April 2023 Final Exams ELECENG 3N03

### Some equations you may need:

### **Diodes**

$$I_F = \frac{V_{bias}}{R_{Limit}}$$

Ideal diode model

$$I_{F} = \frac{V_{bias} - V_{F}}{R_{Limit}}$$

Practical diode model

$$I_F = \frac{V_P}{\pi}$$

Half wave average value

$$I_{\rm F} = \frac{2V_P}{\pi}$$

Full wave average value

$$PIV = V_{P(in)}$$

Peak inverse voltage, half wave rectifier

$$PIV=2V_{P(in)} + 0.7 V$$

Peak inverse voltage, center tapped rectifier

$$PIV = V_{P(out)} + 0.7 V$$

Peak inverse voltage, bridge rectifier

$$V_{p(out)} = V_{P(sec)} - 1.4 V$$

Bridge full wave output

$$V_{n(out)} = V_P - 0.7 V$$

Peak half wave rectifier output (silicon)

$$V_{p(out)} = \frac{V_{sec}}{2} - 0.7 V$$

Center tapped full wave output

Ripple factor(r) = 
$$\frac{V_{r(pp)}}{V_{DC}}$$

Line regulation =  $\left(\frac{\Delta V_{out}}{\Delta V_{in}}\right) 100\%$ 

Load regulation =  $\left(\frac{V_{NL} - V_{FL}}{V_{FL}}\right)$  100%

Zener impedance  $(Z_z) = \frac{\Delta V_z}{\Delta I_z}$ 

# OP-AMP

 $CMRR = \frac{A_{ol}}{A_{cm}}$ 

Common-mode rejection ratio

 $CMRR = 20 \log \left( \frac{A_{ol}}{A_{Cm}} \right)$ 

Common-mode rejection ratio (dB)

Slew rate=  $\frac{\Delta V_{out}}{\Delta t}$ 

Slew rate

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$$A_{cl(NI)} = 1 + \frac{R_f}{R_i}$$

Voltage gain (non-inverting)

$$A_{cl(VF)} = 1$$

Voltage gain (follower)

$$A_{cl(I)} = -\frac{R_f}{R_i}$$

Voltage gain (inverting)

$$V_{UTP} = \frac{R_2}{R_1 + R_2} \left( + V_{\text{out(max)}} \right)$$

Upper trigger point

$$V_{LTP} = \frac{R_2}{R_1 + R_2} \left( -V_{out}(max) \right)$$

Lower trigger point

$$V_{HYS} = V_{UTP} - V_{LTP}$$

Hysteresis voltage

$$V_{out} = -(V_{IN1} + V_{IN2} + ... + V_{INn})$$

*n*-input adder

$$V_{out} = -\frac{R_f}{R_i}(V_{IN1} + V_{IN2} + ... + V_{INn})$$

Adder with gain)

$$V_{out} = -\left(\frac{R_f}{R_1}V_{IN1} + \frac{R_f}{R_2}V_{IN2} + \dots + \frac{R_f}{R_n}V_{INn}\right)$$

Scaling adder with gain

$$\frac{\Delta V_{out}}{\Delta t}$$
  $-\frac{V_{in}}{R_i C}$ 

Integrator output rate of change

$$V_{out} = -\left(\frac{V_c}{t}\right) R_f C$$

Differentiator output voltage with ramp input

### JFET & MOSFET

1. 
$$I_D \cong I_{DSS} (1 - \frac{v_{GS}}{v_{GS(off)}})^2$$

2. 
$$g_m = g_{m0} (1 - \frac{v_{GS}}{v_{GS(off)}})$$

3. 
$$g_{m0} = \frac{2I_{DSS}}{|V_{GS(off)}|}$$

4. 
$$I_D = K(V_{GS} - V_{GS(th)})^2$$

5. 
$$g_m = \frac{\Delta I_D}{\Delta V_{GS}}$$

5. 
$$g_m = \frac{\Delta I_D}{\Delta V_{GS}}$$
  
6.  $R_{IN} = |\frac{V_{GS}}{I_{GSS}}|$ 

7. Self Bias (n-channel J-FET):

$$V_{DS} = V_{DD} - I_D(R_D + R_S)$$
  
8.  $R_S = |\frac{V_{GS}}{I_D}|$ 

$$8. R_S = \left| \frac{v_{GS}}{I_D} \right|$$

9. 
$$R_{DS} \cong \frac{V_{DS}}{I_D}$$

10.  $V_{GS} = (\frac{R_2}{R_1 + R_2}) V_{DD}$ 

E-MOSFET voltage divider bias

#### 11. D-MOSFET:

$$V_{DS} = V_{DD} - I_{DSS}R_D$$

#### Common source amplifier

### (JFET self bias)

- 1.  $I_D = I_{DSS} (1 \frac{I_D R_S}{V_{GS(off)}})^2$
- $2. \quad A_V = -g_m R_d$
- 3.  $R_{in} = R_G ||(\frac{V_{GS}}{I_{GSS}})$

#### **D-MOSFET zero bias**

- 1.  $I_D = I_{DSS}$
- 2.  $A_V = g_m R_d$ 3.  $R_{in} = R_G || (\frac{V_{GS}}{I_{GSS}})$

### **E-MOSFET voltage divider bias**

- 1.  $I_D = K(V_{GS} V_{GS(th)})^2$
- $2. \quad A_V = g_m R_d$
- 3.  $R_{in} = R_1 || R_2 || (\frac{V_{GS}}{I_{GSS}})$

#### Common drain amplifier

#### (JFET self bias)

- 1.  $I_D = I_{DSS} (1 \frac{V_{GS}}{V_{GS(off)}})^2$
- $2. \quad A_V = \frac{g_m R_s}{1 + g_m R_s}$
- 3.  $R_{in} = R_G || (\frac{V_{GS}}{I_{GSS}})$

#### **Common gate Amplifier**

### (JFET self bias)

- 1.  $I_D = I_{DSS} (1 \frac{I_D R_S}{V_{GS(off)}})^2$
- $2. \quad A_V = g_m R_d$
- 3.  $R_{in} = (\frac{1}{g_m})||(R_s)||$

### **Cascode amplifier**

### (Common gate amplifier)

1. 
$$A_V \cong g_{m(CG)}X_L$$

### **Bipolar Junction Transistors**

$$1. \quad I_E = I_C + I_B$$

$$2. \quad \beta_{DC} = \frac{I_C}{I_B}$$

3. 
$$V_{EE} \cong 0.7 V$$

$$4. \quad I_B = \frac{V_{BB} - V_{BE}}{R_B}$$

$$5. \quad V_{CE} = V_{CC} - I_C R_C$$

6. 
$$V_{CB} = V_{CE} - V_{BE}$$
  
7.  $A_V \cong \frac{R_C}{r_e'}$ 

7. 
$$A_V \cong \frac{R_C}{r_e'}$$

8. 
$$V_{CE(cutoff)} = V_{CC}$$

9. 
$$I_{C(sat)} = \frac{V_{CC} - V_{CE(sat)}}{R_C}$$

$$10. I_{B(min)} = \frac{I_{C(sat)}}{\beta_{DC}}$$

Transistor currents

DC current gain

Base-to-emitter voltage (silicon)

Base current

Collector-to-emitter voltage (common-emitter)

Collector-to-base voltage

Approximate ac voltage gain

**Cutoff** condition

Collector saturation current

Minimum base current for saturation

# **BJT Bias Circuits**

# **Voltage-Divider Bias**

1. 
$$V_B \cong \left(\frac{R_2}{R_1 + R_2}\right) V_{CC}$$

$$2. \quad V_E = V_B - V_{BE}$$

3. 
$$I_C \cong I_E = \frac{V_E}{R_E}$$

$$4. \quad V_C = V_{CC} - I_C R_C$$

5. 
$$R_{IN(BASE)} = \frac{\beta_{DC} V_B}{I_E}$$

6. 
$$I_E = \frac{V_{TH} - V_{BE}}{R_E + R_{TH} / \beta_{DC}}$$
7.  $I_E = \frac{-V_{TH} + V_{BE}}{R_E + R_{TH} / \beta_{DC}}$ 
8.  $I_E = \frac{V_{TH} + V_{BE} - V_{EE}}{R_E + R_{TH} / \beta_{DC}}$ 

7. 
$$I_E = \frac{-V_{TH} + V_{BE}}{R_E + R_{TH}/\beta_{DC}}$$

8. 
$$I_E = \frac{V_{TH} + V_{BE} - V_{EE}}{R_E + R_{TH}/\beta_{DC}}$$

For a stiff voltage divider

#### **Emitter Bias**

9. 
$$I_E = \frac{-V_{EE} - V_{BE}}{R_E + R_B/\beta_{DC}}$$

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#### **Base Bias**

10. 
$$V_{CE} = V_{CC} - I_C R_C$$
11. 
$$I_C = \beta_{DC} \left( \frac{V_{CC} - V_{BE}}{R_B} \right)$$

### **Emitter-Feedback Bias**

12. 
$$I_E = \frac{V_{CC} - V_{BE}}{R_E + R_B / \beta_{DC}}$$

#### **Collector-Feedback Bias**

13. 
$$I_C = \frac{V_{CC} - V_{BE}}{R_C + R_B / \beta_{DC}}$$
  
14.  $V_{CE} = V_{CC} - I_C R_C$ 

# **BJT Amplifiers**

$r_e' \cong \frac{25mV}{L_p}$	Internal ac emitter resistance

#### **Common-Emitter**

Common-Emitter	
$R_{in(tot)} = R_1   R_2  R_{in(base)}$	Total amplifier input resistance, voltage-divider bias
$R_{in(base)} = \beta_{ac} r_e'$	Input resistance at base
$R_{out} \cong R_C$	Output resistance
$A = \frac{R_C}{R_C}$	Voltage gain base to collector unloaded

$$A_v = \frac{R_c}{r_e'}$$
 Voltage gain, base-to-collector, unloaded

$$A_v = \frac{R_C}{r'_e + R_E}$$
 Voltage gain without bypass capacitor

$$A_v = \frac{R_c}{r_e'}$$
 Voltage gain, base-to-collector, loaded, bypassed  $R_E$ 

$$A_v \cong \frac{R_C}{R_{E1}}$$
 Voltage gain, swamped amplifier

$$R_{in(base)} = \beta_{ac}(r'_e + R_{E1})$$
 Input resistance at base, swamped amplifier

$$A_i = \frac{I_c}{I_s}$$
 Current gain, input source to collector

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$$A_p = A_v' A_i$$

Power gain

### **Common-Collector (Emitter-Follower)**

$$A_v\cong 1$$

Voltage gain, base-to-emitter

$$R_{in(base)} \cong \beta_{ac} R_e$$

Input resistance at base, loaded

$$R_{out} = \left(\frac{R_s}{\beta_{ac}}\right) || R_E$$

Output resistance

$$A_i = \frac{I_e}{I_{in}}$$

Current gain

$$A_p \cong A_i$$

Power gain

$$R_{in} = \beta_{ac1}\beta_{ac2}R_E$$

Input resistance, Darlington pair

# **Common-Base**

$$A_v \cong \frac{R_c}{r_e'}$$

Voltage gain, emitter-to-collector

$$R_{in(emitter)} \cong r'_e$$

Input resistance at emitter

$$R_{out} \cong R_C$$

Output resistance

$$A_i \cong 1$$

Current gain

$$A_p \cong A_v$$

Power gain

# **Multistage Amplifier**

$$A'_{v} = A_{v1}A_{v2}A_{v3} \dots A_{v}$$

Overall voltage gain

$$A_{v(dB)} = 20 \log A_v$$

Voltage gain expressed in dB