

FINAL EXAM

newa
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1. 1) Hard automation: specialised machines for high-volume manufacturing (i.e., assembly line)

2) Flexible automation: robots in place of specialised machines used in hard automation.

3) Planar robot: robot whose end-effector's motion is limited to a single plane

4) Dextrous workspace: volume of space the end-effector can reach with any desired orientation

2: 1) ${}^C T_D, {}^A T_B, {}^A T_E, {}^E T_D \rightarrow {}^B T_C = ?$

$${}^B T_C = ({}^A T_B)^{-1} \cdot {}^A T_E \cdot {}^E T_D \cdot ({}^C T_D)^{-1}$$

2) Lap 1, $M = \begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$ $S = -1(4) + 5 = 1$

$$f_{85} = \frac{1}{1} | (75(0) + 75(-1) + 75(0) + 130(-1) + 5(75) + 130(-1) + 75(0) + 75(-1) + 75(0)) |$$

$$f_{85} = |-35| = 35$$

3) $A = \text{Trans}(3, 3, 2) * \text{Rot}(Z, 39.7^\circ)$ \therefore it is a valid representation of a frame. the others do not match the transformation matrices.

C not valid bc $\text{Trans}(3, 0.5, 15) * \text{Rot}(Z, -90) * \text{Rot}(X, 30) = \begin{bmatrix} 0 & \sqrt{3}/2 & -1/2 & 3 \\ -1 & 0 & 0 & 0.5 \\ 0 & 1/2 & \sqrt{3}/2 & 15 \\ 0 & 0 & 0 & 1 \end{bmatrix}$

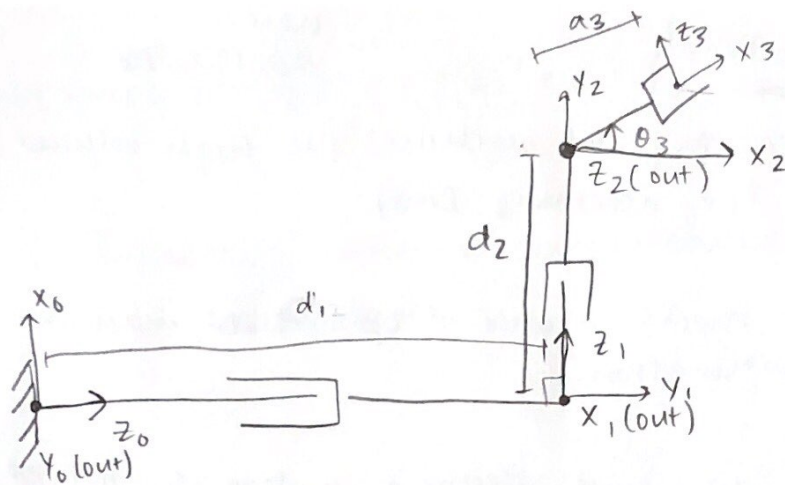
B not valid bc $(\text{Rot}(Z, -90)^{-1} * (\text{Trans}(3, 0.5, 2)^{-1}) * B$
 \Rightarrow see next pg

$$3) (Rot(z, -90)^{-1}) * Trans(3, 0.5, 2)^{-1} * B = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \sqrt{3}/2 & 0 & 0 \\ 0 & 0.5 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

↳ doesn't match a translation/rotation matrix

∴ invalid

3, a)



b)

i	θ_i	d_i	a_i	α_i
1	90°	d_1^*	0	90°
2	90°	d_2^*	0	90°
3	θ_3^*	0	a_3	-90°

joint variables are starred w *

c) See diagram in a

d) by the formula to calculate A matrices from DH parameters:

$$A_1 = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & d_1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$A_2 = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & d_2 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$A_3 = \begin{bmatrix} \cos \theta_3 & 0 & -\sin \theta_3 & a_3 \cos \theta_3 \\ \sin \theta_3 & 0 & \cos \theta_3 & a_3 \sin \theta_3 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T = A_1 * A_2 * A_3$$

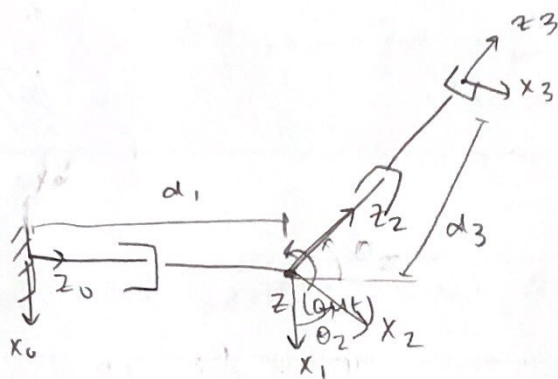
$$T = \begin{bmatrix} \sin \theta_3 & 0 & \cos \theta_3 & d_2 + a_3 \sin \theta_3 \\ 0 & -1 & 0 & 0 \\ \cos \theta_3 & 0 & \sin \theta_3 & d_1 + a_3 \cos \theta_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

3.e) $\phi = \theta_3$

$$P_z = d_1 + c\theta_3 \rightarrow d_1 = P_z - a_3 c\phi$$

$$P_x = d_2 + s\theta_3 \rightarrow d_2 = P_x - a_3 s\phi$$

4.a)



θ_i	d_i	a_i	α_i
θ_1	d_1	0	90°
θ_2	0	0	-90°
0	d_3	0	0°

Say the robot operates in the xy plane $\vec{y} \rightarrow x$

by the formula:

$$T = \begin{bmatrix} c\theta_2 & 0 & -s\theta_2 & -d_3 s\theta_2 \\ 0 & 1 & 0 & 0 \\ s\theta_2 & 0 & c\theta_2 & d_1 + d_3 c\theta_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$P_y = d_3 s\theta_2$$

$$P_x = d_1 + d_3 c\theta_2$$

$$P_z = 0$$

$$J(q) = \begin{bmatrix} \frac{\partial P_x}{\partial d_1} & \frac{\partial P_x}{\partial \theta_2} & \frac{\partial P_x}{\partial d_3} \\ \frac{\partial P_y}{\partial d_1} & \frac{\partial P_y}{\partial \theta_2} & \frac{\partial P_y}{\partial d_3} \\ z_1 z_0 & z_2 z_1 & z_3 z_2 \end{bmatrix} = \begin{bmatrix} 1 & -d_3 s\theta_2 & c\theta_2 \\ 0 & d_3 c\theta_2 & s\theta_2 \\ 0 & 1 & 0 \end{bmatrix}$$

$z_1 = z_3 = 0$ \rightarrow prismatic

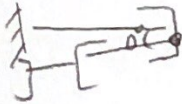
$z_2 = 1$ \rightarrow revolute

$$\begin{bmatrix} \dot{V}_x \\ \dot{V}_y \\ \dot{w}_2 \end{bmatrix} = J(q) \begin{bmatrix} \dot{d}_1 \\ \dot{\theta}_2 \\ \dot{d}_3 \end{bmatrix}$$

b) $|J(q)| = -\sin(\theta_2)$

$-\sin(\theta_2) = 0$ when $\theta_2 = 0, 180^\circ$

4. c)



OR



translation in the y-axis & rotation in z are the two lost DOF

5. Horizontal plane \rightarrow assume $g(q) = 0$.

a)
$$\begin{aligned} P_x &= 0.3 \cos \theta_2 + 0.4 \cos \theta_1 \\ P_y &= 0.3 \sin \theta_2 + 0.4 \sin \theta_1 \end{aligned} \quad \left\{ \begin{aligned} J(q) &= \begin{bmatrix} \frac{\partial P_x}{\partial \theta_1} & \frac{\partial P_x}{\partial \theta_2} \\ \frac{\partial P_y}{\partial \theta_1} & \frac{\partial P_y}{\partial \theta_2} \\ 3_1 z_0 & 3_2 z_1 \end{bmatrix} \end{aligned} \right. \quad \begin{aligned} a_1 &= 0.4 \text{ m } \theta_1 = 35^\circ \\ a_2 &= 0.3 \text{ m } \theta_2 = -75^\circ \end{aligned}$$

$$J(0, \theta) = \begin{bmatrix} -0.3 \sin(35 - 75) - 0.4 \sin(35) & -0.3 \sin(35 - 75) \\ 0.3 \cos(35 - 75) + 0.4 \cos(35) & 0.3 \cos(35 - 75) \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} -0.0366 & 0.1928 \\ 0.5575 & 0.2298 \\ 1 & 1 \end{bmatrix}$$

$$F = \begin{bmatrix} 20 \\ -15 \end{bmatrix} \quad Z = (J(\theta_1, \theta_2))^T F = \begin{bmatrix} -0.0366 & 0.5575 \\ 0.1928 & 0.2298 \end{bmatrix} \begin{bmatrix} 20 \\ -15 \end{bmatrix} = \begin{bmatrix} -9.10 \\ 0.41 \end{bmatrix} \text{ Nm}$$

b) $F = (J(q)^{-1})^T (Z - g(q)) \quad Z = [10 \ 5]^T$

$$F = [J(\theta_1, \theta_2)^{-1}]^T Z = \begin{bmatrix} -1.9827 & 4.8095 \\ 1.6637 & 0.3157 \end{bmatrix} \begin{bmatrix} 10 \\ 5 \end{bmatrix} = \begin{bmatrix} 4.22 \\ 18.22 \end{bmatrix} \text{ N}$$

$$J^{-1}(q) = \frac{1}{(0.3)(0.4)(5(-75))} \begin{bmatrix} 0.2298 & -0.1928 \\ -0.5575 & -0.0366 \end{bmatrix} = \begin{bmatrix} -1.9827 & 1.6637 \\ 4.8095 & 0.3157 \end{bmatrix}$$