{18} + 3, +31, +3111, 10^9 + 21, +33$
- FFT modules:

• Fibonacci numbers:

```
\begin{array}{lll} 1,2:&1\\ 45:&1\,134\,903\,170\\ 46:&1\,836\,311\,903\,\,(max\,\,int)\\ 47:&2\,971\,215\,073\,\,(max\,\,unsigned)\\ 91:&4\,660\,046\,610\,375\,530\,309\\ 92:&7\,540\,113\,804\,746\,346\,429\,\,(max\,\,i64)\\ 93:&12\,200\,160\,415\,121\,876\,738\,\,(max\,\,unsigned\,\,i64)\\ \end{array}
```

• Powers of two

```
\begin{array}{l} 2^{31} = 2\,147\,483\,648 = 2.1\cdot 10^9 \\ 2^{32} = 4\,294\,967\,296 = 4.2\cdot 10^9 \\ 2^{63} = 9\,223\,372\,036\,854\,775\,808 = 9.2\cdot 10^{18} \\ 2^{64} = 18\,446\,744\,073\,709\,551\,616 = 1.8\cdot 10^{19} \end{array}
```

• Highly composite numbers

```
\begin{array}{lll} - \leq 1000: \ d(840) = 32, \leq 10^4: \ d(9\,240) = 64 & 39 \\ + 40 & - \leq 10^5: \ d(83\,160) = 128, \leq 10^6: \ d(720\,720) = 240 & 41 \\ - \leq 10^7: \ d(8\,648\,640) = 448, \leq 10^8: \ d(91\,891\,800) = 768\,43 \\ - \leq 10^9: \ d(931\,170\,240) = 1344 & 45 \\ - \leq 10^{11}: \ d(97\,772\,875\,200) = 4032 & 47 \\ - \leq 10^{12}: \ d(963\,761\,198\,400) = 6720 & 49 \\ - \leq 10^{15}: \ d(866\,421\,317\,361\,600) = 26880 & 51 \\ - \leq 10^{18}: \ d(897\,612\,484\,786\,617\,600) = 103680 & 52 \\ \end{array}
```

#### Misc

- Расстояние между точками по сфере:  $L = R \cdot 57$  arccos( $\cos \theta_1 \cdot \cos \theta_2 + \sin \theta_1 \cdot \sin \theta_2 \cdot \cos(\varphi_1 \varphi_2)$ ),  $\frac{58}{59}$  где  $\theta$  широты (от  $-\frac{\pi}{2}$  до  $\frac{\pi}{2}$ ),  $\varphi$  долготы (от  $-\pi$  60 до  $\pi$ ).
- Объём шарового сегмента:  $V=\pi h^2(R-\frac{1}{3}h)$ , где <sup>63</sup> h— высота от вершины сектора до секущей плос- <sup>65</sup> кости
- Площадь поверхности шарового сегмента: S=68  $2\pi Rh$ , где h— высота.
- 4:15, 5:52, 72• Bell numbers: 0:1, 1:1,2:2, 3:5,8:4140, 9:21147, 7:877,10:115975,73 14:190899322, 75} 11:678570, 12:4213597, 13:27644437, 16:10480142147,  $17:82864869804,7611 pi(11 x) {$ 15:1382958545,  $18:682076806159, \ 19:5832742205057, \ 20:51724158235372, {}^{77}_{78}$  $22{:}4506715738447323, {}^{\cdot \cdot \cdot}_{\mathbf{79}} \}$ 21:474869816156751, 23:44152005855084346
- Catalan numbers: 0:1, 1:1, 2:2, 3:5, 4:14, 5:42, 6:132, 7:429,  $^{82}_{83}$  8:1430, 9:4862, 10:16796, 11:58786, 12:208012, 13:742900, 84 14:2674440, 15:9694845, 16:35357670, 17:129644790,  $^{85}_{86}$  18:477638700, 19:1767263190, 20:6564120420,  $^{87}_{87}$  21:24466267020, 22:91482563640, 23:343059613650,  $^{88}_{24}$  24:1289904147324, 25:4861946401452

## 22 math/stuff.cpp

```
1const int M = 1e6:
 2int phi[M];
 3void calcPhi() {
        for (int i = 1; i < M; ++i)
       for (int i = 1; 1 < m; ++1)
    phi[i] = i;
for (int j = 1; j < M; ++j)
    for (int i = 2 * j; i < M; i += j)
        phi[i] -= phi[j];</pre>
 8
9}
10 int inv[M];
11 void calcInv() {
12
        inv[1] = 1;
        for (int i = 2; i < M; ++i) {
   inv[i] = mul(sub(0, mod / i), inv[mod % i]);</pre>
14
15
             assert(mul(i, inv[i]) == 1);
16
17}
18 int gcd(int a, int b, int &x, int &y) {
        if (a == 0) {
 x = 0, y = 1;
19
20
21
22
        int x1, y1;
        int g = gcd(b % a, a, x1, y1);
x = y1 - x1 * (b / a);
        y = x1;
        assert(a * x + b * y == g);
        return g;
30 int crt(int mod1, int mod2, int rem1, int rem2) {
31    int r = (rem2 - (rem1 % mod2) + mod2) % mod2;
        int x, y;
int g = gcd(mod1, mod2, x, y);
assert(r % g == 0);
33
35
        x \%= mod2;
37
        if (x < 0)
             x += mod2;
38
39
40
        int ans = (x * (r / g)) % mod2;
        ans = ans * mod1 + rem1;
        assert(ans % mod1 == rem1):
        assert(ans % mod2 == rem2);
45
        return ans:
46 }
47
48// primes to N
49 const 11 n = 1000000000000LL;
50 \, \text{const} \, 11 \, L = 1000000;
51int small[L+1];
5211 large[L+1];
53 void calc_pi() {
        for (int i = 1; i <= L; ++i) {
    small[i] = i-1;</pre>
55
             large[i] = n / i - 1;
        for (11 p = 2; p <= L; ++p) {
    if (small[p] == small[p-1]) continue;</pre>
             int cntp = small[p-1];
             11 p2 = p*p;
11 np = n / p;
for (int i = 1; i <= min(L, n / p2); ++i) {</pre>
                  11 x = np / i;
if (x <= L) {</pre>
                        large[i] -= small[x] - cntp;
                     else {
                        large[i] -= large[p*i] - cntp;
             for (int i = L; i \ge p2; --i) {
                   small[i] -= small[i/p] - cntp;
             }
        if (x > L) return small[n/x];
        else return large[x];
81int main() {
        assert(phi[30] == 1 * 2 * 4);
        calcInv();
        int x, y;
        gcd(3, 5, x, y);
        gcd(15, 10, x, y);
crt(15, 13, 2, 5);
        crt(17, 3, 15, 2);
        return 0;
```

#### 23 strings/automaton.cpp

```
lint t[maxn][26], lnk[maxn], len[maxn];
 2int sz:
 3int last;
 5void init() {
       sz = 3;
       last = 1;
 7
       forn(i, 26) t[2][i] = 1;
len[2] = -1;
 9
       lnk[1] = 2;
10
11 }
12
13 void addchar(int c) {
       int nlast = sz++;
len[nlast] = len[last] + 1;
15
       int p = last;
for (; !t[p][c]; p = lnk[p]) {
16
17
           t[p][c] = nlast;
18
19
       int q = t[p][c];
if (len[p] + 1 == len[q]) {
20
21
            lnk[nlast] = q;
23
24
            int clone = sz++;
            len[clone] = len[p] + 1;
lnk[clone] = lnk[q];
lnk[q] = lnk[nlast] = clone;
25
26
27
28
            forn(i, 26) t[clone][i] = t[q][i];
29
            for (; t[p][c] == q; p = lnk[p]) {
30
                t[p][c] = clone;
31
32
33
       last = nlast;
34 }
35
36bool check(const string& s) {
37
       int v = 1;
       for (int c: s) {
38
           c -= 'a'
39
           if (!t[v][c]) return false;
40
41
           v = t[v][c];
42
       return true:
43
44 }
45
46 int main() {
47
       string s;
48
       cin >> s:
       init();
49
       for (int i: s) {
50
51
           addchar(i-'a');
52
53
       forn(i, s.length()) {
54
            assert(check(s.substr(i)));
55
       cout << sz << endl;</pre>
56
57
       return 0;
```

# 24 strings/duval manacher.cpp

```
Строка простая, если строго меньше всех суффиксов <=>
      наименьший циклический сдвиг - первый.
     Декомпозиция Линдона - разбиение s на w1, w2, ... wk -
      простые строки такие, что w1 >= w2 >= \dots wk.
 7int duval(string s) {
      s += s; //remove this to find Lyndon decomposition of s
       int n = s.size();
       int i = 0;
10
11
       int ans = 0;
       //while (i < n) { //for Lyndon decomposition while (i < n / 2) {
12
13
           ans = i;
int j = i + 1, k = i;
while (j < n && s[k] <= s[j]) {</pre>
14
15
16
                if (s[k] < s[j])
17
18
                    k = i;
19
                else
20
                    ++k;
                ++j;
21
           }
22
           while (i \leq k) {
23
                //s.substr(i, j - k) - //next prime string of Lyndon decomposition
24
25
                i += j - k;
26
           }
27
      }
28
29
      return ans:
30 }
31
32//actual odd length is (odd[i]*2-1) 33//actual even length is (even[i]*2)
34 void manacher(const string &s, vi &odd, vi &even) {
35
       int n = s.size();
36
       odd.resize(n);
      int c = -1, r = -1;
forn (i, n) {
37
38
           int k = (r <= i ? 0 : min(odd[2 * c - i], r - i));</pre>
39
40
           while (i + k < n \&\& i - k >= 0 \&\& s[i + k] == s[i - k])
               ++k;
41
           odd[i] = k;
42
43
           if (i + k > r)
                r = i + k, c = i;
44
      }
45
       c = -1, r = -1;
46
47
       even.resize(n - 1);
48
       forn (i, n - 1) \{
           int k = (r <= i ? 0 : min(even[2 * c - i], r - i));</pre>
49
           while (i + k + 1 < n && i - k >= 0 &&
50
                    s[i + k + 1] == s[i - k])
52
                ++k;
           even[i] = k;
53
54
           if (i + k > r)
55
                c = i, r = i + k;
56
      }
57}
59 void test() {
      vector<int> odd, even;
       string s = "aaaabbaaaaa";
       manacher(s, odd, even);
      for (int x: even)
          cerr << x << ' ';
       cerr << '\n';
65
66
       for (int x: odd)
         cerr << x << ' ';
      cerr << '\n';
// 1 2 1 0 5 0 1 2 2 1
68
       // 1 2 2 1 1 1 1 2 3 2 1
70
71 }
72
73int main() {
       cout << duval("ababcabab") << '\n'; // 5</pre>
74
       test();
75
```

56}

#### 25 strings/eertree.cpp

```
1 #include <bits/stdc++.h>
 2using namespace std;
 3 const int maxn = 5000100;
 4 const int inf = 1e9 + 1e5;
 6 char buf[maxn];
 7 char *s = buf + 1;
 8 int to[maxn][2];
 9int suff[maxn];
10 int len[maxn];
11 int sz;
12 int last;
13
14 const int odd = 1;
15 const int even = 2;
16 const int blank = 3;
18 inline void go(int &u, int pos) {
       while (u != blank && s[pos - len[u] - 1] != s[pos])
           u = suff[u];
21}
22
23 void add_char(int pos) {
24
       go(last, pos);
25
       int u = suff[last];
26
       go(u, pos);
       int c = s[pos] - 'a';
if (!to[last][c]) {
27
28
           to[last][c] = sz++;
len[sz - 1] = len[last] + 2;
29
30
            assert(to[u][c]);
31
32
           suff[sz - 1] = to[u][c];
33
       last = to[last][c];
34
35 }
36
37void init() {
       sz = 4;
38
       to[blank][0] = to[blank][1] = even;
39
       len[blank] = suff[blank] = inf;
40
       len[even] = 0, suff[even] = odd;
len[odd] = -1, suff[odd] = blank;
41
42
43
       last = 2:
44 }
45
46 void build() {
      init();
scanf("%s", s);
for (int i = 0; s[i]; ++i)
    add_char(i);
47
48
49
50
51 }
```

# ${\bf 26} \quad strings/suffix\_array.cpp$

```
1string s;
 3int sa[maxn], new_sa[maxn], cls[maxn], new_cls[maxn],
           cnt[maxn], lcp[maxn];
 5int n_cls;
 7void build() {
      n_cls = 256;
forn(i, n) {
           sa[i] = i;
10
           cls[i] = s[i];
11
12
13
       for (int d = 0; d < n; d = d? d*2 : 1) {
14
           forn(i, n) new_sa[i] = (sa[i] - d + n) % n;
forn(i, n_cls) cnt[i] = 0;
15
16
           forn(i, n) ++cnt[cls[i]];
17
           forn(i, n_cls) cnt[i+1] += cnt[i];
18
           for (int i = n-1; i >= 0;
19
                sa[--cnt[cls[new_sa[i]]] = new_sa[i];
20
21
           n cls = 0:
22
           forn(i, n) {
23
                if (i && (cls[sa[i]] != cls[sa[i-1]] ||
24
                         cls[(sa[i]+d)\%n] != cls[(sa[i-1]+d)\%n])) {
25
26
                     ++n_cls;
                }
27
               new_cls[sa[i]] = n_cls;
28
           }
29
           ++n cls:
30
31
           forn(i, n) cls[i] = new_cls[i];
       }
32
33
       // cls is also a inv perm of sa if a string is not cyclic
34
       // (i.e. a position of i-th lexicographical suffix) int val = 0;
35
36
      forn(i, n) {
   if (val) --val;
37
38
           if (val) --val,
if (cls[i] == n-1) continue;
int j = sa[cls[i] + 1];
39
40
           while (i+val != n \&\& j+val != n \&\& s[i+val] == s[j+val])
41
42
                ++val •
43
           lcp[cls[i]] = val;
       }
44
45 }
46
47 int main() {
48
      cin >> s;
       s += '$';
49
50
      n = s.length();
       build();
52
       forn(i, n) {
53
           cout << s.substr(sa[i]) << endl;</pre>
54
           cout << lcp[i] << endl;</pre>
55
       }
```

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#### 27 strings/ukkonen.cpp

```
1string s;
2const int alpha = 26;
4namespace SuffixTree {
      struct Node {
6
          Node *to[alpha];
          Node *lnk, *par;
8
          int 1, r;
10
           Node(int 1, int r): l(1), r(r) {
               memset(to, 0, sizeof(to));
lnk = par = 0;
12
13
14
      };
15
16
      Node *root, *blank, *cur;
17
      int pos;
18
19
      void init() {
20
          root = new Node(0, 0);
           blank = new Node(0, 0);
22
          forn (i, alpha)
              blank->to[i] = root;
          root->lnk = root->par = blank->lnk = blank->par = blank; 118
24
25
26
          pos = 0;
27
28
      int at(int id) {
30
          return s[id];
31
32
33
      void goDown(int 1, int r) {
34
          if (1 >= r)
35
              return;
          if (pos == cur->r) {
36
               int c = at(1);
37
38
               assert(cur->to[c]);
               cur = cur->to[c];
39
               pos = min(cur->r, cur->l + 1);
40
41
          } else {
42
               int delta = min(r - 1, cur->r - pos);
43
44
               1 += delta;
45
               pos += delta;
46
47
           goDown(1, r);
      }
48
49
50
      void goUp() {
          if (pos == cur->r \&\& cur->lnk) {
51
               cur = cur->lnk;
52
               pos = cur->r;
53
54
               return;
55
56
          int l = cur -> l, r = pos;
57
          cur = cur->par->lnk;
           pos = cur->r;
58
59
           goDown(l, r);
60
61
62
      void setParent(Node *a, Node *b) {
63
          assert(a);
64
           a->par = b;
65
           if (b)
66
               b->to[at(a->1)] = a;
67
68
69
      void addLeaf(int id) {
70
           Node *x = new Node(id, inf);
71
           setParent(x, cur);
72
73
74
      void splitNode() {
75
           assert(pos != cur->r);
76
           Node *mid = new Node(cur->1, pos);
77
           setParent(mid, cur->par);
           cur->1 = pos;
78
79
           setParent(cur, mid);
           cur = mid;
81
82
83
      bool canGo(int c) {
          if (pos == cur->r)
85
               return cur->to[c];
           return at(pos) == c;
86
87
88
89
      void fixLink(Node *&bad, Node *newBad) {
           if (bad)
               bad->lnk = cur;
```

```
bad = newBad;
       void addCharOnPos(int id) {
           Node *bad = 0;
           while (!canGo(at(id))) {
               if (cur->r != pos) {
    splitNode();
                    fixLink(bad, cur);
                    bad = cur;
               } else {
                   fixLink(bad, 0);
               addLeaf(id);
               goUp();
           fixLink(bad, 0);
           goDown(id, id + 1);
       int cnt(Node *u, int ml) {
           if (!u)
               return 0;
           int res = min(ml, u->r) - u->l;
           forn (i, alpha)
               res += cnt(u->to[i], ml);
           return res;
       }
       void build(int 1) {
           init();
           forn (i, 1)
               addCharOnPos(i);
       }
126 };
```

#### 28 structures/centroids.cpp

```
1 const int maxn = 100100;
 2const int LG = 18; //2*maxn <= 2^LG</pre>
 4vector<int> g[LG][maxn];
 5int rt[LG][maxn];
 7namespace Cenroids {
 9 int D;
10 int cnt[maxn];
11 int CENTER, BOUND;
13 void pre(int u, int prev = -1) {
       cnt[u] = 1;
       for (int v: g[D][u]) {
15
           if (v == prev)
17
                continue;
           pre(v, u);
            cnt[u] += cnt[v];
19
20
21}
23 void findCenter(int u, int prev = -1, int up = 0) {
24
       int worst = up;
       for (int v: g[D][u]) {
   if (v == prev)
25
26
27
                continue;
           findCenter(v, u, up + cnt[u] - cnt[v]);
worst = max(worst, cnt[v]);
28
29
30
31
       if (worst <= BOUND)</pre>
32
           CENTER = u;
33}
34
35 void markAll(int u, int prev = -1) {
       rt[D][u] = CENTER;
36
       for (int v: g[D][u]) {
   if (v == prev)
37
38
39
               continue:
            g[D + 1][u].push_back(v);
40
            g[D + 1][v].push_back(u);
41
           markAll(v, u);
42
43
44 }
45
46 void decompose(int u, int depth = 0) {
47
       D = depth;
48
       pre(u);
       CENTER = -1, BOUND = cnt[u] / 2;
49
50
       findCenter(u);
51
       assert(CENTER != -1);
52
       markAll(u);
       u = CENTER;
D = depth + 1;
53
54
       for (int v: g[D][u]) {
   auto it = find(g[D][v].begin(), g[D][v].end(), u);
55
56
            assert(it != g[\bar{D}][v].end());
57
58
            g[D][v].erase(it);
59
60
       for (int v: g[D][u])
61
            decompose(v, depth + 1);
62}
63
64};
```

### 29 structures/convex hull trick.cpp

```
2
       WARNING!!!
 3
       - finds maximum of A*x+B
       - double check max coords for int/long long overflow
 5
       - set min x query in put function
        - add lines with non-descending A coefficient
 8struct FastHull {
       int a[maxn];
       11 b[maxn];
10
11
       11 p[maxn];
12
       int c;
13
       FastHull(): c(0) {}
14
15
       11 get(int x) {
16
           if (c == 0)
17
18
                return -infl;
           int pos = upper_bound(p, p + c, x) - p - 1;
assert(pos >= 0);
19
20
           return (11) a[pos] * x + b[pos];
21
22
23
       ll divideCeil(ll p, ll q) {
24
           assert(q > 0);
if (p >= 0)
25
26
                return (p + q - 1) / q;
27
           return -((-p) / q);
28
       }
29
30
       void put(int A, 11 B) {
   while (c > 0) {
      if (a[c - 1] == A && b[c - 1] >= B)
31
32
33
34
                    return;
35
                11 pt = p[c - 1];
                if (a[c - 1] * pt + b[c - 1] < A * pt + B) {
36
37
                     --c:
38
                     continue;
39
40
                11 q = A - a[c - 1];
                11 np = divideCeil(b[c - 1] - B, q);
p[c] = np;
a[c] = A;
41
42
43
44
                b[c] = B;
45
                ++c;
46
                return;
47
           }
48
            if (c == 0) \{
49
                a[c] = A, b[c] = B;
50
                p[c] = -1e9; //min x query
52
                return;
           }
53
54
       }
56};
57
58struct SlowHull {
       vector<pair<int, 11>> v;
60
61
       void put(int a, ll b) {
62
           v.emplace_back(a, b);
63
64
       11 get(11 x) {
65
           11 best = -infl;
66
67
           for (auto p: v)
68
                best = max(best, p.first * x + p.second);
           return best;
69
70
       }
71};
72
73int main() {
       FastHull hull1;
74
       SlowHull hull2;
75
76
       vector<int> as;
       forn (ii, 10000)
77
           as.push_back(rand() % int(1e8));
78
       sort(as.begin(), as.end());
forn (ii, 10000) {
   int b = rand() % int(1e8);
79
80
81
           hull1.put(as[ii], b);
hull2.put(as[ii], b);
int x = rand() % int(2e8 + 1) - int(1e8);
82
83
84
85
           assert(hull1.get(x) == hull2.get(x));
       }
86
87 }
```

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#### 30structures/heavy light.cpp

```
1const int maxn = 100500;
2const int maxd = 17;
 4vector<int> g[maxn];
 6struct Tree {
      vector<int> t;
 8
      int base;
10
      Tree(): base(0) {
11
12
13
      Tree(int n) {
14
           base = 1;
15
           while (base < n)
16
               base *= 2;
17
           t = vector<int>(base * 2, 0);
18
19
20
       void put(int v, int delta) {
21
           assert(v < base);</pre>
22
           v += base;
23
           t[v] += delta;
24
           while (v > 1) {
25
               v /= 2;
26
                t[v] = max(t[v * 2], t[v * 2 + 1]);
27
28
30
       //Careful here: cr = 2 * maxn
       int get(int 1, int r, int v=1, int cl=0, int cr = 2*maxn) {
31
           cr = min(cr, base);
if (1 <= cl && cr <= r)
32
33
34
                return t[v];
35
           if (r <= cl || cr <= 1)
36
                return 0;
           int cc = (cl + cr) / 2;
37
           return max(get(1, r, v * 2, cl, cc),
get(1, r, v * 2 + 1, cc, cr));
38
39
40
      }
41};
42
43 namespace HLD {
       int h[maxn];
44
45
       int timer:
       int in[maxn], out[maxn], cnt[maxn];
46
       int p[maxd][maxn];
47
48
       int vroot[maxn];
49
      int vpos[maxn];
50
       int ROOT;
51
      Tree tree[maxn];
52
      void dfs1(int u, int prev) {
53
           p[0][u] = prev;
54
           in[u] = timer++;
55
           cnt[u] = 1;
56
57
           for (int v: g[u]) {
58
                if (v == prev)
                    continue;
59
                h[v] = h[u] + 1;
60
61
                dfs1(v, u);
62
                cnt[u] += cnt[v];
63
64
           out[u] = timer;
65
66
67
       int dfs2(int u, int prev) {
68
           int to = -1;
69
           for (int v: g[u]) {
70
                if (v == prev)
                    continue;
71
72
                if (to == -1 || cnt[v] > cnt[to])
73
                     to = v;
74
           }
75
           int len = 1;
           for (int v: g[u]) {
   if (v == prev)
76
77
78
                     continue;
79
                if (to == v) {
                    vpos[v] = vpos[u] + 1;
vroot[v] = vroot[u];
81
                     len += dfs2(v, u);
82
83
                     vroot[v] = v;
                     vpos[v] = 0;
86
87
                     dfs2(v, u);
88
89
           if (vroot[u] == u)
                tree[u] = Tree(len);
```

```
return len;
       void init(int n) {
           timer = 0;
           h[ROOT] = 0;
           dfs1(ROOT, ROOT);
           forn (d, maxd -
              forn (i, n)
                  p[d + 1][i] = p[d][p[d][i]];
           vroot[ROOT] = ROOT;
           vpos[ROOT] = 0;
           dfs2(ROOT, ROOT);
           //WARNING: init all trees
       bool isPrev(int u, int v) {
          return in[u] <= in[v] && out[v] <= out[u];
       int lca(int u, int v) {
           for (int d = maxd - 1; d >= 0; --d)
               if (!isPrev(p[d][u], v))
           u = p[d][u];
if (!isPrev(u, v))
              u = p[0][u];
           return u:
       //for\ each\ v:\ h[v] >= toh
       int getv(int u, int toh) {
          int res = 0;
while (h[u] >= toh) {
              res = max(res, tree[rt].get(1, r));
               if (rt == ROOT)
                  break:
               u = p[0][rt];
          }
           return res;
      }
       int get(int u, int v) {
           int w = lca(u, v);
           return max(getv(u, h[w]), getv(v, h[w] + 1));
       void put(int u, int val) {
           int rt = vroot[u];
int pos = vpos[u];
           tree[rt].put(pos, val);
       }
145};
```

# 31 structures/linkcut.cpp

```
1namespace LinkCut {
 3typedef struct _node {
      _node *1, *r, *p, *pp;
int size; bool rev;
       _node();
 8
       explicit _node(nullptr_t) {
           1 = r = p = pp = this;
size = rev = 0;
10
11
12
13
       void push() {
14
           if (rev) {
               1->rev ^= 1; r->rev ^= 1;
15
16
               rev = 0; swap(1,r);
17
18
19
20
      void update();
21}* node;
22
23 node None = new _node(nullptr);
24 node v2n[maxn];
26_node::_node(){
      1 = r = p = pp = None;
      size = 1; rev = false;
28
30
31void _node::update() {
      size = (this != None) + 1->size + r->size;
      1->p = r->p = this;
33
34}
35
36 void rotate(node v) {
      assert(v != None && v->p != None);
37
      assert(!v->rev);
38
39
      assert(!v->p->rev);
      node u = v - p;
40
      if (v == u \rightarrow 1)
41
           `u->1 = v->r, v->r = u;
42
43
       else
          u->r = v->1, v->1 = u;
44
      swap(u->p,v->p);
45
      swap(v->pp,u->pp);
if (v->p != None) {
46
47
           assert(v->p->1 == u || v->p->r == u);
if (v->p->r == u)
48
49
50
               v->p->r = v;
51
           else
               v->p->1 = v;
52
53
54
      u->update();
55
      v->update();
56 }
57
58 void bigRotate(node v) {
      assert(v->p != None);
59
       v->p->p
60
61
      v->p->push();
62
      v->push();
      if (v->p->p != None) {
    if ((v->p->1 == v) ^ (v->p->r == v->p))
63
64
65
               rotate(v->p);
66
           else
67
               rotate(v);
68
69
      rotate(v);
70}
71
72 inline void splay(node v) {
73
      while (v-p != None)
74
           bigRotate(v);
75}
76
77inline void splitAfter(node v) {
78
      v->push();
79
       splay(v);
       v->r->p = None;
      v->r->pp = v;
v->r = None;
81
82
83
       v->update();
84 }
86 void expose(int x) {
      node v = v2n[x];
87
       splitAfter(v);
       while (v->pp != None) {
89
          assert(v->p == None);
           splitAfter(v->pp);
```

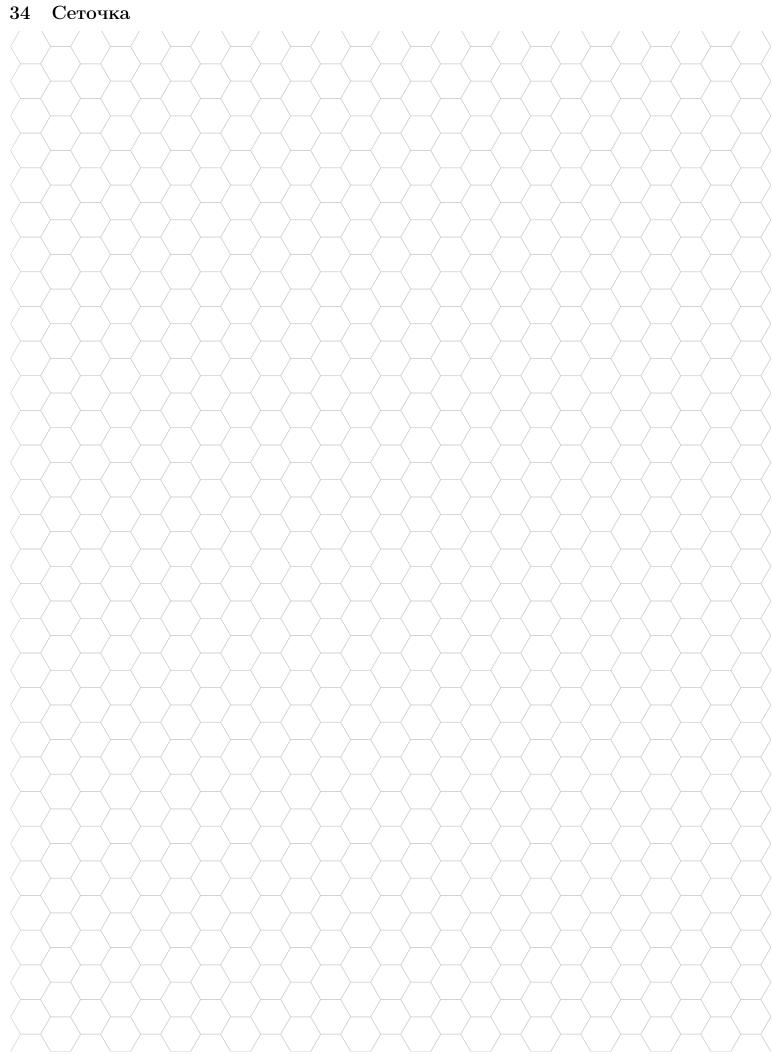
```
assert(v->pp->r == None);
assert(v->pp->p == None);
             assert(!v->pp->rev);
 95
             v \rightarrow pp \rightarrow r = v;
             v->pp->update();
v = v->pp;
 97
             v->r->pp = None;
 99
100
        assert(v->p == None);
101
        splay(v2n[x]);
102}
103
104inline void makeRoot(int x) {
105
        expose(x);
        assert(v2n[x]->p == None);
        assert(v2n[x]->pp == None);
assert(v2n[x]->r == None);
107
108
109
        v2n[x]->rev ^= 1;
110}
111
112 inline void link(int x, int y) {
        makeRoot(x);
v2n[x]->pp = v2n[y];
113
114
115 }
116
117 inline void cut(int x, int y) {
        expose(x);
118
        splay(v2n[y]);
119
        if (v2n[y]-pp != v2n[x]) {
120
             swap(x,y);
121
122
             expose(x);
123
             splay(v2n[y]);
             assert(v2n[y] - pp == v2n[x]);
124
125
        v2n[y]-pp = None;
126
127}
128
129 inline int get(int x, int y) {
130    if (x == y)
131
             return 0;
132
        makeRoot(x);
133
        expose(y);
134
        expose(x);
135
        splay(v2n[y]);
136
        if (v2n[y]-pp != v2n[x])
137
             return -1;
138
        return v2n[y]->size;
139}
140
141}
```

#### 32 structures/ordered set.cpp

```
1 #include <ext/pb_ds/assoc_container.hpp>
2 #include <ext/pb_ds/tree_policy.hpp>
 4typedef __gnu_pbds::tree<int, __gnu_pbds::null_type,</pre>
          std::less<int>,
           __gnu_pbds::rb_tree_tag,
           __gnu_pbds::tree_order_statistics_node_update> oset;
9 #include <iostream>
11int main() {
12
      oset X;
13
      X.insert(1);
      X.insert(2);
14
15
      X.insert(4);
16
      X.insert(8);
17
      X.insert(16);
18
      std::cout << *X.find_by_order(1) << std::endl; // 2
19
      std::cout << *X.find_by_order(2) << std::endl; // 4
20
      std::cout << *X.find_by_order(4) << std::endl; // 16
std::cout << std::boolalpha <</pre>
21
22
23
           (end(X)==X.find_by_order(6)) << std::endl; // true</pre>
24
      25
26
      std::cout << X.order_of_key(3) << std::endl;
std::cout << X.order_of_key(4) << std::endl;
27
28
      std::cout << X.order_of_key(400) << std::endl; // 5
29
```

#### 33 structures/treap.cpp

```
1struct node {
      int x, y;
2
3
      node *1, *r;
      node(int x) : x(x), y(rand()), 1(r=NULL) {}
5};
7void split(node *t, node *&l, node *&r, int x) {
      if (!t) return (void)(l=r=NULL);
8
9
      if (x \le t->x) {
10
          split(t->1, 1, t->1, x), r = t;
11
      } else {
12
          split(t->r, t->r, r, x), 1 = t;
13
14}
15
16 node *merge(node *1, node *r) {
17
      if (!1) return r;
      if (!r) return 1;
19
      if (1->y > r->y)
         1->r = merge(1->r, r);
20
          return 1;
      } else {
          r->1 = merge(1, r->1);
24
          return r;
25
26}
27
28 node *insert(node *t, node *n) {
29
     node *1, *r;
      split(t, 1, r, n->x);
30
      return merge(1, merge(n, r));
31
32}
33
34node *insert(node *t, int x) {
35
     return insert(t, new node(x));
36}
37
38 node *fast_insert(node *t, node *n) {
     if (!t) return n;
39
      node *root = t;
40
      while (true) {
41
         if (n->x < t->x) {
42
              if (!t->1 | | t->1->y < n->y) {
43
                  split(t->1, n->1, n->r, n->x), t->1 = n;
44
45
                  break;
              } else {
46
47
                  t = t->1;
              }
48
          49
50
51
                  split(t->r, n->l, n->r, n->x), t->r = n;
52
                  break;
53
              } else {
54
                  t = t->r;
55
          }
56
57
      }
58
      return root;
59 }
60
61node *fast_insert(node *t, int x) {
62
      return fast_insert(t, new node(x));
63}
64
65int main() {
      node *t = NULL;
66
      forn(i, 1000000) {
          int x = rand();
68
69
          t = fast_insert(t, x);
70
```



# 35 Сеточка

