Running and visualizing the IBAMR tutorials

1 Navier Stokes Ex 1

Open a terminal and log in to one of the clot servers.

ssh username@clot128a.math.utah.edu

where username is your math username. You will be asked to type your password. Create and navigate to a folder that you will use to build the IBAMR examples. Clone the github repository into that directory

```
mkdir ibamr_tutorials && cd ibamr_tutorials
git clone https://github.com/abarret/ibamr_tutorial.git
```

At this point, you will have the IBAMR examples in a directory named <code>ibamr_tutorial</code>. It contains the examples and CMake build system files. Next, we create a build directory and run <code>CMake</code> to generate the Makefiles that can be used to compile the examples. This searches the provided directory for the IBAMR header files and compiled libraries.

```
mkdir build && cd build
cmake ../ibamr_tutorial -DIBAMR_ROOT=/u/ma/barrett/ibamr/ibamr/linux-opt \
   -DCMAKE_CXX_COMPILER=/u/ma/barrett/ibamr/openmpi/4.1.3/bin/mpicxx
```

Note that this uses the same compiler flags that were used to build IBAMR, in this case those are -O3 -march=native. Now we can build the examples.

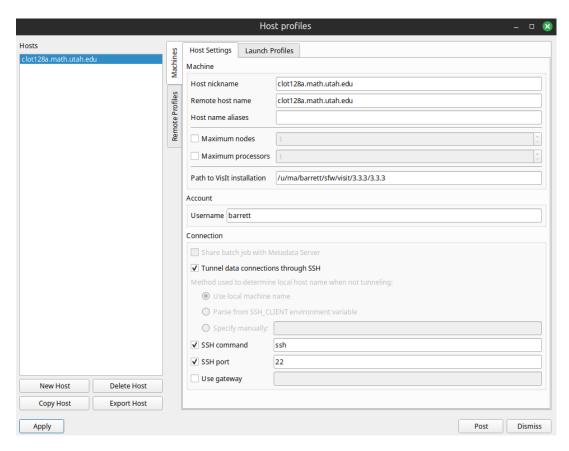
```
make -j4 examples
```

The argument -j4 will parallelize the build and compile at most 4 files at the same time. Once CMake is run correctly, the Makefiles will automatically track changes in depedencies, and automatically determine which files need to be recompiled when running make. Now you can navigate into one of the examples and run it.

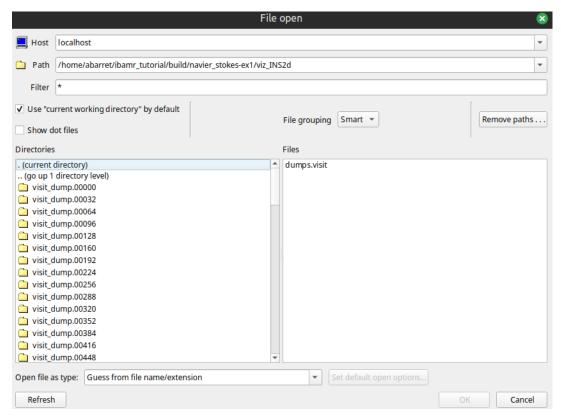
```
cd navier_stokes-ex1
./main2d input2d
```

This example is a simulation of the Kelvin-Helmholtz instability, in which the initial conditions consist of a sharp shear layer with a small perturbation. While this is running, we will open VisIt to visualize the results. At this time, you must use VisIt version 3.3 or 3.4. We will set up VisIt can be run in client-server mode to visualize results remotely. Alternatively, you can download the visualization files to analyze them locally.

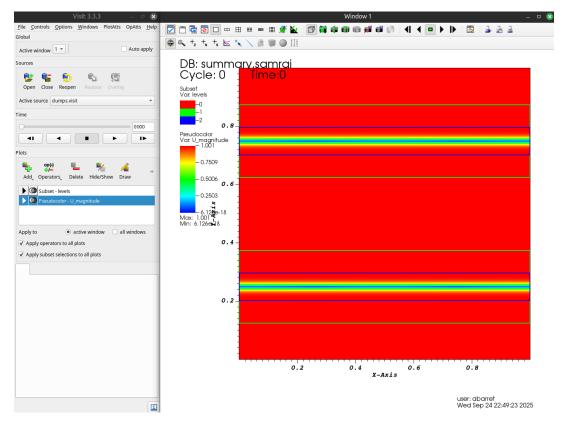
With VisIt open in the Options menu, click the Host profiles button. Create a new host and set it as in the following image. If you are using a different minor version than 3.3, you should use the appropriate VisIt release. Minor versions for the client and the server must match. The path to the VisIt installation should be the path to the executable, without the bin/visit extension.



Click apply and dismiss. Now we can connect to the clot server. Click Open and change the host to clot128a.math.utah.edu. You will be asked for your password. Now navigate to the build directory and open the dumps.visit file



By default, if running with multiple levels, a levels outline will be created by default. Now you can add various plots through the Add button. In particular, we can add a color plot of the velocity magnitude by selecting Add, then Pseudocolor, then U_magnitude.



Make sure to click Draw after adding any plot that you want to visualize. Double click any of the plots in the list to look at different plotting options, setting, e.g. color bars, color tables, line widths, and more. You can animate over time by pressing to play button.

2 IB Ex 1

As before, we want to navigate to the build directory of the IBAMR tutorials.

cd \${HOME}/ibamr_tutorial/build

For this example, we want to build IB-ex1, which is the classic IB simulation of an elastic rubberband.

make IB-ex1 && cd IB-ex1

Note that if make determines that no depedencies have changed, then the tool may correctly not compile anything. In this directory, in addition to the compiled binary and input file, there are several .spring and .vertex files. These files set the initial configuration and elasticity of the immersed structure. There is also a MATLAB file generate_curve2d.m that will generate these input files. Looking at the curve2d_64 files, they begin with

cat curve2d_64.vertex	cat curve2d_64.spring
304	304
6.7857142857142860e-01 5.0000000000000000e-01	0 1 1.9353241079974475e+02 0.000000000000000e+00
6.7853328871213048e-01 5.0723341542964395e-01	1 2 1.9353241079974475e+02 0.000000000000000e+00
6.7841888542630380e-01 5.1446374098708458e-01	2 3 1.9353241079974475e+02 0.000000000000000e+00
6.7822826758319077e-01 5.2168788812000810e-01	3 4 1.9353241079974475e+02 0.000000000000000e+00
6.7796151660833393e-01 5.2890277091531634e-01	4 5 1.9353241079974475e+02 0.000000000000000e+00
6.7761874644879327e-01 5.3610530741732487e-01	5 6 1.9353241079974475e+02 0.000000000000000e+00
6.7720010352447235e-01 5.4329242094427166e-01	6 7 1.9353241079974475e+02 0.000000000000000e+00
6.7670576666557192e-01 5.5046104140257135e-01	7 8 1.9353241079974475e+02 0.000000000000000e+00
6.7613594703620039e-01 5.5760810659825688e-01	8 9 1.9353241079974475e+02 0.000000000000000e+00
6.7549088804417134e-01 5.6473056354504547e-01	9 10 1.9353241079974475e+02 0.000000000000000e+00
6.7477086523702756e-01 5.7182536976847198e-01	10 11 1.9353241079974475e+02 0.000000000000000e+00

The .vertex file prints the number of vertices, followed by the initial position of each vertex. The .spring file prints the number of springs, followed by the Lagrangian index of each vertex that defines a spring. The two constants that follow

are the spring constant and the resting length. The Lagrangian index is set by the order in which vertices are printed in the vertex file.

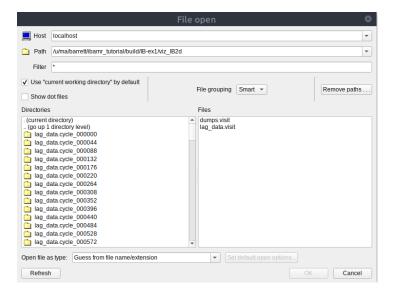
If you open the input file, you will notice the database titled IBStandardInitializer as follows

The structure is named curve2d_64, which points the program to open the files with that base name to initialize the structure. The structure lives on the level number MAX_LEVELS - 1, which is the finest level number. The input file also specified a uniform spring stiffness of K/ds, which overrides the value in the .spring file.

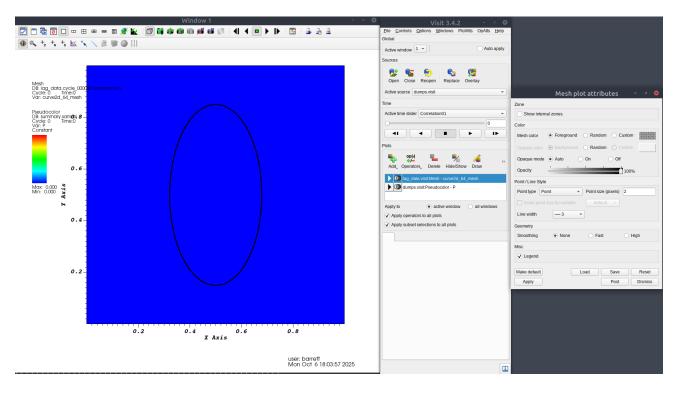
We can run this example in the same way that we ran the Navier-Stokes example

./main2d input2d

As before, we can open visit, click Open, navigate to the example directory, and open the viz_IB2d folder. In addition to the dumps.visit file, which points to the Eulerian data, it also contains a lag_data.visit file, which points to the Lagrangian data.



Open the Lagrangian file, and add a plot of the mesh by selecting Add, the Mesh, the curve2d_64_mesh. Make sure to press Draw to make the plot appear in the window. To increase the width of the line, double click the curve2d_64_mesh option to bring up the Mesh plot attributes window. You can increase the line width, then apply the changes. Also open the dumps.visit file, and add a pressure plot via the Pseudocolor option. VisIt will ask if you want to create a database correlation. These are used to correlate two separate databases and use a single time slider to move advance both databases simultaneously. If opt not to create one, you can create one later through the Controls and Database correlations tab.



As before, you can step through time by pressing the play button.

Now we will add adaptive mesh refinement to this simulation. In the build directory, open the input file, and change MAX_LEVELS from 1 to 2. This will add an additional level of refinement. Note the current refinement ratio is set to 4, so this additional level will have an equivalent uniform grid size of N = 256 points in each direction.

Before we run the simulation, we should make sure that the structure is refined as well. To do this, we need to point the IBStandardInitializer database towards a different structure file, curve2d_256. Note that all the constants computed in the database will automatically adjust for a change in grid spacing.

With the input file modified, we can rerun the example and open the visualization files as described above.

2.1 IBAMR Major Concepts

IBAMR borrows heavily from SAMRAI concepts, and in a lot of ways, is a application that lives on top of SAMRAI's data structures and algorithms.

The PatchHierarchy<NDIM> object manages all Eulerian data and the layout of data on the adaptive grid. It is composed of sequences of PatchLevel<NDIM> objects that are manage data for a specific grid spacing. Each PatchLevel<NDIM> object contains a sequence of Patch<NDIM> objects, each of which consists of a logically rectangular box of grid cells. Data on a patch is stored according to a patch data index, which is represented by an int. Associated patch data can be accessed

from by patch by the Patch<NDIM> member function getPatchData(). Note that patch data can correspond to cell, side, face, edge, or node centered data, and must be casted to the appropriate type before use. Typically, patch data indices are retrieved using the VariableDatabase<NDIM> object, which will map pairs of Variable and VariableContext to patch data indices. The typical policy of IBAMR is for Variable objects to correspond to specific state data, while VariableContext objects correspond to time points. For example, the following code will retrieve the current velocity patch index from an INSStaggeredHierarchyIntegrator object

```
auto var_db = VariableDatabase<NDIM>::getDatabase();
Pointer<SideVariable<NDIM, double>> u_var = ins_integrator->getVelocityVariable();
const int u_idx = var_db->mapVariableAndContextToIndex(u_var, ins_integrator->getCurrentContext());
```

With that patch index, we can compute various quantities on the PatchHierarchy<NDIM>. For example, we can compute the cell centered velocity magnitude by looping across all patches, interpolating velocities to cell centers, and computing the magnitude of the vector. The following code will do that.

```
Pointer<CellVariable<NDIM, double>> u_mag_var = new CellVariable<NDIM, double>("U_MAG");
auto var_db = VariableDatabase<NDIM>::getDatabase();
const int u_mag_idx = var_db->registerVariableAndContext(u_mag_var, var_db->getContext("CTX"));
for (int ln = 0; ln <= patch_hierarchy->getFinestLevelNumber(); ++ln)
{
  Pointer<PatchLevel<NDIM>> level = patch_hierarchy->getPatchLevel(ln);
  level->allocatePatchData(u_mag_idx);
  for (PatchLevel<NDIM>::Iterator p(level); p; p++)
  {
    Pointer<Patch<NDIM>> patch = level->getPatch(p());
    Pointer<CellData<NDIM, double>> u_mag_data = patch->getPatchData(u_mag_idx);
    Pointer<SideData<NDIM, double>> u_data = patch->getPatchData(u_idx);
    for (CellIterator<NDIM> ci(patch->getBox()); ci; ci++)
      const CellIndex<NDIM>& idx = ci();
      double u_mag_sq = 0.0;
      for (int axis = 0; axis < NDIM; ++axis)</pre>
        SideIndex<NDIM> up(idx, axis, 1), low(idx, axis, 0);
        double u = 0.5*((*u_data)(up) + (*u_data)(low));
        u_mag_sq += u * u;
      (*u_mag_data)(idx) = std::sqrt(u_mag_sq);
    }
  }
```

Note that we must allocate the patch data for u_mag_idx before we can use it. Patch data stored with the getCurrentContext() context is always allocated. The scratch and new context data may or may not be allocated. Efficient routines to compute various quantities can be found in the HierarchyMathOps or HierarchyDataOpsReal classes.

The major algorithms used in IBAMR are the HierarchyIntegrator objects, which know how to integrate certain equations on a PatchHierarchy. The main base integrators are

- AdvDiffHierarchyIntegrator which can integrate advection diffusion reaction equations. It can be broken down further into two subclasses
 - AdvDiffSemiImplicitHierarchyIntegrator uses a semi-implicit, method of lines approach to descritize equations.
 - AdvDiffPredictorCorrectorHierarchyIntegrator is an older integrator that does not see much use. I don't know what this does...
- INSHierarchyIntegrator which can integrate various forms of the Navier-Stokes equations. It has several subclasses
 - INSStaggeredHierarchyIntegrator is the standard Navier-Stokes integrator which uses a staggered discretization of the momentum equation, storing velocities as SideVariable<NDIM, double> type and pressure as a CellVariable<NDIM, double> type. This is the standard integrator that should be used in most applications.
 - INSCollocatedHierarchyIntegrator discretizes the momentum equation with a collocated discretization, storing velocities and pressures as CellVariable<NDIM, double> types.

- INSVCStaggeredHierarchyIntegrator discretizes the Navier-Stokes equations with spatially varying viscosity
 and density terms. Note that this utilizes the AdvDiffHierarchyIntegrator class to advect the viscosity and
 density. This class further breaks down into non-conservative and conservative discretizations.
- IBHierarchyIntegrator which can integrator the immersed boundary equations. Currently, the only concrete implementation is the IBExplicitHierarchyIntegrator class, which treats the immersed boundary explicitly in time.

To complement the integrators and provide a method to customize the equations, each integrator can handle specialized source terms, forcing functions, or strategy classes. Below covers some of the typically use cases for each of these integrator classes.

2.1.1 AdvDiffHierarchyIntegrator

Advected variables can be registered with the AdvDiffHierarchyIntegrator object to be integrated in the order in which they are registered. The advection diffusion integrators provide frameworks to set convective discretizations, variable diffusion coefficients, and source terms. For example, in navier_stokes-ex5, a temperature proxy variable used in the Boussinesq approximation is registered in the source code example.cpp:

Convective Operators: The convective discretization is typically set in the input file. For example, in navier_stokes-ex5,

the input file has the following set of options

```
the advection-diffusion solver to use (PREDICTOR_CORRECTOR or SEMI_IMPLICIT)
   ADV DIFF SOLVER TYPE
                                  "SEMI IMPLICIT
   ADV_DIFF_NUM_CYCLES
                                                    // number of cycles of fixed-point iteration
                                  "MIDPOINT_RULE"
24 ADV_DIFF_CONVECTIVE_TS_TYPE =
                                                    // convective time stepping type
                                  "PPM"
25 ADV_DIFF_CONVECTIVE_OP_TYPE =
                                                    // convective differencing discretization type
26 ADV_DIFF_CONVECTIVE_FORM
                                 TRUE
                                                    // whether to explicitly force the pressure to have mean zero
27 NORMALIZE_PRESSURE
186 AdvDiffSemiImplicitHierarchyIntegrator
                                      = START_TIME
                                      = END_TIME
       end time
                                      = GROW_DT
                                      = ADV_DIFF_NUM_CYCLES
       num_cycles
       convective_time_stepping_type = ADV_DIFF_CONVECTIVE_TS_TYPE
       convective_op_type
                                        ADV_DIFF_CONVECTIVE_OP
       convective_difference_form
                                      = ADV_DIFF_CONVECTIVE_FORM
                                      = CFL_MAX
      cfl
      dt_max
                                      = DT_MAX
       tag_buffer
                                        TAG_BUFFER
       enable_logging
                                      = ENABLE LOGGING
```

In this case, the input file sets the convective operator to use the PPM operator, discretized in ADVECTIVE_FORM, using a MIDPOINT_RULE to discretize in time.

IBAMR has several default convective operators to choose from:

- PPM uses a piecewise parabolic method,
- CUI uses a cubic upwinded interpolant method,
- WAVE_PROP uses a wave propagation method,
- CENTERED uses centered differences.

The convective terms can be integrated using MIDPOINT_RULE, TRAPEZOIDAL_RULE, or FORWARD_EULER. Note that TRAPEZOIDAL_RULE is an explicit RK2 method. Each convective operator can discretize the equations in either ADVECTIVE form: $\mathbf{u} \cdot \nabla Q$ or CONSERVATIVE form: $\nabla \cdot (\mathbf{u}Q)$.

Diffusion Coefficients: Uniform diffusion coefficients can be set by the call setDiffusionCoefficient in the AdvDiffHierarchyIr object. If no diffusion coefficient is used, or the diffusion coefficient is exactly equal to 0.0, no diffusion solver will be used. Otherwise, a Krylov solver will be used to solve the resulting implicit system, depending on the time stepping type specified.

Variable diffusion coefficients can be set by registering a variable diffusion coefficient with the AdvDiffHierarchyIntegrator object via the call registerDiffusionCoefficientVariable. Note that the variable registered must be of type SideVariable

Then, a function that specifies the value of the diffusion coefficient should be registered, followed by setting the diffusion variable of the appropriate diffused quantities. For example, assuming DiffusionCoefficient is a class that extends CartGridFunction, the following code will set a variable coefficient for the advected quantity Q_var.

```
Pointer<SideVariable<NDIM, double>> D_var = new SideVariable<NDIM, double>("D");
adv_diff_integrator->registerDiffusionCoefficientVariable(D_var);
Pointer<CartGridFunction> D_fcn = new DiffusionCoefficient();
adv_diff_integrator->setDiffusionCoefficientFunction(D_var, D_fcn);
adv_diff_integrator->setDiffusionCoefficientVariable(Q_var, D_var);
```

Source Terms: Source terms in the advection diffusion integrator can be set in a similar method. A CellVariable<NDIM, double> object must be registered with the integrator. Then, the function that specifies the source must be registered and the source term must be set for the advected variable. If SourceFunction is a class that extends CartGridFunction, the following code will set a source term for the advected quantity Q_var.

```
Pointer<CellVariable<NDIM, double>> R_var = new CellVariable<NDIM, double>("R");
adv_diff_integrator->registerSourceTerm(R_var);
Pointer<CartGridFunction> R_fcn = new SourceFunction();
adv_diff_integrator->setSourceTermFunction(R_var, R_fcn);
adv_diff_integrator->setSourceTerm(Q_var, R_var);
```

2.1.2 INSStaggeredHierarchyIntegrator

The INSHierarchyIntegrator class and derived classes generally know how to solve the Navier-Stokes equations with different data centerings or variable coefficients. Our focus here is on the INSStaggeredHierarchyIntegrator class, although the other classes function similarly. The INSStaggeredHierarchyIntegrator class discretizes the constant coefficient Navier-Stokes equations on a staggerd grid, with the velocity stored as type SideVariable<NDIM, double> and pressure as type CellVariable<NDIM, double>. These integrator classes allow for a substantial amount of customization.

Forcing Functions: The computation of the body force must be done in an extension of the CartGridFunction interface. Note the force must be evaluated in accordance with the grid spacing used for the velocity. For example, if the integrator is of type INSStaggeredHierarchyIntegrator, the data index provided to the forcing function corresponds to type SideData<NDIM, double>. The forcing function can be registered with the INSHierarchyIntegrator with the call registerBodyForceFunction.

Viscoelasticity: Viscoelastic fluids that follow a Maxwell type model can be added via the CFINSForcing class. It requires a derived class of type CFStrategy be written that can compute the right hand side of the upper convective derivative and the transformation from the advected tensor to the stress tensor. Classes for Oldroyd-B, Giesekus, and Rolie-Poly already exist in IBAMR, and can be specified by the fluid_model parameter in the input database.

The class CFINSForcing is a specific implementation of a CartGridFunction whose application of setDataOnPatchHierarchy computes the divergence of the extra stress tensor. Therefore, to add viscoelasticity to a fluid solver, one needs to register the CFINSForcing object with the INSHierarchyIntegrator via the registerBodyForceFunction function.

Boundary Conditions: Boundary conditions can be registered with the Navier-Stokes integrator. Typically, boundary conditions will be read from the input file by the class muParserRobinBcCoef, which can parse strings into mathematical functions. The input file for these conditions specify the a, b, and g coefficients on each box face, for each spatial dimension. Boundary conditions take the form of $a\mathbf{u} + b\mathbf{v} \cdot \mathbf{n} = \mathbf{g}$, in which $\mathbf{v} = -p\mathbb{I} + \frac{\mu}{2}(\nabla \mathbf{u} + \nabla \mathbf{u}^T)$ is the Newtonian stress and μ is the fluid viscosity. Current implementations require that at any physical location, the values of a and b satisfy that either a = 1 or b = 1 and that a + b = 1.

In all cases, periodic boundaries take prescendence over physical boundary conditions. Periodic conditions are specified in the CartesianGeometry database in the input file.

A typical implementation would look like this

```
vector<RobinBcCoefStrategy<NDIM>*> u_bc_coefs(NDIM, nullptr);
for (unsigned int d = 0; d < NDIM; ++d)
  {
  const std::string bc_coefs_name = "u_bc_coefs_" + std::to_string(d);
  const std::string bc_coefs_db_name = "VelocityBcCoefs_" + std::to_string(d);
  u_bc_coefs[d] = new muParserRobinBcCoefs(</pre>
```

```
bc_coefs_name, app_initializer->getComponentDatabase(bc_coefs_db_name), grid_geometry);
  }
time_integrator->registerPhysicalBoundaryConditions(u_bc_coefs);
and the corresponding input file would look like
VelocityBcCoefs_0 {
   acoef_function_0 = "1.0"
   acoef_function_1 = "1.0"
   acoef_function_2 = "1.0"
   acoef_function_3 = "1.0"
   bcoef_function_0 = "0.0"
   bcoef_function_1 = "0.0"
   bcoef_function_2 = "0.0"
   bcoef_function_3 = "0.0"
   gcoef_function_0 = "0.0"
   gcoef_function_1 = "0.0"
   gcoef_function_2 = "0.0"
   gcoef_function_3 = "0.0"
}
```

with another database for VelocityBcCoefs_1. This boundary condition sets up no slip for the horizontal component of the velocity.

2.1.3 IBHierarchyIntegrator

IBStrategy:

IBMethod:

IBFEMethod:

3 Navier Stokes Ex 5

The example navier_stokes-ex5 models stratefied layer of fluids marked by temperature differences. The Boussinesq approximation is used to compute the force of gravity on the system. The temperature of the fluid is modeled by an advection-diffusion equation

$$\frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T = D\nabla^2 T,\tag{1}$$

and an extra force is added to the momentum equation

$$\mathbf{F} = \gamma \mathbf{g}(T - T_0),\tag{2}$$

in which T_0 is the baseline temperature and \mathbf{g} is the force of gravity, here assumed to orient in the negative y direction. As before, we can navigate to the build directory and build the example

```
cd ibamr_tutorials/build && make -j4 examples
cd navier_stokes-ex1
./main2d input2d
```

If we look at the source code, we can see the BoussinesqForcing source and header files as well as the main source example.cpp. The main source code contains very similar code to that of navier-stokes_ex1, with the addition of the AdvDiffHierarchyIntegrator class that is registered with the fluid solver. This new integrator will integrate the temperature in equation (1).

As noted earlier, the variable denoting the temperature T is created and registered with the advection diffusion integrator.

Finally, a BoussinesqForcing object is registered with the integrator

```
// Set up the fluid solver.
time_integrator->registerBodyForceFunction(
new BoussinesqForcing(T_var, adv_diff_integrator, input_db->getDouble("GAMMA")));
```

As noted in the section on forces for the Navier-Stokes integrators, the class BoussinesqForcing is an extension of a CartGridFunction that can evaluate equation (2) on the patch hierarchy. On creation, it takes the variable representing the temperature, the advection diffusion integrator that manages the data, and the parameter γ , as seen in the header file

The corresponding source file BoussinesqForcing.cpp contains two important functions, setDataOnPatchHierarchy and setDataOnPatch.

In order to evaluate the force in equation (2) on cell sides, we must interpolate the cell centered data to the side of a cell, then multiple by $-\gamma$. To do the interpolation, we require one layer of ghost cells to be filled in. The function setDataOnPatchHierarchy allocates scratch data for T_var (if necessary), then fills in ghost cells using the class HierarchyGhostCellInterpolation, which contains general routines to make filling ghost cells easy. Then the function loops over levels and calls setDataOnPatchLevel, which by default will loop over patches and call setDataOnPatch.

The actual computation of the force is done in setDataOnPatch. First, the cell data corresponding to the scratch context is retrieved from the patch. Then, we loop over all cell sides whose normal points in the y direction. We interpolate the cell data to the cell side using simple averaging, and evaluate the force.

```
Pointer<CellData<NDIM, double> > T_scratch_data =

patch->getPatchData(d_T_var, d_adv_diff_hier_integrator->getScratchContext());

const Box<NDIM>& patch_box = patch->getBox();

const int axis = NDIM - 1;

for (Box<NDIM>::Iterator it(SideGeometry<NDIM>::toSideBox(patch_box, axis)); it; it++)

{

SideIndex<NDIM> s_i(it(), axis, 0);

(*F_data)(s_i) = -d_gamma * 0.5 * ((*T_scratch_data)(s_i.toCell(1)) + (*T_scratch_data)(s_i.toCell(0)));

}

return;
```

Adding a Simple Reaction System

We can add a simple reaction system to this model by adding two new advected variables R and Q. Let's say the reaction system will be

$$\frac{\partial Q}{\partial t} + \mathbf{u} \cdot \nabla Q = D_Q \nabla^2 Q - \kappa Q (1 - R),
\frac{\partial R}{\partial t} + \mathbf{u} \cdot \nabla R = D_R \nabla^2 R + \kappa Q (1 - R).$$
(3)

$$\frac{\partial R}{\partial t} + \mathbf{u} \cdot \nabla R = D_R \nabla^2 R + \kappa Q (1 - R). \tag{4}$$

To accomplish this, we need to add two advected quantities, Q and R, and write two source functions QSourceFunction and RSourceFunction. To start, we can checkout the branch that adds a skeleton for these functions.

```
cd ibamr_tutorial/ibamr_tutorial
git pull && git checkout add_source
```

In the source directory navier_stokes-ex5, there should now be two additional files QSourceFunction.h and QSourceFunction.cpp. To complete the QSourceFunction class, we need to be able to evaluate the source term in equation (3). To evaluate this term, we need the values of κ , Q, and R. Therefore, we will need to store the patch data corresponding to Q and R and have a double that corresponds to the value of κ . These will be stored as member variables of the class. We also need to update the constructor to ensure these objects are avaiable upon construction of the object

```
class QSourceFunction : public CartGridFunction
       * \brief Class constructor
      QSourceFunction(SAMRAI::tbox::Pointer<SAMRAI::pdat::CellVariable<NDIM, double> > Q var,
                     SAMRAI::tbox::Pointer<SAMRAI::pdat::CellVariable<NDIM, double> > R_var,
                     SAMRAI::tbox::Pointer<IBAMR::AdvDiffHierarchyIntegrator> adv diff hier integrator,
                     double kappa);
71
72
       Pointer<SAMRAI::pdat::CellVariable<NDIM, double> > d Q var, d R var;
       Pointer<AdvDiffHierarchyIntegrator> d adv diff hier integrator;
73
       double d kappa = std::numeric limits<double>::quiet NaN();
```

In the implementation file, we need to update the constructor to set the appropriate member variables. We also need to update the setDataOnPatch function to correctly evaluate the source function. Note we do not need ghost cell information to evaluate this function. Therefore, the code that filled ghost cells in BoussinesqForcing is not needed here.

```
QSourceFunction::QSourceFunction(Pointer<CellVariable<NDIM, double> > Q_var,
                                Pointer<CellVariable<NDIM, double> > R var
                                Pointer<AdvDiffHierarchyIntegrator> adv_diff_hier_integrator,
                                const double kappa)
   : d_Q_var(Q_var), d_R_var(R_var), d_adv_diff_hier_integrator(adv_diff_hier_integrator), d_kappa(kappa)
  // QSourceFunction
QSourceFunction::setDataOnPatch(const int data idx,
                                 Pointer<Variable<NDIM> > /*var*/,
                                 Pointer<Patch<NDIM> > patch,
                                 const double /*data time*/,
                                 const bool initial time,
                                 Pointer<PatchLevel<NDIM> > /*patch level*/)
    if (initial_time) return;
    Pointer<CellData<NDIM, double> > return data = patch->getPatchData(data idx);
    Pointer<CellData<NDIM, double> > Q data =
        patch->getPatchData(d_Q_var, d_adv_diff_hier_integrator->getCurrentContext());
    Pointer<CellData<NDIM, double> > R data =
        patch->getPatchData(d R var, d adv diff hier integrator->getCurrentContext());
    for (CellIterator<NDIM> ci(patch->getBox()); ci; ci++)
        const CellIndex<NDIM>& idx = ci();
        (*return data)(idx) = -1.0 * d kappa * (*Q data)(idx) * (1.0 - (*R data)(idx));
   / setDataOnPatch
```

We need to do the same for the class RSourceFunction. Because the function for R is the negative of the function for Q, we can simply copy the Q files.

```
cp QSourceFunction.cpp RSourceFunction.cpp cp QSourceFunction.h RSourceFunction.h
```

You will need to make sure the names inside the source and header files are changed to their appropriate class, as well as fixing the sign of the operator. We also need to update the CMakeLists.txt to ensure that the files are compiled.

```
IBAMR ADD EXAMPLE(
      TARGET NAME
17
18
      OUTPUT DIRECTORY
         ${CMAKE BINARY DIR}/navier stokes-ex5"
19
20
21
22
23
24
25
26
27
28
29
      OUTPUT NAME
        main2d
      EXAMPLE GROUP
        examples
      SOURCES
        QSourceFunction.cpp RSourceFunction.cpp BoussinesqForcing.cpp example.cpp
      LINK TARGETS
        IBAMR::IBAMR2d
      INPUT FILES
        input2d
```

Finally, we need to update the main driver to create and register two cell centered variables with the advection diffusion integrator. First, we add the header files to the main routine.

```
37 // Set up application namespace declarations
38 #include <ibamr/app_namespaces.h>
39
40 // Application objects
41 #include "BoussinesqForcing.h"
42 #include "QSourceFunction.h"
43 #include "RSourceFunction.h"
```

Next, we create cell variables corresponding to Q and R. We need to register them with the advection-diffusion solver as well as set coefficients, set advection velocities, and specify boundary and initial conditions. By default, initial conditions are set to 0 and boundary conditions default to linear extrapolation from interior values.

Finally, we need to create source variables that correspond to the sources for Q and R. We register these with the advection-diffusion integrator, as well as register functions that set the source terms. As shown below, when we create the source functions, the rate constant is being read from the input file.

```
Pointer<CellVariable<NDIM, double> > R_var = new CellVariable<NDIM, double>("R");
adv diff integrator->registerTransportedQuantity(Q_var);
adv diff integrator->registerTransportedQuantity(R_var);
adv_diff_integrator->setDiffusionCoefficient(Q_var, input_db->getDouble("Q_DIFF_COEF"));
adv_diff_integrator->setDiffusionCoefficient(R_var, input_db->getDouble("R_DIFF_COEF"));
adv_diff_integrator->setAdvectionVelocity(Q_var, time_integrator->getAdvectionVelocityVariable());
adv_diff_integrator->setAdvectionVelocity(R_var, time_integrator->getAdvectionVelocityVariable());
Pointer<CellVariable<NDIM, double> > Q_src_var = new CellVariable<NDIM, double>("Q_SRC");
Pointer<CellVariable<NDIM, double> > R_src_var = new CellVariable<NDIM, double>("R_SRC");
adv_diff_integrator->registerSourceTerm(Q_src_var);
adv_diff_integrator->registerSourceTerm(R_src_var);
adv_diff_integrator->setSourceTermFunction(
     Q src var, new QSourceFunction(Q var, R var, adv diff integrator, input db->getDouble("RATE")))
adv_diff_integrator->setSourceTermFunction(
R_src_var, new RSourceFunction(Q_var, R_var, adv_diff_integrator, input_db->getDouble("RATE")));
adv_diff_integrator->setSourceTerm(Q_var, Q_src_var);
adv diff integrator->setSourceTerm(R var, R src var);
adv diff integrator->setInitialConditions(
     Q var,
     new muParserCartGridFunction(
          "Q init", app initializer->getComponentDatabase("QInitialConditions"), grid geometry));
```

With this, we can compile and run the new example as before. Make sure you edit the input file to specify the rate parameter RATE and the diffusion coefficients Q_DIFF_COEF and R_DIFF_COEF.

```
cd ibamr_tutorials/build && make -j4 examples
cd navier_stokes-ex5
./main2d input2d
```