

# Table of Laplace Transforms

| $f(t) = \mathcal{L}^{-1}\{F(s)\}$                           | $F(s) = \mathcal{L}\{f(t)\}$   | $f(t) = \mathcal{L}^{-1}\{F(s)\}$                         | $F(s) = \mathcal{L}\{f(t)\}$                                      |
|---|--|---|---|
| 1. 1  | $\frac{1}{s}$  | 2. $e^{at}$   | $\frac{1}{s-a}$   |
| 3. $t^n, n=1,2,3,\dots$                                     | $\frac{n!}{s^{n+1}}$   | 4. $t^p, p > -1$  | $\frac{\Gamma(p+1)}{s^{p+1}}$                                     |
| 5. $\sqrt{t}$   | $\frac{\sqrt{\pi}}{2s^{3/2}}$  | 6. $t^{n-1/2}, n=1,2,3,\dots$                             | $\frac{1 \cdot 3 \cdot 5 \cdots (2n-1)\sqrt{\pi}}{2^n s^{n+1/2}}$ |
| 7. $\sin(at)$   | $\frac{a}{s^2+a^2}$  | 8. $\cos(at)$   | $\frac{s}{s^2+a^2}$   |
| 9. $t \sin(at)$   | $\frac{2as}{(s^2+a^2)^2}$  | 10. $t \cos(at)$  | $\frac{s^2-a^2}{(s^2+a^2)^2}$                                     |
| 11. $\sin(at) - at \cos(at)$                                | $\frac{2a^3}{(s^2+a^2)^2}$   | 12. $\sin(at) + at \cos(at)$                              | $\frac{2as^2}{(s^2+a^2)^2}$                                       |
| 13. $\cos(at) - at \sin(at)$                                | $\frac{s(s^2-a^2)}{(s^2+a^2)^2}$   | 14. $\cos(at) + at \sin(at)$                              | $\frac{s(s^2+3a^2)}{(s^2+a^2)^2}$                                 |
| 15. $\sin(at+b)$  | $\frac{s \sin(b) + a \cos(b)}{s^2+a^2}$  | 16. $\cos(at+b)$  | $\frac{s \cos(b) - a \sin(b)}{s^2+a^2}$                           |
| 17. $\sinh(at)$   | $\frac{a}{s^2-a^2}$  | 18. $\cosh(at)$   | $\frac{s}{s^2-a^2}$   |
| 19. $e^{at} \sin(bt)$                                       | $\frac{b}{(s-a)^2+b^2}$  | 20. $e^{at} \cos(bt)$                                     | $\frac{s-a}{(s-a)^2+b^2}$   |
| 21. $e^{at} \sinh(bt)$                                      | $\frac{b}{(s-a)^2-b^2}$  | 22. $e^{at} \cosh(bt)$                                    | $\frac{s-a}{(s-a)^2-b^2}$   |
| 23. $t^n e^{at}, n=1,2,3,\dots$                             | $\frac{n!}{(s-a)^{n+1}}$   | 24. $f(ct)$   | $\frac{1}{c} F\left(\frac{s}{c}\right)$                           |
| 25. $u_c(t) = u(t-c)$<br><a href="#">Heaviside Function</a> | $\frac{e^{-cs}}{s}$  | 26. $\delta(t-c)$<br><a href="#">Dirac Delta Function</a> | $e^{-cs}$   |
| 27. $u_c(t) f(t-c)$   | $e^{-cs} F(s)$   | 28. $u_c(t) g(t)$   | $e^{-cs} \mathcal{L}\{g(t+c)\}$                                   |
| 29. $e^{at} f(t)$   | $F(s-c)$   | 30. $t^n f(t), n=1,2,3,\dots$                             | $(-1)^n F^{(n)}(s)$   |
| 31. $\frac{1}{t} f(t)$                                      | $\int_s^\infty F(u) du$  | 32. $\int_0^t f(v) dv$                                    | $\frac{F(s)}{s}$  |
| 33. $\int_0^t f(t-\tau) g(\tau) d\tau$                      | $F(s) G(s)$  | 34. $f(t+T) = f(t)$                                       | $\frac{\int_0^T e^{-st} f(t) dt}{1-e^{-sT}}$                      |
| 35. $f'(t)$   | $sF(s) - f(0)$   | 36. $f''(t)$  | $s^2 F(s) - sf'(0) - f''(0)$                                      |
| 37. $f^{(n)}(t)$  | $s^n F(s) - s^{n-1} f(0) - s^{n-2} f'(0) - \dots - sf^{(n-2)}(0) - f^{(n-1)}(0)$ |   |   |