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1 Strategy.txt

- 1 - Проверить руками сэмплы
- Подумать как дебагать после написания
- 2 - Выписать сложные формулы и все +-1
- 2 - Проверить имена файлов
- 3 - Прогнать сэмплы
- Переполнения int, переполнения long long
- 3 - Выход за границу массива: _GLIBCXX_DEBUG
- Переполнения по модулю: в
 - ↳ псевдо-онлайн-генераторе, в функциях-обертках
- Проверить мультитест на разных тестах
- Прогнать минимальный по каждому параметру тест
- 6 - Прогнать псевдо-максимальный тест(немного чисел,
 - ↳ но очень большие или очень маленькие)
- 6 - Представить что не зайдет и заранее написать
 - ↳ assert'ы, прогнать слегка модифицированные тесты
- 7 - cout.precision: в том числе в интерактивных
 - ↳ задачах
- Удалить debug-output, отсечения для тестов,
 - ↳ вернуть оригинальный тахп, удалить
 - ↳ _GLIBCXX_DEBUG
- 8 - Вердикт может врать
- 9 - Если много тестов(>3), дописать в конец каждого
 - ↳ теста ответ, чтобы не забыть
- (WA) Потестить не только ответ, но и содержимое
 - ↳ значимых массивов, переменных
- (WA) Изменить тест так, чтобы ответ не менялся:
 - ↳ поменять координаты местами, сжать/растянуть
 - ↳ координаты, поменять ROOT дерева
- (WA) Подвигать размер блока в корневой или
 - ↳ битсете
- (WA) Поставить assert'ы, возможно написать чекер
 - ↳ с assert'ом
- (WA) Проверить, что программа не печатает
 - ↳ что-либо неожиданное, что должно попадать под
 - ↳ PE: inf - 2, не лекс. мин. решение, одинаковые
 - ↳ числа вместо разных, неправильное количество
 - ↳ чисел, пустой ответ, перечитать output format
- (TL) cin -> scanf -> getchar
- (TL) Упихать в кэш большие массивы, поменять
 - ↳ местами for'ы или измерения массива
- (RE) Проверить формулы на деление на 0, выход за
 - ↳ область определения(sqrt(-eps), acos(1 + eps))
- (WA) Проверить, что ответ влезает в int

2 flows/dinic.cpp

```

1 namespace Dinic {
2 const int maxn = 100100;
3 struct Edge {
4     int to;
5     ll c, f;
6     Edge(int to, ll c): to(to), c(c), f(0) {}
7 };
8
9 vector<Edge> es;
10 vector<int> g[maxn];
11 int q[maxn], d[maxn], pos[maxn];
12 int N, S, T;
13
14 void addEdge(int u, int v, ll c) {
15     g[u].push_back(sz(es));
16     es.emplace_back(v, c);
17     g[v].push_back(sz(es));
18     es.emplace_back(u, 0);
19 }
20
21 bool bfs() {
22     fill(d, d + N, maxn);
23     d[S] = 0, q[0] = S;
24     int rq = 1;
25     forn (lq, rq) {
26         int u = q[lq];
27         for (int id: g[u]) {
28             if (es[id].c == es[id].f)
29                 continue;
30             int v = es[id].to;
31             if (d[v] == maxn) {
32                 d[v] = d[u] + 1;
33                 q[rq++] = v;
34             }
35         }
36     }
37     return d[T] != maxn;
38 }
39
40 ll dfs(int u, ll curf) {
41     if (u == T)
42         return curf;
43     ll ret = 0;
44     for (int &i = pos[u]; i < sz(g[u]); ++i) {
45         int id = g[u][i];
46         int v = es[id].to;
47         ll delta = min(curf, es[id].c - es[id].f);
48         if (delta == 0 || d[v] != d[u] + 1)
49             continue;
50         delta = dfs(v, delta);
51         curf -= delta;
52         ret += delta;
53         es[id].f += delta;
54         es[id ^ 1].f -= delta;
55         if (curf == 0)
56             return ret;
57     }
58     return ret;
59 }
60
61 ll dinic(int S, int T) {
62     Dinic::S = S, Dinic::T = T;
63     ll res = 0;
64     while (bfs()) {
65         fill(pos, pos + N, 0);
66         while (ll cur = dfs(S, infl))
67             res += cur;
68     }
69     return res;
70 }
71
72 } // namespace Dinic
73
74 void test() {
75     Dinic::N = 4;
76     Dinic::addEdge(0, 1, 1);
77     Dinic::addEdge(0, 2, 2);
78     Dinic::addEdge(2, 1, 1);
79     Dinic::addEdge(1, 3, 2);
80     Dinic::addEdge(2, 3, 1);
81     cout << Dinic::dinic(0, 3) << endl; // 3
82 }
83 /*
84 LR-поток находит не максимальный поток.
85 Добавим новый сток S' и исток T'. Заменяем ребро (u, v, l, r)
86 LR-сети на ребра (u, T', l), (S', v, l), (u, v, r - l).
87 Добавим ребро (T, S, k). Ставим значение k=inf, пускаем поток.
88 Проверяем, что все ребра из S' насыщены (иначе ответ не
89 существует). Бинарным поиском находим наименьшее k, что величина
90 потока не изменится. Это k - величина МИНИМАЛЬНОГО потока,
91 удовлетворяющего ограничениям. */

```

3 flows/globalcut.cpp

```

1 #include <bits/stdc++.h>
2 using namespace std;
3 #define forn(i,n) for (int i = 0; i < int(n); ++i)
4 const int inf = 1e9 + 1e5;
5 #define all(x) (x).begin(), (x).end()
6
7 const int maxn = 505;
8 namespace StoerWagner {
9     int g[maxn][maxn];
10     int dist[maxn];
11     bool used[maxn];
12     int n;
13
14     void addEdge(int u, int v, int c) {
15         g[u][v] += c;
16         g[v][u] += c;
17     }
18
19     int run() {
20         vector<int> vertices;
21         forn (i, n)
22             vertices.push_back(i);
23         int mincut = inf;
24         while (vertices.size() > 1) {
25             int u = vertices[0];
26             for (auto v: vertices) {
27                 used[v] = false;
28                 dist[v] = g[u][v];
29             }
30             used[u] = true;
31             forn (ii, vertices.size() - 2) {
32                 for (auto v: vertices)
33                     if (!used[v])
34                         if (used[u] || dist[v] > dist[u])
35                             u = v;
36                 used[u] = true;
37                 for (auto v: vertices)
38                     if (!used[v])
39                         dist[v] += g[u][v];
40             }
41             int t = -1;
42             for (auto v: vertices)
43                 if (!used[v])
44                     t = v;
45             assert(t != -1);
46             mincut = min(mincut, dist[t]);
47             vertices.erase(find(all(vertices), t));
48             for (auto v: vertices)
49                 addEdge(u, v, g[v][t]);
50         }
51         return mincut;
52     }
53 } // namespace StoerWagner
54
55 int main() {
56     StoerWagner::n = 4;
57     StoerWagner::addEdge(0, 1, 5);
58     StoerWagner::addEdge(2, 3, 5);
59     StoerWagner::addEdge(1, 2, 4);
60     cerr << StoerWagner::run() << '\n'; // 4
61 }

```

4 flows/hungary.cpp

```

1// left half is the smaller one
2namespace Hungary {
3const int maxn = 505;
4int a[maxn][maxn];
5int p[2][maxn];
6int match[maxn];
7bool used[maxn];
8int from[maxn];
9int mind[maxn];
10int n, m;
11
12int hungary(int v) {
13    used[v] = true;
14    int u = match[v];
15    int best = -1;
16    forn (i, m + 1) {
17        if (used[i])
18            continue;
19        int nw = a[u][i] - p[0][u] - p[1][i];
20        if (nw <= mind[i]) {
21            mind[i] = nw;
22            from[i] = v;
23        }
24        if (best == -1 || mind[best] > mind[i])
25            best = i;
26    }
27    v = best;
28    int delta = mind[best];
29    forn (i, m + 1) {
30        if (used[i]) {
31            p[1][i] -= delta;
32            p[0][match[i]] += delta;
33        } else
34            mind[i] -= delta;
35    }
36    if (match[v] == -1)
37        return v;
38    return hungary(v);
39}
40
41void check() {
42    int edges = 0, res = 0;
43    forn (i, m)
44        if (match[i] != -1) {
45            ++edges;
46            assert(p[0][match[i]] + p[1][i] == a[match[i]][i]);
47            res += a[match[i]][i];
48        } else
49            assert(p[1][i] == 0);
50    assert(res == -p[1][m]);
51    forn (i, n) forn (j, m)
52        assert(p[0][i] + p[1][j] <= a[i][j]);
53}
54
55int run() {
56    forn (i, n)
57        p[0][i] = 0;
58    forn (i, m + 1) {
59        p[1][i] = 0;
60        match[i] = -1;
61    }
62    forn (i, n) {
63        match[m] = i;
64        fill(used, used + m + 1, false);
65        fill(mind, mind + m + 1, inf);
66        fill(from, from + m + 1, -1);
67        int v = hungary(m);
68        while (v != m) {
69            int w = from[v];
70            match[v] = match[w];
71            v = w;
72        }
73    }
74    check();
75    return -p[1][m];
76}
77} // namespace Hungary

```

5 flows/mincost.cpp

```

1namespace MinCost {
2const ll infc = 1e12;
3
4struct Edge {
5    int to;
6    ll c, f, cost;
7
8    Edge(int to, ll c, ll cost): to(to), c(c), f(0), cost(cost)
9    { }
10};
11
12int N, S, T;
13int totalFlow;
14ll totalCost;
15const int maxn = 505;
16vector<Edge> edge;
17vector<int> g[maxn];
18
19void addEdge(int u, int v, ll c, ll cost) {
20    g[u].push_back(edge.size());
21    edge.emplace_back(v, c, cost);
22    g[v].push_back(edge.size());
23    edge.emplace_back(u, 0, -cost);
24}
25
26ll dist[maxn];
27int fromEdge[maxn];
28
29bool inQueue[maxn];
30bool fordBellman() {
31    forn (i, N)
32        dist[i] = infc;
33    dist[S] = 0;
34    inQueue[S] = true;
35    vector<int> q;
36    q.push_back(S);
37    for (int ii = 0; ii < int(q.size()); ++ii) {
38        int u = q[ii];
39        inQueue[u] = false;
40        for (int e: g[u]) {
41            if (edge[e].f == edge[e].c)
42                continue;
43            int v = edge[e].to;
44            ll nw = edge[e].cost + dist[u];
45            if (nw >= dist[v])
46                continue;
47            dist[v] = nw;
48            fromEdge[v] = e;
49            if (!inQueue[v]) {
50                inQueue[v] = true;
51                q.push_back(v);
52            }
53        }
54    }
55    return dist[T] != infc;
56}
57
58ll pot[maxn];
59bool dijkstra() {
60    typedef pair<ll, int> Pair;
61    priority_queue<Pair, vector<Pair>, greater<Pair>> q;
62    forn (i, N)
63        dist[i] = infc;
64    dist[S] = 0;
65    q.emplace(dist[S], S);
66    while (!q.empty()) {
67        int u = q.top().second;
68        ll cdist = q.top().first;
69        q.pop();
70        if (cdist != dist[u])
71            continue;
72        for (int e: g[u]) {
73            int v = edge[e].to;
74            if (edge[e].c == edge[e].f)
75                continue;
76            ll w = edge[e].cost + pot[u] - pot[v];
77            assert(w >= 0);
78            ll ndist = w + dist[u];
79            if (ndist >= dist[v])
80                continue;
81            dist[v] = ndist;
82            fromEdge[v] = e;
83            q.emplace(dist[v], v);
84        }
85    }
86    if (dist[T] == infc)
87        return false;
88    forn (i, N) {
89        if (dist[i] == infc)
90            continue;
91        pot[i] += dist[i];

```

6 flows/push_relabel.cpp

```

92     }
93     return true;
94 }
95
96 bool push() {
97     //2 variants
98     //if (!fordBellman())
99     if (!dikstra())
100         return false;
101     ++totalFlow;
102     int u = T;
103     while (u != S) {
104         int e = fromEdge[u];
105         totalCost += edge[e].cost;
106         edge[e].f++;
107         edge[e ^ 1].f--;
108         u = edge[e ^ 1].to;
109     }
110     return true;
111 }
112
113 //min-cost-circulation
114 ll d[maxn][maxn];
115 int dfrom[maxn][maxn];
116 int level[maxn];
117 void circulation() {
118     while (true) {
119         int q = 0;
120         fill(d[0], d[0] + N, 0);
121         forn (iter, N) {
122             fill(d[iter + 1], d[iter + 1] + N, infc);
123             forn (u, N)
124                 for (int e: g[u]) {
125                     if (edge[e].c == edge[e].f)
126                         continue;
127                     int v = edge[e].to;
128                     ll ndist = d[iter][u] + edge[e].cost;
129                     if (ndist >= d[iter + 1][v])
130                         continue;
131                     d[iter + 1][v] = ndist;
132                     dfrom[iter + 1][v] = e;
133                 }
134             q ^= 1;
135         }
136         int w = -1;
137         ld mindmax = 1e18;
138         forn (u, N) {
139             ld dmax = -1e18;
140             forn (iter, N)
141                 dmax = max(dmax,
142                     (d[N][u] - d[iter][u]) / ld(N - iter));
143             if (mindmax > dmax)
144                 mindmax = dmax, w = u;
145         }
146         if (mindmax >= 0)
147             break;
148         fill(level, level + N, -1);
149         int k = N;
150         while (level[w] == -1) {
151             level[w] = k;
152             w = edge[dfrom[k-1][w] ^ 1].to;
153         }
154         int k2 = level[w];
155         ll delta = infc;
156         while (k2 > k) {
157             int e = dfrom[k2-1][w];
158             delta = min(delta, edge[e].c - edge[e].f);
159             w = edge[e ^ 1].to;
160         }
161         k2 = level[w];
162         while (k2 > k) {
163             int e = dfrom[k2-1][w];
164             totalCost += edge[e].cost * delta;
165             edge[e].f += delta;
166             edge[e ^ 1].f -= delta;
167             w = edge[e ^ 1].to;
168         }
169     }
170 }
171 // namespace MinCost
172
173 int main() {
174     MinCost::N = 3, MinCost::S = 1, MinCost::T = 2;
175     MinCost::addEdge(1, 0, 3, 5);
176     MinCost::addEdge(0, 2, 4, 6);
177     while (MinCost::push());
178     cout << MinCost::totalFlow << ' '
179          << MinCost::totalCost << '\n'; //3 33
180 }

```

```

1 namespace PushRelabel {
2 const int maxn = 200500;
3
4 struct Edge {
5     int to, c, f;
6 };
7 vector<Edge> edge;
8
9 int n;
10 vector<int> g[maxn];
11 ll e[maxn];
12 int h[maxn];
13 int onH[maxn];
14 int S, T;
15 int ptr[maxn];
16 int relabelTimer;
17
18 void addEdge(int u, int v, int c) {
19     g[u].push_back(sz(edge));
20     edge.push_back({v, c, 0});
21     g[v].push_back(sz(edge));
22     edge.push_back({u, 0, 0});
23 }
24
25 void push(int id, int delta) {
26     int u = edge[id ^ 1].to;
27     int v = edge[id].to;
28     edge[id].f += delta;
29     edge[id ^ 1].f -= delta;
30     e[u] -= delta;
31     e[v] += delta;
32 }
33
34 void gap(int ch) {
35     forn (u, n) {
36         if (h[u] > ch)
37             h[u] = max(h[u], n);
38     }
39 }
40
41 int o[maxn];
42 void globalRelabeling() {
43     int oc = 0;
44     forn (i, n) {
45         h[i] = n;
46         onH[i] = 0;
47     }
48     onH[0] = 1;
49     h[T] = 0;
50     o[oc++] = T;
51     forn (ii, oc) {
52         int u = o[ii];
53         for (int id: g[u]) {
54             if (edge[id ^ 1].c == edge[id ^ 1].f)
55                 continue;
56             int v = edge[id].to;
57             if (h[v] != n)
58                 continue;
59             h[v] = h[u] + 1;
60             onH[h[v]]++;
61             o[oc++] = v;
62         }
63     }
64 }
65
66 void relabel(int u) {
67     int oldh = h[u];
68     int newh = inf;
69     for (int id: g[u]) {
70         if (edge[id].c == edge[id].f)
71             continue;
72         newh = min(newh, h[edge[id].to] + 1);
73     }
74     h[u] = newh;
75     onH[oldh]--;
76     onH[newh]++;
77     if (onH[oldh] == 0)
78         gap(oldh);
79     if (++relabelTimer == n)
80         globalRelabeling(), relabelTimer = 0;
81 }
82
83 void discharge(int u) {
84     while (e[u] > 0) {
85         int &i = ptr[u];
86         if (i == sz(g[u])) {
87             i = 0;
88             relabel(u);
89             if (h[u] >= n)
90                 break;
91             continue;

```

7 geometry/convex_hull_trick.cpp

```

92     } else {
93         int id = g[u][i++];
94         int v = edge[id].to;
95         if (h[v] + 1 != h[u])
96             continue;
97         int delta = min(e[u], ll(edge[id].c - edge[id].f));
98         push(id, delta);
99     }
100 }
101 }
102
103 11 flow(int _S, int _T) {
104     S = _S, T = _T;
105     forn (i, n)
106         ptr[i] = 0, e[i] = 0;
107     for (int id: g[S]) {
108         int delta = edge[id].c;
109         push(id, delta);
110     }
111     globalRelabeling();
112     bool ok = false;
113     while (!ok) {
114         ok = true;
115         forn (u, n) {
116             if (h[u] < n && u != T && e[u] > 0)
117                 discharge(u, ok = false);
118         }
119     }
120     return e[T];
121 }
122
123 } //PushRelabel

```

```

1 struct Hull {
2     vector<pt> top, bot;
3
4     //check: add points in strictly increasing order
5     void append(pt p) {
6         while (sz(bot) > 1 && (p - bot.back()) %
7             (p - *next(bot.rbegin())) >= -eps)
8             bot.pop_back();
9         bot.push_back(p);
10        while (sz(top) > 1 && (p - top.back()) %
11            (p - *next(top.rbegin())) <= eps)
12            top.pop_back();
13        top.push_back(p);
14    }
15
16    pt mostDistant(pt dir) {
17        dir = dir.rot();
18        auto &v = dir.x < 0 ? top : bot;
19        int l = -1, r = sz(v) - 1;
20        while (l + 1 < r) {
21            int c = (l + r) / 2;
22            if (dir % (v[c + 1] - v[c]) > 0)
23                r = c;
24            else
25                l = c;
26        }
27        return v[r];
28    }
29 };

```

8 geometry/halfplanes.cpp

```

1ld det3x3(line a, line b, line c) {
2    return a.c * (b.v % c.v)
3        + b.c * (c.v % a.v)
4        + c.c * (a.v % b.v);
5}
6
7//check: bounding box is included
8vector<pt> halfplanesIntersection(vector<line> l) {
9    sort(all(l), cmpLine); //the strongest constraint is first
10   l.erase(unique(all(l), eqLine), l.end());
11   int n = sz(l);
12   vi st;
13   forn (iter, 2)
14       forn (i, n) {
15           while (sz(st) > 1) {
16               int j = st.back(), k = *next(st.rbegin());
17               if (l[k].v % l[i].v <= eps ||
18                   det3x3(l[k], l[j], l[i]) <= eps)
19                   break;
20               st.pop_back();
21           }
22           st.push_back(i);
23       }
24
25   vi pos(n, -1);
26   bool ok = false;
27   forn (i, sz(st)) {
28       int id = st[i];
29       if (pos[id] != -1) {
30           st = vi(st.begin() + pos[id], st.begin() + i);
31           ok = true;
32           break;
33       } else
34           pos[id] = i;
35   }
36   if (!ok)
37       return {};
38
39   vector<pt> res;
40   pt M{0, 0};
41   int k = sz(st);
42   forn (i, k) {
43       line l1 = l[st[i]], l2 = l[st[(i + 1) % k]];
44       res.push_back(linesIntersection(l1, l2));
45       M = M + res.back();
46   }
47   M = M * (1. / k);
48   for (int id: st)
49       if (l[id].signedDist(M) < -eps)
50           return {};
51   return res;
52}

```

9 geometry/nd_convex_hull.cpp

```

1const int DIM = 4;
2typedef array<ll, DIM> pt;
3pt operator-(const pt &a, const pt &b) {
4    pt res;
5    forn (i, DIM)
6        res[i] = a[i] - b[i];
7    return res;
8}
9typedef array<pt, DIM-1> Edge;
10typedef array<pt, DIM> Face;
11vector<Face> faces;
12
13ll det(pt *a) {
14    int p[DIM];
15    iota(p, p + DIM, 0);
16    ll res = 0;
17    do {
18        ll x = 1;
19        forn (i, DIM) {
20            forn (j, i)
21                if (p[j] > p[i])
22                    x *= -1;
23            x *= a[i][p[i]];
24        }
25        res += x;
26    } while (next_permutation(p, p + DIM));
27    return res;
28}
29
30ll V(Face f, pt pivot) {
31    pt p[DIM];
32    forn (i, DIM)
33        p[i] = f[i] - pivot;
34    return det(p);
35}
36
37void init(vector<pt> p) {
38    forn (i, DIM+1) {
39        Face a;
40        int q = 0;
41        forn (j, DIM+1)
42            if (j != i)
43                a[q++] = p[j];
44        ll v = V(a, p[i]);
45        assert(v != 0);
46        if (v < 0)
47            swap(a[0], a[1]);
48        faces.push_back(a);
49    }
50}
51
52void add(pt p) {
53    vector<Face> newf, bad;
54    for (auto f: faces) {
55        if (V(f, p) < 0)
56            bad.push_back(f);
57        else
58            newf.push_back(f);
59    }
60    if (bad.empty()) {
61        return;
62    }
63    faces = newf;
64    vector<pair<Edge, pt>> edges;
65    for (auto f: bad) {
66        sort(all(f));
67        forn (i, DIM) {
68            Edge e;
69            int q = 0;
70            forn (j, DIM)
71                if (i != j)
72                    e[q++] = f[j];
73            edges.emplace_back(e, f[i]);
74        }
75    }
76    sort(all(edges));
77    forn (i, sz(edges)) {
78        if (i + 1 < sz(edges) &&
79            edges[i + 1].first == edges[i].first) {
80            ++i;
81            continue;
82        }
83        Face f;
84        forn (j, DIM-1)
85            f[j] = edges[i].first[j];
86        f[DIM-1] = p;
87        if (V(f, edges[i].second) < 0)
88            swap(f[0], f[1]);
89        faces.push_back(f);
90    }
91}

```

10 geometry/planar_faces.cpp

```

1 int m, n; // segs, points
2 pair<pt, pt> segs[maxn];
3 pt p[maxn], from, to;
4 map<pt, int> shr;
5 vi e[maxn]; // points adjacent to point
6 int getPoint(pt x) {
7     if (shr.count(x)) return shr[x];
8     p[n] = x;
9     return shr[x] = n++;
10}
11// segIntersection: {bool, point}, true iff exactly one point
12 void genIntersections() {
13     for (i, m) {
14         getPoint(segs[i].fi);
15         getPoint(segs[i].se);
16         for (j, i) {
17             auto t = segmentsIntersection(
18                 segs[i].fi, segs[i].se, segs[j].fi, segs[j].se);
19             if (t.fi) getPoint(t.se);
20         }
21     }
22}
23
24 void genGraph() {
25     for (i, m) {
26         vi pts;
27         for (j, n) if (pointInsideSegment(
28             p[j], segs[i].fi, segs[i].se)) {
29             pts.push_back(j);
30         }
31         sort(all(pts), [](int i, int j) {
32             return p[i] < p[j]; });
33         for (j, pts.size() - 1) {
34             int u = pts[j], v = pts[j+1];
35             e[u].push_back(v);
36             e[v].push_back(u);
37         }
38     }
39     for (i, n) {
40         sort(all(e[i]), [i](int x, int y) {
41             pt a = p[x] - p[i];
42             pt b = p[y] - p[i];
43             if (a.right() != b.right()) return a.right();
44             return a % b > 0;
45         });
46     }
47}
48
49 vector<pt> faces[maxn];
50 bool inner[maxn];
51 int nf;
52 map<pii, int> faceForEdge;
53 vi ef[maxn]; // graph on faces
54
55 void genFaces() {
56     for (i, n) for (int to: e[i]) {
57         if (faceForEdge.count({i, to})) continue;
58         int f = nf++;
59         int v = i, u = to;
60         do {
61             faces[f].push_back(p[v]);
62             faceForEdge[{v, u}] = f;
63             auto it = lower_bound(all(e[u]), v,
64                 [u](int x, int y) {
65                     pt a = p[x] - p[u];
66                     pt b = p[y] - p[u];
67                     if (a.right() != b.right()) return a.right();
68                     return a % b > 0;
69                 });
70             assert(*it == v);
71             if (it == e[u].begin()) it = e[u].end();
72             v = u;
73             u = *--it;
74         } while (v != i || u != to);
75     }
76     for (i, nf) {
77         ld s = 0;
78         for (j, faces[i].size()) {
79             s += faces[i][j] % faces[i][(j+1)%faces[i].size()];
80         }
81         inner[i] = gt(s, 0);
82     }
83     for (v, n) for (int to: e[v]) {
84         int f1 = faceForEdge[{v, to}];
85         int f2 = faceForEdge[{to, v}];
86         if (f1 != f2) {
87             ef[f1].push_back(f2);
88             ef[f2].push_back(f1);
89         }
90     }
91}

```

11 geometry/polygon.cpp

```

1 bool pointInsidePolygon(pt a, pt *p, int n) {
2     double sumAng = 0;
3     for (i, n) {
4         pt A = p[i], B = p[(i + 1) % n];
5         if (pointInsideSegment(a, A, B))
6             return true;
7         sumAng += atan2((A - a) % (B - a), (A - a) * (B - a));
8     }
9     return fabs(sumAng) > 1;
10}
11
12//check: p is oriented ccw
13 bool segmentInsidePolygon(pt a, pt b, pt *p, int n) {
14     if (!pointInsidePolygon((a + b) * .5, p, n))
15         return false;
16     if (ze((a - b).abs()))
17         return true;
18     for (i, n) {
19         pt c = p[i];
20         if (ze((a - c) % (b - c)) &&
21             (a - c) * (b - c) < -eps) {
22             //point inside interval
23             pt pr = p[(i + n - 1) % n];
24             pt nx = p[(i + 1) % n];
25             if ((c - pr) % (nx - c) > eps)
26                 return false;
27             ld s1 = (pr - a) % (b - a);
28             ld s2 = (nx - a) % (b - a);
29             if ((s1 > eps || s2 > eps) &&
30                 (s1 < -eps || s2 < -eps))
31                 return false;
32         }
33         //interval intersection
34         pt d = p[(i + 1) % n];
35         ld s1 = (a - c) % (d - c);
36         ld s2 = (b - c) % (d - c);
37         if (s1 >= -eps && s2 >= -eps)
38             continue;
39         if (s1 <= eps && s2 <= eps)
40             continue;
41
42         s1 = (c - a) % (b - a);
43         s2 = (d - a) % (b - a);
44         if (s1 >= -eps && s2 >= -eps)
45             continue;
46         if (s1 <= eps && s2 <= eps)
47             continue;
48
49         return false;
50     }
51     return true;
52}

```


12 geometry/polygon_tangents.cpp

```

1 struct Cmp {
2     pt M, v0;
3
4     bool operator()(const pt &a, const pt &b) {
5         pt va{v0 * (a - M), v0 % (a - M)};
6         pt vb{v0 * (b - M), v0 % (b - M)};
7         return cmpAngle(va, vb);
8     }
9 };
10
11 struct Hull {
12     vector<pt> h;
13     int n;
14
15     void build() {
16         sort(all(h));
17         h.erase(unique(all(h)), h.end());
18         vector<pt> top, bot;
19         for (auto p: h) {
20             while (sz(bot) > 1 && (p - bot.back()) %
21                 (p - *next(bot.rbegin())) >= -eps)
22                 bot.pop_back();
23             bot.push_back(p);
24             while (sz(top) > 1 && (p - top.back()) %
25                 (p - *next(top.rbegin())) <= eps)
26                 top.pop_back();
27             top.push_back(p);
28         }
29         if (sz(top))
30             top.pop_back();
31         reverse(all(top));
32         if (sz(top))
33             top.pop_back();
34         h = bot;
35         h.insert(h.end(), all(top));
36         n = sz(h);
37     }
38
39     bool visSide(pt a, int i) {
40         return (h[(i + 1) % n] - a) % (h[i % n] - a) > eps;
41     }
42
43     bool vis(pt a, int i) {
44         return visSide(a, i) || visSide(a, i + n - 1);
45     }
46
47     bool isTangent(pt a, int i) {
48         return visSide(a, i) != visSide(a, i + n - 1);
49     }
50
51     int binSearch(int l, int r, pt a) {
52         //tricky binsearch; l < r not necessarily
53         while (abs(l - r) > 1) {
54             int c = (l + r) / 2;
55             if (vis(a, c))
56                 l = c;
57             else
58                 r = c;
59         }
60         assert(isTangent(a, l));
61         return l % n;
62     }
63
64     //check: n >= 3
65     pair<int, int> tangents(pt a) {
66         assert(n >= 3);
67         pt M = (h[0] + h[1] + h[2]) * (1. / 3);
68         if (a == M)
69             return {-1, -1};
70         Cmp cmp{M, h[0] - M};
71         //assert(is_sorted(all(h), cmp));
72         int pos = upper_bound(all(h), a, cmp) - h.begin();
73         pt L = h[(pos + n - 1) % n], R = h[pos % n];
74         if ((R - L) % (a - L) >= -eps)
75             return {-1, -1}; //point inside hull
76         int pos2 = upper_bound(all(h), M*2-a, cmp) - h.begin();
77         assert(pos % n != pos2 % n);
78         if (pos > pos2)
79             pos2 += n;
80         return {binSearch(pos, pos2, a),
81             binSearch(pos + n - 1, pos2 - 1, a)};
82     }
83 };

```

13 geometry/primitives.cpp

```

1 struct line {
2     pt v;
3     ld c; // v * p = c
4
5     //check: p1 != p2
6     line(pt p1, pt p2) {
7         v = (p2 - p1).rot();
8         v = v * (1. / v.abs());
9         c = v * p1;
10    }
11
12    // Convert from ax + by + c = 0
13
14    //check: a^2+b^2 > 0
15    line(ld a, ld b, ld _c): v(pt{a, b}), c(-_c) {
16        ld d = v.abs();
17        v = v * (1. / d);
18        c /= d;
19    }
20
21    //check: v.abs() == 1
22    ld signedDist(pt p) {
23        return v * p - c;
24    }
25 };
26
27 //check: a != b
28 pt lineProjection(pt p, pt a, pt b) {
29     pt v = (b - a).rot();
30     ld s = (p - a) % (b - a);
31     return p + v * (s / v.abs2());
32 }
33
34 ld pointSegmentDist(pt p, pt a, pt b) {
35     if ((p - a) * (b - a) <= 0 || ze((b - a).abs()))
36         return (p - a).abs();
37     if ((p - b) * (a - b) <= 0)
38         return (p - b).abs();
39     return fabs1((p - a) % (p - b)) / (b - a).abs();
40 }
41
42 pt linesIntersection(line l1, line l2) {
43     ld d = l1.v.x * l2.v.y - l1.v.y * l2.v.x;
44     if (ze(d)) {
45         if (eq(l1.c, l2.c)) {
46             //stub: equal lines
47         } else {
48             //stub: empty intersection
49         }
50         return pt{1e18, 1e18};
51     }
52     ld dx = l1.c * l2.v.y - l1.v.y * l2.c;
53     ld dy = l1.v.x * l2.c - l1.c * l2.v.x;
54     return pt{dx / d, dy / d};
55 }
56
57 pt linesIntersection(pt a, pt b, pt c, pt d) {
58     ld s = (b - a) % (d - c);
59     if (ze(s)) {
60         //stub: parallel or equal lines
61         return pt{1e18, 1e18};
62     }
63     ld s1 = (c - a) % (d - a);
64     return a + (b - a) * (s1 / s);
65 }
66
67 bool pointInsideSegment(pt p, pt a, pt b) {
68     if (!ze((p - a) % (p - b)))
69         return false;
70     ld prod = (a - p) * (b - p);
71     return ze(prod) || prod < 0;
72     if (ze(prod)) {
73         //stub: coincides with segment end
74         return true;
75     }
76     return prod < 0;
77 }
78
79 bool checkSegmentIntersection(pt a, pt b, pt c, pt d) {
80     if (ze((a - b) % (c - d))) {
81         if (pointInsideSegment(a, c, d) ||
82             pointInsideSegment(b, c, d) ||
83             pointInsideSegment(c, a, b) ||
84             pointInsideSegment(d, a, b)) {
85             //stub: intersection of parallel segments
86             return true;
87         }
88         return false;
89     }
90     ld s1, s2;
91     for (iter, 2) {

```


14 geometry/svg.cpp

```

92     s1 = (c - a) % (b - a);
93     s2 = (d - a) % (b - a);
94     if (s1 > eps && s2 > eps)
95         return false;
96     if (s1 < -eps && s2 < -eps)
97         return false;
98     swap(a, c), swap(b, d);
99 }
100 return true;
101}
102
103vector<pt> lineCircleIntersection(line l, pt a, ld r) {
104    ld d = l.signedDist(a);
105    pt h = a - l.v * d;
106    if (eq(fabsl(d), r))
107        return {h};
108    else if (fabsl(d) > r)
109        return {};
110    pt w = l.v.rot() * Sqrt(sqr(r) - sqr(d));
111    return {h + w, h - w};
112}
113
114vector<pt> circlesIntersecton(pt a, ld r1, pt b, ld r2) {
115    ld d = (a - b).abs();
116    if (ze(d) && eq(r1, r2)) {
117        //stub: equal circles
118        return {};
119    }
120    // intersection is non-empty iff
121    // triangle with sides r1, r2, d exists
122    ld per = r1 + r2 + d;
123    ld mx = max(max(r1, r2), d);
124    int num = 2;
125    if (eq(mx * 2, per)) {
126        num = 1;
127    } else if (mx * 2 > per)
128        return {};
129    ld part = (sqr(r1) + sqr(d) - sqr(r2)) / ld(2 * d);
130    pt h = a + (b - a) * (part / d);
131    if (num == 1)
132        return {h};
133    ld dh = Sqrt(sqr(r1) - sqr(part));
134    pt w = ((b - a) * (dh / d)).rot();
135    return {h + w, h - w};
136}
137
138vector<pt> circleTangents(pt p, pt a, ld r) {
139    ld d = (p - a).abs();
140    if (eq(r, d))
141        return {p};
142    else if (r > d)
143        return {};
144    ld len = Sqrt(sqr(d) - sqr(r));
145    vector<pt> res;
146    pt vec = (a - p) * (len / sqr(d));
147    for (int sgn: {-1, 1})
148        res.push_back(p + vec.rotCw(pt{len, r * sgn}));
149    return res;
150}
151
152vector<line> circlesBitangents(pt a, ld r1, pt b, ld r2) {
153    ld d = (a - b).abs();
154    if (ze(d) && eq(r1, r2)) {
155        //stub: equal circles
156        return {};
157    }
158
159    vector<line> res;
160    for (int s1: {-1, 1})
161        for (int s2: {-1, 1}) {
162            // inner tangent iff s1 != s2
163            // treat radii as signed
164            ld r = s2 * r2 - s1 * r1;
165            if (eq(fabsl(r), d)) {
166                // incident tangents; need only one copy
167                if (s1 == 1)
168                    continue;
169            } else if (fabsl(r) > d)
170                continue;
171            ld len = Sqrt(sqr(d) - sqr(r));
172            line l(a, a + (b - a).rotCw(pt{len, r}));
173            l.c -= s1 * r1;
174            res.push_back(l);
175        }
176    return res;
177}

```

```

1 struct SVG {
2     FILE *out;
3     ld sc = 50;
4
5     void open() {
6         out = fopen("image.svg", "w");
7         fprintf(out, "<svg xmlns='http://www.w3.org/2000/svg'
            ↳ viewBox='-1000 -1000 2000 2000'>\n");
8     }
9
10    void line(pt a, pt b) {
11        a = a * sc, b = b * sc;
12        fprintf(out, "<line x1='%Lf' y1='%Lf' x2='%Lf' y2='%Lf'
            ↳ stroke='black'>\n", a.x, -a.y, b.x, -b.y);
13    }
14
15    void circle(pt a, ld r = -1, string col = "red") {
16        r = (r == -1 ? 10 : sc * r);
17        a = a * sc;
18        fprintf(out, "<circle cx='%Lf' cy='%Lf' r='%Lf'
            ↳ fill='%s'>\n", a.x, -a.y, r, col.c_str());
19    }
20
21    void text(pt a, string s) {
22        a = a * sc;
23        fprintf(out, "<text x='%Lf' y='%Lf'
            ↳ font-size='10px'>%s</text>\n", a.x, -a.y,
            ↳ s.c_str());
24    }
25
26    void close() {
27        fprintf(out, "</svg>\n");
28        fclose(out);
29        out = 0;
30    }
31
32    ~SVG() {
33        if (out)
34            close();
35    }
36} svg;

```

15 graphs/2sat.cpp

```

1 const int maxn = 200100; //2 x number of variables
2
3 namespace TwoSAT {
4     int n; //number of variables
5     bool used[maxn];
6     vector<int> g[maxn];
7     vector<int> gr[maxn];
8     int comp[maxn];
9     int res[maxn];
10
11     void addEdge(int u, int v) { //u or v
12         g[u].push_back(v ^ 1);
13         g[v].push_back(u ^ 1);
14         gr[u ^ 1].push_back(v);
15         gr[v ^ 1].push_back(u);
16     }
17
18     vector<int> ord;
19     void dfs1(int u) {
20         used[u] = true;
21         for (int v: g[u]) {
22             if (used[v])
23                 continue;
24             dfs1(v);
25         }
26         ord.push_back(u);
27     }
28
29     int COL = 0;
30     void dfs2(int u) {
31         used[u] = true;
32         comp[u] = COL;
33         for (int v: gr[u]) {
34             if (used[v])
35                 continue;
36             dfs2(v);
37         }
38     }
39
40     void mark(int u) {
41         res[u / 2] = u % 2;
42         used[u] = true;
43         for (int v: g[u]) {
44             if (used[v])
45                 continue;
46             mark(v);
47         }
48     }
49
50     bool run() {
51         fill(res, res + 2 * n, -1);
52         fill(used, used + 2 * n, false);
53         forn(i, 2 * n)
54             if (!used[i])
55                 dfs1(i);
56         reverse(ord.begin(), ord.end());
57         assert((int) ord.size() == (2 * n));
58         fill(used, used + 2 * n, false);
59         for (int u: ord) if (!used[u]) {
60             dfs2(u);
61             ++COL;
62         }
63         forn(i, n)
64             if (comp[i * 2] == comp[i * 2 + 1])
65                 return false;
66
67         reverse(ord.begin(), ord.end());
68         fill(used, used + 2 * n, false);
69         for (int u: ord) {
70             if (res[u / 2] != -1) {
71                 continue;
72             }
73             mark(u);
74         }
75         return true;
76     }
77 };
78
79 int main() {
80     TwoSAT::n = 2;
81     TwoSAT::addEdge(0, 2); //x or y
82     TwoSAT::addEdge(0, 3); //x or !y
83     TwoSAT::addEdge(3, 3); //!y or !y
84     assert(TwoSAT::run());
85     cout << TwoSAT::res[0] << ' ' << TwoSAT::res[1] << '\n';
86     //1 0
87 }

```

16 graphs/directed_mst.cpp

```

1 // WARNING: this code wasn't submitted anywhere
2
3 namespace TwoChinese {
4
5     struct Edge {
6         int to, w, id;
7         bool operator<(const Edge& other) const {
8             return to < other.to || (to == other.to && w < other.w);
9         }
10 };
11 typedef vector<vector<Edge>> Graph;
12
13 const int maxn = 2050;
14
15 // global, for supplementary algorithms
16 int b[maxn];
17 int tin[maxn], tup[maxn];
18 int dtime; // counter for tin, tout
19 vector<int> st;
20 int nc; // number of strongly connected components
21 int q[maxn];
22
23 int answer;
24
25 void tarjan(int v, const Graph& e, vector<int>& comp) {
26     b[v] = 1;
27     st.push_back(v);
28     tin[v] = tup[v] = dtime++;
29
30     for (Edge t: e[v]) if (t.w == 0) {
31         int to = t.to;
32         if (b[to] == 0) {
33             tarjan(to, e, comp);
34             tup[v] = min(tup[v], tup[to]);
35         } else if (b[to] == 1) {
36             tup[v] = min(tup[v], tin[to]);
37         }
38     }
39
40     if (tin[v] == tup[v]) {
41         while (true) {
42             int t = st.back();
43             st.pop_back();
44             comp[t] = nc;
45             b[t] = 2;
46             if (t == v) break;
47         }
48         ++nc;
49     }
50 }
51
52 vector<Edge> bfs(
53     const Graph& e, const vi& init, const vi& comp)
54 {
55     int n = e.size();
56     forn(i, n) b[i] = 0;
57     int lq = 0, rq = 0;
58     for (int v: init) b[v] = 1, q[rq++] = v;
59
60     vector<Edge> result;
61
62     while (lq != rq) {
63         int v = q[lq++];
64         for (Edge t: e[v]) if (t.w == 0) {
65             int to = t.to;
66             if (b[to]) continue;
67             if (!comp.empty() && comp[v] != comp[to]) continue;
68             b[to] = 1;
69             q[rq++] = to;
70             result.push_back(t);
71         }
72     }
73
74     return result;
75 }
76
77 // warning: check that each vertex is reachable from root
78 vector<Edge> run(Graph e, int root) {
79     int n = e.size();
80
81     // find minimum incoming weight for each vertex
82     vector<int> minw(n, inf);
83     forn(v, n) for (Edge t: e[v]) {
84         minw[t.to] = min(minw[t.to], t.w);
85     }
86     forn(v, n) for (Edge &t: e[v]) if (t.to != root) {
87         t.w -= minw[t.to];
88     }
89     forn(i, n) if (i != root) answer += minw[i];
90
91     // check if each vertex is reachable from root by zero edges

```

17 graphs/edmonds_matching.cpp

```

92 vector<Edge> firstResult = bfs(e, {root}, {});
93 if ((int)firstResult.size() + 1 == n) {
94     return firstResult;
95 }
96
97 // find strongly connected comp-s and build compressed graph
98 vector<int> comp(n);
99 forn(i, n) b[i] = 0;
100 nc = 0;
101 dtime = 0;
102 forn(i, n) if (!b[i]) tarjan(i, e, comp);
103
104 // multiple edges may be removed here if needed
105 Graph ne(nc);
106 forn(v, n) for (Edge t: e[v]) {
107     if (comp[v] != comp[t.to]) {
108         ne[comp[v]].push_back({comp[t.to], t.w, t.id});
109     }
110 }
111 int oldnc = nc;
112
113 // run recursively on compressed graph
114 vector<Edge> subres = run(ne, comp[root]);
115
116 // find incoming edge id for each component, init queue
117 // if there is an edge (u, v) between different components
118 // than v is added to queue
119 nc = oldnc;
120 vector<int> incomingId(nc);
121 for (Edge e: subres) {
122     incomingId[e.to] = e.id;
123 }
124
125 vector<Edge> result;
126 vector<int> init;
127 init.push_back(root);
128 forn(v, n) for (Edge t: e[v]) {
129     if (incomingId[comp[t.to]] == t.id) {
130         result.push_back(t);
131         init.push_back(t.to);
132     }
133 }
134
135 // run bfs to add edges inside components and return answer
136 vector<Edge> innerEdges = bfs(e, init, comp);
137 result.insert(result.end(), all(innerEdges));
138
139 assert((int)result.size() + 1 == n);
140 return result;
141}
142
143 // namespace TwoChinese
144
145 void test () {
146     auto res = TwoChinese::run({
147         {{1,5,0},{2,5,1}},
148         {{3,1,2}},
149         {{1,2,3},{4,1,4}},
150         {{1,1,5},{4,2,6}},
151         {{2,1,7}}},
152         0);
153     cout << TwoChinese::answer << endl;
154     for (auto e: res) cout << e.id << " ";
155     cout << endl;
156     // 9      0 6 2 7
157 }

```

```

1 int n;
2 vi e[maxn];
3 int mt[maxn], p[maxn], base[maxn], b[maxn], blos[maxn];
4 int q[maxn];
5 int blca[maxn]; // used for lca
6
7 int lca(int u, int v) {
8     forn(i, n) blca[i] = 0;
9     while (true) {
10         u = base[u];
11         blca[u] = 1;
12         if (mt[u] == -1) break;
13         u = p[mt[u]];
14     }
15     while (!blca[base[v]]) {
16         v = p[mt[base[v]]];
17     }
18     return base[v];
19 }
20
21 void mark_path(int v, int b, int ch) {
22     while (base[v] != b) {
23         blos[base[v]] = blos[base[mt[v]]] = 1;
24         p[v] = ch;
25         ch = mt[v];
26         v = p[mt[v]];
27     }
28 }
29
30 int find_path(int root) {
31     forn(i, n) {
32         base[i] = i;
33         p[i] = -1;
34         b[i] = 0;
35     }
36
37     b[root] = 1;
38     q[0] = root;
39     int lq = 0, rq = 1;
40     while (lq != rq) {
41         int v = q[lq++];
42         for (int to: e[v]) {
43             if (base[v] == base[to] || mt[v] == to) continue;
44             if (to==root || (mt[to] != -1 && p[mt[to]] != -1)) {
45                 int curbase = lca(v, to);
46                 forn(i, n) blos[i] = 0;
47                 mark_path(v, curbase, to);
48                 mark_path(to, curbase, v);
49                 forn(i, n) if (blos[base[i]]) {
50                     base[i] = curbase;
51                     if (!b[i]) b[i] = 1, q[rq++] = i;
52                 }
53             } else if (p[to] == -1) {
54                 p[to] = v;
55                 if (mt[to] == -1) {
56                     return to;
57                 }
58                 to = mt[to];
59                 b[to] = 1;
60                 q[rq++] = to;
61             }
62         }
63     }
64 }
65 return -1;
66 }
67
68 int matching() {
69     forn(i, n) mt[i] = -1;
70     int res = 0;
71     forn(i, n) if (mt[i] == -1) {
72         int v = find_path(i);
73         if (v != -1) {
74             ++res;
75             while (v != -1) {
76                 int pv = p[v], ppv = mt[p[v]];
77                 mt[v] = pv, mt[ppv] = v;
78                 v = ppv;
79             }
80         }
81     }
82     return res;
83 }

```

18 graphs/euler_cycle.cpp

```

1 struct Edge {
2     int to, id;
3 };
4
5 bool usedEdge[maxm];
6 vector<Edge> g[maxn];
7 int ptr[maxn];
8
9 vector<int> cycle;
10 void eulerCycle(int u) {
11     while (ptr[u] < sz(g[u]) && usedEdge[g[u][ptr[u]].id])
12         ++ptr[u];
13     if (ptr[u] == sz(g[u]))
14         return;
15     const Edge &e = g[u][ptr[u]];
16     usedEdge[e.id] = true;
17     eulerCycle(e.to);
18     cycle.push_back(e.id);
19     eulerCycle(u);
20 }
21
22 int edges = 0;
23 void addEdge(int u, int v) {
24     g[u].push_back(Edge{v, edges});
25     g[v].push_back(Edge{u, edges++});
26 }

```

19 math/factor.cpp

```

1 //WARNING: only mod <= 1e18
2 ll mul(ll a, ll b, ll mod) {
3     ll res = a * b - (ll(ld(a) * ld(b) / ld(mod)) * mod);
4     while (res < 0)
5         res += mod;
6     while (res >= mod)
7         res -= mod;
8     return res;
9 }
10
11 bool millerRabinTest(ll n, ll a) {
12     if (gcd(n, a) > 1)
13         return false;
14     ll x = n - 1;
15     int l = 0;
16     while (x % 2 == 0) {
17         x /= 2;
18         ++l;
19     }
20     ll c = binpow(a, x, n);
21     for (int i = 0; i < l; ++i) {
22         ll nx = mul(c, c, n);
23         if (nx == 1) {
24             if (c != 1 && c != n - 1)
25                 return false;
26             else
27                 return true;
28         }
29         c = nx;
30     }
31     return c == 1;
32 }
33
34 bool isPrime(ll n) {
35     if (n == 1)
36         return false;
37     if (n % 2 == 0)
38         return n == 2;
39     for (ll a = 2; a < min<ll>(8, n); ++a)
40         if (!millerRabinTest(n, a))
41             return false;
42     return true;
43 }
44
45 //WARNING: p is not sorted
46 void factorize(ll x, vector<ll> &p) {
47     if (x == 1)
48         return;
49     if (isPrime(x)) {
50         p.push_back(x);
51         return;
52     }
53     for (ll d: {2, 3, 5})
54         if (x % d == 0) {
55             p.push_back(d);
56             factorize(x / d, p);
57             return;
58         }
59     while (true) {
60         ll x1 = rr() % (x - 1) + 1;
61         ll x2 = (mul(x1, x1, x) + 1) % x;
62         int i1 = 1, i2 = 2;
63         while (true) {
64             ll c = (x1 + x - x2) % x;
65             if (c == 0)
66                 break;
67             ll g = gcd(c, x);
68             if (g > 1) {
69                 factorize(g, p);
70                 factorize(x / g, p);
71                 return;
72             }
73             if (i1 * 2 == i2) {
74                 i1 *= 2;
75                 x1 = x2;
76             }
77             ++i2;
78             x2 = (mul(x2, x2, x) + 1) % x;
79         }
80     }
81 }

```

20 math/fft.cpp

```

1const int LG = 20;
2typedef complex<ld> base;
3
4vector<base> ang[LG + 5];
5
6void init_fft() {
7    int n = 1 << LG;
8    ld e = acos(-1) * 2 / n;
9    ang[LG].resize(n);
10   forn(i, n)
11       ang[LG][i] = polar(ld(1), e * i);
12
13   for (int k = LG - 1; k >= 0; --k) {
14       ang[k].resize(1 << k);
15       forn(i, 1 << k)
16           ang[k][i] = ang[k + 1][i * 2];
17   }
18}
19
20void fft_rec(base *a, int lg, bool inv) {
21   if (lg == 0)
22       return;
23   int hlen = 1 << (lg - 1);
24   fft_rec(a, lg-1, inv);
25   fft_rec(a + hlen, lg-1, inv);
26
27   forn(i, hlen) {
28       base w = ang[lg][i];
29       if (inv)
30           w = conj(w);
31       base u = a[i];
32       base v = a[i + hlen] * w;
33       a[i] = u + v;
34       a[i + hlen] = u - v;
35   }
36}
37
38void fft(base *a, int lg, bool inv) {
39   int n = 1 << lg;
40   int j = 0, bit;
41   for (int i = 1; i < n; ++i) {
42       for (bit = n >> 1; bit & j; bit >= 1)
43           j ^= bit;
44       j ^= bit;
45       if (i < j)
46           swap(a[i], a[j]);
47   }
48   fft_rec(a, lg, inv);
49   if (inv) {
50       forn(i, n)
51           a[i] /= n;
52   }
53}
54
55void test() {
56   int lg = 3;
57   int n = 1 << lg;
58   init_fft();
59   base a[] = {1,3,5,2,4,6,7,1};
60   fft(a, lg, 0);
61   forn(i, n)
62       cout << a[i].real() << " ";
63   cout << '\n';
64   forn(i, n)
65       cout << a[i].imag() << " ";
66   cout << '\n';
67   // 29 -5.82843 -7 -0.171573 5 -0.171573 -7 -5.82843
68   // 0 -3.41421 6 0.585786 0 -0.585786 -6 3.41421
69}

```

21 math/fft_inv.cpp

```

1vector<int> mul(vector<int> a, vector<int> b,
2               bool carry = true) {
3   int n = sz(a);
4   if (carry) {
5       a.resize(n * 2);
6       b.resize(n * 2);
7   }
8   fft(a.data(), a.size(), false);
9   fft(b.data(), b.size(), false);
10  for (int i = 0; i < sz(a); ++i)
11      a[i] = mul(a[i], b[i]);
12  fft(a.data(), a.size(), true);
13  a.resize(n);
14  return a;
15}
16
17vector<int> inv(vector<int> v) {
18   int n = 1;
19   while (n < sz(v))
20       n <<= 1;
21   v.resize(n, 0);
22   vector<int> res(1, binpow(v[0], mod - 2));
23   for (int k = 1; k < n; k <= 1) {
24       vector<int> A(k * 2, 0);
25       copy(v.begin(), v.begin() + k, A.begin());
26       vector<int> C = res;
27       C.resize(k * 2, 0);
28       A = mul(A, C, false);
29       for (int i = 0; i < 2 * k; ++i)
30           A[i] = sub(0, A[i]);
31       A[0] = sum(A[0], 1);
32       for (int i = 0; i < k; ++i)
33           assert(A[i] == 0);
34       copy(A.begin() + k, A.end(), A.begin());
35       A.resize(k);
36       vector<int> B(k);
37       copy(v.begin() + k, v.begin() + 2 * k, B.begin());
38       C.resize(k);
39       B = mul(B, C);
40       for (int i = 0; i < k; ++i)
41           A[i] = sub(A[i], B[i]);
42       A = mul(A, C);
43       res.resize(k * 2);
44       copy(A.begin(), A.end(), res.begin() + k);
45   }
46   return res;
47}

```

22 math/golden_search.cpp

```

1ld f(ld x) {
2    return 5 * x * x + 100 * x + 1; // -10 is minimum
3}
4
5ld goldenSearch(ld l, ld r) {
6    ld phi = (1 + sqrtl(5)) / 2;
7    ld resphi = 2 - phi;
8    ld x1 = l + resphi * (r - l);
9    ld x2 = r - resphi * (r - l);
10   ld f1 = f(x1);
11   ld f2 = f(x2);
12   forn (iter, 60) {
13       if (f1 < f2) {
14           r = x2;
15           x2 = x1;
16           f2 = f1;
17           x1 = l + resphi * (r - l);
18           f1 = f(x1);
19       } else {
20           l = x1;
21           x1 = x2;
22           f1 = f2;
23           x2 = r - resphi * (r - l);
24           f2 = f(x2);
25       }
26   }
27   return (x1 + x2) / 2;
28}
29
30int main() {
31    std::cout << goldenSearch(-100, 100) << '\n';
32}

```

23 math/numbers.tex

- Simpson and Gauss numerical integration:

$$\int_a^b f(x)dx = (b-a)/6 \cdot (f(a) + 4(f(a+b)/2) + f(b))$$

$$\int_{-1}^1 x_{1,3} = \pm\sqrt{0.6}, x_2 = 0; a_{1,3} = 5/9, a_2 = 8/9$$

- Large primes: $10^{18} + 3, +31, +3111, 10^9 + 21, +33$

- FFT modules:

$$\begin{array}{lll} 1\,107\,296\,257 & 2^{25} \cdot 3 \cdot 11 + 1 & 10 \\ 1\,161\,822\,209 & 2^{22} \cdot 277 + 1 & 3 \\ 1\,261\,007\,895\,663\,738\,881 & 2^{55} \cdot 5 \cdot 7 + 1 & 6 \text{ (check)} \end{array}$$

- Fibonacci numbers:

$$\begin{array}{ll} 1, 2 : & 1 \\ 45 : & 1\,134\,903\,170 \\ 46 : & 1\,836\,311\,903 \text{ (max int)} \\ 47 : & 2\,971\,215\,073 \text{ (max unsigned)} \\ 91 : & 4\,660\,046\,610\,375\,530\,309 \\ 92 : & 7\,540\,113\,804\,746\,346\,429 \text{ (max i64)} \\ 93 : & 12\,200\,160\,415\,121\,876\,738 \text{ (max unsigned i64)} \end{array}$$

- Powers of two

$$\begin{array}{l} 2^{31} = 2\,147\,483\,648 = 2.1 \cdot 10^9 \\ 2^{32} = 4\,294\,967\,296 = 4.2 \cdot 10^9 \\ 2^{63} = 9\,223\,372\,036\,854\,775\,808 = 9.2 \cdot 10^{18} \\ 2^{64} = 18\,446\,744\,073\,709\,551\,616 = 1.8 \cdot 10^{19} \end{array}$$

- Highly composite numbers

$$\begin{array}{l} - \leq 1000: d(840) = 32, \leq 10^4: d(9\,240) = 64 \\ - \leq 10^5: d(83\,160) = 128, \leq 10^6: d(720\,720) = 240 \\ - \leq 10^7: d(8\,648\,640) = 448, \leq 10^8: d(91\,891\,800) = 768 \\ - \leq 10^9: d(931\,170\,240) = 1344 \\ - \leq 10^{11}: d(97\,772\,875\,200) = 4032 \\ - \leq 10^{12}: d(963\,761\,198\,400) = 6720 \\ - \leq 10^{15}: d(866\,421\,317\,361\,600) = 26880 \\ - \leq 10^{18}: d(897\,612\,484\,786\,617\,600) = 103680 \end{array}$$

- Misc

- Расстояние между точками по сфере: $L = R \cdot \arccos(\cos \theta_1 \cdot \cos \theta_2 + \sin \theta_1 \cdot \sin \theta_2 \cdot \cos(\varphi_1 - \varphi_2))$, где θ — широты (от $-\frac{\pi}{2}$ до $\frac{\pi}{2}$), φ — долготы (от $-\pi$ до π).
- Объём шарового сегмента: $V = \pi h^2(R - \frac{1}{3}h)$, где h — высота от вершины сектора до секущей плоскости
- Площадь поверхности шарового сегмента: $S = 2\pi Rh$, где h — высота.

- Bell numbers: 0:1, 1:1, 2:2, 3:5, 4:15, 5:52, 6:203, 7:877, 8:4140, 9:21147, 10:115975, 11:678570, 12:4213597, 13:27644437, 14:190899322, 15:1382958545, 16:10480142147, 17:82864869804, 18:682076806159, 19:5832742205057, 20:51724158235372, 21:474869816156751, 22:4506715738447323, 23:44152005855084346

- Catalan numbers: 0:1, 1:1, 2:2, 3:5, 4:14, 5:42, 6:132, 7:429, 8:1430, 9:4862, 10:16796, 11:58786, 12:208012, 13:742900, 14:2674440, 15:9694845, 16:35357670, 17:129644790, 18:477638700, 19:1767263190, 20:6564120420, 21:24466267020, 22:91482563640, 23:343059613650, 24:1289904147324, 25:4861946401452

24 math/simplex.cpp

```

1 namespace Simplex {
2
3 ld D[maxm][maxn]; // [n+2][m+2]
4 int B[maxm];
5 int N[maxn];
6 ld x[maxn];
7 int n, m;
8
9 //x >= 0, Ax <= b, c^Tx -> max
10 void init(int _n, int _m, ld A[][maxn], ld *b, ld *c) {
11     n = _n, m = _m;
12     forn (i, m)
13         forn (j, n)
14             D[i][j] = -A[i][j];
15     forn (i, m) {
16         D[i][n] = 1;
17         D[i][n + 1] = b[i];
18     }
19     forn (j, n) {
20         D[m][j] = c[j];
21         D[m + 1][j] = 0;
22     }
23     D[m][n + 1] = D[m][n] = D[m + 1][n + 1] = 0;
24     D[m + 1][n] = -1;
25     iota(B, B + m, n);
26     iota(N, N + n, 0);
27     N[n] = -1;
28 }
29
30 void pivot(int b, int nb) {
31     assert(D[b][nb] != 0);
32     ld q = 1. / -D[b][nb];
33     D[b][nb] = -1;
34     forn (i, n + 2)
35         D[b][i] *= q;
36     forn (i, m + 2) {
37         if (i == b)
38             continue;
39         ld coef = D[i][nb];
40         D[i][nb] = 0;
41         forn (j, n + 2)
42             D[i][j] += coef * D[b][j];
43     }
44     swap(B[b], N[nb]);
45 }
46
47 bool betterN(int f, int i, int j) {
48     if (eq(D[f][i], D[f][j]))
49         return N[i] < N[j];
50     return D[f][i] > D[f][j];
51 }
52
53 bool betterB(int nb, int i, int j) {
54     ld ai = D[i][n + 1] / D[i][nb];
55     ld aj = D[j][n + 1] / D[j][nb];
56     if (eq(ai, aj))
57         return B[i] < B[j];
58     return ai > aj;
59 }
60
61 bool simplex(int phase) {
62     int f = phase == 1 ? m : m + 1;
63     while (true) {
64         int nb = -1;
65         forn (i, n + 1) {
66             if (N[i] == -1 && phase == 1)
67                 continue;
68             if (nb == -1 || betterN(f, i, nb))
69                 nb = i;
70         }
71         if (D[f][nb] <= eps)
72             return phase == 1;
73         assert(nb != -1);
74
75         int b = -1;
76         forn (i, m) {
77             if (D[i][nb] >= -eps)
78                 continue;
79             if (b == -1 || betterB(nb, i, b))
80                 b = i;
81         }
82         if (b == -1)
83             return false;
84         pivot(b, nb);
85         if (N[nb] == -1 && phase == 2)
86             return true;
87     }
88 }
89
90 ld solve() {
91     int b = -1;
92     forn (i, m) {
93         if (b == -1 || D[i][n + 1] < D[b][n + 1])
94             b = i;
95     }
96     assert(b != -1);
97     if (D[b][n + 1] < -eps) {
98         pivot(b, n);
99         if (!simplex(2) || D[m + 1][n + 1] < -eps)
100             return -infl;
101     }
102     if (!simplex(1))
103         return infl;
104
105     forn (i, n)
106         x[i] = 0;
107     forn (i, m)
108         if (B[i] < n)
109             x[B[i]] = D[i][n + 1];
110
111     return D[m][n + 1];
112 }
113
114 } // Simplex

```

25 math/stuff.cpp

```

1const int M = 1e6;
2int phi[M];
3void calcPhi() {
4    for (int i = 1; i < M; ++i)
5        phi[i] = i;
6    for (int j = 1; j < M; ++j)
7        for (int i = 2 * j; i < M; i += j)
8            phi[i] -= phi[j];
9}
10int inv[M];
11void calcInv() {
12    inv[1] = 1;
13    for (int i = 2; i < M; ++i) {
14        inv[i] = mul(sub(0, mod / i), inv[mod % i]);
15        assert(mul(i, inv[i]) == 1);
16    }
17}
18int gcd(int a, int b, int &x, int &y) {
19    if (a == 0) {
20        x = 0, y = 1;
21        return b;
22    }
23    int x1, y1;
24    int g = gcd(b % a, a, x1, y1);
25    x = y1 - x1 * (b / a);
26    y = x1;
27    assert(a * x + b * y == g);
28    return g;
29}
30int crt(int mod1, int mod2, int rem1, int rem2) {
31    int r = (rem2 - (rem1 % mod2) + mod2) % mod2;
32    int x, y;
33    int g = gcd(mod1, mod2, x, y);
34    assert(r % g == 0);
35
36    x %= mod2;
37    if (x < 0)
38        x += mod2;
39
40    int ans = (x * (r / g)) % mod2;
41    ans = ans * mod1 + rem1;
42
43    assert(ans % mod1 == rem1);
44    assert(ans % mod2 == rem2);
45    return ans;
46}
47
48// primes to N
49const ll n = 1000000000000LL;
50const ll L = 1000000;
51int small[L+1];
52ll large[L+1];
53void calc_pi() {
54    for (int i = 1; i <= L; ++i) {
55        small[i] = i-1;
56        large[i] = n / i - 1;
57    }
58    for (ll p = 2; p <= L; ++p) {
59        if (small[p] == small[p-1]) continue;
60        int cntp = small[p-1];
61        ll p2 = p*p;
62        ll np = n / p;
63        for (int i = 1; i <= min(L, n / p2); ++i) {
64            ll x = np / i;
65            if (x <= L) {
66                large[i] -= small[x] - cntp;
67            } else {
68                large[i] -= large[p*i] - cntp;
69            }
70        }
71        for (int i = L; i >= p2; --i) {
72            small[i] -= small[i/p] - cntp;
73        }
74    }
75}
76ll pi(ll x) {
77    if (x > L) return small[n/x];
78    else return large[x];
79}
80
81int main() {
82    calcPhi();
83    assert(phi[30] == 1 * 2 * 4);
84    calcInv();
85    int x, y;
86    gcd(3, 5, x, y);
87    gcd(15, 10, x, y);
88    crt(15, 13, 2, 5);
89    crt(17, 3, 15, 2);
90    return 0;
91}

```

26 strings/automaton.cpp

```

1int t[maxn][26], lnk[maxn], len[maxn];
2int sz;
3int last;
4
5void init() {
6    sz = 3;
7    last = 1;
8    forn(i, 26) t[2][i] = 1;
9    len[2] = -1;
10   lnk[1] = 2;
11}
12
13void addchar(int c) {
14    int nlast = sz++;
15    len[nlast] = len[last] + 1;
16    int p = last;
17    for (; !t[p][c]; p = lnk[p]) {
18        t[p][c] = nlast;
19    }
20    int q = t[p][c];
21    if (len[p] + 1 == len[q]) {
22        lnk[nlast] = q;
23    } else {
24        int clone = sz++;
25        len[clone] = len[p] + 1;
26        lnk[clone] = lnk[q];
27        lnk[q] = lnk[nlast] = clone;
28        forn(i, 26) t[clone][i] = t[q][i];
29        for (; t[p][c] == q; p = lnk[p]) {
30            t[p][c] = clone;
31        }
32    }
33    last = nlast;
34}
35
36bool check(const string& s) {
37    int v = 1;
38    for (int c: s) {
39        c -= 'a';
40        if (!t[v][c]) return false;
41        v = t[v][c];
42    }
43    return true;
44}
45
46int main() {
47    string s;
48    cin >> s;
49    init();
50    for (int i: s) {
51        addchar(i-'a');
52    }
53    forn(i, s.length()) {
54        assert(check(s.substr(i)));
55    }
56    cout << sz << endl;
57    return 0;
58}

```

27 strings/duval_manacher.cpp

```

1/*
2  Строка простая, если строго меньше всех суффиксов <=>
3  наименьший циклический сдвиг - первый.
4  Декомпозиция Линдона - разбиение s на w1, w2, ... wk -
5  простые строки такие, что w1 >= w2 >= ... wk.
6*/
7int duval(string s) {
8  s += s; //remove this to find Lyndon decomposition of s
9  int n = s.size();
10 int i = 0;
11 int ans = 0;
12 //while (i < n) { //for Lyndon decomposition
13 while (i < n / 2) {
14   ans = i;
15   int j = i + 1, k = i;
16   while (j < n && s[k] <= s[j]) {
17     if (s[k] < s[j])
18       k = i;
19     else
20       ++k;
21     ++j;
22   }
23   while (i <= k) {
24     //s.substr(i, j - k) -
25     //next prime string of Lyndon decomposition
26     i += j - k;
27   }
28 }
29 return ans;
30}
31
32//actual odd length is (odd[i] * 2 - 1)
33//actual even length is (even[i] * 2)
34void manacher(const string &s, vi &odd, vi &even) {
35  int n = s.size();
36  odd.resize(n);
37  int c = -1, r = -1;
38  forn (i, n) {
39    int k = (r <= i ? 0 : min(odd[2 * c - i], r - i));
40    while (i + k < n && i - k >= 0 && s[i + k] == s[i - k])
41      ++k;
42    odd[i] = k;
43    if (i + k > r)
44      r = i + k, c = i;
45  }
46  c = -1, r = -1;
47  even.resize(n - 1);
48  forn (i, n - 1) {
49    int k = (r <= i ? 0 : min(even[2 * c - i], r - i));
50    while (i + k + 1 < n && i - k >= 0 &&
51           s[i + k + 1] == s[i - k])
52      ++k;
53    even[i] = k;
54    if (i + k > r)
55      c = i, r = i + k;
56  }
57}
58
59void test() {
60  vector<int> odd, even;
61  string s = "aaaabbbaaaaa";
62  manacher(s, odd, even);
63  for (int x: even)
64    cerr << x << ' ';
65  cerr << '\n';
66  for (int x: odd)
67    cerr << x << ' ';
68  cerr << '\n';
69  // 1 2 1 0 5 0 1 2 2 1
70  // 1 2 2 1 1 1 1 2 3 2 1
71}
72
73int main() {
74  cout << duval("ababcabab") << '\n'; // 5
75  test();
76}

```

28 strings/eertree.cpp

```

1#include <bits/stdc++.h>
2using namespace std;
3const int maxn = 5000100;
4const int inf = 1e9 + 1e5;
5
6char buf[maxn];
7char *s = buf + 1;
8int to[maxn][2];
9int suff[maxn];
10int len[maxn];
11int sz;
12int last;
13
14const int odd = 1;
15const int even = 2;
16const int blank = 3;
17
18inline void go(int &u, int pos) {
19  while (u != blank && s[pos - len[u] - 1] != s[pos])
20    u = suff[u];
21}
22
23void add_char(int pos) {
24  go(last, pos);
25  int u = suff[last];
26  go(u, pos);
27  int c = s[pos] - 'a';
28  if (!to[last][c]) {
29    to[last][c] = sz++;
30    len[sz - 1] = len[last] + 2;
31    assert(to[u][c]);
32    suff[sz - 1] = to[u][c];
33  }
34  last = to[last][c];
35}
36
37void init() {
38  sz = 4;
39  to[blank][0] = to[blank][1] = even;
40  len[blank] = suff[blank] = inf;
41  len[even] = 0, suff[even] = odd;
42  len[odd] = -1, suff[odd] = blank;
43  last = 2;
44}
45
46void build() {
47  init();
48  scanf("%s", s);
49  for (int i = 0; s[i]; ++i)
50    add_char(i);
51}

```

29 strings/suffix_array.cpp

```

1string s;
2int n;
3int sa[maxn], new_sa[maxn], cls[maxn], new_cls[maxn],
4    cnt[maxn], lcp[maxn];
5int n_cls;
6
7void build() {
8    n_cls = 256;
9    forn(i, n) {
10        sa[i] = i;
11        cls[i] = s[i];
12    }
13    for (int d = 0; d < n; d = d ? d*2 : 1) {
14
15        forn(i, n) new_sa[i] = (sa[i] - d + n) % n;
16        forn(i, n_cls) cnt[i] = 0;
17        forn(i, n) ++cnt[cls[i]];
18        forn(i, n_cls) cnt[i+1] += cnt[i];
19        for (int i = n-1; i >= 0; --i)
20            sa[--cnt[cls[new_sa[i]]]] = new_sa[i];
21
22        n_cls = 0;
23        forn(i, n) {
24            if (i && (cls[sa[i]] != cls[sa[i-1]] ||
25                cls[(sa[i]+d)%n] != cls[(sa[i-1]+d)%n])) {
26                ++n_cls;
27            }
28            new_cls[sa[i]] = n_cls;
29        }
30        ++n_cls;
31        forn(i, n) cls[i] = new_cls[i];
32    }
33
34    // cls is also a inv perm of sa if a string is not cyclic
35    // (i.e. a position of i-th lexicographical suffix)
36    int val = 0;
37    forn(i, n) {
38        if (val) --val;
39        if (cls[i] == n-1) continue;
40        int j = sa[cls[i] + 1];
41        while (i+val != n && j+val != n && s[i+val] == s[j+val])
42            ++val;
43        lcp[cls[i]] = val;
44    }
45}
46
47int main() {
48    cin >> s;
49    s += '$';
50    n = s.length();
51    build();
52    forn(i, n) {
53        cout << s.substr(sa[i]) << endl;
54        cout << lcp[i] << endl;
55    }
56}

```

30 strings/ukkonen.cpp

```

1string s;
2const int alpha = 26;
3
4namespace SuffixTree {
5    struct Node {
6        Node *to[alpha];
7        Node *lnk, *par;
8        int l, r;
9
10        Node(int l, int r): l(l), r(r) {
11            memset(to, 0, sizeof(to));
12            lnk = par = 0;
13        }
14    };
15
16    Node *root, *blank, *cur;
17    int pos;
18
19    void init() {
20        root = new Node(0, 0);
21        blank = new Node(0, 0);
22        forn(i, alpha)
23            blank->to[i] = root;
24        root->lnk = root->par = blank->lnk = blank->par = blank;
25        cur = root;
26        pos = 0;
27    }
28
29    int at(int id) {
30        return s[id];
31    }
32
33    void goDown(int l, int r) {
34        if (l >= r)
35            return;
36        if (pos == cur->r) {
37            int c = at(l);
38            assert(cur->to[c]);
39            cur = cur->to[c];
40            pos = min(cur->r, cur->l + 1);
41            ++l;
42        } else {
43            int delta = min(r - l, cur->r - pos);
44            l += delta;
45            pos += delta;
46        }
47        goDown(l, r);
48    }
49
50    void goUp() {
51        if (pos == cur->r && cur->lnk) {
52            cur = cur->lnk;
53            pos = cur->r;
54            return;
55        }
56        int l = cur->l, r = pos;
57        cur = cur->par->lnk;
58        pos = cur->r;
59        goDown(l, r);
60    }
61
62    void setParent(Node *a, Node *b) {
63        assert(a);
64        a->par = b;
65        if (b)
66            b->to[at(a->l)] = a;
67    }
68
69    void addLeaf(int id) {
70        Node *x = new Node(id, inf);
71        setParent(x, cur);
72    }
73
74    void splitNode() {
75        assert(pos != cur->r);
76        Node *mid = new Node(cur->l, pos);
77        setParent(mid, cur->par);
78        cur->l = pos;
79        setParent(cur, mid);
80        cur = mid;
81    }
82
83    bool canGo(int c) {
84        if (pos == cur->r)
85            return cur->to[c];
86        return at(pos) == c;
87    }
88
89    void fixLink(Node *&bad, Node *newBad) {
90        if (bad)
91            bad->lnk = cur;

```

31 structures/centroids.cpp

```

92     bad = newBad;
93 }
94
95 void addCharOnPos(int id) {
96     Node *bad = 0;
97     while (!canGo(at(id))) {
98         if (cur->r != pos) {
99             splitNode();
100             fixLink(bad, cur);
101             bad = cur;
102         } else {
103             fixLink(bad, 0);
104         }
105         addLeaf(id);
106         goUp();
107     }
108     fixLink(bad, 0);
109     goDown(id, id + 1);
110 }
111
112 int cnt(Node *u, int ml) {
113     if (!u)
114         return 0;
115     int res = min(ml, u->r) - u->l;
116     forn (i, alpha)
117         res += cnt(u->to[i], ml);
118     return res;
119 }
120
121 void build(int l) {
122     init();
123     forn (i, l)
124         addCharOnPos(i);
125 }
126};

```

```

1const int maxn = 100100;
2const int LG = 18; //2*maxn <= 2^LG
3
4vector<int> g[LG][maxn];
5int rt[LG][maxn];
6int from[LG][maxn];
7
8namespace Cenroids {
9
10int D;
11int cnt[maxn];
12int CENTER, BOUND;
13
14void pre(int u, int prev = -1) {
15     cnt[u] = 1;
16     for (int v: g[D][u]) {
17         if (v == prev)
18             continue;
19         pre(v, u);
20         cnt[u] += cnt[v];
21     }
22}
23
24void findCenter(int u, int prev = -1, int up = 0) {
25     int worst = up;
26     for (int v: g[D][u]) {
27         if (v == prev)
28             continue;
29         findCenter(v, u, up + cnt[u] - cnt[v]);
30         worst = max(worst, cnt[v]);
31     }
32     if (worst <= BOUND)
33         CENTER = u;
34}
35
36void markAll(int u, int prev = -1, int subtree = -1) {
37     rt[D][u] = CENTER;
38     from[D][u] = subtree;
39     for (int v: g[D][u]) {
40         if (v == prev)
41             continue;
42         g[D + 1][u].push_back(v);
43         g[D + 1][v].push_back(u);
44         if (subtree == -1)
45             markAll(v, u, v);
46         else
47             markAll(v, u, subtree);
48     }
49}
50
51void decompose(int u, int depth = 0) {
52     D = depth;
53     pre(u);
54     CENTER = -1, BOUND = cnt[u] / 2;
55     findCenter(u);
56     assert(CENTER != -1);
57     markAll(u);
58     u = CENTER;
59     D = depth + 1;
60     for (int v: g[D][u]) {
61         auto it = find(g[D][v].begin(), g[D][v].end(), u);
62         assert(it != g[D][v].end());
63         g[D][v].erase(it);
64     }
65     for (int v: g[D][u])
66         decompose(v, depth + 1);
67}
68
69};

```

32 structures/heavy_light.cpp

```

1const int maxn = 100500;
2const int maxd = 17;
3
4vector<int> g[maxn];
5
6struct Tree {
7    vector<int> t;
8    int base;
9
10    Tree(): base(0) {
11    }
12
13    Tree(int n) {
14        base = 1;
15        while (base < n)
16            base *= 2;
17        t = vector<int>(base * 2, 0);
18    }
19
20    void put(int v, int delta) {
21        assert(v < base);
22        v += base;
23        t[v] += delta;
24        while (v > 1) {
25            v /= 2;
26            t[v] = max(t[v * 2], t[v * 2 + 1]);
27        }
28    }
29
30    //Careful here: cr = 2 * maxn
31    int get(int l, int r, int v=1, int cl=0, int cr = 2*maxn) {
32        cr = min(cr, base);
33        if (l <= cl && cr <= r)
34            return t[v];
35        if (r <= cl || cr <= l)
36            return 0;
37        int cc = (cl + cr) / 2;
38        return max(get(l, r, v * 2, cl, cc),
39                  get(l, r, v * 2 + 1, cc, cr));
40    }
41};
42
43namespace HLD {
44    int h[maxn];
45    int timer;
46    int in[maxn], out[maxn], cnt[maxn];
47    int p[maxd][maxn];
48    int vroot[maxn];
49    int vpos[maxn];
50    int ROOT;
51    Tree tree[maxn];
52
53    void dfs1(int u, int prev) {
54        p[0][u] = prev;
55        in[u] = timer++;
56        cnt[u] = 1;
57        for (int v: g[u]) {
58            if (v == prev)
59                continue;
60            h[v] = h[u] + 1;
61            dfs1(v, u);
62            cnt[u] += cnt[v];
63        }
64        out[u] = timer;
65    }
66
67    int dfs2(int u, int prev) {
68        int to = -1;
69        for (int v: g[u]) {
70            if (v == prev)
71                continue;
72            if (to == -1 || cnt[v] > cnt[to])
73                to = v;
74        }
75        int len = 1;
76        for (int v: g[u]) {
77            if (v == prev)
78                continue;
79            if (to == v) {
80                vpos[v] = vpos[u] + 1;
81                vroot[v] = vroot[u];
82                len += dfs2(v, u);
83            }
84            else {
85                vroot[v] = v;
86                vpos[v] = 0;
87                dfs2(v, u);
88            }
89        }
90        if (vroot[u] == u)
91            tree[u] = Tree(len);
92
93            return len;
94        }
95
96    void init(int n) {
97        timer = 0;
98        h[ROOT] = 0;
99        dfs1(ROOT, ROOT);
100        for (d, maxd - 1)
101            for (i, n)
102                p[d + 1][i] = p[d][p[d][i]];
103        vroot[ROOT] = ROOT;
104        vpos[ROOT] = 0;
105        dfs2(ROOT, ROOT);
106        //WARNING: init all trees
107    }
108
109    bool isPrev(int u, int v) {
110        return in[u] <= in[v] && out[v] <= out[u];
111    }
112
113    int lca(int u, int v) {
114        for (int d = maxd - 1; d >= 0; --d)
115            if (!isPrev(p[d][u], v))
116                u = p[d][u];
117            if (!isPrev(u, v))
118                u = p[0][u];
119        return u;
120    }
121
122    //for each v: h[v] >= toh
123    int getv(int u, int toh) {
124        int res = 0;
125        while (h[u] >= toh) {
126            int rt = vroot[u];
127            int l = max(0, toh - h[rt]), r = vpos[u] + 1;
128            res = max(res, tree[rt].get(l, r));
129            if (rt == ROOT)
130                break;
131            u = p[0][rt];
132        }
133        return res;
134    }
135
136    int get(int u, int v) {
137        int w = lca(u, v);
138        return max(getv(u, h[w]), getv(v, h[w] + 1));
139    }
140
141    void put(int u, int val) {
142        int rt = vroot[u];
143        int pos = vpos[u];
144        tree[rt].put(pos, val);
145    }
146};

```


33 structures/linkcut.cpp

```

1 namespace LinkCut {
2
3 typedef struct _node {
4     _node *l, *r, *p, *pp;
5     int size; bool rev;
6     _node();
7
8     explicit _node(nullptr_t) {
9         l = r = p = pp = this;
10        size = rev = 0;
11    }
12
13    void push() {
14        if (rev) {
15            l->rev ^= 1; r->rev ^= 1;
16            rev = 0; swap(l,r);
17        }
18    }
19
20    void update();
21 }* node;
22
23 node None = new _node(nullptr);
24 node v2n[maxn];
25
26 _node::_node() {
27     l = r = p = pp = None;
28     size = 1; rev = false;
29 }
30
31 void _node::update() {
32     size = (this != None) + l->size + r->size;
33     l->p = r->p = this;
34 }
35
36 void rotate(node v) {
37     assert(v != None && v->p != None);
38     assert(!v->rev);
39     assert(!v->p->rev);
40     node u = v->p;
41     if (v == u->l)
42         u->l = v->r, v->r = u;
43     else
44         u->r = v->l, v->l = u;
45     swap(u->p, v->p);
46     swap(v->pp, u->pp);
47     if (v->p != None) {
48         assert(v->p->l == u || v->p->r == u);
49         if (v->p->r == u)
50             v->p->r = v;
51         else
52             v->p->l = v;
53     }
54     u->update();
55     v->update();
56 }
57
58 void bigRotate(node v) {
59     assert(v->p != None);
60     v->p->p->push();
61     v->p->push();
62     v->push();
63     if (v->p->p != None) {
64         if ((v->p->l == v) ^ (v->p->p->r == v->p))
65             rotate(v->p);
66         else
67             rotate(v);
68     }
69     rotate(v);
70 }
71
72 inline void splay(node v) {
73     while (v->p != None)
74         bigRotate(v);
75 }
76
77 inline void splitAfter(node v) {
78     v->push();
79     splay(v);
80     v->r->p = None;
81     v->r->pp = v;
82     v->r = None;
83     v->update();
84 }
85
86 void expose(int x) {
87     node v = v2n[x];
88     splitAfter(v);
89     while (v->pp != None) {
90         assert(v->p == None);
91         splitAfter(v->pp);
92         assert(v->pp->r == None);
93         assert(v->pp->p == None);
94         assert(!v->pp->rev);
95         v->pp->r = v;
96         v->pp->update();
97         v = v->pp;
98         v->r->pp = None;
99     }
100    assert(v->p == None);
101    splay(v2n[x]);
102 }
103
104 inline void makeRoot(int x) {
105     expose(x);
106     assert(v2n[x]->p == None);
107     assert(v2n[x]->pp == None);
108     assert(v2n[x]->r == None);
109     v2n[x]->rev ^= 1;
110 }
111
112 inline void link(int x, int y) {
113     makeRoot(x);
114     v2n[x]->pp = v2n[y];
115 }
116
117 inline void cut(int x, int y) {
118     expose(x);
119     splay(v2n[y]);
120     if (v2n[y]->pp != v2n[x]) {
121         swap(x,y);
122         expose(x);
123         splay(v2n[y]);
124         assert(v2n[y]->pp == v2n[x]);
125     }
126     v2n[y]->pp = None;
127 }
128
129 inline int get(int x, int y) {
130     if (x == y)
131         return 0;
132     makeRoot(x);
133     expose(y);
134     expose(x);
135     splay(v2n[y]);
136     if (v2n[y]->pp != v2n[x])
137         return -1;
138     return v2n[y]->size;
139 }
140
141 }

```

34 structures/ordered_set.cpp

```

1#include <ext/pb_ds/assoc_container.hpp>
2#include <ext/pb_ds/tree_policy.hpp>
3
4typedef __gnu_pbds::tree<int, __gnu_pbds::null_type,
5    std::less<int>,
6    __gnu_pbds::rb_tree_tag,
7    __gnu_pbds::tree_order_statistics_node_update> oset;
8
9#include <iostream>
10
11int main() {
12    oset X;
13    X.insert(1);
14    X.insert(2);
15    X.insert(4);
16    X.insert(8);
17    X.insert(16);
18
19    std::cout << *X.find_by_order(1) << std::endl; // 2
20    std::cout << *X.find_by_order(2) << std::endl; // 4
21    std::cout << *X.find_by_order(4) << std::endl; // 16
22    std::cout << std::boolalpha <<
23        (end(X)==X.find_by_order(6)) << std::endl; // true
24
25    std::cout << X.order_of_key(-5) << std::endl; // 0
26    std::cout << X.order_of_key(1) << std::endl; // 0
27    std::cout << X.order_of_key(3) << std::endl; // 2
28    std::cout << X.order_of_key(4) << std::endl; // 2
29    std::cout << X.order_of_key(400) << std::endl; // 5
30}

```

35 structures/treap.cpp

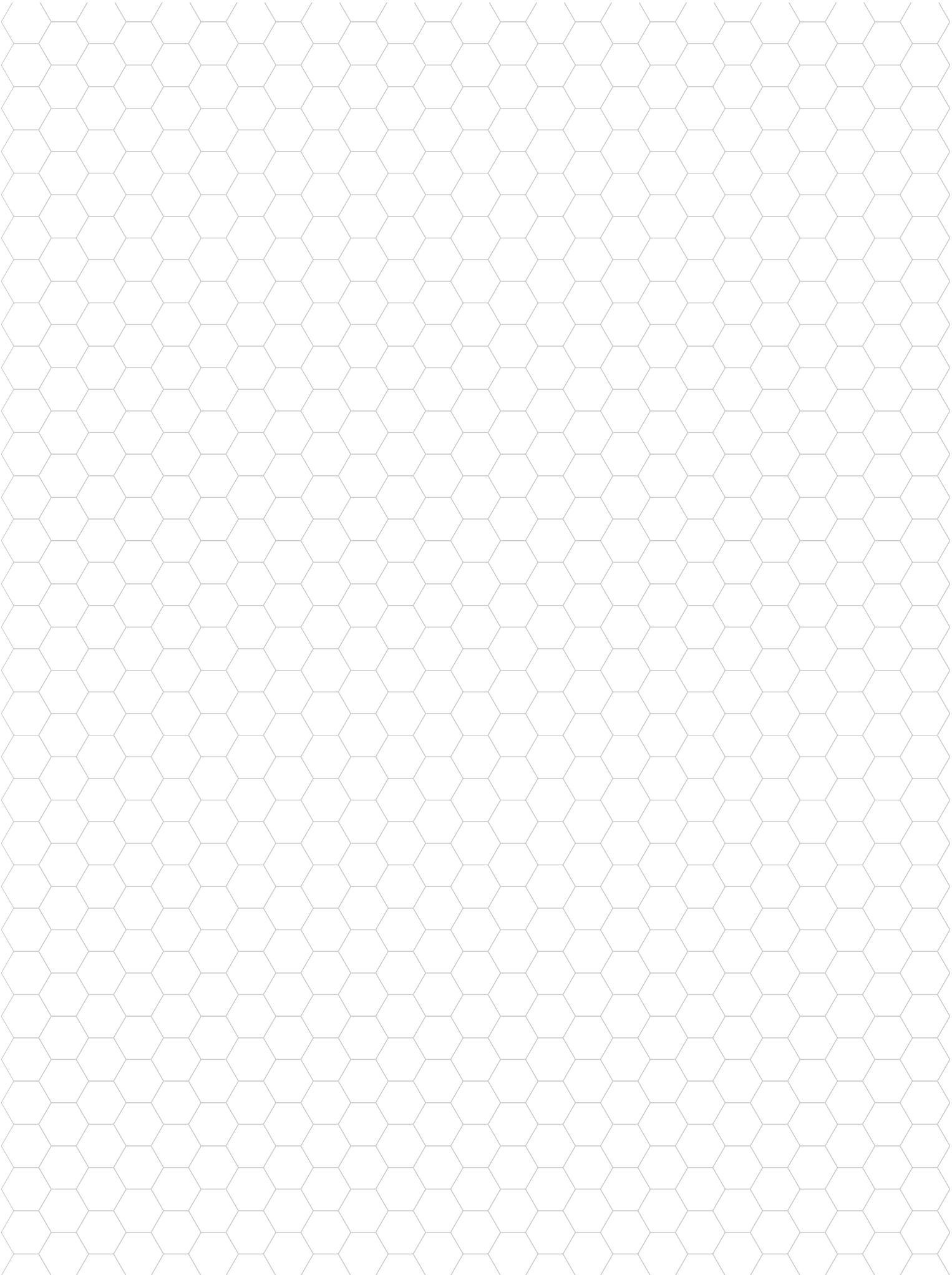
```

1struct node {
2    int x, y;
3    node *l, *r;
4    node(int x) : x(x), y(rand()), l(r=NULL) {}
5};
6
7void split(node *t, node *&l, node *&r, int x) {
8    if (!t) return (void)(l=r=NULL);
9    if (x <= t->x) {
10        split(t->l, l, t->l, x), r = t;
11    } else {
12        split(t->r, t->r, r, x), l = t;
13    }
14}
15
16node *merge(node *l, node *r) {
17    if (!l) return r;
18    if (!r) return l;
19    if (l->y > r->y) {
20        l->r = merge(l->r, r);
21        return l;
22    } else {
23        r->l = merge(l, r->l);
24        return r;
25    }
26}
27
28node *insert(node *t, node *n) {
29    node *l, *r;
30    split(t, l, r, n->x);
31    return merge(l, merge(n, r));
32}
33
34node *insert(node *t, int x) {
35    return insert(t, new node(x));
36}
37
38node *fast_insert(node *t, node *n) {
39    if (!t) return n;
40    node *root = t;
41    while (true) {
42        if (n->x < t->x) {
43            if (!t->l || t->l->y < n->y) {
44                split(t->l, n->l, n->r, n->x), t->l = n;
45                break;
46            } else {
47                t = t->l;
48            }
49        } else {
50            if (!t->r || t->r->y < n->y) {
51                split(t->r, n->l, n->r, n->x), t->r = n;
52                break;
53            } else {
54                t = t->r;
55            }
56        }
57    }
58    return root;
59}
60
61node *fast_insert(node *t, int x) {
62    return fast_insert(t, new node(x));
63}
64
65int main() {
66    node *t = NULL;
67    forn(i, 1000000) {
68        int x = rand();
69        t = fast_insert(t, x);
70    }
71}

```

36

Сеточка



37 Сеточка

