

The Biblical Writings of Nick Halliwell

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intervals in \mathbb{R} : $VC = 2$

axis parallel rectangles in \mathbb{R}^2 : $VC = 4$

circles in \mathbb{R}^2 : $VC = 3$

triangles in \mathbb{R}^2 : $VC = 7$

half spaces in \mathbb{R}^n : $VC = n + 1$

convex polygon: $VC = \infty$

axis parallel rectangles in \mathbb{R}^3 : $VC = n + 1$

convex k-gon: $VC = (2k + 1)$ where k is the number of vertices

convex sets: $VC = \infty$

Disc in \mathbb{R}^2 : $VC = 3$

rectangles in \mathbb{R}^d : $VC = 2d$

$S(A, n) \leq (\frac{n(n+1)}{2} + 1)^d < (n + 1)^{2d}$

convex polygon w/ d-vertices: $VC = 2d + 1$

closed balls in \mathbb{R}^d : $VC \leq d + 2$

squares in plane in \mathbb{R}^2 : $VC = 3$

union of k closed intervals: $VC = 2k$

South west intervals in \mathbb{R}^d : $A = \{(-\infty, a_1] * (-\infty, a_2] \dots * (-\infty, a_j] : a_j \in \mathbb{R}\}$
 $VC = d$

Class H_d of linear separators in \mathbb{R}^d

$H_d = \{x \mapsto \text{sign}(w^T x - b) \mid w \in \mathbb{R}^d, b \in \mathbb{R}\}$

$VC = d + 1$

$h(x) = \text{sign}(\sum_{i=1}^d w_i \phi_i(x) + b)$ where $\phi : \mathcal{X} \rightarrow \mathbb{R}^d$

$VC \leq d + 1$

Set of all linear functions in d variables: $VC = d + 1$

$\mathcal{X} = \mathbb{R}^2$, $\mathcal{A} = \{1_C \mid C \text{ is convex in } \mathbb{R}^2\}$

$VC = \infty$

Let \mathbb{F} be an m-dimensional vector space of real valued functions. $\mathbb{H} = \{1_{f(x) \geq 0} \mid f \in \mathbb{F}\}$, $VC \leq m$

Union of axis aligned rectangles and triangles in dimension 2: $VC = 12$ (axis aligned rectangles in dim 2 = 4, vc dim of triangles is 7, $4 + 7 + 1 = 12$)

circle centered at origin: $VC = 1$

origin centered “bagels”: $VC = 2$