#### 1 Strategy.txt

```
Проверить руками сэмплы
Подумать как дебагать после написания
Выписать сложные формулы и все +-1
Проверить имена файлов
Прогнать сэмплы
Переполнения int, переполнения long long
Выход за границу массива: _GLIBCXX_DEBUG
Переполнения по модулю: в
псевдо-онлайн-генераторе, в функциях-обертках
Проверить мультитест на разных тестах
Прогнать минимальный по каждому параметру тест
Прогнать псевдо-максимальный тест(немного чисел,
 но очень большие или очень маленькие)
Представить что не зайдет и заранее написать
 assert'ы, прогнать слегка модифицированные тесты 22
cout.precision: в том числе в интерактивных
 задачах
Удалить debug-output, отсечения для тестов,
 вернуть оригинальный тахп, удалить
 _GLIBCXX_DEBUG
Вердикт может врать
Если много тестов (>3), дописать в конец каждого
 теста ответ, чтобы не забыть
(WA) Потестить не только ответ, но и содержимое
 значимых массивов, переменных
(WA) Изменить тест так, чтобы ответ не менялся:
поменять координаты местами, сжать/растянуть
 координаты, поменять ROOT дерева
(WA) Подвигать размер блока в корневой или
 битсете
(WA) Поставить assert'ы, возможно написать чекер
 c assert'om
(WA) Проверить, что программа не печатает
 что-либо неожиданное, что должно попадать под
 PE: inf - 2, не лекс. мин. решение, одинаковые
 числа вместо разных, неправильное количество
 чисел, пустой ответ, перечитать output format
(TL) cin -> scanf -> getchar
(TL) Упихать в кэш большие массивы, поменять
 местами for'ы или измерения массива
(RE) Проверить формулы на деление на 0, выход за
 область определения(sqrt(-eps), acos(1 + eps))
(WA) Проверить, что ответ влезает в int
```

## 2 flows/dinic.cpp

```
1namespace Dinic {
2const int maxn = 100100;
 3struct Edge {
       int to;
       11 c, f;
 6
       Edge(int to, 11 c): to(to), c(c), f(0) {}
 7};
 9vector<Edge> es;
10 vector<int> g[maxn];
11 int q[maxn], d[maxn], pos[maxn];
12 int N, S, T;
14 void addEdge(int u, int v, ll c) {
15
       g[u].push_back(sz(es));
       es.emplace_back(v, c);
16
17
       g[v].push_back(sz(es));
18
       es.emplace_back(u, 0);
19 }
20
21bool bfs() {
       fill(d, d + N, maxn);
       d[S] = 0, q[0] = S;
int rq = 1;
24
       forn (lq, rq) {
            int u = q[lq];
for (int id: g[u]) {
   if (es[id].c == es[id].f)
                      continue
                 int v = es[id].to;
                 if (d[v] == maxn) {
    d[v] = d[u] + 1;
31
                      q[rq++] = v;
33
35
            }
36
37
       return d[T] != maxn;
38}
39
4011 dfs(int u, ll curf) {
41    if (u == T)
            return curf;
42
43
       11 \text{ ret} = 0:
       for (int &i = pos[u]; i < sz(g[u]); ++i) {
44
45
            int id = g[u][i];
            int v = es[id].to;
46
            11 delta = min(curf, es[id].c - es[id].f);
47
            if (delta == 0 || d[v] != d[u] + 1)
48
                 continue:
49
            delta = dfs(v, delta);
curf -= delta;
50
51
            ret += delta;
52
            es[id].f += delta;
53
            es[id ^1].f =
54
                               delta;
            if (curf == 0)
55
56
                 return ret:
57
58
       return ret;
59 }
     dinic(int S, int T) {
6111
       Dinic::S = S, Dinic::T = T;
62
63
       11 \text{ res} = 0;
       while (bfs()) {
            fill(pos, pos + N, 0);
while (ll cur = dfs(S, infl))
65
66
67
                 res += cur;
68
69
       return res;
70}
71
72} // namespace Dinic
73
74 void test() {
       Dinic::N = 4;
75
       Dinic::addEdge(0, 1, 1);
       Dinic::addEdge(0, 2, 2);
       Dinic::addEdge(2, 1, 1);
       Dinic::addEdge(1, 3, 2);
       Dinic::addEdge(2, 3, 1);
       cout << Dinic::dinic(0, 3) << endl; // 3</pre>
82}
84 LR-поток находит не максимальный поток.
85 Добавим новый сток S' и исток T'. Заменим ребро (u, v, l, r)
86 LR-сети на ребра (u, T', l), (S', v, l), (u, v, r - l).
87 Добавим ребро (T, S, k). Ставим значение k=inf, пускаем поток.
88 Проверяем, что все ребра из S' насыщены (иначе ответ не
89 существует). Бинпоиском находим наименьшее к, что величина
90 потока не изменится. Это k - величина МИНИМАЛЬНОГО потока,
91 удовлетворяющего ограничениям. */
```

#### 3 flows/globalcut.cpp

```
1 #include <bits/stdc++.h>
2using namespace std;
7const int maxn = 505;
8namespace StoerWagner {
9int g[maxn] [maxn];
10 int dist[maxn];
11 bool used [maxn];
12 int n;
13
14void addEdge(int u, int v, int c) {
15     g[u][v] += c;
16     g[v][u] += c;
17}
18
19 int run() {
      vector<int> vertices;
20
21
      forn (i, n)
          vertices.push_back(i);
23
       int mincut = inf;
24
      while (vertices.size() > 1) {
25
           int u = vertices[0];
26
           for (auto v: vertices) {
               used[v] = false;
dist[v] = g[u][v];
27
28
29
30
           used[u] = true;
           forn (ii, vertices.size() - 2) {
31
               for (auto v: vertices)
32
33
                    if (!used[v])
34
                        if (used[u] || dist[v] > dist[u])
35
                            u = v;
36
               used[u] = true;
37
               for (auto v: vertices)
  if (!used[v])
38
                        dist[v] += g[u][v];
39
40
           int t = -1;
41
           for (auto v: vertices)
42
               if (!used[v])
43
           t = v;
assert(t != -1);
44
45
           mincut = min(mincut, dist[t]);
46
47
           vertices.erase(find(all(vertices), t));
48
           for (auto v: vertices)
               addEdge(u, v, g[v][t]);
49
50
51
      return mincut;
52 }
53}
    // namespace StoerWagner
54
55 int main() {
56
      StoerWagner::n = 4;
      StoerWagner::addEdge(0, 1, 5);
57
58
      StoerWagner::addEdge(2, 3, 5);
      StoerWagner::addEdge(1, 2, 4);
cerr << StoerWagner::run() << '\n'; // 4</pre>
59
60
```

61 }

# 4 flows/hungary.cpp

```
1// left half is the smaller one
 2namespace Hungary {
 3const int maxn = 505;
 4int a[maxn][maxn];
 5int p[2][maxn];
 6int match[maxn];
 7bool used[maxn];
 8int from[maxn];
9int mind[maxn];
10 int n, m;
11
12 int hungary(int v) {
13  used[v] = true;
       int u = match[v];
       int best = -1;
forn (i, m + 1) {
15
17
           if (used[i])
                continue;
           int nw = a[u][i] - p[0][u] - p[1][i];
if (nw <= mind[i]) {</pre>
19
20
21
                mind[i] = nw;
                from[i] = v;
22
           if (best == -1 || mind[best] > mind[i])
24
25
                best = i;
26
27
       v = best;
       int delta = mind[best];
28
29
       forn (i, m + 1) \{
           if (used[i]) {
30
                p[1][i] -= delta;
31
32
                p[0][match[i]] += delta;
33
           } else
                mind[i] -= delta;
34
35
       if (match[v] == -1)
36
37
           return v:
38
       return hungary(v);
39 }
40
41 void check() {
       int edges = 0, res = 0;
42
       forn (i, m)
43
           if (match[i] != -1) {
44
45
                ++edges;
                assert(p[0][match[i]] + p[1][i] == a[match[i]][i]);
46
47
                res += a[match[i]][i];
           } else
48
       assert(p[1][i] == 0);
assert(res == -p[1][m]);
49
50
       forn (i, n) forn (j, m)

assert(p[0][i] + p[1][j] <= a[i][j]);
51
52
53}
54
55 int run() {
       forn (i, n)
56
57
          p[0][i] = 0;
       forn (i, m + 1) {
   p[1][i] = 0;
58
59
           match[i] = -1;
60
61
62
       forn (i, n) {
63
           match[m] = i;
            fill(used, used + m + 1, false);
           fill(mind, mind + m + 1, inf);
fill(from, from + m + 1, -1);
65
66
67
            int v = hungary(m);
           while (v != m) {
    int w = from[v];
68
70
                match[v] = match[w];
71
                 v = w;
72
           }
       check();
       return -p[1][m];
77} // namespace Hungary
```

# 5 flows/mincost.cpp

pot[i] += dist[i];

```
return true;
                                                                               94}
1namespace MinCost {
2const ll infc = 1e12;
                                                                               95
                                                                               96bool push() {
                                                                                      //2 variants
                                                                               97
4struct Edge {
                                                                                       //if (!fordBellman())
       int to;
                                                                                      if (!dikstra())
6
      ll c, f, cost;
                                                                                          return false;
                                                                                      ++totalFlow;
8
      Edge(int to, 11 c, 11 cost): to(to), c(c), f(0), cost(cost)
                                                                                      int u = T;
9
                                                                                      while (u != S) {
10};
                                                                                          int e = fromEdge[u];
                                                                              104
11
                                                                              105
                                                                                           totalCost += edge[e].cost;
12 int N, S, T;
                                                                                          edge[e].f++;
edge[e ^ 1].f--;
                                                                              106
13 int totalFlow;
                                                                              107
1411 totalCost;
                                                                                           u = edge[e ^ 1].to;
                                                                              108
15 const int maxn = 505;
                                                                              109
16 vector < Edge > edge;
                                                                              110
                                                                                      return true;
17 vector<int> g[maxn];
                                                                              111}
                                                                              112
19 void addEdge(int u, int v, ll c, ll cost) {
                                                                              113 //min-cost-circulation
      g[u].push_back(edge.size());
                                                                              114ll d[maxn][maxn];
       edge.emplace_back(v, c, cost);
                                                                              115 int dfrom[maxn][maxn];
22
      g[v].push_back(edge.size());
                                                                              116 int level [maxn];
       edge.emplace_back(u, 0, -cost);
                                                                              117void circulation() {
24}
                                                                                      while (true) {
                                                                              118
                                                                                          int q = 0;
fill(d[0], d[0] + N, 0);
25
                                                                              119
2611 dist[maxn];
                                                                              120
27int fromEdge[maxn];
                                                                                           forn (iter, N) {
    fill(d[iter + 1], d[iter + 1] + N, infc);
                                                                              121
                                                                              122
29bool inQueue[maxn];
                                                                                               forn (u, N)
  for (int e: g[u]) {
    if (edge[e].c == edge[e].f)
                                                                              123
30bool fordBellman() {
                                                                              124
      forn (i, N)
                                                                              125
           dist[i] = infc;
32
                                                                              126
                                                                                                             continue;
      dist[S] = 0;
inQueue[S] = true;
33
                                                                                                         int v = edge[e].to;
ll ndist = d[iter][u] + edge[e].cost;
if (ndist >= d[iter + 1][v])
                                                                              127
34
                                                                              128
       vector<int> q;
35
                                                                              129
36
       q.push_back(S);
                                                                              130
                                                                                                              continue;
      for (int ii = 0; ii < int(q.size()); ++ii) {</pre>
37
                                                                                                         d[iter + 1][v] = ndist;
                                                                              131
           int u = q[ii];
inQueue[u] = false;
38
                                                                              132
                                                                                                         dfrom[iter + 1][v] = e;
39
                                                                                                    }
                                                                              133
           for (int e: g[u]) {
    if (edge[e].f == edge[e].c)
40
                                                                                               q ^= 1;
                                                                              134
41
                                                                              135
                                                                                          }
42
                     continue:
                                                                              136
                                                                                           int w = -1;
                int v = edge[e].to;
43
                                                                              137
                                                                                           ld mindmax = 1e18;
                11 nw = edge[e].cost + dist[u];
44
                                                                                           forn (u, N) {
                                                                              138
                if (nw >= dist[v])
45
                                                                              139
                                                                                               ld dmax = -1e18;
                     continue:
46
                                                                              140
                                                                                               forn (iter, N)
                dist[v] = nw;
47
                                                                                                    dmax = max(dmax,
                                                                              141
                fromEdge[v] = e;
48
                                                                              142
                                                                                                        (d[N][u] - d[iter][u]) / ld(N - iter));
                if (!inQueue[v]) {
49
                                                                                               if (mindmax > dmax)
    mindmax = dmax, w = u;
                                                                              143
50
                     inQueue[v] = true;
                                                                              144
                     q.push_back(v);
51
                                                                              145
                }
52
                                                                              146
                                                                                           if (mindmax >= 0)
           }
53
                                                                              147
54
                                                                              148
                                                                                           fill(level, level + N, -1);
      return dist[T] != infc;
55
                                                                                           int k = N;
                                                                              149
56 }
                                                                              150
                                                                                           while (level[w] == -1) {
57
                                                                                               level[w] = k;
                                                                              151
5811 pot[maxn];
                                                                                                w = edge[dfrom[k--][w] ^ 1].to;
                                                                              152
59bool dikstra() {
                                                                              153
       typedef pair<11, int> Pair;
                                                                                           int k2 = level[w];
61
       priority_queue<Pair, vector<Pair>, greater<Pair>> q;
                                                                                           ll delta = infc;
62
       forn (i, N)
                                                                                           while (k2 > k) {
                                                                              156
63
           dist[i] = infc;
                                                                                               int e = dfrom[k2--][w];
                                                                              157
64
       dist[S] = 0;
                                                                                                delta = min(delta, edge[e].c - edge[e].f);
                                                                              158
       q.emplace(dist[S], S);
65
                                                                                                w = edge[e ^ 1].to;
                                                                              159
       while (!q.empty()) {
66
                                                                              160
67
            int u = q.top().second;
                                                                              161
                                                                                           k2 = level[w];
68
           11 cdist = q.top().first;
                                                                                           while (k2 > k) {
                                                                              162
           q.pop();
69
                                                                                               int e = dfrom[k2--][w];
                                                                              163
70
           if (cdist != dist[u])
                                                                                                totalCost += edge[e].cost * delta;
                                                                              164
71
                continue;
                                                                                               edge[e].f += delta;
edge[e ^ 1].f -= delta;
                                                                              165
           for (int e: g[u]) {
   int v = edge[e].to;
72
                                                                              166
73
                                                                                                w = edge[e ^ 1].to;
                                                                              167
74
                if (edge[e].c == edge[e].f)
                                                                                           }
                                                                              168
75
                     continue;
                                                                                      }
                                                                              169
76
                11 w = edge[e].cost + pot[u] - pot[v];
                                                                              170}
                assert(w >= 0);
ll ndist = w + dist[u];
if (ndist >= dist[v])
77
                                                                              171} // namespace MinCost
78
                                                                              172
79
                                                                              173 int main() {
                     continue;
                                                                                      MinCost::N = 3, MinCost::S = 1, MinCost::T = 2;
MinCost::addEdge(1, 0, 3, 5);
MinCost::addEdge(0, 2, 4, 6);
                                                                              174
                dist[v] = ndist;
81
                                                                              175
                fromEdge[v] = e;
82
                                                                              176
83
                q.emplace(dist[v], v);
                                                                                      while (MinCost::push());
                                                                              177
84
                                                                                      cout << MinCost::totalFlow << ' '</pre>
                                                                              178
85
                                                                                           << MinCost::totalCost << '\n'; //3 33
                                                                              179
      if (dist[T] == infc)
86
                                                                              180 }
87
           return false;
88
       forn (i, N) {
           if (dist[i] == infc)
89
                continue;
```

# 6 flows/push relabel.cpp

```
1namespace PushRelabel {
 2 const int maxn = 200500;
 4struct Edge {
 5
       int to, c, f;
 6};
 7vector<Edge> edge;
10 vector<int> g[maxn];
1111 e[maxn];
12 int h[maxn];
13int onH[maxn];
14 int S, T;
15 int ptr[maxn];
16 int relabelTimer;
17
18void addEdge(int u, int v, int c) {
       g[u].push_back(sz(edge));
20
       edge.push_back({v, c, 0});
21
       g[v].push_back(sz(edge));
22
       edge.push_back({u, 0, 0});
23}
24
25void push(int id, int delta) {
26    int u = edge[id ^ 1].to;
27    int v = edge[id].to;
       edge[id].f += delta;
edge[id ^ 1].f -= delta;
28
30
       e[u] -= delta;
       e[v] += delta;
31
32}
33
34 void gap(int ch) {
35
       forn (u, n) {
36
           if (h[u] > ch)
                h[u] = max(h[u], n);
37
38
39}
40
41 int o[maxn];
42 void globalRelabeling() {
       int oc = 0;
43
       forn (i, n) {
    h[i] = n;
    onH[i] = 0;
44
45
46
47
       onH[0] = 1;
h[T] = 0;
48
49
       o[oc++] = T;
50
       forn (ii, oc) {
51
            int u = o[ii];
52
            for (int id: g[u]) {
   if (edge[id ^ 1].c == edge[id ^ 1].f)
53
54
                continue;
int v = edge[id].to;
if (h[v] != n)
55
56
57
                continue;
h[v] = h[u] + 1;
58
59
60
                 onH[h[v]]++;
61
                 o[oc++] = v;
            }
62
63
       }
64 }
65
66 void relabel(int u) {
67
       int oldh = h[u];
68
       int newh = inf;
69
       for (int id: g[u]) {
70
            if (edge[id].c == edge[id].f)
71
                 continue;
72
            newh = min(newh, h[edge[id].to] + 1);
73
74
       h[u] = newh;
       onH[oldh]--;
75
76
       onH[newh]++;
77
       if (onH[oldh] == 0)
            gap(oldh);
78
79
       if (++relabelTimer == n)
80
            globalRelabeling(), relabelTimer = 0;
81 }
83 void discharge(int u) {
       while (e[u] > 0) {
            int &i = ptr[u];
if (i == sz(g[u])) {
86
                i = 0;
87
                relabel(u);
89
                if (h[u] >= n)
                     break;
```

continue;

```
92
             } else {
 93
                  int id = g[u][i++];
                  int v = edge[id].to;
if (h[v] + 1 != h[u])
 94
 95
                       continue;
 97
                  int delta = min(e[u], ll(edge[id].c - edge[id].f));
                  push(id, delta);
 99
             }
        }
100
101 }
10311 flow(int _S, int _T) {
104    S = _S, T = _T;
105
        forn (i, n)
            ptr[i] = 0, e[i] = 0;
106
        for (int id: g[S]) {
   int delta = edge[id].c;
107
108
109
             push(id, delta);
110
        globalRelabeling();
111
112
        bool ok = false;
        while (!ok) {
113
             ok = true;
114
             forn (u, n) {
   if (h[u] < n && u != T && e[u] > 0)
115
116
                       discharge(u), ok = false;
117
118
        }
119
        return e[T];
120
121 }
122
123} //PushRelabel
```

# 7 geometry/chan.cpp

```
1mt19937 rr(111);
 21d rndEps() {
        return (ld(rr()) / rr.max() - 0.5) * 1e-7;
 4}
 6typedef tuple<int, int, int> Face;
 7 const ld infc = 1e100;
 9int n;
10pt p[maxn];
11
12 namespace Chan {
13pt _p[maxn];
14
15ld turny(int p1, int p2, int p3) {
16    return (p[p2].x - p[p1].x) * (p[p3].y - p[p1].y) -
17    (p[p3].x - p[p1].x) * (p[p2].y - p[p1].y);
18}
19
20//replace\ y\ with\ z
21ld turnz(int p1, int p2, int p3) {
22  return (p[p2].x - p[p1].x) * (p[p3].z - p[p1].z) -
23  (p[p3].x - p[p1].x) * (p[p2].z - p[p1].z);
24}
25
26ld gett(int p1, int p2, int p3) {
        if (p1 == -1 || p2 == -1 || p3 == -1)
             return infc;
        ld ty = turny(p1, p2, p3);
if (ty >= 0)
30
31
             return infc;
32
33
             return turnz(p1, p2, p3) / ty;
34}
35
36 void act(int i) {
        if (p[i].onHull) {
37
             p[p[i].nx].pr = p[i].pr;
p[p[i].pr].nx = p[i].nx;
38
39
40
        } else {
41
             p[p[i].nx].pr = p[p[i].pr].nx = i;
42
        p[i].onHull ^= 1;
43
44}
45
46ld updt(vector<int> &V) {
47
        if (V.empty())
48
            return infc;
        int id = V.back();
49
        if (p[id].onHull)
50
             return gett(p[id].pr, p[id].nx, id);
51
52
        else
             return gett(p[id].pr, id, p[id].nx);
53
54}
55
56 //builds lower hull
57vector<int> buildHull(int 1, int r) {
        if (1 + 1 >= r) {
    p[1].pr = p[1].nx = -1;
58
59
             p[1].onHull = true;
60
61
             return {};
62
63
        int mid = (1 + r) / 2;
        auto L = buildHull(1, mid);
auto R = buildHull(mid, r);
64
65
        reverse(all(L));
66
67
        reverse(all(R));
        int u = mid - 1, v = mid;
while (true) {
68
69
             if (p[u].pr != -1 &&
(turny(p[u].pr, u, v) <= 0))
70
71
             u = p[u].pr;
else if (p[v].nx != -1 &&
72
73
74
                        (turny(u, v, p[v].nx) <= 0))
75
                   v = p[v].nx;
76
             else
77
                  break;
78
79
        ld t[6];
        t[0] = updt(L);
t[1] = updt(R);
81
82
        vector<int> A;
83
        while (true) {
             t[2] = gett(p[u].pr, v, u);
t[3] = gett(u, p[u].nx, v);
t[4] = gett(u, p[v].pr, v);
t[5] = gett(u, p[v].nx, v);
86
87
             ld nt = infc;
89
             int type = -1;
             forn (i, 6)
```

```
92
                    if (t[i] < nt)
                         nt = t[i], type = i;
               if (nt >= infc)
 94
 95
                    break;
 97
               if (type == 0) {
                    act(L.back());
if (L.back() < u)
 99
100
                         A.push_back(L.back());
               L.pop_back();
t[0] = updt(L);
} else if (type == 1) {
101
103
                    act(R.back());
104
105
                     if (R.back() > v)
                         A.push_back(R.back());
106
              R.pop_back();
t[1] = updt(R);
} else if (type == 2) {
107
108
109
                    A.push_back(u);
110
              u = p[u].pr;
} else if (type == 3) {
111
112
               A.push_back(u = p[u].nx);
} else if (type == 4) {
113
114
              A.push_back(v = p[v].pr);
} else if (type == 5) {
115
116
                    A.push_back(v);
117
                    v = p[v].nx;
118
119
120
         assert(L.empty() && R.empty());
121
122
         p[u].nx = v, p[v].pr = u;
for (int i = u + 1; i < v; ++i)
    p[i].onHull = false;
for (int i = sz(A) - 1; i >= 0; --i) {
123
124
125
126
              int id = A[i];
if (id <= u || id >= v) {
    if (u == id)
127
128
129
                    u = p[u].pr;
if (v == id)
v = p[v].nx;
130
131
132
                    act(id);
133
134
               } else {
135
                    p[id].pr = u, p[id].nx = v;
136
                     act(id);
137
                    if (id >= mid)
138
                         v = id;
139
                    else
140
                          u = id;
141
              }
         }
142
143
         return A;
144}
145
146//faces are oriented ccw if look from the outside
147 vector < Face > getFaces() {
         forn (i, n) {
148
              _p[i] = p[i];
p[i].x += rndEps();
p[i].y += rndEps();
149
150
151
               p[i].z += rndEps();
152
               p[i].id = i;
153
154
155
          sort(p, p + n, [](const pt &a, const pt &b) {
156
                         return a.x < b.x;
                    });
157
          vector<Face> faces;
158
          forn (q, 2) {
159
               auto movie = buildHull(0, n);
160
               for (int x: movie) {
161
                    int id = p[x].id;
int pid = p[p[x].pr].id;
int nid = p[p[x].nx].id;
if (!p[x].onHull)
162
163
164
165
166
                         faces.emplace_back(pid, id, nid);
                    else
  faces.emplace_back(pid, nid, id);
167
168
169
                    act(x);
170
               }
               forn (i, n) {
171
                    p[i].y *= -1;
p[i].z *= -1;
172
173
              }
174
175
         forn (i, n)
p[i] = _p[i];
176
177
         return faces;
178
179}
180
181} //namespace Chan
```

52 }

### 8 geometry/convex hull trick.cpp

```
1struct Hull {
      vector<pt> top, bot;
 3
       //check: add points in strictly increasing order
 5
       void append(pt p) {
           while (sz(bot) > 1 && (p - bot.back()) %
                        (p - *next(bot.rbegin())) >= -eps)
               bot.pop_back();
           bot.push_back(p);
           while (sz(top) > 1 && (p - top.back()) %
10
                         (p - *next(top.rbegin())) <= eps)</pre>
11
               top.pop_back();
12
13
           top.push_back(p);
      }
14
15
      pt mostDistant(pt dir) {
16
           dir = dir.rot();
auto &v = dir.x < 0 ? top : bot;</pre>
17
18
           int 1 = -1, r = sz(v) - 1;
while (1 + 1 < r) {
19
20
21
               int c = (1 + r) / 2;
                if (dir \% (v[c + 1] - v[c]) > 0)
22
23
                   r = c;
24
               else
25
                    1 = c;
26
27
           return v[r];
28
29 }:
```

# 9 geometry/halfplanes.cpp

```
4
            + c.c * (a.v % b.v);
5}
7//check: bounding box is included
8vector<pt> halfplanesIntersection(vector<line> 1) {
      sort(all(1), cmpLine); //the strongest constraint is first
      1.erase(unique(all(1), eqLine), 1.end());
11
      int n = sz(1);
      vi st;
13
      forn (iter, 2)
          forn (i, n) {
15
               while (sz(st) > 1) {
                   int j = st.back(), k = *next(st.rbegin());
17
                   if (1[k].v % 1[i].v <= eps ||
                            det3x3(1[k], 1[j], 1[i]) \le eps)
19
                   st.pop_back();
20
21
               }
               st.push_back(i);
          }
24
      vi pos(n, -1);
bool ok = false;
25
26
      forn (i, sz(st)) {
    int id = st[i];
27
28
29
          if (pos[id] != -1) {
               st = vi(st.begin() + pos[id], st.begin() + i);
30
               ok = true;
31
32
               break:
33
          } else
               pos[id] = i;
34
35
      if (!ok)
36
          return {};
37
38
39
      vector<pt> res;
      pt M{0, 0};
int k = sz(st);
40
41
      forn (i, k) {
    line l1 = l[st[i]], l2 = l[st[(i + 1) % k]];
42
43
          res.push_back(linesIntersection(11, 12));
44
45
          M = M + res.back();
46
      M = M * (1. / k);
for (int id: st)
47
48
          if (1[id].signedDist(M) < -eps)</pre>
49
50
               return {};
51
      return res;
```

# 10 geometry/nd convex hull.cpp

```
1const int DIM = 4;
2typedef array<11, DIM> pt;
 3pt operator-(const pt &a, const pt &b) {
       pt res;
       forn (i, DIM)
 6
           res[i] = a[i] - b[i];
       return res;
 8}
9typedef array<pt, DIM-1> Edge;
10typedef array<pt, DIM> Face;
11 vector < Face > faces;
1311 det(pt *a) {
14
       int p[DIM];
       iota(p, p + DIM, 0);
15
                = 0;
16
       ll res
17
18
            11 x = 1;
            forn (i, DIM) {
19
20
                 forn (j, i)
21
                     if (p[j] > p[i])
22
                 x *= a[i][p[i]];
24
            }
25
            res += x:
26
       } while (next_permutation(p, p + DIM));
27
       return res;
28}
3011 V(Face f, pt pivot) {
       pt p[DIM];
31
       forn (i, DIM)
p[i] = f[i] - pivot;
32
33
34
       return det(p);
35 }
36
37 void init(vector<pt> p) {
38  forn (i, DIM+1) {
39
           Face a;
            int q = 0;
forn (j, DIM+1)
    if (j != i)
40
41
42
                     a[q++] = p[j];
43
            11 v = V(a, p[i]);
44
45
            assert(v != \bar{0});
            if (v < 0)
46
                 swap(a[0], a[1]);
47
48
            faces.push_back(a);
49
50 }
51
52 void add(pt p) {
       vector<Face> newf, bad;
for (auto f: faces) {
53
54
            if (V(f, p) < 0)
55
                 bad.push_back(f);
56
57
58
                 newf.push_back(f);
59
60
       if (bad.empty()) {
61
            return;
62
63
       vector<pair<Edge, pt>> edges;
for (auto f: bad) {
64
65
66
            sort(all(f));
67
            forn (i, DIM) {
                 Edge e;
int q = 0;
68
69
                 forn (j, DIM)
if (i != j)
70
71
                           e[q++] = f[j];
72
73
                 edges.emplace_back(e, f[i]);
74
            }
75
76
       sort(all(edges));
77
       forn (i, sz(edges)) {
78
            if (i + 1 < sz(edges) &&
79
                           edges[i + 1].first == edges[i].first) {
81
                 continue;
83
            Face f;
            forn (j, DIM-1)
                 f[j] = edges[i].first[j];
            f[DIM-1] = p;
            if (V(f, edges[i].second) < 0)
    swap(f[0], f[1]);</pre>
87
89
            faces.push_back(f);
```

# 11 geometry/planar faces.cpp

```
lint m, n; // segs, points
2pair<pt, pt> segs[maxn];
 3pt p[maxn], from, to;
 4map<pt, int> shr;
 5vi e[maxn]; // points adjacent to point
 6int getPoint(pt x) {
       if (shr.count(x)) return shr[x];
       p[n] = x;
 8
       return shr[x] = n++;
10}
11// segIntersection: {bool, point}, true iff exactly one point
12 void genIntersections() {
13
       forn(i, m) {
14
            getPoint(segs[i].fi);
15
            getPoint(segs[i].se);
            forn(j, i) {
16
17
                 auto t = segmentsIntersection(
18
                      segs[i].fi, segs[i].se, segs[j].fi, segs[j].se);
                 if (t.fi) getPoint(t.se);
19
            }
20
       }
21
22}
24 void genGraph() {
       forn(i, m) {
25
26
            vi pts;
            forn(j, n) if (pointInsideSegment(
                           p[j], segs[i].fi, segs[i].se)) {
28
                 pts.push_back(j);
30
            sort(all(pts), [](int i, int j) {
    return p[i] < p[j]; });
forn(j, pts.size() - 1) {
    int u = pts[j], v = pts[j+1];</pre>
31
32
33
                 e[u].push_back(v);
35
36
                 e[v].push_back(u);
37
38
       forn(i, n) {
39
            sort(all(e[i]), [i](int x, int y) {
   pt a = p[x] - p[i];
   pt b = p[y] - p[i];
   if (a.right() != b.right()) return a.right();
40
41
42
43
                 return a^{"}, b > 0;
44
45
            }):
       }
46
47 }
48
49 vector<pt> faces[maxn];
50 bool inner [maxn];
51 int nf;
52 map<pii, int> faceForEdge;
53 vi ef[maxn]; // graph on faces
54
55 void genFaces() {
       forn(i, n) for (int to: e[i]) {
   if (faceForEdge.count({i, to})) continue;
56
57
            int f = nf++;
int v = i, u = to;
58
59
60
                 faces[f].push_back(p[v]);
61
62
                 faceForEdge[{v, u}] = f;
63
                 auto it = lower_bound(all(e[u]), v,
                       [u] (int x, int y) {
                           pt a = p[x] - p[u];
pt b = p[y] - p[u];
65
66
67
                           if (a.right()!=b.right()) return a.right();
68
                           return a % b > 0;
69
70
                 assert(*it == v);
71
                 if (it == e[u].begin()) it = e[u].end();
                 v = u;
u = *--it;
72
73
74
            } while (v != i || u != to);
75
       forn(i, nf) {
            forn(j, faces[i].size()) {
                 s += faces[i][j] % faces[i][(j+1)%faces[i].size()];
            inner[i] = gt(s, 0);
       forn(v, n) for (int to: e[v]) {
            int f1 = faceForEdge[{v, to}];
            int f2 = faceForEdge[{to, v}];
            if (f1 != f2) {
                 ef[f1].push_back(f2);
87
                 ef[f2].push_back(f1);
89
       }
90
```

#### 12 geometry/polygon.cpp

```
1bool pointInsidePolygon(pt a, pt *p, int n) {
 2
       double sumAng = 0;
 3
       forn (i, n) {
 4
            pt A = p[i], B = p[(i + 1) \% n];
 5
            if (pointInsideSegment(a, A, B))
                 return true;
 7
            sumAng += atan2((A - a) \% (B - a), (A - a) * (B - a));
 8
 9
       return fabs(sumAng) > 1;
10}
11
12//check: p is oriented ccw
13bool segmentInsidePolygon(pt a, pt b, pt *p, int n) {
       if (!pointInsidePolygon((a + b) * .5, p, n))
            return false;
       if (ze((a - b).abs()))
17
           return true;
       forn (i, n) {
            pt c = p[i];
19
            if (ze((a - c) % (b - c)) && (a - c) * (b - c) < -eps) {
20
21
                 //point inside interval
23
                pt pr = p[(i + n - 1) \% n];
                pt nx = p[(i + 1) % n];
if ((c - pr) % (nx - c) > eps)
24
25
                     return false;
26
                ld s1 = (pr - a) % (b - a);
ld s2 = (nx - a) % (b - a);
27
28
                 if ((s1 > eps |\cdot| s2 > eps) &&
29
                          (s1 < -eps || s2 < -eps))
30
31
                     return false;
32
33
            //interval intersection
            pt d = p[(i + 1) % n];
ld s1 = (a - c) % (d - c);
ld s2 = (b - c) % (d - c);
34
35
36
            if (s1 >= -eps && s2 >= -eps)
37
38
                continue;
            if (s1 <= eps && s2 <= eps)
39
                 continue:
40
41
            s1 = (c - a) \% (b - a);

s2 = (d - a) \% (b - a);
42
43
            if (s1 >= -eps && s2 >= -eps)
44
                 continue;
45
            if (s1 <= eps && s2 <= eps)
46
47
                 continue;
48
49
            return false;
50
51
       return true;
52 }
```

# 13 geometry/polygon tangents.cpp

```
1struct Cmp {
       pt M, v0;
       bool operator()(const pt &a, const pt &b) {
  pt va{v0 * (a - M), v0 % (a - M)};
  pt vb{v0 * (b - M), v0 % (b - M)};
            return cmpAngle(va, vb);
 9};
10
11struct Hull {
12
       vector<pt> h;
13
       int n;
14
       void build() {
15
            sort(all(h));
16
            h.erase(unique(all(h)), h.end());
17
            vector<pt> top, bot;
for (auto p: h) {
18
19
                 while (sz(bot) > 1 && (p - bot.back()) %
20
                           (p - *next(bot.rbegin())) >= -eps)
21
                      bot.pop_back();
22
                 bot.push_back(p);
while (sz(top) > 1 && (p - top.back()) %
23
24
                           (p - *next(top.rbegin())) <= eps)</pre>
25
                      top.pop_back();
26
27
                 top.push_back(p);
            }
28
            if (sz(top))
29
                 top.pop_back();
30
            reverse(all(top));
31
32
            if (sz(top))
33
                top.pop_back();
            h = bot;
34
            h.insert(h.end(), all(top));
35
36
            n = sz(h);
       }
37
38
       bool visSide(pt a, int i) {
    return (h[(i + 1) % n] - a) % (h[i % n] - a) > eps;
39
40
41
42
43
       bool vis(pt a, int i) {
            return visSide(a, i) || visSide(a, i + n - 1);
44
       }
45
46
47
       bool isTangent(pt a, int i) {
48
            return visSide(a, i) != visSide(a, i + n - 1);
49
50
       int binSearch(int 1, int r, pt a) {
52
            //tricky binsearch; l <
                                          r not necessarily
            while (abs(1 - r) > 1) {
53
54
                 int c = (1 + r) / 2;
                 if (vis(a, c))
55
                      1 = c;
56
                 else
57
                      r = c;
            }
            assert(isTangent(a, 1));
60
61
            return 1 % n;
62
63
       //check: n >= 3
       pair<int, int> tangents(pt a) {
65
            assert(n >= 3);
66
            pt M = (h[0] + h[1] + h[2]) * (1. / 3);
67
            if (a == M)
68
            return {-1, -1};
Cmp cmp{M, h[0] - M};
69
70
            //assert(is_sorted(all(h), cmp));
71
            int pos = upper_bound(all(h), a, cmp) - h.begin();
pt L = h[(pos + n - 1) % n], R = h[pos % n];
if ((R - L) % (a - L) >= -eps)
72
73
74
                return {-1, -1}; //point inside hull
75
            int pos2 = upper_bound(all(h), M*2-a, cmp) - h.begin();
76
            assert(pos % n != pos2 % n);
77
            if (pos > pos2)
pos2 += n;
78
79
            return {binSearch(pos, pos2, a),
binSearch(pos + n - 1, pos2 - 1, a)};
80
81
       }
82
83 }:
```

# 14 geometry/primitives.cpp

```
1struct line {
        ld c; // v * p = c
         //check: p1 != p2
        line(pt p1, pt p2) {
    v = (p2 - p1).rot();
    v = v * (1. / v.abs());
 8
             c = v * p1;
 9
10
11
12
        // Convert from ax + by + c = 0
13
14
         //check: a^2+b^2 > 0
15
        line(ld a, ld b, ld _c): v(pt{a, b}), c(-_c) {
             ld d = v.abs();
16
             v = v * (1. / d);
17
18
             c /= d;
19
20
         //check: v.abs() == 1
22
        ld signedDist(pt p) {
23
             return v * p - c;
24
25};
26
27 //check: a != b
28pt lineProjection(pt p, pt a, pt b) {
29    pt v = (b - a).rot();
        ld s = (p - a) % (b - a);
30
        return p + v * (s / v.abs2());
31
32}
33
341d pointSegmentDist(pt p, pt a, pt b) {
35    if ((p - a) * (b - a) <= 0 || ze((b - a).abs()))
36    return (p - a).abs();
37    if ((p - b) * (a - b) <= 0)
        return (p - b).abs();
return fabsl((p - a) % (p - b)) / (b - a).abs();
38
39
40 }
41
42pt linesIntersection(line 11, line 12) {
43    ld d = 11.v.x * 12.v.y - 11.v.y * 12.v.x;
        if (ze(d)) {
44
             if (eq(11.c, 12.c)) {
//stub: equal lines
45
46
47
             } else {
48
                   //stub: empty intersection
49
50
             return pt{1e18, 1e18};
51
        ld dx = 11.c * 12.v.y - 11.v.y * 12.c;
ld dy = 11.v.x * 12.c - 11.c * 12.v.x;
return pt{dx / d, dy / d};
52
53
54
55 }
56
57pt linesIntersection(pt a, pt b, pt c, pt d) {
58    ld s = (b - a) % (d - c);
        if (ze(s)) {
59
60
              //stub: parallel or equal lines
61
             return pt{1e18, 1e18};
62
        ld s1 = (c - a) \% (d - a);
63
64
        return a + (b - a) * (s1 / s);
65}
66
67bool pointInsideSegment(pt p, pt a, pt b) {
        if (!ze((p - a) \% (p - b)))
69
             return false;
        ld prod = (a - p) * (b - p);
return ze(prod) || prod < 0;</pre>
70
71
72
        if (ze(prod)) {
73
              //stub: coincides with segment end
74
             return true;
75
76
        return prod < 0;</pre>
77}
78
79bool checkSegmentIntersection(pt a, pt b, pt c, pt d) {
        if (ze((a - b) % (c - d))) {
              if (pointInsideSegment(a, c, d) ||
                  pointInsideSegment(b, c, d) || pointInsideSegment(c, a, b) ||
                   pointInsideSegment(d, a, b)) {
                   //stub: intersection of parallel segments
86
                   return true;
87
88
             return false;
89
        forn (iter, 2) {
```

```
s1 = (c - a) \% (b - a);

s2 = (d - a) \% (b - a);
              if (s1 > eps && s2 > eps)
                  return false;
 95
              if (s1 < -eps && s2 < -eps)
                  return false;
 97
              swap(a, c), swap(b, d);
 99
100
        return true;
101 }
103vector<pt> lineCircleIntersection(line 1, pt a, ld r) {
        ld d = 1.signedDist(a);
104
105
         pt h = a - 1.v * d;
         if (eq(fabsl(d), r))
107
             return {h};
108
         else if (fabsl(d) > r)
109
            return {};
        pt w = 1.v.rot() * Sqrt(sqr(r) - sqr(d));
110
        return \{h + w, h - w\};
111
112 }
113
114vector<pt> circlesIntersction(pt a, ld r1, pt b, ld r2) {
        ld d = (a - b).abs();
115
         if (ze(d) && eq(r1, r2)) {
116
              //stub: equal circles
117
             return {};
118
119
        // intersection is non-empty iff
120
         // triangle with sides r1, r2, d exists
121
        ld per = r1 + r2 + d;
122
        1d mx = max(max(r1, r2), d);
123
        int num = 2;
if (eq(mx * 2, per)) {
    num = 1;
}
124
125
126
127
        } else if (mx * 2 > per)
128
             return {};
        ld part = (sqr(r1) + sqr(d) - sqr(r2)) / ld(2 * d);
pt h = a + (b - a) * (part / d);
if (num == 1)
129
130
131
132
             return {h};
        ld dh = Sqrt(sqr(r1) - sqr(part));
pt w = ((b - a) * (dh / d)).rot();
return {h + w, h - w};
133
134
135
136 }
137
138 vector p circleTangents(pt p, pt a, ld r) { 139    ld d = p a.abs();
140
         if (eq(r, d))
        return {p};
else if (r > d)
141
142
143
             return {};
144
         ld len = Sqrt(sqr(d) - sqr(r));
        vector<pt> res;
pt vec = (a - p) * (len / sqr(d));
for (int sgn: {-1, 1})
145
146
147
             res.push_back(p + vec.rotCw(pt{len, r * sgn}));
148
149
150}
151
152 vector < line > circles Bitangents (pt a, ld r1, pt b, ld r2) {
         1d d = (a - b).abs();
153
154
         if (ze(d) && eq(r1, r2)) {
              //stub: equal circles
155
             return {};
156
157
158
159
         vector<line> res;
        for (int s1: {-1, 1})
for (int s2: {-1, 1}) {
160
161
                 // inner tangent iff s1 != s2
// treat radii as signed
162
163
                  1d r = s2 * r2 - s1 * r1;
164
                  if (eq(fabsl(r), d)) {
165
166
                            incident tangents; need only one copy
                       if (s1 == 1)
167
                            continue;
168
                  } else if (fabsl(r) > d)
169
170
                       continue;
                  ld len = Sqrt(sqr(d) - sqr(r));
171
                  line l(a, a + (b - a).rotCw(pt{len, r}));
l.c -= s1 * r1;
172
173
174
                  res.push_back(1);
             }
175
176
        return res:
177 }
```

# 15 geometry/svg.cpp

```
1struct SVG {
 3
       FILE *out;
 4
       ld sc = 50;
 5
       void open() {
 7
            out = fopen("image.svg", "w");
            fprintf(out, "<svg xmlns='http://www.w3.org/2000/svg'</pre>
 8
              \rightarrow viewBox='-1000 -1000 2000 2000'>\n");
 9
10
       void line(pt a, pt b) {
   a = a * sc, b = b * sc;
   fprintf(out, "<line x1='%Lf' y1='%Lf' x2='%Lf' y2='%Lf'</pre>
11
12

    stroke='black'/>\n", a.x, -a.y, b.x, -b.y);

14
15
       void circle(pt a, ld r = -1, string col = "red") {
16
           r = (r = -1 ? 10 : sc * r);
17
            a = a * sc;
18
19
           fprintf(out, "<circle cx='%Lf' cy='%Lf' r='%Lf'</pre>
             \hookrightarrow fill='%s'/>\n", a.x, -a.y, r, col.c_str());
20
21
22
       void text(pt a, string s) {
23
            a = a * sc;
           fprintf(out, "<text x='%Lf' y='%Lf'</pre>
24
            → font-size='10px'>%s</text>\n", a.x, -a.y,
→ s.c_str());
25
26
27
       void close() {
28
           fprintf(out, "</svg>\n");
29
            fclose(out);
30
           out = 0;
31
32
33
       ~SVG() {
34
           if (out)
35
                close():
       }
36
37} svg;
```

### 16 graphs/2sat.cpp

```
1 const int maxn = 200100; //2 x number of variables
 3namespace TwoSAT {
       int n; //number of variables
 5
       bool used[maxn];
       vector<int> g[maxn];
vector<int> gr[maxn];
       int comp[maxn];
       int res[maxn];
10
11
       void addEdge(int u, int v) { //u or v
            g[u].push_back(v ^ 1);
g[v].push_back(u ^ 1);
13
            gr[u ^ 1].push_back(v);
gr[v ^ 1].push_back(u);
17
       vector<int> ord;
       void dfs1(int u) {
19
            used[u] = true;
20
            for (int v: g[u]) {
                if (used[v])
                      continue;
                 dfs1(v);
25
26
            ord.push_back(u);
27
28
       int COL = 0;
29
       void dfs2(int u) {
30
            used[u] = true;
comp[u] = COL;
31
32
            for (int v: gr[u]) {
    if (used[v])
33
34
35
                      continue;
36
                 dfs2(v);
            }
37
       }
38
39
       void mark(int u) {
40
            res[u / 2] = u % 2;
used[u] = true;
41
42
            for (int v: g[u]) {
43
                 if (used[v])
44
45
                      continue;
                 mark(v);
46
            }
47
       }
48
49
       bool run() {
50
            fill(res, res + 2 * n, -1);
51
            fill(used, used + 2 * n, false);
52
            forn (i, 2 * n)
if (!used[i])
53
54
55
                     dfs1(i);
56
            reverse(ord.begin(), ord.end());
57
            assert((int) ord.size() == (2 * n));
58
            fill(used, used + 2 * n, false);
59
            for (int u: ord) if (!used[u]) {
60
                 dfs2(u);
61
                 ++COL;
62
            7
63
            forn (i, n)
                 if (comp[i * 2] == comp[i * 2 + 1])
65
                      return false;
66
67
            reverse(ord.begin(), ord.end());
68
            fill(used, used + 2 * n, false);
            for (int u: ord) {
70
                 if (res[u / 2] != -1) {
71
                      continue;
72
73
                 mark(u):
            }
74
75
            return true;
       }
76
77};
78
79int main() {
       TwoSAT::n = 2;
80
       TwoSAT::addEdge(0, 2); //x or y
TwoSAT::addEdge(0, 3); //x or !y
TwoSAT::addEdge(3, 3); //!y or !y
assert(TwoSAT::run());
81
83
       cout << TwoSAT::res[0] << ' ' << TwoSAT::res[1] << '\n';</pre>
85
86
87}
```

vector<Edge> firstResult = bfs(e, {root}, {});

```
17 \quad {\rm graphs/directed\_mst.cpp}
```

```
if ((int)firstResult.size() + 1 == n) {
                                                                                       return firstResult;
                                                                            94
 1// WARNING: this code wasn't submitted anywhere
                                                                            95
 3namespace TwoChinese {
                                                                            97
                                                                                   // find stongly connected comp-s and build compressed graph
                                                                                   vector<int> comp(n);
 5struct Edge {
                                                                                   forn(i, n) b[i] = 0;
                                                                            99
 6
      int to, w, id;
                                                                           100
                                                                                   nc = 0;
      bool operator<(const Edge& other) const {</pre>
                                                                                   dtime = 0;
           return to < other.to || (to == other.to && w < other.w); 102
 8
                                                                                   forn(i, n) if (!b[i]) tarjan(i, e, comp);
 9
                                                                           103
10 };
                                                                           104
                                                                                   // multiple edges may be removed here if needed
11typedef vector<vector<Edge>> Graph;
                                                                           105
                                                                                   Graph ne(nc);
12
                                                                                   forn(v, n) for (Edge t: e[v]) {
    if (comp[v] != comp[t.to]) ...
                                                                           106
13 const int maxn = 2050;
                                                                           107
                                                                                            ne[comp[v]].push_back({comp[t.to], t.w, t.id});
                                                                           108
15// global, for supplementary algorithms
                                                                           109
16 int b[maxn];
                                                                           110
17int tin[maxn], tup[maxn];
                                                                                   int oldnc = nc;
                                                                           111
18 int dtime; // counter for tin, tout
                                                                           112
19 vector<int> st;
                                                                                   // run recursively on compressed graph
vector<Edge> subres = run(ne, comp[root]);
                                                                           113
20 int nc; // number of strongly connected components
                                                                           114
21int q[maxn];
                                                                           115
                                                                                      find incoming edge id for each component, init queue
                                                                           116
                                                                                   // if there is an edge (u, v) between different components
                                                                           117
                                                                                   // than v is added to queue
                                                                           118
25 void tarjan(int v, const Graph& e, vector<int>& comp) {
                                                                           119
                                                                                   nc = oldnc:
      b[v] = 1;
                                                                                   vector<int> incomingId(nc);
                                                                           120
27
       st.push_back(v);
                                                                                   for (Edge e: subres) {
                                                                           121
       tin[v] = tup[v] = dtime++;
28
                                                                                       incomingId[e.to] = e.id;
                                                                           122
                                                                           123
30
       for (Edge t: e[v]) if (t.w == 0) {
                                                                           124
           int to = t.to;
if (b[to] == 0) {
31
                                                                                   vector<Edge> result;
vector<int> init;
                                                                           125
32
                                                                           126
           tarjan(to, e, comp);
  tup[v] = min(tup[v], tup[to]);
} else if (b[to] == 1) {
33
                                                                           127
                                                                                   init.push_back(root);
34
                                                                                   forn(v, n) for (Edge t: e[v]) {
                                                                           128
35
                                                                                       if (incomingId[comp[t.to]] == t.id) {
                                                                           129
36
               tup[v] = min(tup[v], tin[to]);
                                                                           130
                                                                                            result.push_back(t);
37
                                                                           131
                                                                                            init.push_back(t.to);
38
      }
                                                                           132
                                                                                       }
39
                                                                                   }
                                                                           133
       if (tin[v] == tup[v]) {
40
                                                                           134
41
           while (true) {
                                                                           135
                                                                                   // run bfs to add edges inside components and return answer
               int t = st.back();
42
                                                                                   vector<Edge> innerEdges = bfs(e, init, comp);
                                                                           136
               st.pop_back();
comp[t] = nc;
43
                                                                                   result.insert(result.end(), all(innerEdges));
                                                                           137
44
                                                                           138
               b[t] = 2;
45
                                                                           139
                                                                                   assert((int)result.size() + 1 == n);
               if (t == v) break;
46
                                                                           140
                                                                                   return result;
47
           }
                                                                           141}
48
           ++nc:
                                                                           142
49
      }
                                                                           143} // namespace TwoChinese
50 }
                                                                           144
51
                                                                           145\, {	t void} test () {
52 vector < Edge > bfs(
                                                                                   auto res = TwoChinese::run({
                                                                           146
53
       const Graph& e, const vi& init, const vi& comp)
                                                                           147
                                                                                       {{1,5,0},{2,5,1}},
54 €
                                                                                       {{3,1,2}},
                                                                           148
55
       int n = e.size():
                                                                                       {{1,2,3},{4,1,4}},
{{1,1,5},{4,2,6}},
                                                                           149
      forn(i, n) b[i] = 0;
int lq = 0, rq = 0;
56
                                                                           150
57
                                                                                       {{2,1,7}}},
                                                                           151
      for (int v: init) b[v] = 1, q[rq++] = v;
58
                                                                           152
59
                                                                                   cout << TwoChinese::answer << endl;</pre>
                                                                           153
60
       vector<Edge> result;
                                                                           154
                                                                                   for (auto e: res) cout << e.id << " ";
61
                                                                                   cout << endl;</pre>
                                                                           155
62
      while (lq != rq) {
                                                                                             0 6 2 7
                                                                           156
                                                                                   // 9
           int \bar{v} = q[lq++];
63
                                                                           157}
           for (Edge t: e[v]) if (t.w == 0) {
   int to = t.to;
64
65
66
                if (b[to]) continue;
67
                if (!comp.empty() && comp[v] != comp[to]) continue;
               b[to] = 1;
q[rq++] = to;
68
69
70
                result.push_back(t);
71
72
      }
73
74
       return result;
75 }
77// warning: check that each vertex is reachable from root
78vector<Edge> run(Graph e, int root) {
79
       int n = e.size();
       // find minimum incoming weight for each vertex
       vector<int> minw(n, inf);
82
83
       forn(v, n) for (Edge t: e[v]) {
84
           minw[t.to] = min(minw[t.to], t.w);
85
86
       forn(v, n) for (Edge &t: e[v]) if (t.to != root) {
87
           t.w -= minw[t.to];
88
89
       forn(i, n) if (i != root) answer += minw[i];
       // check if each vertex is reachable from root by zero edges
```

# 18 graphs/dominator tree.cpp

```
1struct Dom {
3
      vector<vi> e, re; // graph (on v), reverse graph (on id)
      vi id, p, sdom, dom, dsu, best;
      vector<vi> bucket;
      int dtime = 0;
      Dom(int n) : n(n), e(n), re(n), id(n, -1), p(n),
          sdom(n), dom(n), dsu(n), best(n), bucket(n)
11
12
13
      void find(int v) {
          if (v != dsu[v]) {
14
               find(dsu[v]);
15
               if (sdom[best[dsu[v]]] <= sdom[best[v]]) {</pre>
16
17
                   best[v] = best[dsu[v]];
18
               dsu[v] = dsu[dsu[v]];
19
20
21
22
23
      void dfs1(int v) {
24
          id[v] = dtime++;
25
           for (int to: e[v]) {
               if (id[to] == -1) {
26
                   dfs1(to);
27
                   p[id[to]] = id[v];
28
29
30
               re[id[to]].push_back(id[v]);
31
          }
      }
32
33
      void pre() {
34
           dfs1(0);
35
           iota(all(best), 0);
36
37
           iota(all(sdom), 0);
38
           iota(all(dsu), 0);
39
40
41
      void run() {
          pre();
42
           for (int v = n-1; v >= 0; --v) {
43
44
               for (int w: bucket[v]) {
                   find(w);
45
46
                   dom[w] = best[w];
47
48
               for (int u: re[v]) {
                   find(u);
sdom[v] = min(sdom[v], sdom[best[u]]);
49
50
52
                   bucket[sdom[v]].pb(v);
dsu[v] = p[v]; // unite(v, p[v])
53
54
55
56
          }
57
           for (int v = 1; v < n; ++v) {
               if (dom[v] != sdom[v]) {
60
                   dom[v] = dom[dom[v]];
61
62
           vi ndom(n), rev(n);
           forn(i, n) rev[id[i]] = i;
65
66
           forn(i, n) ndom[i] = rev[dom[id[i]]];
67
           dom = ndom:
68
69 }:
```

### 19 graphs/edmonds matching.cpp

```
2vi e[maxn];
 3int mt[maxn], p[maxn], base[maxn], b[maxn], blos[maxn];
 4int q[maxn];
 5int blca[maxn]; // used for lca
 7 int lca(int u, int v) {
8  forn(i, n) blca[i] = 0;
       while (true) {
           u = base[u];
10
11
           blca[u] = 1;
           if (mt[u] == -1) break;
12
13
           u = p[mt[u]];
14
       while (!blca[base[v]]) {
15
16
           v = p[mt[base[v]]];
17
18
       return base[v];
19}
20
21void mark_path(int v, int b, int ch) {
22  while (base[v] != b) {
           blos[base[v]] = blos[base[mt[v]]] = 1;
23
           p[v] = ch;
24
           ch = mt[v];
25
           v = p[mt[v]];
26
       }
27
28 }
29
30 int find_path(int root) {
31
       forn(i, n) {
           base[i] = i;
p[i] = -1;
b[i] = 0;
32
33
34
       }
35
36
       b[root] = 1:
37
38
       q[0] = root;
       int lq = 0, rq = 1;
while (lq != rq) {
39
40
41
           int v = q[lq++];
            for (int to: e[v]) {
42
43
                if (base[v] == base[to] || mt[v] == to) continue;
                 if (to==root || (mt[to] != -1 && p[mt[to]] != -1)) {
44
                     int curbase = lca(v, to);
forn(i, n) blos[i] = 0;
45
46
47
                     mark_path(v, curbase, to);
48
                     mark_path(to, curbase, v);
49
                     forn(i, n) if (blos[base[i]]) {
                          base[i] = curbase;
50
                          if (!b[i]) b[i] = 1, q[rq++] = i;
52
                     }
                } else if (p[to] == -1) {
                     p[to] = v;
54
                     if (mt[to] == -1) {
                          return to;
56
57
                     to = mt[to];
                     b[to] = 1;
q[rq++] = to;
60
61
           }
63
65
       return -1;
66}
67
68int matching() {
       forn(i, n) mt[i] = -1;
69
70
       int res = 0;
       forn(i, n) if (mt[i] == -1) {
71
            int v = find_path(i);
72
           if (v != -1)^{-1}
73
74
                 ++res;
                while (v != -1) {
75
                     int pv = p[v], ppv = mt[p[v]];
mt[v] = pv, mt[pv] = v;
76
77
78
                     v = ppv;
79
80
           }
81
82
       return res;
83 }
```

#### 20 graphs/euler cycle.cpp

```
1struct Edge {
        int to, id;
 3};
 5bool usedEdge[maxm];
 6vector<Edge> g[maxn];
 7int ptr[maxn];
9vector<int> cycle;
10void eulerCycle(int u) {
        while (ptr[u] < sz(g[u]) && usedEdge[g[u][ptr[u]].id])
11
        ++ptr[u];
if (ptr[u] == sz(g[u]))
13
           return;
14
        const Edge &e = g[u][ptr[u]];
usedEdge[e.id] = true;
15
16
17
        eulerCycle(e.to);
        cycle.push_back(e.id);
18
        eulerCycle(u);
19
20}
21
22 int edges = 0;
23 void addEdge(int u, int v) {
        g[u].push_back(Edge{v, edges});
g[v].push_back(Edge{u, edges++});
25
```

# $21 \quad math/factor.cpp$

```
1//WARNING: only mod <= 1e18
211 mul(11 a, 11 b, 11 mod) {
3     ll res = a * b - (ll(ld(a) * ld(b) / ld(mod)) * mod);
4     while (res < 0)
 5
           res += mod;
       while (res >= mod)
 6
 7
           res -= mod;
 8
       return res;
9}
10
11bool millerRabinTest(ll n, ll a) {
       if (gcd(n, a) > 1)
13
            return false;
       11 x = n - 1;
14
       int 1 = 0;
while (x % 2 == 0) {
15
17
            x /= 2;
18
19
       11 c = binpow(a, x, n);
for (int i = 0; i < 1; ++i) {</pre>
20
21
            11 nx = mul(c, c, n);
22
            if (nx == 1) {
                 if (c != 1 && c != n - 1)
24
25
                      return false;
26
                  else
27
                      return true;
            }
28
29
            c = nx;
       }
30
31
       return c == 1;
32 }
33
34bool isPrime(ll n) {
       if (n == 1)
35
36
           return false;
       if (n \% 2 == 0)
37
       return n == 2;
for (ll a = 2; a < min<ll>(8, n); ++a)
38
39
            if (!millerRabinTest(n, a))
40
41
                return false;
       return true:
42
43 }
44
45 //WARNING: p is not sorted
46 void factorize(ll x, vector<ll> &p) {
47
       if (x == 1)
48
            return;
       if (isPrime(x)) {
   p.push_back(x);
49
50
51
            return;
52
       for (11 d: {2, 3, 5})
if (x % d == 0) {
53
54
55
                p.push_back(d);
56
                 factorize(x / d, p);
57
            }
58
59
       while (true) {
            ll x1 = rr() % (x - 1) + 1;

ll x2 = (mul(x1, x1, x) + 1) % x;

int i1 = 1, i2 = 2;
60
61
62
63
            while (true) {
                 ll c = (x1 + x - x2) \% x;
if (c == 0)
65
66
                      break;
                 11 g = gcd(c, x);
if (g > 1) {
67
68
                      factorize(g, p);
factorize(x / g, p);
70
71
                      return;
72
73
                 if (i1 * 2 == i2) {
                      i1 *= 2;
74
75
                      x1 = x2;
76
                  ++i2;
77
                 x2 = (mul(x2, x2, x) + 1) \% x;
78
79
            }
       }
80
```

## 22 math/fft.cpp

```
1 const int LG = 20;
 2typedef complex<ld> base;
 4vector<base> ang[LG + 5];
 6void init_fft() {
        int n = 1 << LG;</pre>
       ld e = acosl(-1) * 2 / n;
 9
       ang[LG].resize(n);
10
            ang[LG][i] = polar(ld(1), e * i);
11
12
       for (int k = LG - 1; k >= 0; --k) {
13
            ang[k].resize(1 << k);
forn(i, 1 << k)</pre>
15
                 ang[k][i] = ang[k + 1][i * 2];
16
17
18}
20 void fft_rec(base *a, int lg, bool inv) {
        if (lg == 0)
        return;
int hlen = 1 << (lg - 1);
23
       fft_rec(a, lg-1, inv);
24
25
       fft_rec(a + hlen, lg-1, inv);
26
27
       forn (i, hlen) {
28
            base w = ang[lg][i];
29
            if (inv)
30
                w = conj(w);
            base u = a[i];
31
            base v = a[i + hlen] * w;
32
33
            a[i] = u + v;
            a[i + hlen] = u - v;
34
35
36}
37
38 void fft(base *a, int lg, bool inv) {
39    int n = 1 << lg;
       int n = 1 << ig;
int j = 0, bit;
for (int i = 1; i < n; ++i) {
    for (bit = n >> 1; bit & j; bit >>= 1)
40
41
42
            j ^= bit;
j ^= bit;
43
44
            if (i < j)
45
                 swap(a[i], a[j]);
46
47
       fft_rec(a, lg, inv);
48
       if (inv) {
    forn(i, n)
49
50
51
                 a[i] /= n;
52
53}
54
55 void test() {
       int lg = 3;
int n = 1 << lg;</pre>
56
57
58
       init_fft();
       base a[] = \{1,3,5,2,4,6,7,1\};
59
60
       fft(a, lg, 0);
61
       forn(i, n)
       cout << a[i].real() << " ";
cout << '\n';
62
63
64
       forn(i, n)
       cout << a[i].imag() << " ";
cout << '\n';
// 29 -5.82843 -7 -0.171573 5 -0.171573 -7 -5.82843</pre>
65
66
67
```

// 0 -3.41421 6 0.585786 0 -0.585786 -6 3.41421

# 23 math/fft inv.cpp

```
1vector <int> mul(vector <int> a, vector <int> b,
               bool carry = true) {
         int n = sz(a);
         if (carry) {
               a.resize(n * 2);
               b.resize(n * 2);
         fft(a.data(), a.size(), false);
fft(b.data(), b.size(), false);
for (int i = 0; i < sz(a); ++i)</pre>
10
               a[i] = mul(a[i], b[i]);
11
12
         fft(a.data(), a.size(), true);
13
         a.resize(n);
14
         return a;
15}
16
17 vector <int> inv(vector <int> v) {
         int n = 1;
18
         while (n < sz(v))
19
             n <<= 1;
20
         v.resize(n, 0);
21
         v.resize(n, 0);
vector <int> res(1, binpow(v[0], mod - 2));
for (int k = 1; k < n; k <<= 1) {
    vector <int> A(k * 2, 0);
    copy(v.begin(), v.begin() + k, A.begin());
    vector <int> C = res;
    copy(v.begin(), v.begin() + k, A.begin());
22
23
24
25
26
               C.resize(k * 2, 0);
27
               Glesize(k * 2, 0),
A = mul(A, C, false);
for (int i = 0; i < 2 * k; ++i)
    A[i] = sub(0, A[i]);</pre>
28
29
30
               A[0] = sum(A[0], 1);
for (int i = 0; i < k; ++i)
assert(A[i] == 0);
copy(A.begin() + k, A.end(), A.begin());
31
32
33
34
               A.resize(k);
vector <int> B(k);
35
36
               copy(v.begin() + k, v.begin() + 2 * k, B.begin());
37
38
               C.resize(k);
39
               B = mul(B, C);
               for (int i = 0; i < k; ++i)
40
               A[i] = sub(A[i], B[i]);
A = mul(A, C);
41
42
               res.resize(k * 2);
43
                copy(A.begin(), A.end(), res.begin() + k);
44
45
46
         return res;
```

# 24 math/golden search.cpp

```
11d f(1d x) {
       return 5 * x * x + 100 * x + 1; //-10 is minimum
3}
51d goldenSearch(ld 1, ld r) {
       ld phi = (1 + sqrt1(5)) / 2;
ld resphi = 2 - phi;
       ld x1 = 1 + resphi * (r - 1);
ld x2 = r - resphi * (r - 1);
       1d f1 = f(x1);
       1d f2 = f(x2);
11
       forn (iter, 60) {
    if (f1 < f2) {
12
13
                r = x2;
x2 = x1;
14
15
                 f2 = f1;
16
                 x1 = 1 + resphi * (r - 1);
17
                 f1 = f(x1);
18
19
            } else {
                 1 = x1;
20
21
                 x1 = x2;
                 f1 = f2;
22
23
                 x2 = r - resphi * (r - 1);
24
                 f2 = f(x2);
25
26
27
       return (x1 + x2) / 2;
28}
29
30 int main() {
       std::cout << goldenSearch(-100, 100) << '\n';
32 }
```

#### 25 math/numbers.tex

• Simpson and Gauss numerical integration:

$$\int_{a}^{b} f(x) dx = (b - a)/6 \cdot (f(a) + 4(f(a + b)/2) + f(b))$$
$$\int_{-1}^{1}, x_{1,3} = \pm \sqrt{0.6}, x_2 = 0; a_{1,3} = 5/9, a_2 = 8/9$$

- Large primes:  $10^{18} + 3, +31, +3111, 10^9 + 21, +33$
- FFT modules:

```
\begin{array}{lll} 1\,107\,296\,257 & 2^{25}\cdot 3\cdot 11 + 1 & 10 \\ 1\,161\,822\,209 & 2^{22}\cdot 277 + 1 & 3 \\ 1\,261\,007\,895\,663\,738\,881 & 2^{55}\cdot 5\cdot 7 + 1 & 6 \text{ (check)} \end{array}
```

• Fibonacci numbers:

```
\begin{array}{lll} 1,2:&1\\ 45:&1\,134\,903\,170\\ 46:&1\,836\,311\,903\;(max\;int)\\ 47:&2\,971\,215\,073\;(max\;unsigned)\\ 91:&4\,660\,046\,610\,375\,530\,309\\ 92:&7\,540\,113\,804\,746\,346\,429\;(max\;i64)\\ 93:&12\,200\,160\,415\,121\,876\,738\;(max\;unsigned\;i64)\\ \end{array}
```

• Powers of two

$$2^{31} = 2147483648 = 2.1 \cdot 10^{9}$$

$$2^{32} = 4294967296 = 4.2 \cdot 10^{9}$$

$$2^{63} = 9223372036854775808 = 9.2 \cdot 10^{18}$$

$$2^{64} = 18446744073709551616 = 1.8 \cdot 10^{19}$$

• Highly composite numbers

$$- \le 1000: d(840) = 32, \le 10^4: d(9240) = 64$$

$$- \le 10^5: d(83160) = 128, \le 10^6: d(720720) = 240$$

$$- \le 10^7: d(8648640) = 448, \le 10^8: d(91891800) = 768$$

$$- \le 10^9: d(931170240) = 1344$$

$$- \le 10^{11}: d(97772875200) = 4032$$

$$- \le 10^{12}: d(963761198400) = 6720$$

$$- \le 10^{15}: d(866421317361600) = 26880$$

$$- \le 10^{18}: d(897612484786617600) = 103680$$

- Misc
  - Расстояние между точками по сфере:  $L = R \cdot \arccos(\cos\theta_1 \cdot \cos\theta_2 + \sin\theta_1 \cdot \sin\theta_2 \cdot \cos(\varphi_1 \varphi_2))$ , где  $\theta$  широты (от  $-\frac{\pi}{2}$  до  $\frac{\pi}{2}$ ),  $\varphi$  долготы (от  $-\pi$  до  $\pi$ ).
  - Объём шарового сегмента:  $V = \pi h^2 (R \frac{1}{3}h)$ , где h высота от вершины сектора до секущей плоскости
  - Площадь поверхности шарового сегмента:  $S=2\pi Rh$ , где h высота.
- 2:2,• Bell numbers: 0:1, 1:1, 3:5,4:15,6:203,7:877, 8:4140, 9:21147, 10:115975, 14:190899322. 11:678570, 12:4213597, 13:27644437, 17:82864869804, 16:10480142147, 15:1382958545, 18:682076806159, 19:5832742205057, 20:51724158235372, 21:474869816156751, 22:4506715738447323, 23:44152005855084346
- Catalan numbers: 0:1, 1:1, 2:2, 3:5, 4:14, 5:42, 6:132, 7:429, 8:1430, 9:4862, 10:16796, 11:58786, 12:208012, 13:742900, 14:2674440, 15:9694845, 16:35357670, 17:129644790, 18:477638700, 19:1767263190, 20:6564120420, 21:24466267020, 22:91482563640, 23:343059613650, 24:1289904147324, 25:4861946401452

# 26 math/quadratic equation.cpp

```
1vector<ld> sqrRoots(ld a, ld b, ld c) {
2    ld d = b * b - 4 * a * c;
3    if (ze(d))
               return \{-b / (2 * a)\};
         if (d < 0)
 6
              return {};
         d = sqrtl(d);
 8
         if (ze(b)) {
              ld x1 = -d / (2 * a);
ld x2 = d / (2 * a);
if (x1 > x2)
 9
10
11
12
                     swap(x1, x2);
13
               return {x1, x2};
14
        __ sgn = b > 0 ? 1 : -1;
ld x1 = (-b - sgn * d) / (2 * a);
ld x2 = c / (a * x1);
if (x1 > x2)
16
17
18
         if (x1 > x2)
              swap(x1, x2);
         return {x1, x2};
```

# 27 math/simplex.cpp

```
1namespace Simplex {
 31d D[maxm][maxn]; // [n+2][m+2]
 4int B[maxm];
 5int N[maxn];
 6ld x[maxn];
 7 int n, m;
 9//x \ge 0, Ax \le b, c^Tx - max
10 void init(int _n, int _m, ld A[][maxn], ld *b, ld *c) {
       n = _n, m = _m;
forn (i, m)
11
12
        forn (j, n)
    D[i][j] = -A[i][j];
forn (i, m) {
13
14
15
16
            D[i][n] = 1;
17
             D[i][n + 1] = b[i];
18
       forn (j, n) {
    D[m][j] = c[j];
19
20
21
             D[m + 1][j] = 0;
22
        D[m][n + 1] = D[m][n] = D[m + 1][n + 1] = 0;
        D[m + 1][n] = -1;
        iota(B, B + m, n);
26
        iota(N, N + n, 0);
27
        N[n] = -1;
28}
30 void pivot(int b, int nb) {
       assert(D[b][nb] != 0);
31
       ld q = 1. / -D[b] [nb];
D[b] [nb] = -1;
forn (i, n + 2)
32
33
           n (i, n -
D[b][i] *= q;
m + 2) {
35
       forn (i, m + 2)
if (i == b)
36
37
38
                 continue
             ld coef = D[i][nb];
39
            D[i][nb] = 0;
forn (j, n + 2)
    D[i][j] += coef * D[b][j];
40
41
42
43
        swap(B[b], N[nb]);
44
45 }
46
47bool betterN(int f, int i, int j) {
48    if (eq(D[f][i], D[f][j]))
49        return N[i] < N[j];
50
        return D[f][i] > D[f][j];
51 }
52
53bool betterB(int nb, int i, int j) {
54    ld ai = D[i][n + 1] / D[i][nb];
55    ld aj = D[j][n + 1] / D[j][nb];
56
       if (eq(ai, aj))
57
            return B[i] < B[j];</pre>
58
        return ai > aj;
59 }
60
61bool simplex(int phase) {
        int f = phase == 1 ? m : m + 1;
62
63
        while (true) {
             int nb = -1;
forn (i, n + 1) {
    if (N[i] == -1 && phase == 1)
64
65
66
67
                       continue;
68
                  if (nb == -1 || betterN(f, i, nb))
                       nb = i;
69
70
             if (D[f][nb] <= eps)
71
72
                  return phase == 1;
73
             assert(nb != -1);
74
75
             int b = -1;
76
             forn (i, m) {
77
                  if (D[i][nb] >= -eps)
78
                       continue;
79
                  if (b == -1 \mid \mid betterB(nb, i, b))
             if (b == -1)
                  return false;
             pivot(b, nb);
if (N[nb] == -1 && phase == 2)
85
86
                  return true;
        }
87
88}
901d solve() {
       int b = -1;
```

```
forn (i, m) \{
 93
            if (b == -1 \mid \mid D[i][n + 1] < D[b][n + 1])
 94
 95
       assert(b != -1);
if (D[b][n + 1] < -eps) {
 96
 97
 98
            pivot(b, n);
99
            if (!simplex(2) || D[m + 1][n + 1] < -eps)
100
                return -infl;
101
       if (!simplex(1))
102
103
            return infl;
104
105
       forn (i, n)
           x[i] = 0;
106
107
       forn (i, m)
            if (B[i] < n)
108
109
                x[B[i]] = D[i][n + 1];
110
       return D[m][n + 1];
111
112}
113
114} //Simplex
```

# 28 math/stuff.cpp

```
1const int M = 1e6;
 2int phi[M];
 3void calcPhi() {
        for (int i = 1; i < M; ++i)
        for (int i = 1; i < M; ++1)
    phi[i] = i;
for (int j = 1; j < M; ++j)
    for (int i = 2 * j; i < M; i += j)
        phi[i] -= phi[j];</pre>
 6
 8
9}
10 int inv[M];
11void calcInv() {
12
        inv[1] = 1;
        for (int i = 2; i < M; ++i) {
   inv[i] = mul(sub(0, mod / i), inv[mod % i]);</pre>
13
14
15
              assert(mul(i, inv[i]) == 1);
16
        }
17}
18 int gcd(int a, int b, int &x, int &y) {
        if (a == 0) {
 x = 0, y = 1;
19
20
21
             return b;
        }
22
        int x1, y1;
        int g = gcd(b % a, a, x1, y1);
x = y1 - x1 * (b / a);
24
25
26
        y = x1;
        assert(a * x + b * y == g);
28
        return g;
30 int crt(int mod1, int mod2, int rem1, int rem2) {
31    int r = (rem2 - (rem1 % mod2) + mod2) % mod2;
        int x, y;
int g = gcd(mod1, mod2, x, y);
assert(r % g == 0);
33
34
35
36
        x \%= mod2;
37
        if (x < 0)
             x += mod2;
38
39
        int ans = (x * (r / g)) % mod2;
40
        ans = ans * mod1 + rem1;
41
42
        assert(ans % mod1 == rem1);
43
        assert(ans % mod2 == rem2);
44
45
        return ans:
46 }
47
48 // primes to N
49 const 11 n = 1000000000000LL;
50 \, \text{const} \, 11 \, L = 1000000;
51 int small[L+1];
5211 large[L+1];
53void calc_pi() {
54    for (int i = 1; i <= L; ++i) {
55         small[i] = i-1;
56         large[i] = n / i - 1;
57
        for (ll p = 2; p <= L; ++p) {
    if (small[p] == small[p-1]) continue;</pre>
58
59
              int cntp = small[p-1];
60
             11 p2 = p*p;
11 np = n / p;
for (int i = 1; i <= min(L, n / p2); ++i) {</pre>
61
62
63
                   11 x = np / i;
if (x <= L) {</pre>
64
65
                        large[i] -= small[x] - cntp;
66
                   } else {
67
68
                        large[i] -= large[p*i] - cntp;
                   }
69
70
71
             for (int i = L; i >= p2; --i) {
72
                   small[i] = small[i/p] - cntp;
73
             }
        }
74
75}
7611 pi(11 x) {
77
        if (x > L) return small[n/x];
78
        else return large[x];
79}
81 int main() {
       calcPhi();
        assert(phi[30] == 1 * 2 * 4);
        calcInv();
        int x, y;
gcd(3, 5, x, y);
85
        gcd(15, 10, x, y);
crt(15, 13, 2, 5);
        crt(17, 3, 15, 2);
        return 0;
```

#### 29 strings/automaton.cpp

```
lint t[maxn][26], lnk[maxn], len[maxn];
 2int sz:
 3int last;
 5void init() {
       sz = 3;
       last = 1;
 7
       forn(i, 26) t[2][i] = 1;
len[2] = -1;
 9
       lnk[1] = 2;
10
11 }
12
13 void addchar(int c) {
       int nlast = sz++;
len[nlast] = len[last] + 1;
15
       int p = last;
for (; !t[p][c]; p = lnk[p]) {
16
17
           t[p][c] = nlast;
18
19
       int q = t[p][c];
if (len[p] + 1 == len[q]) {
20
21
            lnk[nlast] = q;
23
24
            int clone = sz++;
            len[clone] = len[p] + 1;
lnk[clone] = lnk[q];
lnk[q] = lnk[nlast] = clone;
25
26
27
28
            forn(i, 26) t[clone][i] = t[q][i];
29
            for (; t[p][c] == q; p = lnk[p]) {
30
                t[p][c] = clone;
31
32
33
       last = nlast;
34 }
35
36bool check(const string& s) {
37
       int v = 1;
       for (int c: s) {
38
           c -= 'a'
39
           if (!t[v][c]) return false;
40
41
           v = t[v][c];
42
       return true:
43
44 }
45
46 int main() {
47
       string s;
48
       cin >> s:
       init();
49
       for (int i: s) {
50
51
           addchar(i-'a');
52
53
       forn(i, s.length()) {
54
            assert(check(s.substr(i)));
55
       cout << sz << endl;</pre>
56
57
       return 0;
```

# 30 strings/duval manacher.cpp

```
Строка простая, если строго меньше всех суффиксов <=>
      наименьший циклический сдвиг - первый.
     Декомпозиция Линдона - разбиение s на w1, w2, ... wk -
      простые строки такие, что w1 >= w2 >= \dots wk.
 7int duval(string s) {
      s += s; //remove this to find Lyndon decomposition of s
       int n = s.size();
       int i = 0;
10
11
       int ans = 0;
       //while (i < n) { //for Lyndon decomposition while (i < n / 2) {
12
13
           ans = i;
int j = i + 1, k = i;
while (j < n && s[k] <= s[j]) {</pre>
14
15
16
                if (s[k] < s[j])
17
18
                    k = i;
19
                else
20
                    ++k;
                ++j;
21
           }
22
           while (i \leq k) {
23
                //s.substr(i, j - k) - //next prime string of Lyndon decomposition
24
25
                i += j - k;
26
           }
27
      }
28
29
      return ans:
30 }
31
32//actual odd length is (odd[i]*2-1) 33//actual even length is (even[i]*2)
34 void manacher(const string &s, vi &odd, vi &even) {
35
       int n = s.size();
36
       odd.resize(n);
      int c = -1, r = -1;
forn (i, n) {
37
38
           int k = (r <= i ? 0 : min(odd[2 * c - i], r - i));</pre>
39
40
           while (i + k < n \&\& i - k >= 0 \&\& s[i + k] == s[i - k])
               ++k;
41
           odd[i] = k;
42
43
           if (i + k > r)
                r = i + k, c = i;
44
      }
45
       c = -1, r = -1;
46
47
       even.resize(n - 1);
48
       forn (i, n - 1) \{
           int k = (r <= i ? 0 : min(even[2 * c - i], r - i));</pre>
49
           while (i + k + 1 < n && i - k >= 0 &&
50
                    s[i + k + 1] == s[i - k])
52
                ++k;
           even[i] = k;
53
54
           if (i + k > r)
55
                c = i, r = i + k;
56
      }
57}
59 void test() {
      vector<int> odd, even;
       string s = "aaaabbaaaaa";
       manacher(s, odd, even);
      for (int x: even)
          cerr << x << ' ';
       cerr << '\n';
65
66
       for (int x: odd)
         cerr << x << ' ';
      cerr << '\n';
// 1 2 1 0 5 0 1 2 2 1
68
       // 1 2 2 1 1 1 1 2 3 2 1
70
71 }
72
73int main() {
       cout << duval("ababcabab") << '\n'; // 5</pre>
74
       test();
75
```

56}

#### 31 strings/eertree.cpp

```
1 #include <bits/stdc++.h>
 2using namespace std;
 3 const int maxn = 5000100;
 4 const int inf = 1e9 + 1e5;
 6 char buf[maxn];
 7 char *s = buf + 1;
 8 int to[maxn][2];
 9int suff[maxn];
10 int len[maxn];
11 int sz;
12 int last;
13
14 const int odd = 1;
15 const int even = 2;
16 const int blank = 3;
18 inline void go(int &u, int pos) {
       while (u != blank && s[pos - len[u] - 1] != s[pos])
           u = suff[u];
21}
22
23 void add_char(int pos) {
24
       go(last, pos);
25
       int u = suff[last];
26
       go(u, pos);
       int c = s[pos] - 'a';
if (!to[last][c]) {
27
28
           to[last][c] = sz++;
len[sz - 1] = len[last] + 2;
29
30
            assert(to[u][c]);
31
32
           suff[sz - 1] = to[u][c];
33
       last = to[last][c];
34
35 }
36
37void init() {
       sz = 4;
38
       to[blank][0] = to[blank][1] = even;
39
       len[blank] = suff[blank] = inf;
40
       len[even] = 0, suff[even] = odd;
len[odd] = -1, suff[odd] = blank;
41
42
43
       last = 2:
44 }
45
46 void build() {
      init();
scanf("%s", s);
for (int i = 0; s[i]; ++i)
    add_char(i);
47
48
49
50
51 }
```

# $32 ext{ strings/suffix\_array.cpp}$

```
1string s;
 3int sa[maxn], new_sa[maxn], cls[maxn], new_cls[maxn],
           cnt[maxn], lcp[maxn];
 5int n_cls;
 7void build() {
      n_cls = 256;
forn(i, n) {
           sa[i] = i;
10
           cls[i] = s[i];
11
12
13
       for (int d = 0; d < n; d = d? d*2 : 1) {
14
           forn(i, n) new_sa[i] = (sa[i] - d + n) % n;
forn(i, n_cls) cnt[i] = 0;
15
16
           forn(i, n) ++cnt[cls[i]];
17
           forn(i, n_cls) cnt[i+1] += cnt[i];
18
           for (int i = n-1; i >= 0;
19
                sa[--cnt[cls[new_sa[i]]] = new_sa[i];
20
21
           n cls = 0:
22
           forn(i, n) {
23
                if (i && (cls[sa[i]] != cls[sa[i-1]] ||
24
                         cls[(sa[i]+d)\%n] != cls[(sa[i-1]+d)\%n])) {
25
26
                     ++n_cls;
                }
27
               new_cls[sa[i]] = n_cls;
28
           }
29
           ++n_cls;
30
31
           forn(i, n) cls[i] = new_cls[i];
       }
32
33
       // cls is also a inv perm of sa if a string is not cyclic
34
       // (i.e. a position of i-th lexicographical suffix) int val = 0;
35
36
      forn(i, n) {
   if (val) --val;
37
38
           if (val) --val,
if (cls[i] == n-1) continue;
int j = sa[cls[i] + 1];
39
40
           while (i+val != n && j+val != n && s[i+val] == s[j+val])
41
42
                ++val •
43
           lcp[cls[i]] = val;
       }
44
45 }
46
47 int main() {
48
      cin >> s;
       s += '$';
49
50
      n = s.length();
       build();
52
       forn(i, n) {
53
           cout << s.substr(sa[i]) << endl;</pre>
54
           cout << lcp[i] << endl;</pre>
55
       }
```

95

97

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123

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125

# strings/ukkonen.cpp

```
1string s;
2const int alpha = 26;
4namespace SuffixTree {
      struct Node {
          Node *to[alpha];
          Node *lnk, *par;
8
          int 1, r;
10
           Node(int 1, int r): l(1), r(r) {
               memset(to, 0, sizeof(to));
lnk = par = 0;
12
13
14
      };
15
16
      Node *root, *blank, *cur;
17
      int pos;
18
19
      void init() {
20
          root = new Node(0, 0);
           blank = new Node(0, 0);
22
          forn (i, alpha)
              blank->to[i] = root;
          root->lnk = root->par = blank->lnk = blank->par = blank; 118
24
25
          cur = root;
26
          pos = 0;
27
28
      int at(int id) {
30
          return s[id] - 'a';
31
32
33
      void goDown(int 1, int r) {
34
          if (1 >= r)
35
              return;
36
          if (pos == cur->r) {
               int c = at(1);
37
38
               assert(cur->to[c]);
               cur = cur->to[c];
39
               pos = min(cur->r, cur->l + 1);
40
41
          } else {
42
               int delta = min(r - 1, cur->r - pos);
43
44
               1 += delta;
45
               pos += delta;
46
47
           goDown(1, r);
      }
48
49
50
      void goUp() {
          if (pos == cur->r \&\& cur->lnk) {
51
               cur = cur->lnk;
52
               pos = cur->r;
53
54
               return;
55
56
          int l = cur -> l, r = pos;
57
          cur = cur->par->lnk;
           pos = cur->r;
58
59
           goDown(l, r);
60
61
62
      void setParent(Node *a, Node *b) {
63
          assert(a);
64
           a->par = b;
65
           if (b)
66
               b->to[at(a->1)] = a;
67
68
69
      void addLeaf(int id) {
70
           Node *x = new Node(id, inf);
71
           setParent(x, cur);
72
73
74
      void splitNode() {
75
           assert(pos != cur->r);
76
           Node *mid = new Node(cur->1, pos);
77
           setParent(mid, cur->par);
           cur->1 = pos;
78
79
           setParent(cur, mid);
           cur = mid;
81
82
83
      bool canGo(int c) {
          if (pos == cur->r)
85
               return cur->to[c];
           return at(pos) == c;
86
87
88
89
      void fixLink(Node *&bad, Node *newBad) {
           if (bad)
               bad->lnk = cur;
```

```
bad = newBad;
       void addCharOnPos(int id) {
           Node *bad = 0;
           while (!canGo(at(id))) {
               if (cur->r != pos) {
    splitNode();
                    fixLink(bad, cur);
                    bad = cur;
               } else {
                   fixLink(bad, 0);
               addLeaf(id);
               goUp();
           fixLink(bad, 0);
           goDown(id, id + 1);
       int cnt(Node *u, int ml) {
           if (!u)
               return 0;
           int res = min(ml, u->r) - u->l;
           forn (i, alpha)
               res += cnt(u->to[i], ml);
           return res;
       }
       void build(int 1) {
           init();
           forn (i, 1)
               addCharOnPos(i);
       }
126};
```

### 34 structures/centroids.cpp

```
1 const int maxn = 100100;
 2const int LG = 18; //2*maxn <= 2^LG</pre>
 4vector<int> g[LG][maxn];
 5int rt[LG][maxn];
 6int from[LG][maxn];
 8namespace Cenroids {
10 int D;
11 int cnt[maxn];
12 int CENTER, BEST;
13
14 void pre(int u, int prev = -1) {
       cnt[u] = 1;
       for (int v: g[D][u]) {
17
           if (v == prev)
                continue;
           pre(v, u);
           cnt[u] += cnt[v];
20
21
22}
24 void findCenter(int u, int prev = -1, int up = 0) {
25
       int worst = up;
       for (int v: g[D][u]) {
   if (v == prev)
      continue;
26
27
28
29
            findCenter(v, u, up + cnt[u] - cnt[v]);
30
            worst = max(worst, cnt[v]);
31
32
       if (worst < BEST) {
33
            CENTER = u;
34
           BEST = worst;
35
36}
37
38 void markAll(int u, int prev = -1, int subtree = -1) {
       rt[D][u] = CENTER;
from[D][u] = subtree;
39
40
       for (int v: g[D][u]) {
   if (v == prev)
41
42
                continue;
43
           g[D + 1][u].push_back(v);
g[D + 1][v].push_back(u);
if (subtree == -1)
44
45
46
47
                markAll(v, u, v);
48
            else
                markAll(v, u, subtree);
49
50
51 }
52
53 void decompose(int u, int depth = 0) {
54
       D = depth;
55
       pre(u);
       CENTER = -1, BEST = 1e9;
56
       findCenter(u);
57
58
       assert(CENTER != -1);
59
       u = CENTER;
60
       markAll(u);
61
       D = depth + 1;
62
       for (int v: g[D][u]) {
63
            auto it = find(g[D][v].begin(), g[D][v].end(), u);
64
            assert(it != g[D][v].end());
65
            g[D][v].erase(it);
66
67
       for (int v: g[D][u])
68
            decompose(v, depth + 1);
71};
```

# 35 structures/heavy\_light.cpp

```
1 const int maxn = 100500;
2 const int maxd = 17;
 4vector<int> g[maxn];
 6struct Tree {
       vector<int> t;
 8
       int base;
10
       Tree(): base(0) {
11
12
13
       Tree(int n) {
14
           base = 1;
15
           while (base < n)
               base *= 2;
16
17
           t = vector<int>(base * 2, 0);
18
19
       void put(int v, int delta) {
20
           assert(v < base);</pre>
22
           v += base;
           t[v] += delta;
           while (v > 1) {
v /= 2;
26
                t[v] = max(t[v * 2], t[v * 2 + 1]);
           }
27
28
30
       //Careful here: cr = 2 * maxn
       int get(int 1, int r, int v=1, int cl=0, int cr = 2*maxn) {
31
           cr = min(cr, base);
if (1 <= c1 && cr <= r)
32
33
                return t[v];
35
           if (r <= cl || cr <= 1)
               return 0;
           int cc = (cl + cr) / 2;
37
           return max(get(1, r, v * 2, cl, cc),
get(1, r, v * 2 + 1, cc, cr));
38
39
40
41};
42
43 namespace HLD {
       int h[maxn];
44
45
       int timer;
       int in[maxn], out[maxn], cnt[maxn];
46
       int p[maxd][maxn];
47
48
       int vroot[maxn];
       int vpos[maxn];
49
       int ROOT;
50
       Tree tree[maxn];
51
52
       void dfs1(int u, int prev) {
53
           p[0][u] = prev;
54
           in[u] = timer++;
55
           cnt[u] = 1;
56
57
           for (int v: g[u]) {
               if (v == prev)
58
59
                    continue;
                h[v] = h[u] + 1;
60
61
                dfs1(v, u);
62
                cnt[u] += cnt[v];
63
           7
           out[u] = timer;
65
66
67
       int dfs2(int u, int prev) {
68
           int to = -1;
69
           for (int v: g[u]) {
70
                if (v == prev)
                     continue;
71
72
                if (to == -1 || cnt[v] > cnt[to])
73
                     to = v;
74
           }
75
           int len = 1;
           for (int v: g[u]) {
   if (v == prev)
76
77
                     continue;
                if (to == v) {
79
                    vpos[v] = vpos[u] + 1;
vroot[v] = vroot[u];
                    len += dfs2(v, u);
                     vroot[v] = v;
                     vpos[v] = 0;
86
87
                    dfs2(v, u);
88
89
           if (vroot[u] == u)
                tree[u] = Tree(len);
```

```
return len;
 93
 94
 95
        void init(int n) {
             timer = 0;
h[ROOT] = 0;
 96
 97
             dfs1(ROOT, ROOT);
 99
             forn (d, maxd - 1)
                 forn (i, n)
100
101
                      p[d + 1][i] = p[d][p[d][i]];
             vroot[ROOT] = ROOT;
102
             vpos[ROOT] = 0;
103
             dfs2(ROOT, ROOT);
104
105
             //WARNING: init all trees
106
107
108
        bool isPrev(int u, int v) {
109
             return in[u] <= in[v] && out[v] <= out[u];
110
111
        int lca(int u, int v) {
112
             for (int d = maxd - 1; d >= 0; --d)
if (!isPrev(p[d][u], v))
113
114
             u = p[d][u];
if (!isPrev(u, v))
115
116
117
                 u = p[0][u];
118
             return u;
119
120
        //for\ each\ v:\ h[v] >= toh
121
        int getv(int u, int toh) {
   int res = 0;
   while (h[u] >= toh) {
122
123
124
                 int rt = vroot[u];
int l = max(0, toh - h[rt]), r = vroos[u] + 1;
125
126
127
                 res = max(res, tree[rt].get(1, r));
                 if (rt == ROOT)
128
                      break;
129
130
                 u = p[0][rt];
131
             }
132
             return res;
        }
133
134
135
        int get(int u, int v) {
136
             int w = lca(u, v);
137
             return max(getv(u, h[w]), getv(v, h[w] + 1));
138
139
140
        void put(int u, int val) {
             int rt = vroot[u];
int pos = vpos[u];
141
142
143
             tree[rt].put(pos, val);
144
```

145};

# 36 structures/linkcut.cpp

```
1namespace LinkCut {
 3typedef struct _node {
      _node *1, *r, *p, *pp;
int size; bool rev;
       _node();
 8
       explicit _node(nullptr_t) {
           1 = r = p = pp = this;
size = rev = 0;
10
11
12
13
      void push() {
14
          if (rev) {
               1->rev ^= 1; r->rev ^= 1;
15
               rev = 0; swap(1,r);
16
17
18
19
      void update();
20
21}* node;
22
23 node None = new _node(nullptr);
24 node v2n[maxn];
26_node::_node(){
     1 = r = p = pp = None;
      size = 1; rev = false;
28
29 }
30
31void _node::update() {
      size = (this != None) + 1->size + r->size;
32
      1->p = r->p = this;
33
34}
35
36 void rotate(node v) {
      assert(v != None && v->p != None);
37
      assert(!v->rev);
38
      assert(!v->p->rev);
39
      node u = v->p;
if (v == u->1)
40
41
           u->1 = v->r, v->r = u;
42
43
      else
          u->r = v->1, v->1 = u;
44
45
      swap(u->p,v->p);
      swap(v->pp,u->pp);
if (v->p != None) {
46
47
           assert(v->p->1 == u \mid \mid v->p->r == u);
48
           if (v->p->r == u)
49
               v->p->r = v;
50
51
           else
               v->p->1 = v;
52
53
54
      u->update();
55
      v->update();
56 }
57
58 void bigRotate(node v) {
59
      assert(v->p != None);
      v->p->p-
61
      v->p->push();
62
      v->push();
      if (v->p->p != None) {
    if ((v->p->1 == v) ^ (v->p->r == v->p))
63
65
                rotate(v->p);
66
           else
67
                rotate(v);
68
69
      rotate(v);
70}
71
72 inline void splay(node v) {
73
      while (v-p != None)
74
           bigRotate(v);
75}
76
77 inline void splitAfter(node v) {
      v->push();
      splay(v);
      v->r->p = None;
      v->r->pp = v;
v->r = None;
      v->update();
84}
86 void expose(int x) {
      node v = v2n[x];
87
      splitAfter(v);
      while (v->pp != None) {
   assert(v->p == None);
           splitAfter(v->pp);
```

```
assert(v->pp->r == None);
             assert(v->pp->p == None);
 93
 94
             assert(!v->pp->rev);
 95
             v - pp - r = v;
             v->pp->update();
v = v->pp;
 97
 98
             v->r->pp = None;
 99
100
        assert(v->p == None);
101
        splay(v2n[x]);
102}
103
104 inline void makeRoot(int x) {
105
        expose(x);
        assert(v2n[x]->p == None);
106
        assert(v2n[x]->pp == None);
assert(v2n[x]->r == None);
107
108
109
        v2n[x]->rev ^= 1;
110}
111
112inline void link(int x, int y) {
        makeRoot(x);
v2n[x]->pp = v2n[y];
113
114
115}
116
117 inline void cut(int x, int y) {
118
        expose(x);
        splay(v2n[y]);
119
        if (v2n[y]->pp != v2n[x]) {
    swap(x,y);
120
121
122
             expose(x);
             splay(v2n[y]);
assert(v2n[y]->pp == v2n[x]);
123
124
125
        v2n[y] - pp = None;
126
127}
128
129 inline int get(int x, int y) {
130    if (x == y)
            return 0;
131
132
        makeRoot(x);
133
        expose(y);
134
        expose(x);
135
        splay(v2n[y]);
136
        if (v2n[y]-pp != v2n[x])
137
             return -1;
138
        return v2n[y]->size;
139}
140
```

141}

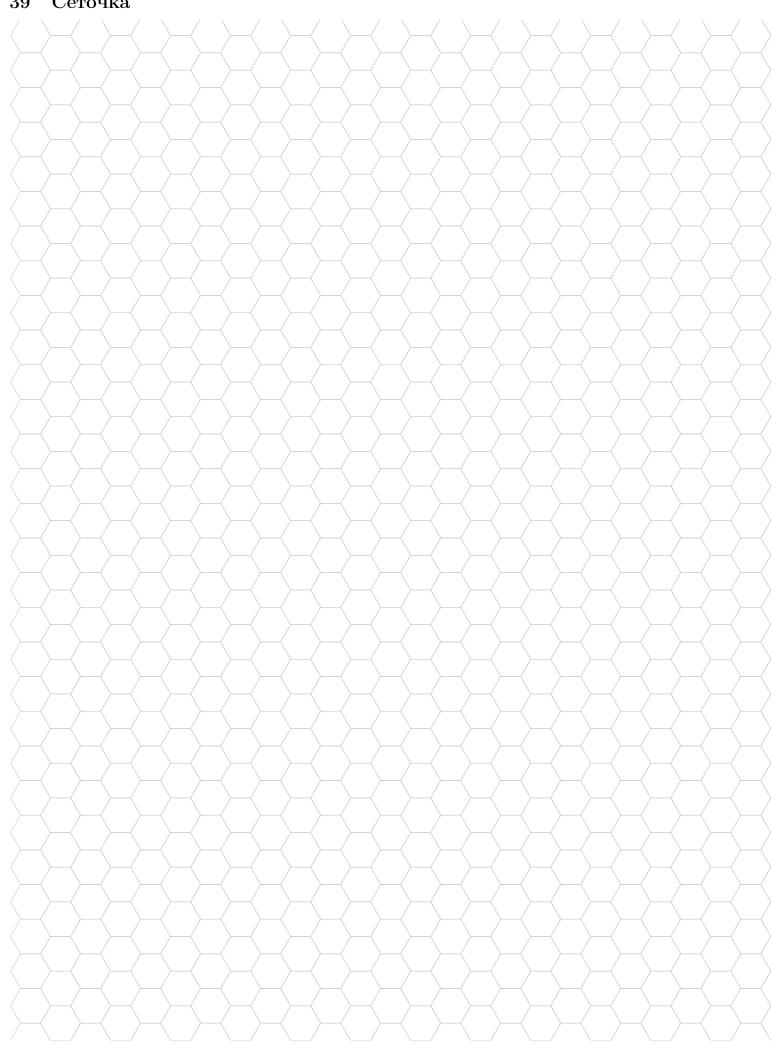
# 37 structures/ordered set.cpp

```
1 #include <ext/pb_ds/assoc_container.hpp>
 2 #include <ext/pb_ds/tree_policy.hpp>
 4typedef __gnu_pbds::tree<int, __gnu_pbds::null_type,</pre>
           std::less<int>,
           __gnu_pbds::rb_tree_tag,
           __gnu_pbds::tree_order_statistics_node_update> oset;
 9 #include <iostream>
10
11int main() {
12
      oset X;
13
      X.insert(1);
      X.insert(2);
14
15
      X.insert(4);
16
      X.insert(8);
17
      X.insert(16);
18
      std::cout << *X.find_by_order(1) << std::endl; // 2 std::cout << *X.find_by_order(2) << std::endl; // 4
19
20
      std::cout << *X.find_by_order(4) << std::endl; // 16
std::cout << std::boolalpha <</pre>
21
22
           (end(X)==X.find_by_order(6)) << std::endl; // true</pre>
23
24
      25
26
27
28
       std::cout << X.order_of_key(400) << std::endl; // 5
29
30 }
```

#### 38 structures/treap.cpp

```
1struct node {
 2
      int x, y;
      node *1, *r;
 3
      \label{eq:node_int} \mbox{node(int } \mbox{x) : } \mbox{x(x), y(rand()), l(r=NULL) } \mbox{\{}\}
 4
 5};
 7void split(node *t, node *&l, node *&r, int x) {
       if (!t) return (void)(l=r=NULL);
 9
       if (x \le t->x) {
10
           split(t->1, 1, t->1, x), r = t;
11
      } else {
12
           split(t->r, t->r, r, x), l = t;
13
14}
16node *merge(node *1, node *r) {
17
      if (!1) return r;
       if (!r) return 1;
      if (1->y > r->y) {
 1->r = merge(1->r, r);
20
           return 1;
      } else {
23
           r->1 = merge(1, r->1);
24
           return r;
25
26}
27
28 node *insert(node *t, node *n) {
      node *1, *r;
split(t, 1, r, n->x);
29
30
31
      return merge(1, merge(n, r));
32}
33
34node *insert(node *t, int x) {
35
      return insert(t, new node(x));
36}
37
38node *fast_insert(node *t, node *n) {
      if (!t) return n;
39
40
      node *root = t;
      while (true) {
41
          if (n->x < t->x) {
    if (!t->l || t->l->y < n->y) {
42
43
44
                    split(t->1, n->1, n->r, n->x), t->1 = n;
45
                    break;
46
               } else {
                    t = t - > 1;
47
               }
48
           } else {
49
               if (!t->r || t->r->y < n->y) {
50
51
                    split(t->r, n->l, n->r, n->x), t->r = n;
52
                    break;
53
               } else {
54
                    t = t->r;
55
           }
56
57
58
      return root;
59}
60
61node *fast_insert(node *t, int x) {
62
      return fast_insert(t, new node(x));
63}
65int main() {
      node *t = NULL;
67
      forn(i, 1000000) {
68
           int x = rand();
           t = fast_insert(t, x);
70
```

#### 39 Сеточка



# 40 Сеточка

