

### In-Class Test (#3)

Name \_\_\_\_\_  
Student Number \_\_\_\_\_

ROBOTICS 4K03

INSTRUCTOR NAME: Fengjun Yan

DURATION OF EXAMINATION: 50 MINS

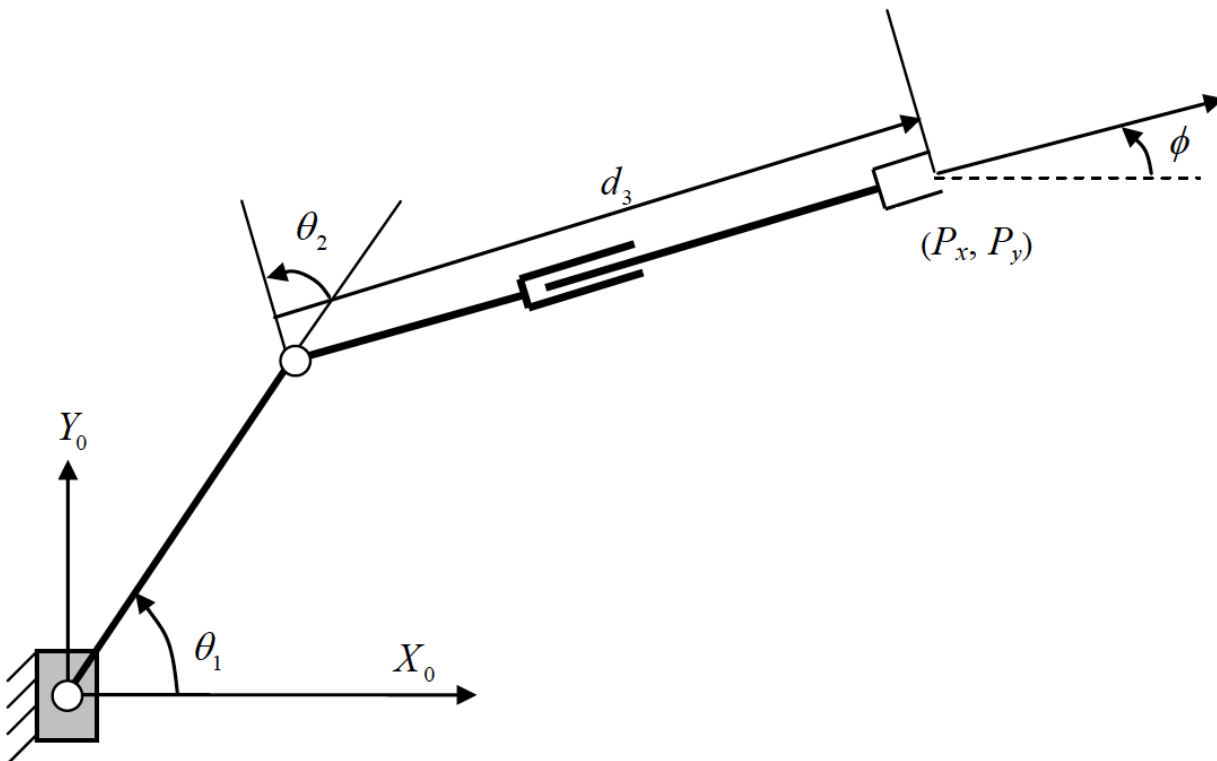
Nov. 15th, 2021

THIS EXAMINATION PAPER INCLUDES 2 PAGES AND 2 QUESTIONS.

Use of Casio FX-991 calculator.

Questions:

1. (45 points) A RRP planar robot is shown in the following figure. Its joint variables are  $\theta_1$  and  $\theta_2$ , and  $d_3$ . Its end-effector position and orientation are given by  $P_x$  and  $P_y$ , and  $\phi$ . Derive the inverse kinematics equations for this robot.



2. (55 points)

The planar PPR robot shown in the figure operates in the vertical plane (*i.e.* gravity acts in the  $-Y_0$  direction). The masses of the links are concentrated at points A, B and C as shown.

Derive the Lagrangian function  $L$  and calculate the force/torque for the  $i$ th joint only. ( $i$  depends on the first letter of your Last Name:  $i=1$ , when the first letter of your Last Name is from A-I;  $i=2$ , when the first letter of your Last Name is from J-R;  $i=3$ , when the first letter of your Last Name is from S-Z)

