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1 Strategy.txt

- 1 - Проверить руками сэмплы
- Подумать как дебагать после написания
- 2 - Выписать сложные формулы и все +-1
- 2 - Проверить имена файлов
- Прогнать сэмплы
- 3 - Переполнения int, переполнения long long
- Выход за границу массива: _GLIBCXX_DEBUG
- 4 - Переполнения по модулю: в
 - ↪ псевдо-онлайн-генераторе, в функциях-обертках
- 5 - Проверить мультитест на разных тестах
- 6 - Прогнать минимальный по каждому параметру тест
- Прогнать псевдо-максимальный тест(немного
- 6 ↪ чисел, но очень большие или очень маленькие)
- Представить что не зайдет и заранее написать
 - ↪ assert'ы, прогнать слегка модифицированные
 - ↪ тесты
- 7 - cout.precision: в том числе в интерактивных
 - ↪ задачах
- 8 - Удалить debug-output, отсеечения для тестов,
 - ↪ вернуть оригинальный main, удалить
 - ↪ _GLIBCXX_DEBUG
- 9 - Вердикт может врать
- 10 - Если много тестов(>3), дописать в конец каждого
 - ↪ теста ответ, чтобы не забыть
- (WA) Потестить не только ответ, но и содержимое
 - ↪ значимых массивов, переменных
- (WA) Изменить тест так, чтобы ответ не менялся:
 - ↪ поменять координаты местами, сжать/растянуть
 - ↪ координаты, поменять ROOT дерева
- (WA) Подвигать размер блока в корневой или
 - ↪ битсете
- (WA) Поставить assert'ы, возможно написать
 - ↪ чекер с assert'ом
- (WA) Проверить, что программа не печатает
 - ↪ что-либо неожиданное, что должно попадать под
 - ↪ PE: inf - 2, не лекс. мин. решение, одинаковые
 - ↪ числа вместо разных, неправильное количество
 - ↪ чисел, пустой ответ, перечитать output format
- (TL) cin -> scanf -> getchar
- (TL) Упихать в кэш большие массивы, поменять
 - ↪ местами for'ы или измерения массива
- (RE) Проверить формулы на деление на 0, выход
 - ↪ за область определения(sqrt(-eps), acos(1 +
 - ↪ eps))

2 flows/globalcut.cpp

```

1#include <bits/stdc++.h>
2using namespace std;
3#define forn(i,n) for (int i = 0; i < int(n); ++i)
4const int inf = 1e9 + 1e5;
5
6const int maxn = 505;
7namespace StoerWagner {
8    int g[maxn][maxn];
9    int dist[maxn];
10    bool used[maxn];
11    int n;
12
13    void addEdge(int u, int v, int c) {
14        g[u][v] += c;
15        g[v][u] += c;
16    }
17
18    int run() {
19        vector<int> vertices;
20        forn (i, n)
21            vertices.push_back(i);
22        int mincut = inf;
23        while (vertices.size() > 1) {
24            int u = vertices[0];
25            for (auto v: vertices) {
26                used[v] = false;
27                dist[v] = g[u][v];
28            }
29            used[u] = true;
30            forn (ii, vertices.size() - 2) {
31                for (auto v: vertices)
32                    if (!used[v])
33                        if (used[u] || dist[v] > dist[u])
34                            u = v;
35                used[u] = true;
36                for (auto v: vertices)
37                    if (!used[v])
38                        dist[v] += g[u][v];
39            }
40            int t = -1;
41            for (auto v: vertices)
42                if (!used[v])
43                    t = v;
44            assert(t != -1);
45            mincut = min(mincut, dist[t]);
46            vertices.erase(find(vertices.begin(), vertices.end(), t));
47            for (auto v: vertices)
48                addEdge(u, v, g[v][t]);
49        }
50        return mincut;
51    }
52};
53
54int main() {
55    StoerWagner::n = 4;
56    StoerWagner::addEdge(0, 1, 5);
57    StoerWagner::addEdge(2, 3, 5);
58    StoerWagner::addEdge(1, 2, 4);
59    cerr << StoerWagner::run() << '\n';
60}

```

3 flows/hungary.cpp

```

1// left half is the smaller one
2namespace Hungary {
3    const int maxn = 505;
4    int a[maxn][maxn];
5    int p[2][maxn];
6    int match[maxn];
7    bool used[maxn];
8    int from[maxn];
9    int mind[maxn];
10    int n, m;
11
12    int hungary(int v) {
13        used[v] = true;
14        int u = match[v];
15        int best = -1;
16        forn (i, m + 1) {
17            if (used[i])
18                continue;
19            int nw = a[u][i] - p[0][u] - p[1][i];
20            if (nw <= mind[i]) {
21                mind[i] = nw;
22                from[i] = v;
23            }
24            if (best == -1 || mind[best] > mind[i])
25                best = i;
26        }
27        v = best;
28        int delta = mind[best];
29        forn (i, m + 1) {
30            if (used[i]) {
31                p[1][i] -= delta;
32                p[0][match[i]] += delta;
33            } else
34                mind[i] -= delta;
35        }
36        if (match[v] == -1)
37            return v;
38        return hungary(v);
39    }
40
41    void check() {
42        int edges = 0, res = 0;
43        forn (i, m)
44            if (match[i] != -1) {
45                ++edges;
46                assert(p[0][match[i]] + p[1][i] == a[match[i]][i]);
47                res += a[match[i]][i];
48            } else
49                assert(p[1][i] == 0);
50        assert(res == -p[1][m]);
51        forn (i, n) forn (j, m)
52            assert(p[0][i] + p[1][j] <= a[i][j]);
53    }
54
55    int run() {
56        forn (i, n)
57            p[0][i] = 0;
58        forn (i, m + 1) {
59            p[1][i] = 0;
60            match[i] = -1;
61        }
62        forn (i, n) {
63            match[m] = i;
64            fill(used, used + m + 1, false);
65            fill(mind, mind + m + 1, inf);
66            fill(from, from + m + 1, -1);
67            int v = hungary(m);
68            while (v != m) {
69                int w = from[v];
70                match[v] = match[w];
71                v = w;
72            }
73        }
74        check();
75        return -p[1][m];
76    }
77};

```

4 flows/mincost.cpp

```

1 namespace MinCost {
2     const ll infc = 1e12;
3
4     struct Edge {
5         int to;
6         ll c, f, cost;
7
8         Edge(int to, ll c, ll cost): to(to), c(c), f(0), cost(cost) {}
9     };
10 };
11
12 int N, S, T;
13 int totalFlow;
14 ll totalCost;
15 const int maxn = 505;
16 vector<Edge> edge;
17 vector<int> g[maxn];
18
19 void addEdge(int u, int v, ll c, ll cost) {
20     g[u].push_back(edge.size());
21     edge.emplace_back(v, c, cost);
22     g[v].push_back(edge.size());
23     edge.emplace_back(u, 0, -cost);
24 }
25
26 ll dist[maxn];
27 int fromEdge[maxn];
28
29 bool inQueue[maxn];
30 bool fordBellman() {
31     forn (i, N)
32         dist[i] = infc;
33     dist[S] = 0;
34     inQueue[S] = true;
35     vector<int> q;
36     q.push_back(S);
37     for (int ii = 0; ii < int(q.size()); ++ii) {
38         int u = q[ii];
39         inQueue[u] = false;
40         for (int e: g[u]) {
41             if (edge[e].f == edge[e].c)
42                 continue;
43             int v = edge[e].to;
44             ll nw = edge[e].cost + dist[u];
45             if (nw >= dist[v])
46                 continue;
47             dist[v] = nw;
48             fromEdge[v] = e;
49             if (!inQueue[v]) {
50                 inQueue[v] = true;
51                 q.push_back(v);
52             }
53         }
54     }
55     return dist[T] != infc;
56 }
57
58 ll pot[maxn];
59 bool dikstra() {
60     priority_queue<pair<ll, int>, vector<pair<ll, int>>,
61     ↪ greater<pair<ll, int>>> q;
62     forn (i, N)
63         dist[i] = infc;
64     dist[S] = 0;
65     q.emplace(dist[S], S);
66     while (!q.empty()) {
67         int u = q.top().second;
68         ll cdist = q.top().first;
69         q.pop();
70         if (cdist != dist[u])
71             continue;
72         for (int e: g[u]) {
73             int v = edge[e].to;
74             if (edge[e].c == edge[e].f)
75                 continue;
76             ll w = edge[e].cost + pot[u] - pot[v];
77             assert(w >= 0);
78             ll ndist = w + dist[u];
79             if (ndist >= dist[v])
80                 continue;
81             dist[v] = ndist;
82             fromEdge[v] = e;
83             q.emplace(dist[v], v);
84         }
85     }
86     if (dist[T] == infc)
87         return false;
88     forn (i, N) {
89         if (dist[i] == infc)
90             continue;
91         pot[i] += dist[i];
92     }
93     return true;
94 }
95
96 bool push() {
97     //2 variants
98     //if (!fordBellman())
99     if (!dikstra())
100         return false;
101     ++totalFlow;
102     int u = T;
103     while (u != S) {
104         int e = fromEdge[u];
105         totalCost += edge[e].cost;
106         edge[e].f++;
107         edge[e ^ 1].f--;
108         u = edge[e ^ 1].to;
109     }
110     return true;
111 }
112
113 int main() {
114     MinCost::N = 3, MinCost::S = 1, MinCost::T = 2;
115     MinCost::addEdge(1, 0, 3, 5);
116     MinCost::addEdge(0, 2, 4, 6);
117     while (MinCost::push());
118     cout << MinCost::totalFlow << ' ' << MinCost::totalCost << '\n';
119     ↪ //3 33

```

5 geometry/primitives.cpp

```

1#include <bits/stdc++.h>
2#define forn(i, n) for (int i = 0; i < int(n); ++i)
3using namespace std;
4typedef long double ld;
5
6const ld eps = 1e-9;
7
8bool eq(ld a, ld b) { return fabsl(a - b) < eps; }
9bool le(ld a, ld b) { return b - a > -eps; }
10bool ge(ld a, ld b) { return a - b > -eps; }
11bool lt(ld a, ld b) { return b - a > eps; }
12bool gt(ld a, ld b) { return a - b > eps; }
13ld sqr(ld x) { return x * x; }
14
15inline void gassert(bool expr) {
16#ifdef LOCAL
17    assert(expr);
18#endif
19}
20
21struct pt {
22    ld x, y;
23
24    pt operator+(const pt &p) const { return pt{x + p.x, y + p.y}; }
25    pt operator-(const pt &p) const { return pt{x - p.x, y - p.y}; }
26    ld operator*(const pt &p) const { return x * p.x + y * p.y; }
27    ld operator%(const pt &p) const { return x * p.y - y * p.x; }
28
29    pt operator*(const ld &a) const { return pt{x * a, y * a}; }
30    pt operator/(const ld &a) const { gassert(!eq(a, 0)); return pt{x
↵    a, y / a}; }
31    void operator*=(const ld &a) { x *= a, y *= a; }
32    void operator/=(const ld &a) { gassert(!eq(a, 0)); x /= a, y /= a;
↵    }
33
34    bool operator<(const pt &p) const {
35        if (eq(x, p.x)) return lt(y, p.y);
36        return x < p.x;
37    }
38
39    bool operator==(const pt &p) const { return eq(x, p.x) && eq(y,
↵    p.y); }
40    bool operator!=(const pt &p) const { return !(*this == p); }
41
42    pt rot() { return pt{-y, x}; }
43    ld abs() const { return hypotl(x, y); }
44    ld abs2() const { return x * x + y * y; }
45};
46
47istream &operator>>(istream &in, pt &p) { return in >> p.x >> p.y; }
48ostream &operator<<(ostream &out, const pt &p) { return out << p.x <<
↵    ' ' << p.y; }
49
50//WARNING! do not forget to normalize vector (a,b)
51struct line {
52    ld a, b, c;
53
54    line(pt p1, pt p2) {
55        gassert(p1 != p2);
56        pt n = (p2 - p1).rot();
57        n /= n.abs();
58        a = n.x, b = n.y;
59        c = -(n * p1);
60    }
61
62    line(ld _a, ld _b, ld _c): a(_a), b(_b), c(_c) {
63        ld d = pt{a, b}.abs();
64        gassert(!eq(d, 0));
65        a /= d, b /= d, c /= d;
66    }
67
68    ld signedDist(pt p) {
69        return p * pt{a, b} + c;
70    }
71};
72
73ld pointSegmentDist(pt p, pt a, pt b) {
74    ld res = min((p - a).abs(), (p - b).abs());
75    if (a != b && ge((p - a) * (b - a), 0) && ge((p - b) * (a - b), 0))
76        res = min(res, fabsl((p - a) % (b - a)) / (b - a).abs());
77    return res;
78}
79
80pt linesIntersection(line l1, line l2) {
81    ld D = l1.a * l2.b - l1.b * l2.a;
82    if (eq(D, 0)) {
83        if (eq(l1.c, l2.c)) {
84            //equal lines
85        } else {
86            //no intersection
87        }
88    }
89    ld dx = -l1.c * l2.b + l1.b * l2.c;
90    ld dy = -l1.a * l2.c + l1.c * l2.a;
91    pt res{dx / D, dy / D};
92
93    gassert(eq(l1.signedDist(res), 0));
94    gassert(eq(l2.signedDist(res), 0));
95    return res;
96}
97bool pointInsideSegment(pt p, pt a, pt b) {
98    if (!eq((p - a) % (b - a), 0))
99        return false;
100    return le((a - p) * (b - p), 0);
101}
102
103bool checkSegmentIntersection(pt a, pt b, pt c, pt d) {
104    if (eq((a - b) % (c - d), 0)) {
105        if (pointInsideSegment(a, c, d) || pointInsideSegment(b, c, d)
↵    ||
106            pointInsideSegment(c, a, b) || pointInsideSegment(d, a,
↵    b)) {
107            //intersection of parallel segments
108            return true;
109        }
110        return false;
111    }
112
113    ld s1, s2;
114
115    s1 = (c - a) % (b - a);
116    s2 = (d - a) % (b - a);
117    if (gt(s1, 0) && gt(s2, 0))
118        return false;
119    if (lt(s1, 0) && lt(s2, 0))
120        return false;
121
122    swap(a, c), swap(b, d);
123
124    s1 = (c - a) % (b - a);
125    s2 = (d - a) % (b - a);
126    if (gt(s1, 0) && gt(s2, 0))
127        return false;
128    if (lt(s1, 0) && lt(s2, 0))
129        return false;
130
131    return true;
132}
133
134//WARNING! run checkSegmentIntersection before and process parallel case
↵    manually
135pt segmentsIntersection(pt a, pt b, pt c, pt d) {
136    ld S = (b - a) % (d - c);
137    ld s1 = (c - a) % (d - a);
138    return a + (b - a) / S * s1;
139}
140
141vector<pt> circlesIntersection(pt a, ld r1, pt b, ld r2) {
142    ld d2 = (a - b).abs2();
143    ld d = (a - b).abs();
144
145    if (a == b && eq(r1, r2)) {
146        //equal circles
147    }
148    if (lt(sqr(r1 + r2), d2) || gt(sqr(r1 - r2), d2)) {
149        //empty intersection
150        return {};
151    }
152    int num = 2;
153    if (eq(sqr(r1 + r2), d2) || eq(sqr(r1 - r2), d2))
154        num = 1;
155    ld cosa = (sqr(r1) + d2 - sqr(r2)) / ld(2 * r1 * d);
156    ld oh = cosa * r1;
157    pt h = a + ((b - a) / d * oh);
158    if (num == 1)
159        return {h};
160    ld hp = sqrtl(max(0.L, 1 - cosa * cosa)) * r1;
161
162    pt w = ((b - a) / d * hp).rot();
163    return {h + w, h - w};
164}
165
166//a is circle center, p is point
167vector<pt> circleTangents(pt a, ld r, pt p) {
168    ld d2 = (a - p).abs2();
169    ld d = (a - p).abs();
170
171    if (gt(sqr(r), d2)) {
172        //no tangents
173        return {};
174    }
175    if (eq(sqr(r), d2)) {
176        //point lies on circle - one tangent
177        return {p};
178    }
179
180    pt B = p - a;
181    pt H = B * sqr(r) / d2;
182    ld h = sqrtl(d2 - sqr(r)) * ld(r) / d;
183    pt w = (B / d * h).rot();
184    H = H + a;
185    return {H + w, H - w};
186}
4

```

```

187
188 vector<pt> lineCircleIntersection(line l, pt a, ld r) {
189     ld d = l.signedDist(a);
190     if (gt(fabs1(d), r))
191         return {};
192     pt h = a - pt{l.a, l.b} * d;
193     if (eq(fabs1(d), r))
194         return {h};
195     pt w = pt{l.a, l.b}.rot() * sqrt1(max<ld>(0, sqr(r) - sqr(d)));
196     return {h + w, h - w};
197 }
198
199 //modified magic from e-mazz
200 vector<line> commonTangents(pt a, ld r1, pt b, ld r2) {
201     if (a == b && eq(r1, r2)) {
202         //equal circles
203         return {};
204     }
205     vector<line> res;
206     pt c = b - a;
207     ld z = c.abs2();
208     for (int i = -1; i <= 1; i += 2)
209         for (int j = -1; j <= 1; j += 2) {
210             ld r = r2 * j - r1 * i;
211             ld d = z - sqr(r);
212             if (lt(d, 0))
213                 continue;
214             d = sqrt1(max<ld>(0, d));
215             pt magic = pt{r, d} / z;
216             line l(magic * c, magic % c, r1 * i);
217             l.c -= pt{l.a, l.b} * a;
218             res.push_back(l);
219         }
220     return res;
221 }

```

6 geometry/svg.cpp

```

1 struct SVG {
2     FILE *out;
3     ld sc = 50;
4
5     void open() {
6         out = fopen("image.svg", "w");
7         fprintf(out, "<svg xmlns='http://www.w3.org/2000/svg'
↪ viewBox='-1000 -1000 2000 2000'>\n");
8     }
9
10    void line(pt a, pt b) {
11        a = a * sc, b = b * sc;
12        fprintf(out, "<line x1='%Lf' y1='%Lf' x2='%Lf' y2='%Lf'
↪ stroke='black'/>\n", a.x, -a.y, b.x, -b.y);
13    }
14
15    void circle(pt a, ld r = -1) {
16        r = (r == -1 ? 10 : sc * r);
17        a = a * sc;
18        fprintf(out, "<circle cx='%Lf' cy='%Lf' r='%Lf'
↪ fill='red'/>\n", a.x, -a.y, r);
19    }
20
21    void text(pt a, string s) {
22        a = a * sc;
23        fprintf(out, "<text x='%Lf' y='%Lf'
↪ font-size='10px'>%s</text>\n", a.x, -a.y, s.c_str());
24    }
25
26    void close() {
27        fprintf(out, "</svg>\n");
28        fclose(out);
29    }
30 } svg;

```

7 graphs/2sat.cpp

```

1const int maxn = 200100; //2 x number of variables
2
3namespace TwoSAT {
4    int n; //number of variables
5    bool used[maxn];
6    vector<int> g[maxn];
7    vector<int> gr[maxn];
8    int comp[maxn];
9    int res[maxn];
10
11    void addEdge(int u, int v) { //u or v
12        g[u].push_back(v ^ 1);
13        g[v].push_back(u ^ 1);
14        gr[u ^ 1].push_back(v);
15        gr[v ^ 1].push_back(u);
16    }
17
18    vector<int> ord;
19    void dfs1(int u) {
20        used[u] = true;
21        for (int v: g[u]) {
22            if (used[v])
23                continue;
24            dfs1(v);
25        }
26        ord.push_back(u);
27    }
28
29    int COL = 0;
30    void dfs2(int u) {
31        used[u] = true;
32        comp[u] = COL;
33        for (int v: gr[u]) {
34            if (used[v])
35                continue;
36            dfs2(v);
37        }
38    }
39
40    void mark(int u) {
41        res[u / 2] = u % 2;
42        used[u] = true;
43        for (int v: g[u]) {
44            if (used[v])
45                continue;
46            mark(v);
47        }
48    }
49
50    bool run() {
51        fill(res, res + 2 * n, -1);
52        fill(used, used + 2 * n, false);
53        for (i, 2 * n)
54            if (!used[i])
55                dfs1(i);
56        reverse(ord.begin(), ord.end());
57        assert((int) ord.size() == (2 * n));
58        fill(used, used + 2 * n, false);
59        for (int u: ord) if (!used[u]) {
60            dfs2(u);
61            ++COL;
62        }
63        for (i, n)
64            if (comp[i * 2] == comp[i * 2 + 1])
65                return false;
66
67        reverse(ord.begin(), ord.end());
68        fill(used, used + 2 * n, false);
69        for (int u: ord) {
70            if (res[u / 2] != -1) {
71                continue;
72            }
73            mark(u);
74        }
75        return true;
76    }
77};
78
79int main() {
80    TwoSAT::n = 2;
81    TwoSAT::addEdge(0, 2); //x or y
82    TwoSAT::addEdge(0, 3); //x or !y
83    TwoSAT::addEdge(3, 3); //!y or !y
84    assert(TwoSAT::run());
85    cout << TwoSAT::res[0] << ' ' << TwoSAT::res[1] << '\n'; //1 0
86}

```

8 math/fft_recursive.cpp

```

1const int sz = 1<<20;
2
3int revb[sz];
4vector<base> ang[21];
5
6void init(int n) {
7    int lg = 0;
8    while ((1<<lg) != n) {
9        ++lg;
10    }
11    for (i, n) {
12        revb[i] = (revb[i>>1]>>1)^((i&1)<<(lg-1));
13    }
14
15    ld e = M_PI * 2 / n;
16    ang[lg].resize(n);
17    for (i, n) {
18        ang[lg][i] = { cos(e * i), sin(e * i) };
19    }
20
21    for (int k = lg - 1; k >= 0; --k) {
22        ang[k].resize(1 << k);
23        for (i, 1<<k) {
24            ang[k][i] = ang[k+1][i*2];
25        }
26    }
27}
28
29void fft_rec(base *a, int lg, bool rev) {
30    if (lg == 0) {
31        return;
32    }
33    int len = 1 << (lg - 1);
34    fft_rec(a, lg-1, rev);
35    fft_rec(a+len, lg-1, rev);
36
37    for (i, len) {
38        base w = ang[lg][i];
39        if (rev) w.im *= -1;
40        base u = a[i];
41        base v = a[i+len] * w;
42        a[i] = u + v;
43        a[i+len] = u - v;
44    }
45}
46
47void fft(base *a, int n, bool rev) {
48    for (i, n) {
49        int j = revb[i];
50        if (i < j) swap(a[i], a[j]);
51    }
52    int lg = 0;
53    while ((1<<lg) != n) {
54        ++lg;
55    }
56    fft_rec(a, lg, rev);
57    if (rev) for (i, n) {
58        a[i] = a[i] * (1.0 / n);
59    }
60}
61
62const int maxn = 1050000;
63
64int n;
65base a[maxn];
66base b[maxn];
67
68void test() {
69    int n = 8;
70    init(n);
71    base a[8] = {1,3,5,2,4,6,7,1};
72    fft(a, n, 0);
73    for (i, n) cout << a[i].re << " "; cout << endl;
74    for (i, n) cout << a[i].im << " "; cout << endl;
75    // 29 -5.82843 -7 -0.171573 5 -0.171573 -7 -5.82843
76    // 0 -3.41421 6 0.585786 0 -0.585786 -6 3.41421
77}

```

9 math/golden_search.cpp

```
1ld f(ld x) {
2    return 5 * x * x + 100 * x + 1; // -10 is minimum
3}
4
5ld goldenSearch(ld l, ld r) {
6    ld phi = (1 + sqrtl(5)) / 2;
7    ld resphi = 2 - phi;
8    ld x1 = l + resphi * (r - l);
9    ld x2 = r - resphi * (r - l);
10   ld f1 = f(x1);
11   ld f2 = f(x2);
12   forn (iter, 60) {
13       if (f1 < f2) {
14           r = x2;
15           x2 = x1;
16           f2 = f1;
17           x1 = l + resphi * (r - l);
18           f1 = f(x1);
19       } else {
20           l = x1;
21           x1 = x2;
22           f1 = f2;
23           x2 = r - resphi * (r - l);
24           f2 = f(x2);
25       }
26   }
27   return (x1 + x2) / 2;
28}
29
30int main() {
31    std::cout << goldenSearch(-100, 100) << '\n';
32}
```

10 math/numbers.txt

Simpson's numerical integration:
integral from a to b $f(x) dx =$
 $(b - a) / 6 * (f(a) + 4 * f((a + b) / 2) + f(b))$

Gauss 5-th order numerical integration:
integral from -1 to 1
 $x_1, x_3 = \pm \sqrt{0.6}$, $x_2 = 0$
 $a_1, a_3 = 5/9$, $a_2 = 8/9$

large primes: $10^{18} + 3$, $+31$, $+3111$

fft modules for 2^{**20} :
7340033 13631489 26214401 28311553 70254593
976224257 (largest less 10^{**9})

fibonacci numbers:
1, 2: 1
46: 1836311903 (max int)
47: 2971215073 (max unsigned)
92: 7540113804746346429 (max i64)
93: 12200160415121876738 (max unsigned i64)

$2^{**31} = 2147483648 = 2.1e9$
 $2^{**32} = 4294967296 = 4.2e9$
 $2^{**63} = 9223372036854775808 = 9.2e18$
 $2^{**64} = 18446744073709551616 = 1.8e19$

highly composite: todo

11 strings/automaton.cpp

```

1 int t[maxn][26], lnk[maxn], len[maxn];
2 int sz;
3 int last;
4
5 void init() {
6     sz = 3;
7     last = 1;
8     forn(i, 26) t[2][i] = 1;
9     len[2] = -1;
10    lnk[1] = 2;
11}
12
13 void addchar(int c) {
14     int nlast = sz++;
15     len[nlast] = len[last] + 1;
16     int p = last;
17     for (; !t[p][c]; p = lnk[p]) {
18         t[p][c] = nlast;
19     }
20     int q = t[p][c];
21     if (len[p] + 1 == len[q]) {
22         lnk[nlast] = q;
23     } else {
24         int clone = sz++;
25         len[clone] = len[p] + 1;
26         lnk[clone] = lnk[q];
27         lnk[q] = lnk[nlast] = clone;
28         forn(i, 26) t[clone][i] = t[q][i];
29         for (; t[p][c] == q; p = lnk[p]) {
30             t[p][c] = clone;
31         }
32     }
33     last = nlast;
34}
35
36 bool check(const string& s) {
37     int v = 1;
38     for (int c: s) {
39         c -= 'a';
40         if (!t[v][c]) return false;
41         v = t[v][c];
42     }
43     return true;
44}
45
46 int main() {
47     string s;
48     cin >> s;
49     init();
50     for (int i: s) {
51         addchar(i - 'a');
52     }
53     forn(i, s.length()) {
54         assert(check(s.substr(i)));
55     }
56     cout << sz << endl;
57     return 0;
58}

```

12 strings/suffix_array.cpp

```

1 string s;
2 int n;
3 int sa[maxn], new_sa[maxn], cls[maxn], new_cls[maxn],
4     cnt[maxn], lcp[maxn];
5 int n_cls;
6
7 void build() {
8     n_cls = 256;
9     forn(i, n) {
10         sa[i] = i;
11         cls[i] = s[i];
12     }
13     for (int d = 0; d < n; d = d ? d*2 : 1) {
14
15         forn(i, n) new_sa[i] = (sa[i] - d + n) % n;
16         forn(i, n_cls) cnt[i] = 0;
17         forn(i, n) ++cnt[cls[i]];
18         forn(i, n_cls) cnt[i+1] += cnt[i];
19         for (int i = n-1; i >= 0; --i)
20             sa[--cnt[cls[new_sa[i]]]] = new_sa[i];
21
22         n_cls = 0;
23         forn(i, n) {
24             if (i && (cls[sa[i]] != cls[sa[i-1]] ||
25                 cls[(sa[i] + d) % n] != cls[(sa[i-1] + d) % n])) {
26                 ++n_cls;
27             }
28             new_cls[sa[i]] = n_cls;
29         }
30         ++n_cls;
31         forn(i, n) cls[i] = new_cls[i];
32     }
33
34     // cls is also a inv permutation of sa if a string is not cyclic
35     // (i.e. a position of i-th lexicographical suffix)
36     int val = 0;
37     forn(i, n) {
38         if (val) --val;
39         if (cls[i] == n-1) continue;
40         int j = sa[cls[i] + 1];
41         while (i + val != n && j + val != n && s[i+val] == s[j+val])
42             ++val;
43         lcp[cls[i]] = val;
44     }
45}
46
47 int main() {
48     cin >> s;
49     s += '$';
50     n = s.length();
51     build();
52     forn(i, n) {
53         cout << s.substr(sa[i]) << endl;
54         cout << lcp[i] << endl;
55     }
56}

```


13 strings/ukkonen.cpp

```
1#include <bits/stdc++.h>
2using namespace std;
3#define sz(x) ((int) (x).size())
4#define forn(i,n) for (int i = 0; i < int(n); ++i)
5const int inf = int(1e9) + int(1e5);
6
7string s;
8const int alpha = 26;
9
10namespace SuffixTree {
11    struct Node {
12        Node *to[alpha];
13        Node *lnk, *par;
14        int l, r;
15
16        Node(int l, int r): l(l), r(r) {
17            memset(to, 0, sizeof(to));
18            lnk = par = 0;
19        }
20    };
21
22    Node *root, *blank, *cur;
23    int pos;
24
25    void init() {
26        root = new Node(0, 0);
27        blank = new Node(0, 0);
28        forn (i, alpha)
29            blank->to[i] = root;
30        root->lnk = root->par = blank->lnk = blank->par = blank;
31        cur = root;
32        pos = 0;
33    }
34
35    int at(int id) {
36        return s[id];
37    }
38
39    void goDown(int l, int r) {
40        if (l >= r)
41            return;
42        if (pos == cur->r) {
43            int c = at(l);
44            assert(cur->to[c]);
45            cur = cur->to[c];
46            pos = min(cur->r, cur->l + 1);
47            ++l;
48        } else {
49            int delta = min(r - l, cur->r - pos);
50            l += delta;
51            pos += delta;
52        }
53        goDown(l, r);
54    }
55
56    void goUp() {
57        if (pos == cur->r && cur->lnk) {
58            cur = cur->lnk;
59            pos = cur->r;
60            return;
61        }
62        int l = cur->l, r = pos;
63        cur = cur->par->lnk;
64        pos = cur->r;
65        goDown(l, r);
66    }
67
68    void setParent(Node *a, Node *b) {
69        assert(a);
70        a->par = b;
71        if (b)
72            b->to[at(a->l)] = a;
73    }
74
75    void addLeaf(int id) {
76        Node *x = new Node(id, inf);
77        setParent(x, cur);
78    }
79
80    void splitNode() {
81        assert(pos != cur->r);
82        Node *mid = new Node(cur->l, pos);
83        setParent(mid, cur->par);
84        cur->l = pos;
85        setParent(cur, mid);
86        cur = mid;
87    }
88
89    bool canGo(int c) {
90        if (pos == cur->r)
91            return cur->to[c];
92        return at(pos) == c;
93    }
94
95    void fixLink(Node *&bad, Node *newBad) {
96        if (bad)
97            bad->lnk = cur;
98        bad = newBad;
99    }
100
101    void addCharOnPos(int id) {
102        Node *bad = 0;
103        while (!canGo(at(id))) {
104            if (cur->r != pos) {
105                splitNode();
106                fixLink(bad, cur);
107                bad = cur;
108            } else {
109                fixLink(bad, 0);
110            }
111            addLeaf(id);
112            goUp();
113        }
114        fixLink(bad, 0);
115        goDown(id, id + 1);
116    }
117
118    int cnt(Node *u, int ml) {
119        if (!u)
120            return 0;
121        int res = min(ml, u->r) - u->l;
122        forn (i, alpha)
123            res += cnt(u->to[i], ml);
124        return res;
125    }
126
127    void build(int l) {
128        init();
129        forn (i, l)
130            addCharOnPos(i);
131    }
132};
133
134int main() {
135    cin >> s;
136    SuffixTree::build(s.size());
137}
```

14 structures/convex_hull_trick.cpp 15 structures/heavy_light.cpp

```

1/*
2  WARNING!!!
3  - finds maximum of A*x+B
4  - double check max coords for int/long long overflow
5  - set min x query in put function
6  - add lines with non-descending A coefficient
7*/
8struct FastHull {
9    int a[maxn];
10   ll b[maxn];
11   ll p[maxn];
12   int c;
13
14   FastHull(): c(0) {}
15
16   ll get(int x) {
17       if (c == 0)
18           return -infll;
19       int pos = upper_bound(p, p + c, x) - p - 1;
20       assert(pos >= 0);
21       return (ll) a[pos] * x + b[pos];
22   }
23
24   ll divideCeil(ll p, ll q) {
25       assert(q > 0);
26       if (p >= 0)
27           return (p + q - 1) / q;
28       return -((-p) / q);
29   }
30
31   void put(int A, ll B) {
32       while (c > 0) {
33           if (a[c - 1] == A && b[c - 1] >= B)
34               return;
35           ll pt = p[c - 1];
36           if (a[c - 1] * pt + b[c - 1] < A * pt + B) {
37               --c;
38               continue;
39           }
40           ll q = A - a[c - 1];
41           ll np = divideCeil(b[c - 1] - B, q);
42           p[c] = np;
43           a[c] = A;
44           b[c] = B;
45           ++c;
46           return;
47       }
48       if (c == 0) {
49           a[c] = A, b[c] = B;
50           p[c] = -1e9; //min x query
51           ++c;
52           return;
53       }
54   }
55 };
56
57
58struct SlowHull {
59   vector<pair<int, ll>> v;
60
61   void put(int a, ll b) {
62       v.emplace_back(a, b);
63   }
64
65   ll get(ll x) {
66       ll best = -infll;
67       for (auto p: v)
68           best = max(best, p.first * x + p.second);
69       return best;
70   }
71 };
72
73int main() {
74   FastHull hull1;
75   SlowHull hull2;
76   vector<int> as;
77   forn (ii, 10000)
78       as.push_back(rand() % int(1e8));
79   sort(as.begin(), as.end());
80   forn (ii, 10000) {
81       int b = rand() % int(1e8);
82       hull1.put(as[ii], b);
83       hull2.put(as[ii], b);
84       int x = rand() % int(2e8 + 1) - int(1e8);
85       assert(hull1.get(x) == hull2.get(x));
86   }
87 }

```

```

1const int maxn = 100500;
2const int maxd = 17;
3
4vector<int> g[maxn];
5
6struct Tree {
7   vector<int> t;
8   int base;
9
10  Tree(): base(0) {}
11
12
13  Tree(int n) {
14      base = 1;
15      while (base < n)
16          base *= 2;
17      t = vector<int>(base * 2, 0);
18  }
19
20  void put(int v, int delta) {
21      assert(v < base);
22      v += base;
23      t[v] += delta;
24      while (v > 1) {
25          v /= 2;
26          t[v] = max(t[v * 2], t[v * 2 + 1]);
27      }
28  }
29
30  //Careful here: cr = 2 * maxn
31  int get(int l, int r, int v = 1, int cl = 0, int cr = 2 * maxn) {
32      cr = min(cr, base);
33      if (l <= cl && cr <= r)
34          return t[v];
35      if (r <= cl || cr <= l)
36          return 0;
37      int cc = (cl + cr) / 2;
38      return max(get(l, r, v * 2, cl, cc), get(l, r, v * 2 + 1, cc,
39          ↪ cr));
40  }
41
42namespace HLD {
43   int h[maxn];
44   int timer;
45   int in[maxn], out[maxn], cnt[maxn];
46   int p[maxd][maxn];
47   int vroot[maxn];
48   int vpos[maxn];
49   int ROOT;
50   Tree tree[maxn];
51
52   void dfs1(int u, int prev) {
53       p[0][u] = prev;
54       in[u] = timer++;
55       cnt[u] = 1;
56       for (int v: g[u]) {
57           if (v == prev)
58               continue;
59           h[v] = h[u] + 1;
60           dfs1(v, u);
61           cnt[u] += cnt[v];
62       }
63       out[u] = timer;
64   }
65
66   int dfs2(int u, int prev) {
67       int to = -1;
68       for (int v: g[u]) {
69           if (v == prev)
70               continue;
71           if (to == -1 || cnt[v] > cnt[to])
72               to = v;
73       }
74       int len = 1;
75       for (int v: g[u]) {
76           if (v == prev)
77               continue;
78           if (to == v) {
79               vpos[v] = vpos[u] + 1;
80               vroot[v] = vroot[u];
81               len += dfs2(v, u);
82           }
83           else {
84               vroot[v] = v;
85               vpos[v] = 0;
86               dfs2(v, u);
87           }
88       }
89       if (vroot[u] == u)
90           tree[u] = Tree(len);
91       return len;
92   }
93
94   void init(int n) {

```

```

95     timer = 0;
96     h[ROOT] = 0;
97     dfs1(ROOT, ROOT);
98     forn (d, maxd - 1)
99         forn (i, n)
100             p[d + 1][i] = p[d][p[d][i]];
101     vroot[ROOT] = ROOT;
102     vpos[ROOT] = 0;
103     dfs2(ROOT, ROOT);
104     //WARNING: init all trees
105 }
106
107 bool isPrev(int u, int v) {
108     return in[u] <= in[v] && out[v] <= out[u];
109 }
110
111 int lca(int u, int v) {
112     for (int d = maxd - 1; d >= 0; --d)
113         if (!isPrev(p[d][u], v))
114             u = p[d][u];
115     if (!isPrev(u, v))
116         u = p[0][u];
117     return u;
118 }
119
120 //for each v: h[v] >= toh
121 int getv(int u, int toh) {
122     int res = 0;
123     while (h[u] >= toh) {
124         int rt = vroot[u];
125         int l = max(0, toh - h[rt]), r = vpos[u] + 1;
126         res = max(res, tree[rt].get(l, r));
127         if (rt == ROOT)
128             break;
129         u = p[0][rt];
130     }
131     return res;
132 }
133
134 int get(int u, int v) {
135     int w = lca(u, v);
136     return max(getv(u, h[w]), getv(v, h[w] + 1));
137 }
138
139 void put(int u, int val) {
140     int rt = vroot[u];
141     int pos = vpos[u];
142     tree[rt].put(pos, val);
143 }
144};

```

16 structures/ordered_set.cpp

```

1 #include <ext/pb_ds/assoc_container.hpp>
2 #include <ext/pb_ds/tree_policy.hpp>
3
4 typedef __gnu_pbds::tree<int, __gnu_pbds::null_type, std::less<int>,
5     __gnu_pbds::rb_tree_tag,
6     __gnu_pbds::tree_order_statistics_node_update> oset;
7
8 #include <iostream>
9
10 int main() {
11     oset X;
12     X.insert(1);
13     X.insert(2);
14     X.insert(4);
15     X.insert(8);
16     X.insert(16);
17
18     std::cout << *X.find_by_order(1) << std::endl; // 2
19     std::cout << *X.find_by_order(2) << std::endl; // 4
20     std::cout << *X.find_by_order(4) << std::endl; // 16
21     std::cout << std::boolalpha << (end(X) == X.find_by_order(6)) <<
22         std::endl; // true
23
24     std::cout << X.order_of_key(-5) << std::endl; // 0
25     std::cout << X.order_of_key(1) << std::endl; // 0
26     std::cout << X.order_of_key(3) << std::endl; // 2
27     std::cout << X.order_of_key(4) << std::endl; // 2
28     std::cout << X.order_of_key(400) << std::endl; // 5
29 }

```

17 structures/splay.cpp

```
1#include <bits/stdc++.h>
2using namespace std;
3#define forn(i, n) for (int i = 0; i < (int)(n); ++i)
4
5const int maxn = 100500;
6
7struct node;
8void updson(node* p, node* v, node* was);
9
10struct node {
11    int val;
12    node *l, *r, *p;
13    node() {}
14    node(int val) : val(val), l(r=p=NULL) {}
15
16    bool isRoot() const { return !p; }
17    bool isRight() const { return p && p->r == this; }
18    bool isLeft() const { return p && p->l == this; }
19    void setLeft(node* t) {
20        if (t) t->p = this;
21        l = t;
22    }
23    void setRight(node *t) {
24        if (t) t->p = this;
25        r = t;
26    }
27};
28
29void updson(node *p, node *v, node *was) {
30    if (p) {
31        if (p->l == was) p->l = v;
32        else p->r = v;
33    }
34    if (v) v->p = p;
35}
36
37void rightRotate(node *v) {
38    assert(v && v->l);
39    node *u = v->l;
40    node *p = v->p;
41    v->setLeft(u->r);
42    u->setRight(v);
43    updson(p, u, v);
44}
45
46void leftRotate(node *v) {
47    assert(v && v->r);
48    node *u = v->r;
49    node *p = v->p;
50    v->setRight(u->l);
51    u->setLeft(v);
52    updson(p, u, v);
53}
54
55void splay(node *v) {
56    while (v->p) {
57        if (!v->p->p) {
58            if (v->isLeft()) rightRotate(v->p);
59            else leftRotate(v->p);
60        } else if (v->isLeft() && v->p->isLeft()) {
61            rightRotate(v->p->p);
62            rightRotate(v->p);
63        } else if (v->isRight() && v->p->isRight()) {
64            leftRotate(v->p->p);
65            leftRotate(v->p);
66        } else if (v->isLeft()) {
67            rightRotate(v->p);
68            leftRotate(v->p);
69        } else {
70            leftRotate(v->p);
71            rightRotate(v->p);
72        }
73    }
74    v->p = NULL;
75}
76
77node *insert(node *t, node *n) {
78    if (!t) return n;
79    int x = n->val;
80    while (true) {
81        if (x < t->val) {
82            if (t->l) {
83                t = t->l;
84            } else {
85                t->setLeft(n);
86                t = t->l;
87                break;
88            }
89        } else {
90            if (t->r) {
91                t = t->r;
92            } else {
93                t->setRight(n);
94                t = t->r;
95                break;
96            }
97        }
98    }
99    splay(t);
100    return t;
101}
102
103node *insert(node *t, int x) {
104    return insert(t, new node(x));
105}
106
107int main() {
108    node *t = NULL;
109    forn(i, 1000000) {
110        int x = rand();
111        t = insert(t, x);
112    }
113    return 0;
114}
```

```
96    }
97    }
98    }
99    splay(t);
100    return t;
101}
102
103node *insert(node *t, int x) {
104    return insert(t, new node(x));
105}
106
107int main() {
108    node *t = NULL;
109    forn(i, 1000000) {
110        int x = rand();
111        t = insert(t, x);
112    }
113    return 0;
114}
```

18 structures/treap.cpp

```
1 struct node {
2     int x, y;
3     node *l, *r;
4     node(int x) : x(x), y(rand()), l(r=NULL) {}
5 };
6
7 void split(node *t, node *&l, node *&r, int x) {
8     if (!t) return (void)(l=r=NULL);
9     if (x <= t->x) {
10         split(t->l, l, t->l, x), r = t;
11     } else {
12         split(t->r, t->r, r, x), l = t;
13     }
14 }
15
16 node *merge(node *l, node *r) {
17     if (!l) return r;
18     if (!r) return l;
19     if (l->y > r->y) {
20         l->r = merge(l->r, r);
21         return l;
22     } else {
23         r->l = merge(l, r->l);
24         return r;
25     }
26 }
27
28 node *insert(node *t, node *n) {
29     node *l, *r;
30     split(t, l, r, n->x);
31     return merge(l, merge(n, r));
32 }
33
34 node *insert(node *t, int x) {
35     return insert(t, new node(x));
36 }
37
38 node *fast_insert(node *t, node *n) {
39     if (!t) return n;
40     node *root = t;
41     while (true) {
42         if (n->x < t->x) {
43             if (!t->l || t->l->y < n->y) {
44                 split(t->l, n->l, n->r, n->x), t->l = n;
45                 break;
46             } else {
47                 t = t->l;
48             }
49         } else {
50             if (!t->r || t->r->y < n->y) {
51                 split(t->r, n->l, n->r, n->x), t->r = n;
52                 break;
53             } else {
54                 t = t->r;
55             }
56         }
57     }
58     return root;
59 }
60
61 node *fast_insert(node *t, int x) {
62     return fast_insert(t, new node(x));
63 }
64
65 int main() {
66     node *t = NULL;
67     forn(i, 1000000) {
68         int x = rand();
69         t = fast_insert(t, x);
70     }
71 }
```