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## 1 Strategy.txt

- Проверить руками сэмплы
- Подумать как дебагать после написания
- Выписать сложные формулы и все +-1
- Проверить имена файлов
- Прогнать сэмплы
- Переполнения int, переполнения long long
- Выход за границу массива: \_GLIBCXX\_DEBUG
- Переполнения по модулю: в
  - псевдо-онлайн-генераторе, в функциях-обертках
- Проверить мультитест на разных тестах
- Прогнать минимальный по каждому параметру тест
- Прогнать псевдо-максимальный тест(немного чисел,
  - но очень большие или очень маленькие)
- Представить что не зайдет и заранее написать
  - assert'ы, прогнать слегка модифицированные тесты
- cout.precision: в том числе в интерактивных
  - задачах
- Удалить debug-output, отсечения для тестов,
  - вернуть оригинальный maxn, удалить
  - \_GLIBCXX\_DEBUG
- Вердикт может врать
- Если много тестов(>3), дописать в конец каждого
  - теста ответ, чтобы не забыть
- (WA) Потестить не только ответ, но и содержимое
  - значимых массивов, переменных
- (WA) Изменить тест так, чтобы ответ не менялся:
  - поменять координаты местами, сжать/растянуть
  - координаты, поменять ROOT дерева
- (WA) Подвигать размер блока в корневой или
  - битсете
- (WA) Поставить assert'ы, возможно написать чекер
  - с assert'ом
- (WA) Проверить, что программа не печатает
  - что-либо неожиданное, что должно попадать под
  - PE: inf - 2, не лекс. мин. решение, одинаковые
  - числа вместо разных, неправильное количество
  - чисел, пустой ответ, перечитать output format
- (TL) cin -> scanf -> getchar
- (TL) Упихать в кэш большие массивы, поменять
  - местами for'ы или измерения массива
- (RE) Проверить формулы на деление на 0, выход за
  - область определения(sqrt(-eps), acos(1 + eps))
- (WA) Проверить, что ответ влезает в int

## 2 flows/dinic.cpp

```

1 namespace Dinic {
2 const int maxn = 100100;
3 struct Edge {
4     int to;
5     ll c, f;
6     Edge(int to, ll c): to(to), c(c), f(0) {}
7 };
8
9 vector<Edge> es;
10 vector<int> g[maxn];
11 int q[maxn], d[maxn], pos[maxn];
12 int N, S, T;
13
14 void addEdge(int u, int v, ll c) {
15     g[u].push_back(sz(es));
16     es.emplace_back(v, c);
17     g[v].push_back(sz(es));
18     es.emplace_back(u, 0);
19 }
20
21 bool bfs() {
22     fill(d, d + N, maxn);
23     d[S] = 0, q[0] = S;
24     int rq = 1;
25     forn (lq, rq) {
26         int u = q[lq];
27         for (int id: g[u]) {
28             if (es[id].c == es[id].f)
29                 continue;
30             int v = es[id].to;
31             if (d[v] == maxn) {
32                 d[v] = d[u] + 1;
33                 q[rq++] = v;
34             }
35         }
36     }
37     return d[T] != maxn;
38 }
39
40 ll dfs(int u, ll curf) {
41     if (u == T)
42         return curf;
43     ll ret = 0;
44     for (int &i = pos[u]; i < sz(g[u]); ++i) {
45         int id = g[u][i];
46         int v = es[id].to;
47         ll delta = min(curf, es[id].c - es[id].f);
48         if (delta == 0 || d[v] != d[u] + 1)
49             continue;
50         delta = dfs(v, delta);
51         curf -= delta;
52         ret += delta;
53         es[id].f += delta;
54         es[id ^ 1].f -= delta;
55         if (curf == 0)
56             return ret;
57     }
58     return ret;
59 }
60
61 ll dinic(int S, int T) {
62     Dinic::S = S, Dinic::T = T;
63     ll res = 0;
64     while (bfs()) {
65         fill(pos, pos + N, 0);
66         while (ll cur = dfs(S, inf))
67             res += cur;
68     }
69     return res;
70 }
71
72 // namespace Dinic
73
74 void test() {
75     Dinic::N = 4;
76     Dinic::addEdge(0, 1, 1);
77     Dinic::addEdge(0, 2, 2);
78     Dinic::addEdge(2, 1, 1);
79     Dinic::addEdge(1, 3, 2);
80     Dinic::addEdge(2, 3, 1);
81     cout << Dinic::dinic(0, 3) << endl; // 3
82 }
83
84 LR-поток находит не максимальный поток.
85 Добавим новый сток S' и исток T'. Заменим ребро (u, v, l, r)
86 LR-сети на ребра (u, T', l), (S', v, l), (u, v, r - l).
87 Добавим ребро (T, S, k). Ставим значение k=inf, пускаем поток.
88 Проверяем, что все ребра из S' насыщены (иначе ответ не
89 существует). Бинарным поиском находим наименьшее k, что величина
90 потока не изменится. Это k - величина МИНИМАЛЬНОГО потока,
91 удовлетворяющего ограничениям. */

```

### 3 flows/globalcut.cpp

```

1#include <bits/stdc++.h>
2using namespace std;
3#define forn(i,n) for (int i = 0; i < int(n); ++i)
4const int inf = 1e9 + 1e5;
5#define all(x) (x).begin(), (x).end()
6
7const int maxn = 505;
8namespace StoerWagner {
9int g[maxn][maxn];
10int dist[maxn];
11bool used[maxn];
12int n;
13
14void addEdge(int u, int v, int c) {
15    g[u][v] += c;
16    g[v][u] += c;
17}
18
19int run() {
20    vector<int> vertices;
21    forn (i, n)
22        vertices.push_back(i);
23    int mincut = inf;
24    while (vertices.size() > 1) {
25        int u = vertices[0];
26        for (auto v: vertices) {
27            used[v] = false;
28            dist[v] = g[u][v];
29        }
30        used[u] = true;
31        forn (ii, vertices.size() - 2) {
32            for (auto v: vertices)
33                if (!used[v])
34                    if (used[u] || dist[v] > dist[u])
35                        u = v;
36            used[u] = true;
37            for (auto v: vertices)
38                if (!used[v])
39                    dist[v] += g[u][v];
40        }
41        int t = -1;
42        for (auto v: vertices)
43            if (!used[v])
44                t = v;
45        assert(t != -1);
46        mincut = min(mincut, dist[t]);
47        vertices.erase(find(all(vertices), t));
48        for (auto v: vertices)
49            addEdge(u, v, g[v][t]);
50    }
51    return mincut;
52}
53} // namespace StoerWagner
54
55int main() {
56    StoerWagner::n = 4;
57    StoerWagner::addEdge(0, 1, 5);
58    StoerWagner::addEdge(2, 3, 5);
59    StoerWagner::addEdge(1, 2, 4);
60    cerr << StoerWagner::run() << '\n'; // 4
61}

```

### 4 flows/hungary.cpp

```

1// left half is the smaller one
2namespace Hungary {
3const int maxn = 505;
4int a[maxn][maxn];
5int p[2][maxn];
6int match[maxn];
7bool used[maxn];
8int from[maxn];
9int mind[maxn];
10int n, m;
11
12int hungary(int v) {
13    used[v] = true;
14    int u = match[v];
15    int best = -1;
16    forn (i, m + 1) {
17        if (used[i])
18            continue;
19        int nw = a[u][i] - p[0][u] - p[1][i];
20        if (nw <= mind[i]) {
21            mind[i] = nw;
22            from[i] = v;
23        }
24        if (best == -1 || mind[best] > mind[i])
25            best = i;
26    }
27    v = best;
28    int delta = mind[best];
29    forn (i, m + 1) {
30        if (used[i]) {
31            p[1][i] -= delta;
32            p[0][match[i]] += delta;
33        } else
34            mind[i] -= delta;
35    }
36    if (match[v] == -1)
37        return v;
38    return hungary(v);
39}
40
41void check() {
42    int edges = 0, res = 0;
43    forn (i, m)
44        if (match[i] != -1) {
45            ++edges;
46            assert(p[0][match[i]] + p[1][i] == a[match[i]][i]);
47            res += a[match[i]][i];
48        } else
49            assert(p[1][i] == 0);
50    assert(res == -p[1][m]);
51    forn (i, n) forn (j, m)
52        assert(p[0][i] + p[1][j] <= a[i][j]);
53}
54
55int run() {
56    forn (i, n)
57        p[0][i] = 0;
58    forn (i, m + 1) {
59        p[1][i] = 0;
60        match[i] = -1;
61    }
62    forn (i, n) {
63        match[m] = i;
64        fill(used, used + m + 1, false);
65        fill(mind, mind + m + 1, inf);
66        fill(from, from + m + 1, -1);
67        int v = hungary(m);
68        while (v != m) {
69            int w = from[v];
70            match[v] = match[w];
71            v = w;
72        }
73    }
74    check();
75    return -p[1][m];
76}
77} // namespace Hungary

```

## 5 flows/mincost.cpp

```

1 namespace MinCost {
2 const ll infc = 1e12;
3
4 struct Edge {
5     int to;
6     ll c, f, cost;
7
8     Edge(int to, ll c, ll cost): to(to), c(c), f(0), cost(cost) {
9         {}
10};
11
12 int N, S, T;
13 int totalFlow;
14 ll totalCost;
15 const int maxn = 505;
16 vector<Edge> edge;
17 vector<int> g[maxn];
18
19 void addEdge(int u, int v, ll c, ll cost) {
20     g[u].push_back(edge.size());
21     edge.emplace_back(v, c, cost);
22     g[v].push_back(edge.size());
23     edge.emplace_back(u, 0, -cost);
24}
25
26 ll dist[maxn];
27 int fromEdge[maxn];
28
29 bool inQueue[maxn];
30 bool fordBellman() {
31     for (i, N)
32         dist[i] = infc;
33     dist[S] = 0;
34     inQueue[S] = true;
35     vector<int> q;
36     q.push_back(S);
37     for (int ii = 0; ii < int(q.size()); ++ii) {
38         int u = q[ii];
39         inQueue[u] = false;
40         for (int e: g[u]) {
41             if (edge[e].f == edge[e].c)
42                 continue;
43             int v = edge[e].to;
44             ll nw = edge[e].cost + dist[u];
45             if (nw >= dist[v])
46                 continue;
47             dist[v] = nw;
48             fromEdge[v] = e;
49             if (!inQueue[v]) {
50                 inQueue[v] = true;
51                 q.push_back(v);
52             }
53         }
54     }
55     return dist[T] != infc;
56}
57
58 ll pot[maxn];
59 bool dikstra() {
60     typedef pair<ll, int> Pair;
61     priority_queue<Pair, vector<Pair>, greater<Pair>> q;
62     for (i, N)
63         dist[i] = infc;
64     dist[S] = 0;
65     q.emplace(dist[S], S);
66     while (!q.empty()) {
67         int u = q.top().second;
68         ll cdist = q.top().first;
69         q.pop();
70         if (cdist != dist[u])
71             continue;
72         for (int e: g[u]) {
73             int v = edge[e].to;
74             if (edge[e].c == edge[e].f)
75                 continue;
76             ll w = edge[e].cost + pot[u] - pot[v];
77             assert(w >= 0);
78             ll ndist = w + dist[u];
79             if (ndist >= dist[v])
80                 continue;
81             dist[v] = ndist;
82             fromEdge[v] = e;
83             q.emplace(dist[v], v);
84         }
85     }
86     if (dist[T] == infc)
87         return false;
88     for (i, N) {
89         if (dist[i] == infc)
90             continue;
91         pot[i] += dist[i];
92     }
93     return true;
94}
95
96 bool push() {
97     //2 variants
98     //if (!fordBellman())
99     if (!dikstra())
100         return false;
101     ++totalFlow;
102     int u = T;
103     while (u != S) {
104         int e = fromEdge[u];
105         totalCost += edge[e].cost;
106         edge[e].f++;
107         edge[e ^ 1].f--;
108         u = edge[e ^ 1].to;
109     }
110     return true;
111}
112
113 //min-cost-circulation
114 ll d[maxn][maxn];
115 int dfrom[maxn][maxn];
116 int level[maxn];
117 void circulation() {
118     while (true) {
119         int q = 0;
120         fill(d[0], d[0] + N, 0);
121         for (iter, N) {
122             fill(d[iter + 1], d[iter + 1] + N, infc);
123             for (u, N)
124                 for (int e: g[u]) {
125                     if (edge[e].c == edge[e].f)
126                         continue;
127                     int v = edge[e].to;
128                     ll ndist = d[iter][u] + edge[e].cost;
129                     if (ndist >= d[iter + 1][v])
130                         continue;
131                     d[iter + 1][v] = ndist;
132                     dfrom[iter + 1][v] = e;
133                 }
134             q ^= 1;
135         }
136         int w = -1;
137         ld mindmax = 1e18;
138         for (u, N) {
139             ld dmax = -1e18;
140             for (iter, N)
141                 dmax = max(dmax,
142                     (d[N][u] - d[iter][u]) / ld(N - iter));
143             if (mindmax > dmax)
144                 mindmax = dmax, w = u;
145         }
146         if (mindmax >= 0)
147             break;
148         fill(level, level + N, -1);
149         int k = N;
150         while (level[w] == -1) {
151             level[w] = k;
152             w = edge[dfrom[k--]][w ^ 1].to;
153         }
154         int k2 = level[w];
155         ll delta = infc;
156         while (k2 > k) {
157             int e = dfrom[k2--][w];
158             delta = min(delta, edge[e].c - edge[e].f);
159             w = edge[e ^ 1].to;
160         }
161         k2 = level[w];
162         while (k2 > k) {
163             int e = dfrom[k2--][w];
164             totalCost += edge[e].cost * delta;
165             edge[e].f += delta;
166             edge[e ^ 1].f -= delta;
167             w = edge[e ^ 1].to;
168         }
169     }
170}
171 // namespace MinCost
172
173 int main() {
174     MinCost::N = 3, MinCost::S = 1, MinCost::T = 2;
175     MinCost::addEdge(1, 0, 3, 5);
176     MinCost::addEdge(0, 2, 4, 6);
177     while (MinCost::push());
178     cout << MinCost::totalFlow << ' '
179         << MinCost::totalCost << '\n'; //3 33
180}

```

## 6 flows/push\_relabel.cpp

```

1 namespace PushRelabel {
2 const int maxn = 200500;
3
4 struct Edge {
5     int to, c, f;
6 };
7 vector<Edge> edge;
8
9 int n;
10 vector<int> g[maxn];
11 int e[maxn];
12 int h[maxn];
13 int onH[maxn];
14 int S, T;
15 int ptr[maxn];
16 int relabelTimer;
17
18 void addEdge(int u, int v, int c) {
19     g[u].push_back(sz(edge));
20     edge.push_back({v, c, 0});
21     g[v].push_back(sz(edge));
22     edge.push_back({u, 0, 0});
23 }
24
25 void push(int id, int delta) {
26     int u = edge[id ^ 1].to;
27     int v = edge[id].to;
28     edge[id].f += delta;
29     edge[id ^ 1].f -= delta;
30     e[u] -= delta;
31     e[v] += delta;
32 }
33
34 void gap(int ch) {
35     forn (u, n) {
36         if (h[u] > ch)
37             h[u] = max(h[u], n);
38     }
39 }
40
41 int o[maxn];
42 void globalRelabeling() {
43     int oc = 0;
44     forn (i, n) {
45         h[i] = n;
46         onH[i] = 0;
47     }
48     onH[0] = 1;
49     h[T] = 0;
50     o[oc++] = T;
51     forn (ii, oc) {
52         int u = o[ii];
53         for (int id: g[u]) {
54             if (edge[id ^ 1].c == edge[id ^ 1].f)
55                 continue;
56             int v = edge[id].to;
57             if (h[v] != n)
58                 continue;
59             h[v] = h[u] + 1;
60             onH[h[v]]++;
61             o[oc++] = v;
62         }
63     }
64 }
65
66 void relabel(int u) {
67     int oldh = h[u];
68     int newh = inf;
69     for (int id: g[u]) {
70         if (edge[id].c == edge[id].f)
71             continue;
72         newh = min(newh, h[edge[id].to] + 1);
73     }
74     h[u] = newh;
75     onH[oldh]--;
76     onH[newh]++;
77     if (onH[oldh] == 0)
78         gap(oldh);
79     if (++relabelTimer == n)
80         globalRelabeling(), relabelTimer = 0;
81 }
82
83 void discharge(int u) {
84     while (e[u] > 0) {
85         int &i = ptr[u];
86         if (i == sz(g[u])) {
87             i = 0;
88             relabel(u);
89             if (h[u] >= n)
90                 break;
91             continue;
92         } else {
93             int id = g[u][i++];
94             int v = edge[id].to;
95             if (h[v] + 1 != h[u])
96                 continue;
97             int delta = min(e[u], ll(edge[id].c - edge[id].f));
98             push(id, delta);
99         }
100     }
101 }
102
103 int flow(int _S, int _T) {
104     S = _S, T = _T;
105     forn (i, n)
106         ptr[i] = 0, e[i] = 0;
107     for (int id: g[S]) {
108         int delta = edge[id].c;
109         push(id, delta);
110     }
111     globalRelabeling();
112     bool ok = false;
113     while (!ok) {
114         ok = true;
115         forn (u, n) {
116             if (h[u] < n && u != T && e[u] > 0)
117                 discharge(u), ok = false;
118         }
119     }
120     return e[T];
121 }
122
123 } //PushRelabel

```

## 7 geometry/chan.cpp

```

1mt19937 rr(111);
2ld rndEps() {
3    return (ld(rr()) / rr.max() - 0.5) * 1e-7;
4}
5
6typedef tuple<int, int, int> Face;
7const ld infc = 1e100;
8
9int n;
10pt p[maxn];
11
12namespace Chan {
13pt _p[maxn];
14
15ld turny(int p1, int p2, int p3) {
16    return (p[p2].x - p[p1].x) * (p[p3].y - p[p1].y) -
17           (p[p3].x - p[p1].x) * (p[p2].y - p[p1].y);
18}
19
20//replace y with z
21ld turnz(int p1, int p2, int p3) {
22    return (p[p2].x - p[p1].x) * (p[p3].z - p[p1].z) -
23           (p[p3].x - p[p1].x) * (p[p2].z - p[p1].z);
24}
25
26ld gett(int p1, int p2, int p3) {
27    if (p1 == -1 || p2 == -1 || p3 == -1)
28        return infc;
29    ld ty = turny(p1, p2, p3);
30    if (ty >= 0)
31        return infc;
32    else
33        return turnz(p1, p2, p3) / ty;
34}
35
36void act(int i) {
37    if (p[i].onHull) {
38        p[p[i].nx].pr = p[i].pr;
39        p[p[i].pr].nx = p[i].nx;
40    } else {
41        p[p[i].nx].pr = p[p[i].pr].nx = i;
42    }
43    p[i].onHull ^= 1;
44}
45
46ld updt(vector<int> &V) {
47    if (V.empty())
48        return infc;
49    int id = V.back();
50    if (p[id].onHull)
51        return gett(p[id].pr, p[id].nx, id);
52    else
53        return gett(p[id].pr, id, p[id].nx);
54}
55
56//builds lower hull
57vector<int> buildHull(int l, int r) {
58    if (l + 1 >= r) {
59        p[l].pr = p[l].nx = -1;
60        p[l].onHull = true;
61        return {};
62    }
63    int mid = (l + r) / 2;
64    auto L = buildHull(l, mid);
65    auto R = buildHull(mid, r);
66    reverse(all(L));
67    reverse(all(R));
68    int u = mid - 1, v = mid;
69    while (true) {
70        if (p[u].pr != -1 &&
71            (turny(p[u].pr, u, v) <= 0))
72            u = p[u].pr;
73        else if (p[v].nx != -1 &&
74            (turny(u, v, p[v].nx) <= 0))
75            v = p[v].nx;
76        else
77            break;
78    }
79
80    ld t[6];
81    t[0] = updt(L);
82    t[1] = updt(R);
83    vector<int> A;
84    while (true) {
85        t[2] = gett(p[u].pr, v, u);
86        t[3] = gett(u, p[u].nx, v);
87        t[4] = gett(u, p[v].pr, v);
88        t[5] = gett(u, p[v].nx, v);
89        ld nt = infc;
90        int type = -1;
91        for (i, 6)

```

```

92            if (t[i] < nt)
93                nt = t[i], type = i;
94        if (nt >= infc)
95            break;
96
97        if (type == 0) {
98            act(L.back());
99            if (L.back() < u)
100                A.push_back(L.back());
101            L.pop_back();
102            t[0] = updt(L);
103        } else if (type == 1) {
104            act(R.back());
105            if (R.back() > v)
106                A.push_back(R.back());
107            R.pop_back();
108            t[1] = updt(R);
109        } else if (type == 2) {
110            A.push_back(u);
111            u = p[u].pr;
112        } else if (type == 3) {
113            A.push_back(u = p[u].nx);
114        } else if (type == 4) {
115            A.push_back(v = p[v].pr);
116        } else if (type == 5) {
117            A.push_back(v);
118            v = p[v].nx;
119        }
120    }
121    assert(L.empty() && R.empty());
122
123    p[u].nx = v, p[v].pr = u;
124    for (int i = u + 1; i < v; ++i)
125        p[i].onHull = false;
126    for (int i = sz(A) - 1; i >= 0; --i) {
127        int id = A[i];
128        if (id <= u || id >= v) {
129            if (u == id)
130                u = p[u].pr;
131            if (v == id)
132                v = p[v].nx;
133            act(id);
134        } else {
135            p[id].pr = u, p[id].nx = v;
136            act(id);
137            if (id >= mid)
138                v = id;
139            else
140                u = id;
141        }
142    }
143    return A;
144}
145
146//faces are oriented ccw if look from the outside
147vector<Face> getFaces() {
148    for (i, n) {
149        _p[i] = p[i];
150        p[i].x += rndEps();
151        p[i].y += rndEps();
152        p[i].z += rndEps();
153        p[i].id = i;
154    }
155    sort(p, p + n, [](const pt &a, const pt &b) {
156        return a.x < b.x;
157    });
158    vector<Face> faces;
159    for (q, 2) {
160        auto movie = buildHull(0, n);
161        for (int x: movie) {
162            int id = p[x].id;
163            int pid = p[p[x].pr].id;
164            int nid = p[p[x].nx].id;
165            if (!p[x].onHull)
166                faces.emplace_back(pid, id, nid);
167            else
168                faces.emplace_back(pid, nid, id);
169            act(x);
170        }
171        for (i, n) {
172            p[i].y *= -1;
173            p[i].z *= -1;
174        }
175    }
176    for (i, n)
177        p[i] = _p[i];
178    return faces;
179}
180
181} //namespace Chan

```

## 8 geometry/convex\_hull\_trick.cpp

```

1 struct Hull {
2     vector<pt> top, bot;
3
4     //check: add points in strictly increasing order
5     void append(pt p) {
6         while (sz(bot) > 1 && (p - bot.back()) %
7             (p - *next(bot.rbegin())) >= -eps)
8             bot.pop_back();
9         bot.push_back(p);
10        while (sz(top) > 1 && (p - top.back()) %
11            (p - *next(top.rbegin())) <= eps)
12            top.pop_back();
13        top.push_back(p);
14    }
15
16    pt mostDistant(pt dir) {
17        dir = dir.rot();
18        auto &v = dir.x < 0 ? top : bot;
19        int l = -1, r = sz(v) - 1;
20        while (l + 1 < r) {
21            int c = (l + r) / 2;
22            if (dir % (v[c + 1] - v[c]) > 0)
23                r = c;
24            else
25                l = c;
26        }
27        return v[r];
28    }
29};

```

## 9 geometry/halfplanes.cpp

```

1 ld det3x3(line a, line b, line c) {
2     return a.c * (b.v % c.v)
3         + b.c * (c.v % a.v)
4         + c.c * (a.v % b.v);
5 }
6
7 //check: bounding box is included
8 vector<pt> halfplanesIntersection(vector<line> l) {
9     sort(all(l), cmpLine); //the strongest constraint is first
10    l.erase(unique(all(l), eqLine), l.end());
11    int n = sz(l);
12    vi st;
13    forn (iter, 2)
14        forn (i, n) {
15            while (sz(st) > 1) {
16                int j = st.back(), k = *next(st.rbegin());
17                if (l[k].v % l[i].v <= eps ||
18                    det3x3(l[k], l[j], l[i]) <= eps)
19                    break;
20                st.pop_back();
21            }
22            st.push_back(i);
23        }
24
25    vi pos(n, -1);
26    bool ok = false;
27    forn (i, sz(st)) {
28        int id = st[i];
29        if (pos[id] != -1) {
30            st = vi(st.begin() + pos[id], st.begin() + i);
31            ok = true;
32            break;
33        } else
34            pos[id] = i;
35    }
36    if (!ok)
37        return {};
38
39    vector<pt> res;
40    pt M{0, 0};
41    int k = sz(st);
42    forn (i, k) {
43        line l1 = l[st[i]], l2 = l[st[(i + 1) % k]];
44        res.push_back(linesIntersection(l1, l2));
45        M = M + res.back();
46    }
47    M = M * (1. / k);
48    for (int id: st)
49        if (l[id].signedDist(M) < -eps)
50            return {};
51    return res;
52}

```

## 10 geometry/nd\_convex\_hull.cpp

```

1const int DIM = 4;
2typedef array<ll, DIM> pt;
3pt operator-(const pt &a, const pt &b) {
4    pt res;
5    forn (i, DIM)
6        res[i] = a[i] - b[i];
7    return res;
8}
9typedef array<pt, DIM-1> Edge;
10typedef array<pt, DIM> Face;
11vector<Face> faces;
12
13ll det(pt *a) {
14    int p[DIM];
15    iota(p, p + DIM, 0);
16    ll res = 0;
17    do {
18        ll x = 1;
19        forn (i, DIM) {
20            forn (j, i)
21                if (p[j] > p[i])
22                    x *= -1;
23            x *= a[i][p[i]];
24        }
25        res += x;
26    } while (next_permutation(p, p + DIM));
27    return res;
28}
29
30ll V(Face f, pt pivot) {
31    pt p[DIM];
32    forn (i, DIM)
33        p[i] = f[i] - pivot;
34    return det(p);
35}
36
37void init(vector<pt> p) {
38    forn (i, DIM+1) {
39        Face a;
40        int q = 0;
41        forn (j, DIM+1)
42            if (j != i)
43                a[q++] = p[j];
44        ll v = V(a, p[i]);
45        assert(v != 0);
46        if (v < 0)
47            swap(a[0], a[1]);
48        faces.push_back(a);
49    }
50}
51
52void add(pt p) {
53    vector<Face> newf, bad;
54    for (auto f: faces) {
55        if (V(f, p) < 0)
56            bad.push_back(f);
57        else
58            newf.push_back(f);
59    }
60    if (bad.empty()) {
61        return;
62    }
63    faces = newf;
64    vector<pair<Edge, pt>> edges;
65    for (auto f: bad) {
66        sort(all(f));
67        forn (i, DIM) {
68            Edge e;
69            int q = 0;
70            forn (j, DIM)
71                if (i != j)
72                    e[q++] = f[j];
73            edges.emplace_back(e, f[i]);
74        }
75    }
76    sort(all(edges));
77    forn (i, sz(edges)) {
78        if (i + 1 < sz(edges) &&
79            edges[i + 1].first == edges[i].first) {
80            ++i;
81            continue;
82        }
83        Face f;
84        forn (j, DIM-1)
85            f[j] = edges[i].first[j];
86        f[DIM-1] = p;
87        if (V(f, edges[i].second) < 0)
88            swap(f[0], f[1]);
89        faces.push_back(f);
90    }
91}

```

## 11 geometry/planar\_faces.cpp

```

1int m, n; // segs, points
2pair<pt, pt> segs[maxn];
3pt p[maxn], from, to;
4map<pt, int> shr;
5vi e[maxn]; // points adjacent to point
6int getPoint(pt x) {
7    if (shr.count(x)) return shr[x];
8    p[n] = x;
9    return shr[x] = n++;
10}
11// segIntersection: {bool, point}, true iff exactly one point
12void genIntersections() {
13    forn (i, m) {
14        getPoint(segs[i].fi);
15        getPoint(segs[i].se);
16        forn (j, i) {
17            auto t = segmentsIntersection(
18                segs[i].fi, segs[i].se, segs[j].fi, segs[j].se);
19            if (t.fi) getPoint(t.se);
20        }
21    }
22}
23
24void genGraph() {
25    forn (i, m) {
26        vi pts;
27        forn (j, n) if (pointInsideSegment(
28            p[j], segs[i].fi, segs[i].se)) {
29            pts.push_back(j);
30        }
31        sort(all(pts), [](int i, int j) {
32            return p[i] < p[j]; });
33        forn (j, pts.size() - 1) {
34            int u = pts[j], v = pts[j+1];
35            e[u].push_back(v);
36            e[v].push_back(u);
37        }
38    }
39    forn (i, n) {
40        sort(all(e[i]), [](int x, int y) {
41            pt a = p[x] - p[i];
42            pt b = p[y] - p[i];
43            if (a.right() != b.right()) return a.right();
44            return a % b > 0;
45        });
46    }
47}
48
49vector<pt> faces[maxn];
50bool inner[maxn];
51int nf;
52map<pii, int> faceForEdge;
53vi ef[maxn]; // graph on faces
54
55void genFaces() {
56    forn (i, n) for (int to: e[i]) {
57        if (faceForEdge.count({i, to})) continue;
58        int f = nf++;
59        int v = i, u = to;
60        do {
61            faces[f].push_back(p[v]);
62            faceForEdge[{v, u}] = f;
63            auto it = lower_bound(all(e[u]), v,
64                [u] (int x, int y) {
65                    pt a = p[x] - p[u];
66                    pt b = p[y] - p[u];
67                    if (a.right() != b.right()) return a.right();
68                    return a % b > 0;
69                });
70            assert(*it == v);
71            if (it == e[u].begin()) it = e[u].end();
72            v = u;
73            u = *--it;
74        } while (v != i || u != to);
75    }
76    forn (i, nf) {
77        ld s = 0;
78        forn (j, faces[i].size()) {
79            s += faces[i][j] % faces[i][(j+1)%faces[i].size()];
80        }
81        inner[i] = gt(s, 0);
82    }
83    forn (v, n) for (int to: e[v]) {
84        int f1 = faceForEdge[{v, to}];
85        int f2 = faceForEdge[{to, v}];
86        if (f1 != f2) {
87            ef[f1].push_back(f2);
88            ef[f2].push_back(f1);
89        }
90    }
91}

```



## 12 geometry/polygon.cpp

```

1 bool pointInsidePolygon(pt a, pt *p, int n) {
2     double sumAng = 0;
3     forn (i, n) {
4         pt A = p[i], B = p[(i + 1) % n];
5         if (pointInsideSegment(a, A, B))
6             return true;
7         sumAng += atan2((A - a) % (B - a), (A - a) * (B - a));
8     }
9     return fabs(sumAng) > 1;
10 }
11
12 //check: p is oriented ccw
13 bool segmentInsidePolygon(pt a, pt b, pt *p, int n) {
14     if (!pointInsidePolygon((a + b) * .5, p, n))
15         return false;
16     if (ze((a - b).abs()))
17         return true;
18     forn (i, n) {
19         pt c = p[i];
20         if (ze((a - c) % (b - c)) &&
21             (a - c) * (b - c) < -eps) {
22             //point inside interval
23             pt pr = p[(i + n - 1) % n];
24             pt nx = p[(i + 1) % n];
25             if ((c - pr) % (nx - c) > eps)
26                 return false;
27             ld s1 = (pr - a) % (b - a);
28             ld s2 = (nx - a) % (b - a);
29             if ((s1 > eps || s2 > eps) &&
30                 (s1 < -eps || s2 < -eps))
31                 return false;
32         }
33         //interval intersection
34         pt d = p[(i + 1) % n];
35         ld s1 = (a - c) % (d - c);
36         ld s2 = (b - c) % (d - c);
37         if (s1 >= -eps && s2 >= -eps)
38             continue;
39         if (s1 <= eps && s2 <= eps)
40             continue;
41
42         s1 = (c - a) % (b - a);
43         s2 = (d - a) % (b - a);
44         if (s1 >= -eps && s2 >= -eps)
45             continue;
46         if (s1 <= eps && s2 <= eps)
47             continue;
48
49         return false;
50     }
51     return true;
52 }

```

## 13 geometry/polygon\_tangents.cpp

```

1 struct Cmp {
2     pt M, v0;
3
4     bool operator()(const pt &a, const pt &b) {
5         pt va{v0 * (a - M), v0 % (a - M)};
6         pt vb{v0 * (b - M), v0 % (b - M)};
7         return cmpAngle(va, vb);
8     }
9 };
10
11 struct Hull {
12     vector<pt> h;
13     int n;
14
15     void build() {
16         sort(all(h));
17         h.erase(unique(all(h)), h.end());
18         vector<pt> top, bot;
19         for (auto p: h) {
20             while (sz(bot) > 1 && (p - bot.back()) %
21                 (p - *next(bot.rbegin())) >= -eps)
22                 bot.pop_back();
23             bot.push_back(p);
24             while (sz(top) > 1 && (p - top.back()) %
25                 (p - *next(top.rbegin())) <= eps)
26                 top.pop_back();
27             top.push_back(p);
28         }
29         if (sz(top))
30             top.pop_back();
31         reverse(all(top));
32         if (sz(top))
33             top.pop_back();
34         h = bot;
35         h.insert(h.end(), all(top));
36         n = sz(h);
37     }
38
39     bool visSide(pt a, int i) {
40         return (h[(i + 1) % n] - a) % (h[i % n] - a) > eps;
41     }
42
43     bool vis(pt a, int i) {
44         return visSide(a, i) || visSide(a, i + n - 1);
45     }
46
47     bool isTangent(pt a, int i) {
48         return visSide(a, i) != visSide(a, i + n - 1);
49     }
50
51     int binSearch(int l, int r, pt a) {
52         //tricky binsearch; l < r not necessarily
53         while (abs(l - r) > 1) {
54             int c = (l + r) / 2;
55             if (vis(a, c))
56                 l = c;
57             else
58                 r = c;
59         }
60         assert(isTangent(a, l));
61         return l % n;
62     }
63
64     //check: n >= 3
65     pair<int, int> tangents(pt a) {
66         assert(n >= 3);
67         pt M = (h[0] + h[1] + h[2]) * (1. / 3);
68         if (a == M)
69             return {-1, -1};
70         Cmp cmp{M, h[0] - M};
71         //assert(is_sorted(all(h), cmp));
72         int pos = upper_bound(all(h), a, cmp) - h.begin();
73         pt L = h[(pos + n - 1) % n], R = h[pos % n];
74         if ((R - L) % (a - L) >= -eps)
75             return {-1, -1}; //point inside hull
76         int pos2 = upper_bound(all(h), M*2-a, cmp) - h.begin();
77         assert(pos % n != pos2 % n);
78         if (pos > pos2)
79             pos2 += n;
80         return {binSearch(pos, pos2, a),
81             binSearch(pos + n - 1, pos2 - 1, a)};
82     }
83 };

```

## 14 geometry/primitives.cpp

```

1 struct line {
2     pt v;
3     ld c; //  $v \cdot p = c$ 
4
5     //check:  $p_1 \neq p_2$ 
6     line(pt p1, pt p2) {
7         v = (p2 - p1).rot();
8         v = v * (1. / v.abs());
9         c = v * p1;
10    }
11
12    // Convert from  $ax + by + c = 0$ 
13
14    //check:  $a^2 + b^2 > 0$ 
15    line(ld a, ld b, ld _c): v(pt{a, b}), c(-_c) {
16        ld d = v.abs();
17        v = v * (1. / d);
18        c /= d;
19    }
20
21    //check:  $v.abs() == 1$ 
22    ld signedDist(pt p) {
23        return v * p - c;
24    }
25};
26
27//check:  $a \neq b$ 
28pt lineProjection(pt p, pt a, pt b) {
29    pt v = (b - a).rot();
30    ld s = (p - a) % (b - a);
31    return p + v * (s / v.abs2());
32}
33
34ld pointSegmentDist(pt p, pt a, pt b) {
35    if ((p - a) * (b - a) <= 0 || ze((b - a).abs()))
36        return (p - a).abs();
37    if ((p - b) * (a - b) <= 0)
38        return (p - b).abs();
39    return fabs1((p - a) % (p - b)) / (b - a).abs();
40}
41
42pt linesIntersection(line l1, line l2) {
43    ld d = l1.v.x * l2.v.y - l1.v.y * l2.v.x;
44    if (ze(d)) {
45        if (eq(l1.c, l2.c)) {
46            //stub: equal lines
47        } else {
48            //stub: empty intersection
49        }
50        return pt{1e18, 1e18};
51    }
52    ld dx = l1.c * l2.v.y - l1.v.y * l2.c;
53    ld dy = l1.v.x * l2.c - l1.c * l2.v.x;
54    return pt{dx / d, dy / d};
55}
56
57pt linesIntersection(pt a, pt b, pt c, pt d) {
58    ld s = (b - a) % (d - c);
59    if (ze(s)) {
60        //stub: parallel or equal lines
61        return pt{1e18, 1e18};
62    }
63    ld s1 = (c - a) % (d - a);
64    return a + (b - a) * (s1 / s);
65}
66
67bool pointInsideSegment(pt p, pt a, pt b) {
68    if (!ze((p - a) % (p - b)))
69        return false;
70    ld prod = (a - p) * (b - p);
71    return ze(prod) || prod < 0;
72    if (ze(prod)) {
73        //stub: coincides with segment end
74        return true;
75    }
76    return prod < 0;
77}
78
79bool checkSegmentIntersection(pt a, pt b, pt c, pt d) {
80    if (ze((a - b) % (c - d))) {
81        if (pointInsideSegment(a, c, d) ||
82            pointInsideSegment(b, c, d) ||
83            pointInsideSegment(c, a, b) ||
84            pointInsideSegment(d, a, b)) {
85            //stub: intersection of parallel segments
86            return true;
87        }
88        return false;
89    }
90    ld s1, s2;
91    forn (iter, 2) {
92        s1 = (c - a) % (b - a);
93        s2 = (d - a) % (b - a);
94        if (s1 > eps && s2 > eps)
95            return false;
96        if (s1 < -eps && s2 < -eps)
97            return false;
98        swap(a, c), swap(b, d);
99    }
100    return true;
101}
102
103vector<pt> lineCircleIntersection(line l, pt a, ld r) {
104    ld d = l.signedDist(a);
105    pt h = a - l.v * d;
106    if (eq(fabs1(d), r))
107        return {h};
108    else if (fabs1(d) > r)
109        return {};
110    pt w = l.v.rot() * Sqrt(sqr(r) - sqr(d));
111    return {h + w, h - w};
112}
113
114vector<pt> circlesIntersecton(pt a, ld r1, pt b, ld r2) {
115    ld d = (a - b).abs();
116    if (ze(d) && eq(r1, r2)) {
117        //stub: equal circles
118        return {};
119    }
120    // intersection is non-empty iff
121    // triangle with sides r1, r2, d exists
122    ld per = r1 + r2 + d;
123    ld mx = max(max(r1, r2), d);
124    int num = 2;
125    if (eq(mx * 2, per)) {
126        num = 1;
127    } else if (mx * 2 > per)
128        return {};
129    ld part = (sqr(r1) + sqr(d) - sqr(r2)) / ld(2 * d);
130    pt h = a + (b - a) * (part / d);
131    if (num == 1)
132        return {h};
133    ld dh = Sqrt(sqr(r1) - sqr(part));
134    pt w = ((b - a) * (dh / d)).rot();
135    return {h + w, h - w};
136}
137
138vector<pt> circleTangents(pt p, pt a, ld r) {
139    ld d = (p - a).abs();
140    if (eq(r, d))
141        return {p};
142    else if (r > d)
143        return {};
144    ld len = Sqrt(sqr(d) - sqr(r));
145    vector<pt> res;
146    pt vec = (a - p) * (len / sqr(d));
147    for (int sgn: {-1, 1})
148        res.push_back(p + vec.rotCw(pt{len, r * sgn}));
149    return res;
150}
151
152vector<line> circlesBitangents(pt a, ld r1, pt b, ld r2) {
153    ld d = (a - b).abs();
154    if (ze(d) && eq(r1, r2)) {
155        //stub: equal circles
156        return {};
157    }
158
159    vector<line> res;
160    for (int s1: {-1, 1})
161        for (int s2: {-1, 1}) {
162            // inner tangent iff s1 != s2
163            // treat radii as signed
164            ld r = s2 * r2 - s1 * r1;
165            if (eq(fabs1(r), d)) {
166                // incident tangents; need only one copy
167                if (s1 == 1)
168                    continue;
169            } else if (fabs1(r) > d)
170                continue;
171            ld len = Sqrt(sqr(d) - sqr(r));
172            line l(a, a + (b - a).rotCw(pt{len, r}));
173            l.c -= s1 * r1;
174            res.push_back(l);
175        }
176    return res;
177}

```

## 15 geometry/svg.cpp

```

1 struct SVG {
2
3     FILE *out;
4     ld sc = 50;
5
6     void open() {
7         out = fopen("image.svg", "w");
8         fprintf(out, "<svg xmlns='http://www.w3.org/2000/svg'
9             ↪ viewBox='-1000 -1000 2000 2000'>\n");
10    }
11
12    void line(pt a, pt b) {
13        a = a * sc, b = b * sc;
14        fprintf(out, "<line x1='%Lf' y1='%Lf' x2='%Lf' y2='%Lf'
15            ↪ stroke='black'/>\n", a.x, -a.y, b.x, -b.y);
16    }
17
18    void circle(pt a, ld r = -1, string col = "red") {
19        r = (r == -1 ? 10 : sc * r);
20        a = a * sc;
21        fprintf(out, "<circle cx='%Lf' cy='%Lf' r='%Lf'
22            ↪ fill='%s'/>\n", a.x, -a.y, r, col.c_str());
23    }
24
25    void text(pt a, string s) {
26        a = a * sc;
27        fprintf(out, "<text x='%Lf' y='%Lf'
28            ↪ font-size='10px'>s</text>\n", a.x, -a.y,
29            ↪ s.c_str());
30    }
31
32    void close() {
33        fprintf(out, "</svg>\n");
34        fclose(out);
35        out = 0;
36    }
37
38    ~SVG() {
39        if (out)
40            close();
41    }
42 }
43
44 SVG svg;

```

## 16 graphs/2sat.cpp

```

1 const int maxn = 200100; //2 * number of variables
2
3 namespace TwoSAT {
4     int n; //number of variables
5     bool used[maxn];
6     vector<int> g[maxn];
7     vector<int> gr[maxn];
8     int comp[maxn];
9     int res[maxn];
10
11     void addEdge(int u, int v) { //u or v
12         g[u].push_back(v ^ 1);
13         g[v].push_back(u ^ 1);
14         gr[u ^ 1].push_back(v);
15         gr[v ^ 1].push_back(u);
16     }
17
18     vector<int> ord;
19     void dfs1(int u) {
20         used[u] = true;
21         for (int v: g[u]) {
22             if (used[v])
23                 continue;
24             dfs1(v);
25         }
26         ord.push_back(u);
27     }
28
29     int COL = 0;
30     void dfs2(int u) {
31         used[u] = true;
32         comp[u] = COL;
33         for (int v: gr[u]) {
34             if (used[v])
35                 continue;
36             dfs2(v);
37         }
38     }
39
40     void mark(int u) {
41         res[u / 2] = u % 2;
42         used[u] = true;
43         for (int v: g[u]) {
44             if (used[v])
45                 continue;
46             mark(v);
47         }
48     }
49
50     bool run() {
51         fill(res, res + 2 * n, -1);
52         fill(used, used + 2 * n, false);
53         for (i, 2 * n)
54             if (!used[i])
55                 dfs1(i);
56         reverse(ord.begin(), ord.end());
57         assert((int) ord.size() == (2 * n));
58         fill(used, used + 2 * n, false);
59         for (int u: ord) if (!used[u]) {
60             dfs2(u);
61             ++COL;
62         }
63         for (i, n)
64             if (comp[i * 2] == comp[i * 2 + 1])
65                 return false;
66
67         reverse(ord.begin(), ord.end());
68         fill(used, used + 2 * n, false);
69         for (int u: ord) {
70             if (res[u / 2] != -1) {
71                 continue;
72             }
73             mark(u);
74         }
75         return true;
76     }
77 }
78
79 int main() {
80     TwoSAT::n = 2;
81     TwoSAT::addEdge(0, 2); //x or y
82     TwoSAT::addEdge(0, 3); //x or !y
83     TwoSAT::addEdge(3, 3); //!y or !y
84     assert(TwoSAT::run());
85     cout << TwoSAT::res[0] << ' ' << TwoSAT::res[1] << '\n';
86     //1 0
87 }

```

## 17 graphs/directed\_mst.cpp

```

1 struct Edge {
2     int v, to, id, w;
3     bool operator<(const Edge& other) const {
4         return w < other.w;
5     }
6 };
7 typedef pair<multiset<Edge>*, int> Set; // real value: x-Set.se
8 Set merge(Set a, Set b) {
9     if (a.fi == NULL) return b;
10    if (b.fi->size() > a.fi->size()) swap(a, b);
11    for (Edge e: *b.fi) {
12        a.fi->insert(Edge{e.v, e.to, e.id, e.w - b.se + a.se});
13    }
14    return a;
15 }
16 Edge take(Set& set) {
17     auto e = *set.fi->begin();
18     set.fi->erase(set.fi->begin());
19     assert(e.w >= set.se);
20     e.w -= set.se;
21     set.se += e.w;
22     return e;
23 }
24
25 int n;
26 int p[maxn];
27 int get(int x) { return x == p[x] ? x : (p[x] = get(p[x])); }
28
29 Set out[maxn]; // outgoing edges from v, endpoints swapped
30 int b[maxn], top[maxn], done[maxn];
31 int nc;
32 int root;
33 vector<int> edges;
34 vi cycle[maxn];
35 vi st;
36 i64 res;
37 Edge in[maxn];
38
39 void restore(Edge e) {
40     edges.push_back(e.id);
41     int v = e.v;
42     int prev = v;
43     while (v != -1) {
44         done[v] = true;
45         if (v >= n) {
46             for (int x: cycle[v]) {
47                 if (x != prev) {
48                     top[x] = -1;
49                     restore(in[x]);
50                 }
51             }
52         }
53         prev = v;
54         v = top[v];
55     }
56 }
57
58 void solve() {
59     for (i = 1; i <= n; i++) p[i] = i, top[i] = -1;
60     nc = n;
61     root = 0;
62     done[root] = true;
63     for (start = 1; start <= n; start++) {
64         st = {start};
65         b[start] = 1;
66         while (!done[st[0]]) {
67             int v = st.back();
68             b[v] = 1;
69             if (done[v]) {
70                 assert(st.size() >= 2);
71                 st.pop_back();
72                 assert(!done[st.back()]);
73                 restore(in[st.back()]);
74                 assert(done[st.back()]);
75                 continue;
76             }
77             assert(!out[v].fi->empty());
78             auto e = take(out[v]);
79             in[v] = e;
80             res += e.w;
81             int to = get(e.to);
82             if (to == v) continue;
83             if (b[to] && !done[to]) {
84                 while (true) {
85                     int u = st.back();
86                     st.pop_back();
87                     top[u] = nc;
88                     p[get(u)] = nc;
89                     out[nc] = merge(out[nc], out[u]);
90                     cycle[nc].push_back(u);
91                     if (u == to) break;

```

```

92                 }
93                 st.push_back(nc);
94                 b[nc] = 1;
95                 ++nc;
96             } else {
97                 st.push_back(to);
98             }
99         }
100     }
101     for (i = 1; i <= n; i++) assert(done[i]);
102     assert((int)edges.size() == n-1);
103     cout << res << endl;
104 }
105
106 void scan() {
107     int m;
108     scanf("%d", &m);
109     for (i = 1; i <= m; i++) out[i].fi = new multiset<Edge>();
110     for (i = 1; i <= m; i++) {
111         int u, v, w;
112         scanf("%d%d%d", &u, &v, &w);
113         --u, --v;
114         out[v].fi->insert(Edge{v, u, i, w});
115     }
116 }

```

## 18 graphs/directed\_mst\_ev.cpp

```

1// WARNING: this code wasn't submitted anywhere
2
3namespace TwoChinese {
4
5struct Edge {
6    int to, w, id;
7    bool operator<(const Edge& other) const {
8        return to < other.to || (to == other.to && w < other.w);
9    }
10};
11typedef vector<vector<Edge>> Graph;
12
13const int maxn = 2050;
14
15// global, for supplementary algorithms
16int b[maxn];
17int tin[maxn], tup[maxn];
18int dtime; // counter for tin, tout
19vector<int> st;
20int nc; // number of strongly connected components
21int q[maxn];
22
23int answer;
24
25void tarjan(int v, const Graph& e, vector<int>& comp) {
26    b[v] = 1;
27    st.push_back(v);
28    tin[v] = tup[v] = dtime++;
29
30    for (Edge t: e[v]) if (t.w == 0) {
31        int to = t.to;
32        if (b[to] == 0) {
33            tarjan(to, e, comp);
34            tup[v] = min(tup[v], tup[to]);
35        } else if (b[to] == 1) {
36            tup[v] = min(tup[v], tin[to]);
37        }
38    }
39
40    if (tin[v] == tup[v]) {
41        while (true) {
42            int t = st.back();
43            st.pop_back();
44            comp[t] = nc;
45            b[t] = 2;
46            if (t == v) break;
47        }
48        ++nc;
49    }
50}
51
52vector<Edge> bfs(
53    const Graph& e, const vi& init, const vi& comp)
54{
55    int n = e.size();
56    forn(i, n) b[i] = 0;
57    int lq = 0, rq = 0;
58    for (int v: init) b[v] = 1, q[rq++] = v;
59
60    vector<Edge> result;
61
62    while (lq != rq) {
63        int v = q[lq++];
64        for (Edge t: e[v]) if (t.w == 0) {
65            int to = t.to;
66            if (b[to]) continue;
67            if (!comp.empty() && comp[v] != comp[to]) continue;
68            b[to] = 1;
69            q[rq++] = to;
70            result.push_back(t);
71        }
72    }
73
74    return result;
75}
76
77// warning: check that each vertex is reachable from root
78vector<Edge> run(Graph e, int root) {
79    int n = e.size();
80
81    // find minimum incoming weight for each vertex
82    vector<int> minw(n, inf);
83    forn(v, n) for (Edge t: e[v]) {
84        minw[t.to] = min(minw[t.to], t.w);
85    }
86    forn(v, n) for (Edge &t: e[v]) if (t.to != root) {
87        t.w -= minw[t.to];
88    }
89    forn(i, n) if (i != root) answer += minw[i];
90
91    // check if each vertex is reachable from root by zero edges
92    vector<Edge> firstResult = bfs(e, {root}, {});
93    if ((int)firstResult.size() + 1 == n) {
94        return firstResult;
95    }
96
97    // find stongly connected comp-s and build compressed graph
98    vector<int> comp(n);
99    forn(i, n) b[i] = 0;
100    nc = 0;
101    dtime = 0;
102    forn(i, n) if (!b[i]) tarjan(i, e, comp);
103
104    // multiple edges may be removed here if needed
105    Graph ne(nc);
106    forn(v, n) for (Edge t: e[v]) {
107        if (comp[v] != comp[t.to]) {
108            ne[comp[v]].push_back({comp[t.to], t.w, t.id});
109        }
110    }
111    int oldnc = nc;
112
113    // run recursively on compressed graph
114    vector<Edge> subres = run(ne, comp[root]);
115
116    // find incoming edge id for each component, init queue
117    // if there is an edge (u, v) between different components
118    // than v is added to queue
119    nc = oldnc;
120    vector<int> incomingId(nc);
121    for (Edge e: subres) {
122        incomingId[e.to] = e.id;
123    }
124
125    vector<Edge> result;
126    vector<int> init;
127    init.push_back(root);
128    forn(v, n) for (Edge t: e[v]) {
129        if (incomingId[comp[t.to]] == t.id) {
130            result.push_back(t);
131            init.push_back(t.to);
132        }
133    }
134
135    // run bfs to add edges inside components and return answer
136    vector<Edge> innerEdges = bfs(e, init, comp);
137    result.insert(result.end(), all(innerEdges));
138
139    assert((int)result.size() + 1 == n);
140    return result;
141}
142
143} // namespace TwoChinese
144
145void test () {
146    auto res = TwoChinese::run({
147        {{1,5,0},{2,5,1}},
148        {{3,1,2}},
149        {{1,2,3},{4,1,4}},
150        {{1,1,5},{4,2,6}},
151        {{2,1,7}}},
152        0);
153    cout << TwoChinese::answer << endl;
154    for (auto e: res) cout << e.id << " ";
155    cout << endl;
156    // 9    0 6 2 7
157}

```

## 19 graphs/dominator\_tree.cpp

```

1 struct Dom {
2     int n;
3     vector<vi> e, re; // graph (on v), reverse graph (on id)
4     vi id, p, sdom, dom, dsu, best;
5     vector<vi> bucket;
6     int dtime = 0;
7
8     Dom() {}
9     Dom(int n) : n(n), e(n), re(n), id(n, -1), p(n),
10        sdom(n), dom(n), dsu(n), best(n), bucket(n)
11    {}
12
13    void find(int v) {
14        if (v != dsu[v]) {
15            find(dsu[v]);
16            if (sdom[best[dsu[v]]] <= sdom[best[v]]) {
17                best[v] = best[dsu[v]];
18            }
19            dsu[v] = dsu[dsu[v]];
20        }
21    }
22
23    void dfs1(int v) {
24        id[v] = dtime++;
25        for (int to: e[v]) {
26            if (id[to] == -1) {
27                dfs1(to);
28                p[id[to]] = id[v];
29            }
30            re[id[to]].push_back(id[v]);
31        }
32    }
33
34    void pre() {
35        dfs1(0);
36        iota(all(best), 0);
37        iota(all(sdom), 0);
38        iota(all(dsu), 0);
39    }
40
41    void run() {
42        pre();
43        for (int v = n-1; v >= 0; --v) {
44            for (int w: bucket[v]) {
45                find(w);
46                dom[w] = best[w];
47            }
48            for (int u: re[v]) {
49                find(u);
50                sdom[v] = min(sdom[v], sdom[best[u]]);
51            }
52            if (v) {
53                bucket[sdom[v]].pb(v);
54                dsu[v] = p[v]; // unite(v, p[v])
55            }
56        }
57
58        for (int v = 1; v < n; ++v) {
59            if (dom[v] != sdom[v]) {
60                dom[v] = dom[dom[v]];
61            }
62        }
63
64        vi ndom(n), rev(n);
65        for (i, n) rev[id[i]] = i;
66        for (i, n) ndom[i] = rev[dom[id[i]]];
67        dom = ndom;
68    }
69};

```

## 20 graphs/edmonds\_matching.cpp

```

1 int n;
2 vi e[maxn];
3 int mt[maxn], p[maxn], base[maxn], b[maxn], blos[maxn];
4 int q[maxn];
5 int blca[maxn]; // used for lca
6
7 int lca(int u, int v) {
8     for (i, n) blca[i] = 0;
9     while (true) {
10         u = base[u];
11         blca[u] = 1;
12         if (mt[u] == -1) break;
13         u = p[mt[u]];
14     }
15     while (!blca[base[v]]) {
16         v = p[mt[base[v]]];
17     }
18     return base[v];
19 }
20
21 void mark_path(int v, int b, int ch) {
22     while (base[v] != b) {
23         blos[base[v]] = blos[base[mt[v]]] = 1;
24         p[v] = ch;
25         ch = mt[v];
26         v = p[mt[v]];
27     }
28 }
29
30 int find_path(int root) {
31     for (i, n) {
32         base[i] = i;
33         p[i] = -1;
34         b[i] = 0;
35     }
36
37     b[root] = 1;
38     q[0] = root;
39     int lq = 0, rq = 1;
40     while (lq != rq) {
41         int v = q[lq++];
42         for (int to: e[v]) {
43             if (base[v] == base[to] || mt[v] == to) continue;
44             if (to == root || (mt[to] != -1 && p[mt[to]] != -1)) {
45                 int curbase = lca(v, to);
46                 for (i, n) blos[i] = 0;
47                 mark_path(v, curbase, to);
48                 mark_path(to, curbase, v);
49                 for (i, n) if (blos[base[i]]) {
50                     base[i] = curbase;
51                     if (!b[i]) b[i] = 1, q[rq++] = i;
52                 }
53             } else if (p[to] == -1) {
54                 p[to] = v;
55                 if (mt[to] == -1) {
56                     return to;
57                 }
58                 to = mt[to];
59                 b[to] = 1;
60                 q[rq++] = to;
61             }
62         }
63     }
64 }
65 return -1;
66 }
67
68 int matching() {
69     for (i, n) mt[i] = -1;
70     int res = 0;
71     for (i, n) if (mt[i] == -1) {
72         int v = find_path(i);
73         if (v != -1) {
74             ++res;
75             while (v != -1) {
76                 int pv = p[v], ppv = mt[p[v]];
77                 mt[v] = pv, mt[ppv] = v;
78                 v = ppv;
79             }
80         }
81     }
82     return res;
83 }

```

## 21 graphs/euler\_cycle.cpp

```

1 struct Edge {
2     int to, id;
3 };
4
5 bool usedEdge[maxn];
6 vector<Edge> g[maxn];
7 int ptr[maxn];
8
9 vector<int> cycle;
10 void eulerCycle(int u) {
11     while (ptr[u] < sz(g[u]) && usedEdge[g[u][ptr[u]].id])
12         ++ptr[u];
13     if (ptr[u] == sz(g[u]))
14         return;
15     const Edge &e = g[u][ptr[u]];
16     usedEdge[e.id] = true;
17     eulerCycle(e.to);
18     cycle.push_back(e.id);
19     eulerCycle(u);
20 }
21
22 int edges = 0;
23 void addEdge(int u, int v) {
24     g[u].push_back(Edge{v, edges});
25     g[v].push_back(Edge{u, edges++});
26 }

```

## 22 graphs/min\_automaton.cpp

```

1 vi inc[maxn][A];
2 int lst[maxn], pos[maxn], part[maxn];
3 int lp[maxn], rp[maxn], nrp[maxn];
4 int upd[maxn], used[maxn], inq[maxn];
5 vector<int> q;
6 int dtype;
7 int np; // number of classes
8 vector<int> toRefine[A];
9
10 void doSwap(int x, int y) {
11     swap(lst[pos[x]], lst[pos[y]]);
12     swap(pos[x], pos[y]);
13 }
14
15 void refine(const vi& a) {
16     ++dtype;
17     vector<int> updated;
18     for (int x: a) {
19         if (used[x] == dtype) continue;
20         used[x] = dtype;
21
22         int p = part[x];
23         if (upd[p] != dtype) {
24             upd[p] = dtype;
25             nrp[p] = rp[p];
26             updated.pb(p);
27         }
28
29         doSwap(x, lst[nrp[p]-1]);
30         --nrp[p];
31     }
32
33     for (int p: updated) {
34         if (lp[p] == nrp[p]) continue;
35         lp[np] = nrp[p];
36         rp[np] = rp[p];
37         rp[p] = nrp[p];
38         for (int i = lp[np]; i < rp[np]; ++i) {
39             part[lst[i]] = np;
40         }
41
42         if (inq[p] || rp[np] - lp[np] < rp[p] - lp[p]) {
43             inq[np] = 1;
44             q.push_back(np);
45         } else {
46             inq[p] = 1;
47             q.push_back(p);
48         }
49
50         ++np;
51     }
52 }
53
54 void solve() {
55     forn(i, n) lst[i] = i;
56     sort(lst, lst+n, [](int i, int j) {
57         return col[i] < col[j];
58     });
59
60     forn(i, n) {
61         if (i && col[lst[i]] != col[lst[i-1]]) {
62             rp[np] = i;
63             lp[++np] = i;
64         }
65         part[lst[i]] = np;
66         pos[lst[i]] = i;
67     }
68     rp[np++] = n;
69
70     forn(i, np) {
71         inq[i] = 1;
72         q.push_back(i);
73     }
74
75     forn(i, q.size()) {
76         int p = q[i];
77         inq[p] = false;
78         forn(c, A) {
79             toRefine[c].clear();
80             for (int id = lp[p]; id < rp[p]; ++id) {
81                 toRefine[c].insert(
82                     toRefine[c].end(), all(inc[lst[id]][c]));
83             }
84         }
85         forn(c, A) if (!toRefine[c].empty()) {
86             refine(toRefine[c]);
87         }
88     }
89
90     forn(i, n) printf("%d\n", part[i] + 1);
91 }

```

## 23 math/factor.cpp

```

1//WARNING: only mod <= 1e18
2ll mul(ll a, ll b, ll mod) {
3    ll res = a * b - (ll(ld(a) * ld(b) / ld(mod)) * mod);
4    while (res < 0)
5        res += mod;
6    while (res >= mod)
7        res -= mod;
8    return res;
9}
10
11bool millerRabinTest(ll n, ll a) {
12    if (gcd(n, a) > 1)
13        return false;
14    ll x = n - 1;
15    int l = 0;
16    while (x % 2 == 0) {
17        x /= 2;
18        ++l;
19    }
20    ll c = binpow(a, x, n);
21    for (int i = 0; i < l; ++i) {
22        ll nx = mul(c, c, n);
23        if (nx == 1) {
24            if (c != 1 && c != n - 1)
25                return false;
26            else
27                return true;
28        }
29        c = nx;
30    }
31    return c == 1;
32}
33
34bool isPrime(ll n) {
35    if (n == 1)
36        return false;
37    if (n % 2 == 0)
38        return n == 2;
39    for (ll a = 2; a < min<ll>(8, n); ++a)
40        if (!millerRabinTest(n, a))
41            return false;
42    return true;
43}
44
45//WARNING: p is not sorted
46void factorize(ll x, vector<ll> &p) {
47    if (x == 1)
48        return;
49    if (isPrime(x)) {
50        p.push_back(x);
51        return;
52    }
53    for (ll d: {2, 3, 5})
54        if (x % d == 0) {
55            p.push_back(d);
56            factorize(x / d, p);
57            return;
58        }
59    while (true) {
60        ll x1 = rr() % (x - 1) + 1;
61        ll x2 = (mul(x1, x1, x) + 1) % x;
62        int i1 = 1, i2 = 2;
63        while (true) {
64            ll c = (x1 + x - x2) % x;
65            if (c == 0)
66                break;
67            ll g = gcd(c, x);
68            if (g > 1) {
69                factorize(g, p);
70                factorize(x / g, p);
71                return;
72            }
73            if (i1 * 2 == i2) {
74                i1 *= 2;
75                x1 = x2;
76            }
77            ++i2;
78            x2 = (mul(x2, x2, x) + 1) % x;
79        }
80    }
81}

```

## 24 math/fft.cpp

```

1const int LG = 20;
2typedef complex<ld> base;
3
4vector<base> ang[LG + 5];
5
6void init_fft() {
7    int n = 1 << LG;
8    ld e = acosl(-1) * 2 / n;
9    ang[LG].resize(n);
10    forn(i, n)
11        ang[LG][i] = polar(ld(1), e * i);
12
13    for (int k = LG - 1; k >= 0; --k) {
14        ang[k].resize(1 << k);
15        forn(i, 1 << k)
16            ang[k][i] = ang[k + 1][i * 2];
17    }
18}
19
20void fft_rec(base *a, int lg, bool inv) {
21    if (lg == 0)
22        return;
23    int hlen = 1 << (lg - 1);
24    fft_rec(a, lg - 1, inv);
25    fft_rec(a + hlen, lg - 1, inv);
26
27    forn(i, hlen) {
28        base w = ang[lg][i];
29        if (inv)
30            w = conj(w);
31        base u = a[i];
32        base v = a[i + hlen] * w;
33        a[i] = u + v;
34        a[i + hlen] = u - v;
35    }
36}
37
38void fft(base *a, int lg, bool inv) {
39    int n = 1 << lg;
40    int j = 0, bit;
41    for (int i = 1; i < n; ++i) {
42        for (bit = n >> 1; bit & j; bit >>= 1)
43            j ^= bit;
44        j ^= bit;
45        if (i < j)
46            swap(a[i], a[j]);
47    }
48    fft_rec(a, lg, inv);
49    if (inv) {
50        forn(i, n)
51            a[i] /= n;
52    }
53}
54
55void test() {
56    int lg = 3;
57    int n = 1 << lg;
58    init_fft();
59    base a[] = {1, 3, 5, 2, 4, 6, 7, 1};
60    fft(a, lg, 0);
61    forn(i, n)
62        cout << a[i].real() << " ";
63    cout << '\n';
64    forn(i, n)
65        cout << a[i].imag() << " ";
66    cout << '\n';
67    // 29 -5.82843 -7 -0.171573 5 -0.171573 -7 -5.82843
68    // 0 -3.41421 6 0.585786 0 -0.585786 -6 3.41421
69}

```



## 25 math/fft\_inv.cpp

```

1 vector <int> mul(vector <int> a, vector <int> b,
2     bool carry = true) {
3     int n = sz(a);
4     if (carry) {
5         a.resize(n * 2);
6         b.resize(n * 2);
7     }
8     fft(a.data(), a.size(), false);
9     fft(b.data(), b.size(), false);
10    for (int i = 0; i < sz(a); ++i)
11        a[i] = mul(a[i], b[i]);
12    fft(a.data(), a.size(), true);
13    a.resize(n);
14    return a;
15}
16
17 vector <int> inv(vector <int> v) {
18     int n = 1;
19     while (n < sz(v))
20         n <= 1;
21     v.resize(n, 0);
22     vector <int> res(1, binpow(v[0], mod - 2));
23     for (int k = 1; k < n; k <= 1) {
24         vector <int> A(k * 2, 0);
25         copy(v.begin(), v.begin() + k, A.begin());
26         vector <int> C = res;
27         C.resize(k * 2, 0);
28         A = mul(A, C, false);
29         for (int i = 0; i < 2 * k; ++i)
30             A[i] = sub(0, A[i]);
31         A[0] = sum(A[0], 1);
32         for (int i = 0; i < k; ++i)
33             assert(A[i] == 0);
34         copy(A.begin() + k, A.end(), A.begin());
35         A.resize(k);
36         vector <int> B(k);
37         copy(v.begin() + k, v.begin() + 2 * k, B.begin());
38         C.resize(k);
39         B = mul(B, C);
40         for (int i = 0; i < k; ++i)
41             A[i] = sub(A[i], B[i]);
42         A = mul(A, C);
43         res.resize(k * 2);
44         copy(A.begin(), A.end(), res.begin() + k);
45     }
46     return res;
47}

```

## 26 math/golden\_search.cpp

```

1 ld f(ld x) {
2     return 5 * x * x + 100 * x + 1; // -10 is minimum
3 }
4
5 ld goldenSearch(ld l, ld r) {
6     ld phi = (1 + sqrt(5)) / 2;
7     ld resphi = 2 - phi;
8     ld x1 = l + resphi * (r - l);
9     ld x2 = r - resphi * (r - l);
10    ld f1 = f(x1);
11    ld f2 = f(x2);
12    forn (iter, 60) {
13        if (f1 < f2) {
14            r = x2;
15            x2 = x1;
16            f2 = f1;
17            x1 = l + resphi * (r - l);
18            f1 = f(x1);
19        } else {
20            l = x1;
21            x1 = x2;
22            f1 = f2;
23            x2 = r - resphi * (r - l);
24            f2 = f(x2);
25        }
26    }
27    return (x1 + x2) / 2;
28}
29
30 int main() {
31     std::cout << goldenSearch(-100, 100) << '\n';
32}

```

## 27 math/numbers.tex

- Simpson and Gauss numerical integration:

$$\int_a^b f(x)dx = (b-a)/6 \cdot (f(a) + 4(f(a+b)/2) + f(b))$$

$$\int_{-1}^1, x_{1,3} = \pm\sqrt{0.6}, x_2 = 0; a_{1,3} = 5/9, a_2 = 8/9$$

- Large primes:  $10^{18} + 3, +31, +3111, 10^9 + 21, +33$

- FFT modules:

$$\begin{array}{lll} 1\ 107\ 296\ 257 & 2^{25} \cdot 3 \cdot 11 + 1 & 10 \\ 1\ 161\ 822\ 209 & 2^{22} \cdot 277 + 1 & 3 \\ 1\ 261\ 007\ 895\ 663\ 738\ 881 & 2^{55} \cdot 5 \cdot 7 + 1 & 6 \text{ (check)} \end{array}$$

- Fibonacci numbers:

$$\begin{array}{ll} 1, 2 : & 1 \\ 45 : & 1\ 134\ 903\ 170 \\ 46 : & 1\ 836\ 311\ 903 \text{ (max int)} \\ 47 : & 2\ 971\ 215\ 073 \text{ (max unsigned)} \\ 91 : & 4\ 660\ 046\ 610\ 375\ 530\ 309 \\ 92 : & 7\ 540\ 113\ 804\ 746\ 346\ 429 \text{ (max i64)} \\ 93 : & 12\ 200\ 160\ 415\ 121\ 876\ 738 \text{ (max unsigned i64)} \end{array}$$

- Powers of two

$$\begin{array}{l} 2^{31} = 2\ 147\ 483\ 648 = 2.1 \cdot 10^9 \\ 2^{32} = 4\ 294\ 967\ 296 = 4.2 \cdot 10^9 \\ 2^{63} = 9\ 223\ 372\ 036\ 854\ 775\ 808 = 9.2 \cdot 10^{18} \\ 2^{64} = 18\ 446\ 744\ 073\ 709\ 551\ 616 = 1.8 \cdot 10^{19} \end{array}$$

- Highly composite numbers

$$\begin{array}{l} - \leq 1000: d(840) = 32, \leq 10^4: d(9\ 240) = 64 \\ - \leq 10^5: d(83\ 160) = 128, \leq 10^6: d(720\ 720) = 240 \\ - \leq 10^7: d(8\ 648\ 640) = 448, \leq 10^8: d(91\ 891\ 800) = 768 \\ - \leq 10^9: d(931\ 170\ 240) = 1344 \\ - \leq 10^{11}: d(97\ 772\ 875\ 200) = 4032 \\ - \leq 10^{12}: d(963\ 761\ 198\ 400) = 6720 \\ - \leq 10^{15}: d(866\ 421\ 317\ 361\ 600) = 26880 \\ - \leq 10^{18}: d(897\ 612\ 484\ 786\ 617\ 600) = 103680 \end{array}$$

- Misc

- Расстояние между точками по сфере:  $L = R \cdot \arccos(\cos \theta_1 \cdot \cos \theta_2 + \sin \theta_1 \cdot \sin \theta_2 \cdot \cos(\varphi_1 - \varphi_2))$ , где  $\theta$  — широты (от  $-\frac{\pi}{2}$  до  $\frac{\pi}{2}$ ),  $\varphi$  — долготы (от  $-\pi$  до  $\pi$ ).
- Объём шарового сегмента:  $V = \pi h^2(R - \frac{1}{3}h)$ , где  $h$  — высота от вершины сектора до секущей плоскости
- Площадь поверхности шарового сегмента:  $S = 2\pi Rh$ , где  $h$  — высота.

- Bell numbers: 0:1, 1:1, 2:2, 3:5, 4:15, 5:52, 6:203, 7:877, 8:4140, 9:21147, 10:115975, 11:678570, 12:4213597, 13:27644437, 14:190899322, 15:1382958545, 16:10480142147, 17:82864869804, 18:682076806159, 19:5832742205057, 20:51724158235372, 21:474869816156751, 22:4506715738447323, 23:44152005855084346

- Catalan numbers: 0:1, 1:1, 2:2, 3:5, 4:14, 5:42, 6:132, 7:429, 8:1430, 9:4862, 10:16796, 11:58786, 12:208012, 13:742900, 14:2674440, 15:9694845, 16:35357670, 17:129644790, 18:477638700, 19:1767263190, 20:6564120420, 21:24466267020, 22:91482563640, 23:343059613650, 24:1289904147324, 25:4861946401452

## 28 math/quadratic\_equation.cpp

```
1 vector<ld> sqrRoots(ld a, ld b, ld c) {
2     ld d = b * b - 4 * a * c;
3     if (ze(d))
4         return {-b / (2 * a)};
5     if (d < 0)
6         return {};
7     d = sqrtl(d);
8     if (ze(b)) {
9         ld x1 = -d / (2 * a);
10        ld x2 = d / (2 * a);
11        if (x1 > x2)
12            swap(x1, x2);
13        return {x1, x2};
14    }
15    ld sgn = b > 0 ? 1 : -1;
16    ld x1 = (-b - sgn * d) / (2 * a);
17    ld x2 = c / (a * x1);
18    if (x1 > x2)
19        swap(x1, x2);
20    return {x1, x2};
21 }
```

## 29 math/simplex.cpp

```

1 namespace Simplex {
2
3 ld D[maxm][maxn]; // [n+2][m+2]
4 int B[maxm];
5 int N[maxn];
6 ld x[maxn];
7 int n, m;
8
9 //x >= 0, Ax <= b, c^T x -> max
10 void init(int _n, int _m, ld A[][maxn], ld *b, ld *c) {
11     n = _n, m = _m;
12     forn (i, m)
13         forn (j, n)
14             D[i][j] = -A[i][j];
15     forn (i, m) {
16         D[i][n] = 1;
17         D[i][n + 1] = b[i];
18     }
19     forn (j, n) {
20         D[m][j] = c[j];
21         D[m + 1][j] = 0;
22     }
23     D[m][n + 1] = D[m][n] = D[m + 1][n + 1] = 0;
24     D[m + 1][n] = -1;
25     iota(B, B + m, n);
26     iota(N, N + n, 0);
27     N[n] = -1;
28 }
29
30 void pivot(int b, int nb) {
31     assert(D[b][nb] != 0);
32     ld q = 1. / -D[b][nb];
33     D[b][nb] = -1;
34     forn (i, n + 2)
35         D[b][i] *= q;
36     forn (i, m + 2) {
37         if (i == b)
38             continue;
39         ld coef = D[i][nb];
40         D[i][nb] = 0;
41         forn (j, n + 2)
42             D[i][j] += coef * D[b][j];
43     }
44     swap(B[b], N[nb]);
45 }
46
47 bool betterN(int f, int i, int j) {
48     if (eq(D[f][i], D[f][j]))
49         return N[i] < N[j];
50     return D[f][i] > D[f][j];
51 }
52
53 bool betterB(int nb, int i, int j) {
54     ld ai = D[i][n + 1] / D[i][nb];
55     ld aj = D[j][n + 1] / D[j][nb];
56     if (eq(ai, aj))
57         return B[i] < B[j];
58     return ai > aj;
59 }
60
61 bool simplex(int phase) {
62     int f = phase == 1 ? m : m + 1;
63     while (true) {
64         int nb = -1;
65         forn (i, n + 1) {
66             if (N[i] == -1 && phase == 1)
67                 continue;
68             if (nb == -1 || betterN(f, i, nb))
69                 nb = i;
70         }
71         if (D[f][nb] <= eps)
72             return phase == 1;
73         assert(nb != -1);
74
75         int b = -1;
76         forn (i, m) {
77             if (D[i][nb] >= -eps)
78                 continue;
79             if (b == -1 || betterB(nb, i, b))
80                 b = i;
81         }
82         if (b == -1)
83             return false;
84         pivot(b, nb);
85         if (N[nb] == -1 && phase == 2)
86             return true;
87     }
88 }
89
90 ld solve() {
91     int b = -1;
92     forn (i, m) {
93         if (b == -1 || D[i][n + 1] < D[b][n + 1])
94             b = i;
95     }
96     assert(b != -1);
97     if (D[b][n + 1] < -eps) {
98         pivot(b, n);
99         if (!simplex(2) || D[m + 1][n + 1] < -eps)
100             return -infl;
101     }
102     if (!simplex(1))
103         return infl;
104
105     forn (i, n)
106         x[i] = 0;
107     forn (i, m)
108         if (B[i] < n)
109             x[B[i]] = D[i][n + 1];
110
111     return D[m][n + 1];
112 }
113
114 //Simplex

```

## 30 math/stuff.cpp

```

1 const int M = 1e6;
2 int phi[M];
3 void calcPhi() {
4     for (int i = 1; i < M; ++i)
5         phi[i] = i;
6     for (int j = 1; j < M; ++j)
7         for (int i = 2 * j; i < M; i += j)
8             phi[i] -= phi[j];
9 }
10 int inv[M];
11 void calcInv() {
12     inv[1] = 1;
13     for (int i = 2; i < M; ++i) {
14         inv[i] = mul(sub(0, mod / i), inv[mod % i]);
15         assert(mul(i, inv[i]) == 1);
16     }
17 }
18 int gcd(int a, int b, int &x, int &y) {
19     if (a == 0) {
20         x = 0, y = 1;
21         return b;
22     }
23     int x1, y1;
24     int g = gcd(b % a, a, x1, y1);
25     x = y1 - x1 * (b / a);
26     y = x1;
27     assert(a * x + b * y == g);
28     return g;
29 }
30 int crt(int mod1, int mod2, int rem1, int rem2) {
31     int r = (rem2 - (rem1 % mod2) + mod2) % mod2;
32     int x, y;
33     int g = gcd(mod1, mod2, x, y);
34     assert(r % g == 0);
35
36     x %= mod2;
37     if (x < 0)
38         x += mod2;
39
40     int ans = (x * (r / g)) % mod2;
41     ans = ans * mod1 + rem1;
42
43     assert(ans % mod1 == rem1);
44     assert(ans % mod2 == rem2);
45     return ans;
46 }
47
48 // primes to N
49 const ll n = 1000000000000LL;
50 const ll L = 1000000;
51 int small[L+1];
52 ll large[L+1];
53 void calc_pi() {
54     for (int i = 1; i <= L; ++i) {
55         small[i] = i-1;
56         large[i] = n / i - 1;
57     }
58     for (ll p = 2; p <= L; ++p) {
59         if (small[p] == small[p-1]) continue;
60         int cntp = small[p-1];
61         ll p2 = p*p;
62         ll np = n / p;
63         for (int i = 1; i <= min(L, n / p2); ++i) {
64             ll x = np / i;
65             if (x <= L) {
66                 large[i] -= small[x] - cntp;
67             } else {
68                 large[i] -= large[p*i] - cntp;
69             }
70         }
71         for (int i = L; i >= p2; --i) {
72             small[i] -= small[i/p] - cntp;
73         }
74     }
75 }
76 ll pi(ll x) {
77     if (x > L) return small[n/x];
78     else return large[x];
79 }
80
81 int main() {
82     calcPhi();
83     assert(phi[30] == 1 * 2 * 4);
84     calcInv();
85     int x, y;
86     gcd(3, 5, x, y);
87     gcd(15, 10, x, y);
88     crt(15, 13, 2, 5);
89     crt(17, 3, 15, 2);
90     return 0;
91 }

```

## 31 python/libs.py

```

1 """ Decimal """
2 from decimal import Decimal as D
3 from decimal import getcontext
4 from decimal import FloatOperation
5 from decimal import ROUND_DOWN
6 getcontext().prec = 50
7 getcontext().traps[FloatOperation] = True
8 #getcontext().rounding = ROUND_05UP
9
10 a = D('3.14') # Correct
11 #a = D(3.14) # Wrong!
12 print(a ** D('0.123'))
13 print(a % D('1.5'))
14 print(D(2).sqrt())
15 print(D(1).exp())
16 print(D('10').ln())
17 print(D('10').log10())
18 print(D('3.15').quantize(D('0.1'))) # 3.2
19 print(D('3.15').quantize(D('0.1'), rounding=ROUND_DOWN)) # 3.1
20 print()
21
22 def pi():
23     """Compute Pi to the current precision. """
24     getcontext().prec += 2 # extra digits for intermediate steps
25     three = D(3) # substitute "three=3.0" for regular floats
26     lasts, t, s, n, na, d, da = 0, three, 3, 1, 0, 0, 24
27     while s != lasts:
28         lasts = s
29         n, na = n+na, na+8
30         d, da = d+da, da+32
31         t = (t * n) / d
32         s += t
33     getcontext().prec -= 2
34     return +s # unary plus applies the new precision
35
36 def cos(x):
37     """Return the cosine of x as measured in radians.
38     The Taylor series approximation works best for a small x.
39     For larger values, first compute x = x % (2 * pi). """
40     getcontext().prec += 2
41     i, lasts, s, fact, num, sign = 0, 0, 1, 1, 1, 1
42     while s != lasts:
43         lasts = s
44         i += 2
45         fact *= i * (i-1)
46         num *= x * x
47         sign *= -1
48         s += num / fact * sign
49     getcontext().prec -= 2
50     return +s
51
52 def sin(x):
53     """Return the sine of x as measured in radians.
54     The Taylor series approximation works best for a small x.
55     For larger values, first compute x = x % (2 * pi). """
56     getcontext().prec += 2
57     i, lasts, s, fact, num, sign = 1, 0, x, 1, x, 1
58     while s != lasts:
59         lasts = s
60         i += 2
61         fact *= i * (i-1)
62         num *= x * x
63         sign *= -1
64         s += num / fact * sign
65     getcontext().prec -= 2
66     return +s
67
68 """ Fraction """
69
70 from fractions import Fraction as F
71 from math import pi
72 print(F(16, -10)) # -8/5
73 print(F(123)) # 123
74 print(F('-.125')) # -1/8
75 print(F(pi).limit_denominator(30)) # 22/7
76 print(F(1, 2) ** 31) # 1/2147483648

```

## 32 strings/automaton.cpp

```

1 int t[maxn][26], lnk[maxn], len[maxn];
2 int sz;
3 int last;
4
5 void init() {
6     sz = 3;
7     last = 1;
8     forn(i, 26) t[2][i] = 1;
9     len[2] = -1;
10    lnk[1] = 2;
11}
12
13 void addchar(int c) {
14     int nlast = sz++;
15     len[nlast] = len[last] + 1;
16     int p = last;
17     for (; !t[p][c]; p = lnk[p]) {
18         t[p][c] = nlast;
19     }
20     int q = t[p][c];
21     if (len[p] + 1 == len[q]) {
22         lnk[nlast] = q;
23     } else {
24         int clone = sz++;
25         len[clone] = len[p] + 1;
26         lnk[clone] = lnk[q];
27         lnk[q] = lnk[nlast] = clone;
28         forn(i, 26) t[clone][i] = t[q][i];
29         for (; t[p][c] == q; p = lnk[p]) {
30             t[p][c] = clone;
31         }
32     }
33     last = nlast;
34 }
35
36 bool check(const string& s) {
37     int v = 1;
38     for (int c: s) {
39         c -= 'a';
40         if (!t[v][c]) return false;
41         v = t[v][c];
42     }
43     return true;
44 }
45
46 int main() {
47     string s;
48     cin >> s;
49     init();
50     for (int i: s) {
51         addchar(i - 'a');
52     }
53     forn(i, s.length()) {
54         assert(check(s.substr(i)));
55     }
56     cout << sz << endl;
57     return 0;
58 }

```

## 33 strings/duval\_manacher.cpp

```

1 /*
2  Строка простая, если строго меньше всех суффиксов <=>
3  наименьший циклический сдвиг - первый.
4  Декомпозиция Линдона - разбиение s на w1, w2, ... wk -
5  простые строки такие, что w1 >= w2 >= ... wk.
6 */
7 int duval(string s) {
8     s += s; //remove this to find Lyndon decomposition of s
9     int n = s.size();
10    int i = 0;
11    int ans = 0;
12    //while (i < n) { //for Lyndon decomposition
13    while (i < n / 2) {
14        ans = i;
15        int j = i + 1, k = i;
16        while (j < n && s[k] <= s[j]) {
17            if (s[k] < s[j])
18                k = i;
19            else
20                ++k;
21            ++j;
22        }
23        while (i <= k) {
24            //s.substr(i, j - k) -
25            //next prime string of Lyndon decomposition
26            i += j - k;
27        }
28    }
29    return ans;
30 }
31
32 //actual odd length is (odd[i] * 2 - 1)
33 //actual even length is (even[i] * 2)
34 void manacher(const string& s, vi &odd, vi &even) {
35     int n = s.size();
36     odd.resize(n);
37     int c = -1, r = -1;
38     forn (i, n) {
39         int k = (r <= i ? 0 : min(odd[2 * c - i], r - i));
40         while (i + k < n && i - k >= 0 && s[i + k] == s[i - k])
41             ++k;
42         odd[i] = k;
43         if (i + k > r)
44             r = i + k, c = i;
45     }
46     c = -1, r = -1;
47     even.resize(n - 1);
48     forn (i, n - 1) {
49         int k = (r <= i ? 0 : min(even[2 * c - i], r - i));
50         while (i + k + 1 < n && i - k >= 0 &&
51             s[i + k + 1] == s[i - k])
52             ++k;
53         even[i] = k;
54         if (i + k > r)
55             c = i, r = i + k;
56     }
57 }
58
59 void test() {
60     vector<int> odd, even;
61     string s = "aaaabbaaaaa";
62     manacher(s, odd, even);
63     for (int x: even)
64         cerr << x << ' ';
65     cerr << '\n';
66     for (int x: odd)
67         cerr << x << ' ';
68     cerr << '\n';
69     // 1 2 1 0 5 0 1 2 2 1
70     // 1 2 2 1 1 1 1 2 3 2 1
71 }
72
73 int main() {
74     cout << duval("ababcabab") << '\n'; // 5
75     test();
76 }

```

## 34 strings/eertree.cpp

```

1#include <bits/stdc++.h>
2using namespace std;
3const int maxn = 5000100;
4const int inf = 1e9 + 1e5;
5
6char buf[maxn];
7char *s = buf + 1;
8int to[maxn][2];
9int suff[maxn];
10int len[maxn];
11int sz;
12int last;
13
14const int odd = 1;
15const int even = 2;
16const int blank = 3;
17
18inline void go(int &u, int pos) {
19    while (u != blank && s[pos - len[u] - 1] != s[pos])
20        u = suff[u];
21}
22
23void add_char(int pos) {
24    go(last, pos);
25    int u = suff[last];
26    go(u, pos);
27    int c = s[pos] - 'a';
28    if (!to[last][c]) {
29        to[last][c] = sz++;
30        len[sz - 1] = len[last] + 2;
31        assert(to[u][c]);
32        suff[sz - 1] = to[u][c];
33    }
34    last = to[last][c];
35}
36
37void init() {
38    sz = 4;
39    to[blank][0] = to[blank][1] = even;
40    len[blank] = suff[blank] = inf;
41    len[even] = 0, suff[even] = odd;
42    len[odd] = -1, suff[odd] = blank;
43    last = 2;
44}
45
46void build() {
47    init();
48    scanf("%s", s);
49    for (int i = 0; s[i]; ++i)
50        add_char(i);
51}

```

## 35 strings/suffix\_array.cpp

```

1string s;
2int n;
3int sa[maxn], new_sa[maxn], cls[maxn], new_cls[maxn],
4    cnt[maxn], lcp[maxn];
5int n_cls;
6
7void build() {
8    n_cls = 256;
9    forn(i, n) {
10        sa[i] = i;
11        cls[i] = s[i];
12    }
13    for (int d = 0; d < n; d = d ? d*2 : 1) {
14
15        forn(i, n) new_sa[i] = (sa[i] - d + n) % n;
16        forn(i, n_cls) cnt[i] = 0;
17        forn(i, n) ++cnt[cls[i]];
18        forn(i, n_cls) cnt[i+1] += cnt[i];
19        for (int i = n-1; i >= 0; --i)
20            sa[--cnt[cls[new_sa[i]]]] = new_sa[i];
21
22        n_cls = 0;
23        forn(i, n) {
24            if (i && (cls[sa[i]] != cls[sa[i-1]] ||
25                cls[(sa[i]+d)%n] != cls[(sa[i-1]+d)%n])) {
26                ++n_cls;
27            }
28            new_cls[sa[i]] = n_cls;
29        }
30        ++n_cls;
31        forn(i, n) cls[i] = new_cls[i];
32    }
33
34    // cls is also a inv perm of sa if a string is not cyclic
35    // (i.e. a position of i-th lexicographical suffix)
36    int val = 0;
37    forn(i, n) {
38        if (val) --val;
39        if (cls[i] == n-1) continue;
40        int j = sa[cls[i] + 1];
41        while (i+val != n && j+val != n && s[i+val] == s[j+val])
42            ++val;
43        lcp[cls[i]] = val;
44    }
45}
46
47int main() {
48    cin >> s;
49    s += '$';
50    n = s.length();
51    build();
52    forn(i, n) {
53        cout << s.substr(sa[i]) << endl;
54        cout << lcp[i] << endl;
55    }
56}

```

## 36 strings/ukkonen.cpp

```

1string s;
2const int alpha = 26;
3
4namespace SuffixTree {
5    struct Node {
6        Node *to[alpha];
7        Node *lnk, *par;
8        int l, r;
9
10        Node(int l, int r): l(l), r(r) {
11            memset(to, 0, sizeof(to));
12            lnk = par = 0;
13        }
14    };
15
16    Node *root, *blank, *cur;
17    int pos;
18
19    void init() {
20        root = new Node(0, 0);
21        blank = new Node(0, 0);
22        forn (i, alpha)
23            blank->to[i] = root;
24        root->lnk = root->par = blank->lnk = blank->par = blank;
25        cur = root;
26        pos = 0;
27    }
28
29    int at(int id) {
30        return s[id] - 'a';
31    }
32
33    void goDown(int l, int r) {
34        if (l >= r)
35            return;
36        if (pos == cur->r) {
37            int c = at(l);
38            assert(cur->to[c]);
39            cur = cur->to[c];
40            pos = min(cur->r, cur->l + 1);
41            ++l;
42        } else {
43            int delta = min(r - l, cur->r - pos);
44            l += delta;
45            pos += delta;
46        }
47        goDown(l, r);
48    }
49
50    void goUp() {
51        if (pos == cur->r && cur->lnk) {
52            cur = cur->lnk;
53            pos = cur->r;
54            return;
55        }
56        int l = cur->l, r = pos;
57        cur = cur->par->lnk;
58        pos = cur->r;
59        goDown(l, r);
60    }
61
62    void setParent(Node *a, Node *b) {
63        assert(a);
64        a->par = b;
65        if (b)
66            b->to[at(a->l)] = a;
67    }
68
69    void addLeaf(int id) {
70        Node *x = new Node(id, inf);
71        setParent(x, cur);
72    }
73
74    void splitNode() {
75        assert(pos != cur->r);
76        Node *mid = new Node(cur->l, pos);
77        setParent(mid, cur->par);
78        cur->l = pos;
79        setParent(cur, mid);
80        cur = mid;
81    }
82
83    bool canGo(int c) {
84        if (pos == cur->r)
85            return cur->to[c];
86        return at(pos) == c;
87    }
88
89    void fixLink(Node *&bad, Node *newBad) {
90        if (bad)
91            bad->lnk = cur;
92            bad = newBad;
93    }
94
95    void addCharOnPos(int id) {
96        Node *bad = 0;
97        while (!canGo(at(id))) {
98            if (cur->r != pos) {
99                splitNode();
100                fixLink(bad, cur);
101                bad = cur;
102            } else {
103                fixLink(bad, 0);
104            }
105            addLeaf(id);
106            goUp();
107        }
108        fixLink(bad, 0);
109        goDown(id, id + 1);
110    }
111
112    int cnt(Node *u, int ml) {
113        if (!u)
114            return 0;
115        int res = min(ml, u->r) - u->l;
116        forn (i, alpha)
117            res += cnt(u->to[i], ml);
118        return res;
119    }
120
121    void build(int l) {
122        init();
123        forn (i, l)
124            addCharOnPos(i);
125    }
126};

```

## 37 structures/centroids.cpp

```

1 const int maxn = 100100;
2 const int LG = 18; //2*maxn <= 2^LG
3
4 vector<int> g[LG][maxn];
5 int rt[LG][maxn];
6 int from[LG][maxn];
7
8 namespace Cenroids {
9
10 int D;
11 int cnt[maxn];
12 int CENTER, BEST;
13
14 void pre(int u, int prev = -1) {
15     cnt[u] = 1;
16     for (int v: g[D][u]) {
17         if (v == prev)
18             continue;
19         pre(v, u);
20         cnt[u] += cnt[v];
21     }
22 }
23
24 void findCenter(int u, int prev = -1, int up = 0) {
25     int worst = up;
26     for (int v: g[D][u]) {
27         if (v == prev)
28             continue;
29         findCenter(v, u, up + cnt[u] - cnt[v]);
30         worst = max(worst, cnt[v]);
31     }
32     if (worst < BEST) {
33         CENTER = u;
34         BEST = worst;
35     }
36 }
37
38 void markAll(int u, int prev = -1, int subtree = -1) {
39     rt[D][u] = CENTER;
40     from[D][u] = subtree;
41     for (int v: g[D][u]) {
42         if (v == prev)
43             continue;
44         g[D + 1][u].push_back(v);
45         g[D + 1][v].push_back(u);
46         if (subtree == -1)
47             markAll(v, u, v);
48         else
49             markAll(v, u, subtree);
50     }
51 }
52
53 void decompose(int u, int depth = 0) {
54     D = depth;
55     pre(u);
56     CENTER = -1, BEST = 1e9;
57     findCenter(u);
58     assert(CENTER != -1);
59     u = CENTER;
60     markAll(u);
61     D = depth + 1;
62     for (int v: g[D][u]) {
63         auto it = find(g[D][v].begin(), g[D][v].end(), u);
64         assert(it != g[D][v].end());
65         g[D][v].erase(it);
66     }
67     for (int v: g[D][u])
68         decompose(v, depth + 1);
69 }
70
71 };

```

## 38 structures/heavy\_light.cpp

```

1 const int maxn = 100500;
2 const int maxd = 17;
3
4 vector<int> g[maxn];
5
6 struct Tree {
7     vector<int> t;
8     int base;
9
10     Tree(): base(0) {
11     }
12
13     Tree(int n) {
14         base = 1;
15         while (base < n)
16             base *= 2;
17         t = vector<int>(base * 2, 0);
18     }
19
20     void put(int v, int delta) {
21         assert(v < base);
22         v += base;
23         t[v] += delta;
24         while (v > 1) {
25             v /= 2;
26             t[v] = max(t[v * 2], t[v * 2 + 1]);
27         }
28     }
29
30     //Careful here: cr = 2 * maxn
31     int get(int l, int r, int v=1, int cl=0, int cr = 2*maxn) {
32         cr = min(cr, base);
33         if (l <= cl && cr <= r)
34             return t[v];
35         if (r <= cl || cr <= 1)
36             return 0;
37         int cc = (cl + cr) / 2;
38         return max(get(l, r, v * 2, cl, cc),
39                   get(l, r, v * 2 + 1, cc, cr));
40     }
41 };
42
43 namespace HLD {
44     int h[maxn];
45     int timer;
46     int in[maxn], out[maxn], cnt[maxn];
47     int p[maxd][maxn];
48     int vroot[maxn];
49     int vpos[maxn];
50     int ROOT;
51     Tree tree[maxn];
52
53     void dfs1(int u, int prev) {
54         p[0][u] = prev;
55         in[u] = timer++;
56         cnt[u] = 1;
57         for (int v: g[u]) {
58             if (v == prev)
59                 continue;
60             h[v] = h[u] + 1;
61             dfs1(v, u);
62             cnt[u] += cnt[v];
63         }
64         out[u] = timer;
65     }
66
67     int dfs2(int u, int prev) {
68         int to = -1;
69         for (int v: g[u]) {
70             if (v == prev)
71                 continue;
72             if (to == -1 || cnt[v] > cnt[to])
73                 to = v;
74         }
75         int len = 1;
76         for (int v: g[u]) {
77             if (v == prev)
78                 continue;
79             if (to == v) {
80                 vpos[v] = vpos[u] + 1;
81                 vroot[v] = vroot[u];
82                 len += dfs2(v, u);
83             }
84             else {
85                 vroot[v] = v;
86                 vpos[v] = 0;
87                 dfs2(v, u);
88             }
89         }
90         if (vroot[u] == u)
91             tree[u] = Tree(len);

```



## 39 structures/linkcut.cpp

```

92     return len;
93 }
94
95 void init(int n) {
96     timer = 0;
97     h[ROOT] = 0;
98     dfs1(ROOT, ROOT);
99     forn (d, maxd - 1)
100         forn (i, n)
101             p[d + 1][i] = p[d][p[d][i]];
102     vroot[ROOT] = ROOT;
103     vpos[ROOT] = 0;
104     dfs2(ROOT, ROOT);
105     //WARNING: init all trees
106 }
107
108 bool isPrev(int u, int v) {
109     return in[u] <= in[v] && out[v] <= out[u];
110 }
111
112 int lca(int u, int v) {
113     for (int d = maxd - 1; d >= 0; --d)
114         if (!isPrev(p[d][u], v))
115             u = p[d][u];
116     if (!isPrev(u, v))
117         u = p[0][u];
118     return u;
119 }
120
121 //for each v: h[u] >= toh
122 int getv(int u, int toh) {
123     int res = 0;
124     while (h[u] >= toh) {
125         int rt = vroot[u];
126         int l = max(0, toh - h[rt]), r = vpos[u] + 1;
127         res = max(res, tree[rt].get(l, r));
128         if (rt == ROOT)
129             break;
130         u = p[0][rt];
131     }
132     return res;
133 }
134
135 int get(int u, int v) {
136     int w = lca(u, v);
137     return max(getv(u, h[w]), getv(v, h[w] + 1));
138 }
139
140 void put(int u, int val) {
141     int rt = vroot[u];
142     int pos = vpos[u];
143     tree[rt].put(pos, val);
144 }
145};

```

```

1namespace LinkCut {
2
3typedef struct _node {
4    _node *l, *r, *p, *pp;
5    int size; bool rev;
6    _node();
7
8    explicit _node(nullptr_t) {
9        l = r = p = pp = this;
10        size = rev = 0;
11    }
12
13    void push() {
14        if (rev) {
15            l->rev ^= 1; r->rev ^= 1;
16            rev = 0; swap(l, r);
17        }
18    }
19
20    void update();
21}* node;
22
23node None = new _node(nullptr);
24node v2n[maxn];
25
26_node::_node(){
27    l = r = p = pp = None;
28    size = 1; rev = false;
29}
30
31void _node::update() {
32    size = (this != None) + l->size + r->size;
33    l->p = r->p = this;
34}
35
36void rotate(node v) {
37    assert(v != None && v->p != None);
38    assert(!v->rev);
39    assert(!v->p->rev);
40    node u = v->p;
41    if (v == u->l)
42        u->l = v->r, v->r = u;
43    else
44        u->r = v->l, v->l = u;
45    swap(u->p, v->p);
46    swap(v->pp, u->pp);
47    if (v->p != None) {
48        assert(v->p->l == u || v->p->r == u);
49        if (v->p->r == u)
50            v->p->r = v;
51        else
52            v->p->l = v;
53    }
54    u->update();
55    v->update();
56}
57
58void bigRotate(node v) {
59    assert(v->p != None);
60    v->p->p->push();
61    v->p->push();
62    v->push();
63    if (v->p->p != None) {
64        if ((v->p->l == v) ^ (v->p->p->r == v->p))
65            rotate(v->p);
66        else
67            rotate(v);
68    }
69    rotate(v);
70}
71
72inline void splay(node v) {
73    while (v->p != None)
74        bigRotate(v);
75}
76
77inline void splitAfter(node v) {
78    v->push();
79    splay(v);
80    v->r->p = None;
81    v->r->pp = v;
82    v->r = None;
83    v->update();
84}
85
86void expose(int x) {
87    node v = v2n[x];
88    splitAfter(v);
89    while (v->pp != None) {
90        assert(v->p == None);
91        splitAfter(v->pp);

```

## 40 structures/ordered\_set.cpp

```

92     assert(v->pp->r == None);
93     assert(v->pp->p == None);
94     assert(!v->pp->rev);
95     v->pp->r = v;
96     v->pp->update();
97     v = v->pp;
98     v->r->pp = None;
99 }
100 assert(v->p == None);
101 splay(v2n[x]);
102}
103
104inline void makeRoot(int x) {
105    expose(x);
106    assert(v2n[x]->p == None);
107    assert(v2n[x]->pp == None);
108    assert(v2n[x]->r == None);
109    v2n[x]->rev ^= 1;
110}
111
112inline void link(int x, int y) {
113    makeRoot(x);
114    v2n[x]->pp = v2n[y];
115}
116
117inline void cut(int x, int y) {
118    expose(x);
119    splay(v2n[y]);
120    if (v2n[y]->pp != v2n[x]) {
121        swap(x,y);
122        expose(x);
123        splay(v2n[y]);
124        assert(v2n[y]->pp == v2n[x]);
125    }
126    v2n[y]->pp = None;
127}
128
129inline int get(int x, int y) {
130    if (x == y)
131        return 0;
132    makeRoot(x);
133    expose(y);
134    expose(x);
135    splay(v2n[y]);
136    if (v2n[y]->pp != v2n[x])
137        return -1;
138    return v2n[y]->size;
139}
140
141}

```

```

1 #include <ext/pb_ds/assoc_container.hpp>
2 #include <ext/pb_ds/tree_policy.hpp>
3
4 typedef __gnu_pbds::tree<int, __gnu_pbds::null_type,
5     std::less<int>,
6     __gnu_pbds::rb_tree_tag,
7     __gnu_pbds::tree_order_statistics_node_update> oset;
8
9 #include <iostream>
10
11 int main() {
12     oset X;
13     X.insert(1);
14     X.insert(2);
15     X.insert(4);
16     X.insert(8);
17     X.insert(16);
18
19     std::cout << *X.find_by_order(1) << std::endl; // 2
20     std::cout << *X.find_by_order(2) << std::endl; // 4
21     std::cout << *X.find_by_order(4) << std::endl; // 16
22     std::cout << std::boolalpha <<
23         (end(X)==X.find_by_order(6)) << std::endl; // true
24
25     std::cout << X.order_of_key(-5) << std::endl; // 0
26     std::cout << X.order_of_key(1) << std::endl; // 0
27     std::cout << X.order_of_key(3) << std::endl; // 2
28     std::cout << X.order_of_key(4) << std::endl; // 2
29     std::cout << X.order_of_key(400) << std::endl; // 5
30}

```

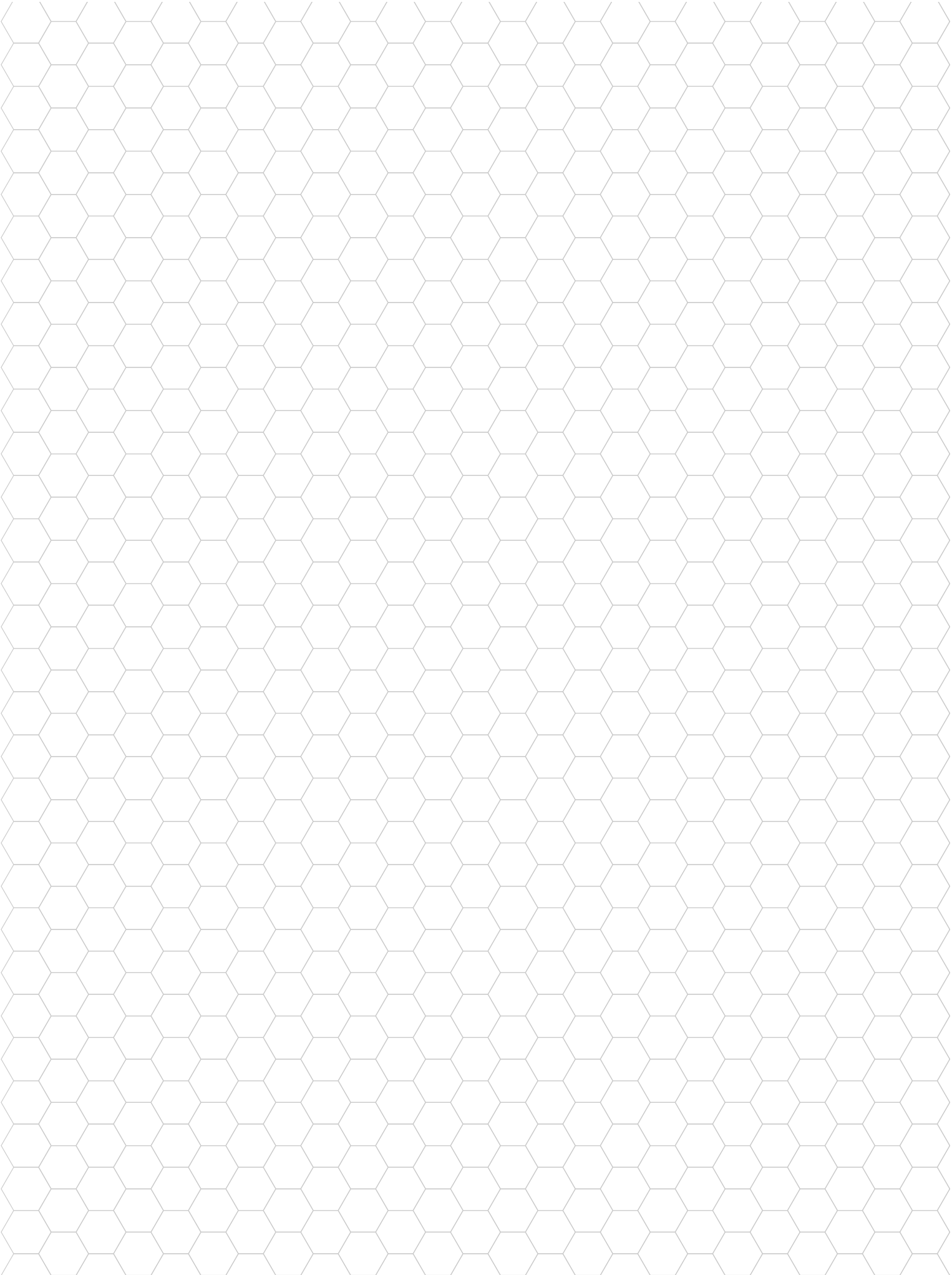
## 41 structures/treap.cpp

```

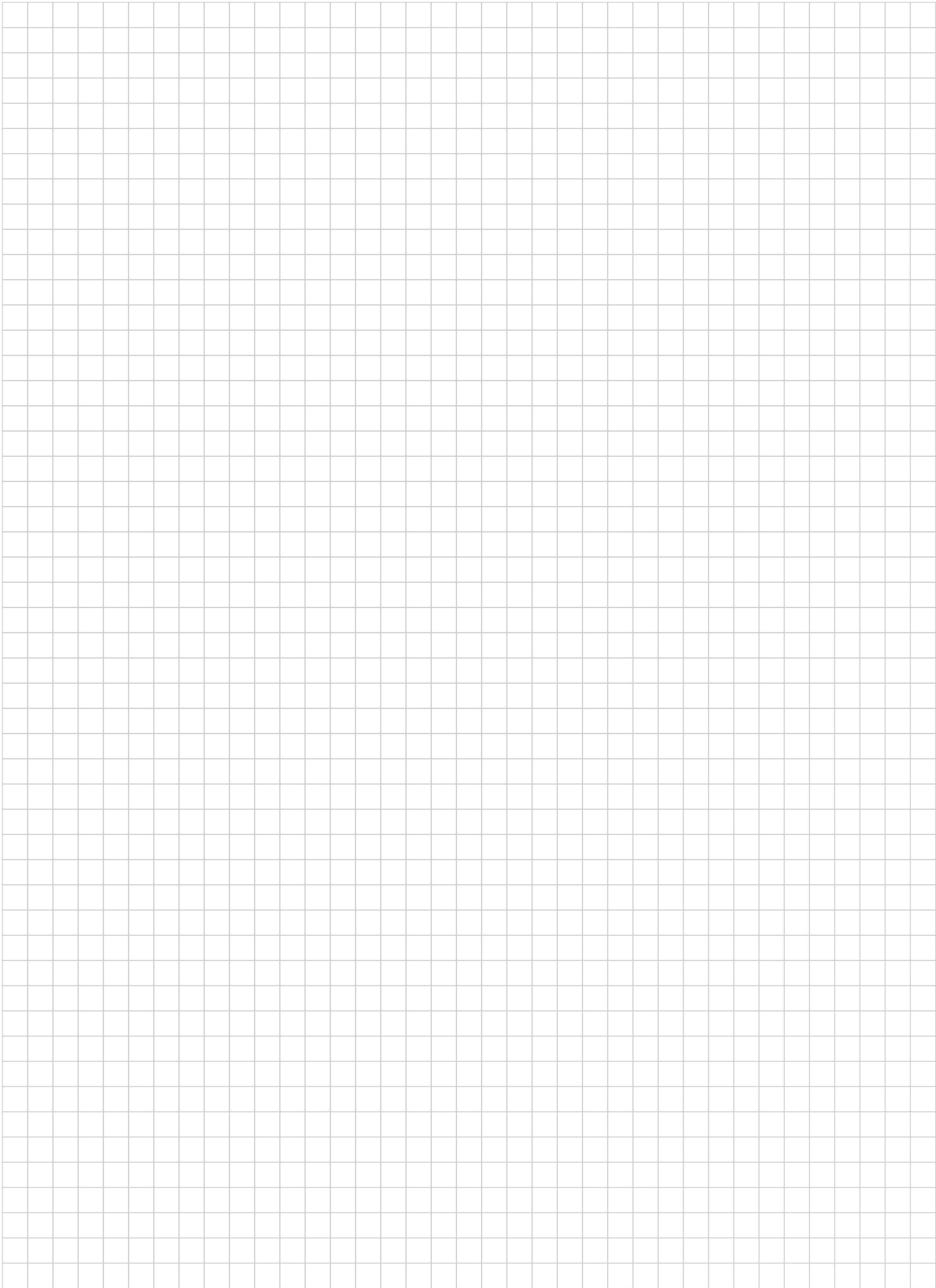
1 struct node {
2     int x, y;
3     node *l, *r;
4     node(int x) : x(x), y(rand()), l(r=NULL) {}
5 };
6
7 void split(node *t, node *&l, node *&r, int x) {
8     if (!t) return (void)(l=r=NULL);
9     if (x <= t->x) {
10         split(t->l, l, t->l, x), r = t;
11     } else {
12         split(t->r, t->r, r, x), l = t;
13     }
14 }
15
16 node *merge(node *l, node *r) {
17     if (!l) return r;
18     if (!r) return l;
19     if (l->y > r->y) {
20         l->r = merge(l->r, r);
21         return l;
22     } else {
23         r->l = merge(l, r->l);
24         return r;
25     }
26 }
27
28 node *insert(node *t, node *n) {
29     node *l, *r;
30     split(t, l, r, n->x);
31     return merge(l, merge(n, r));
32 }
33
34 node *insert(node *t, int x) {
35     return insert(t, new node(x));
36 }
37
38 node *fast_insert(node *t, node *n) {
39     if (!t) return n;
40     node *root = t;
41     while (true) {
42         if (n->x < t->x) {
43             if (!t->l || t->l->y < n->y) {
44                 split(t->l, n->l, n->r, n->x), t->l = n;
45                 break;
46             } else {
47                 t = t->l;
48             }
49         } else {
50             if (!t->r || t->r->y < n->y) {
51                 split(t->r, n->l, n->r, n->x), t->r = n;
52                 break;
53             } else {
54                 t = t->r;
55             }
56         }
57     }
58     return root;
59 }
60
61 node *fast_insert(node *t, int x) {
62     return fast_insert(t, new node(x));
63 }
64
65 int main() {
66     node *t = NULL;
67     forn(i, 1000000) {
68         int x = rand();
69         t = fast_insert(t, x);
70     }
71 }

```

42    Сеточка



43    Сеточка



44 Сеточка

