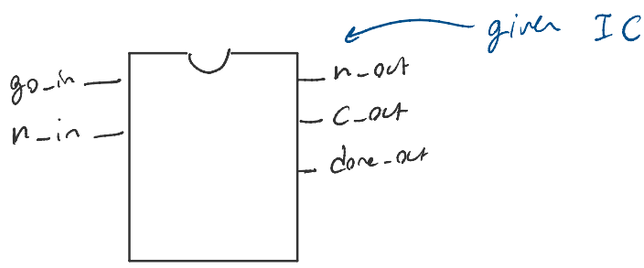
MR - Stop

April 11, 2022 5:42 PM

→ collatz algorithm

$$C_{n+1} = \begin{cases} C_n/2 & \text{if } x\%2 = 0 \\ 3(C_n)+1 & \text{if } x\%2 = 1 \end{cases}$$

→ collatz conjecture: if you perform collatz algorithm on a number enough, you will reach 1



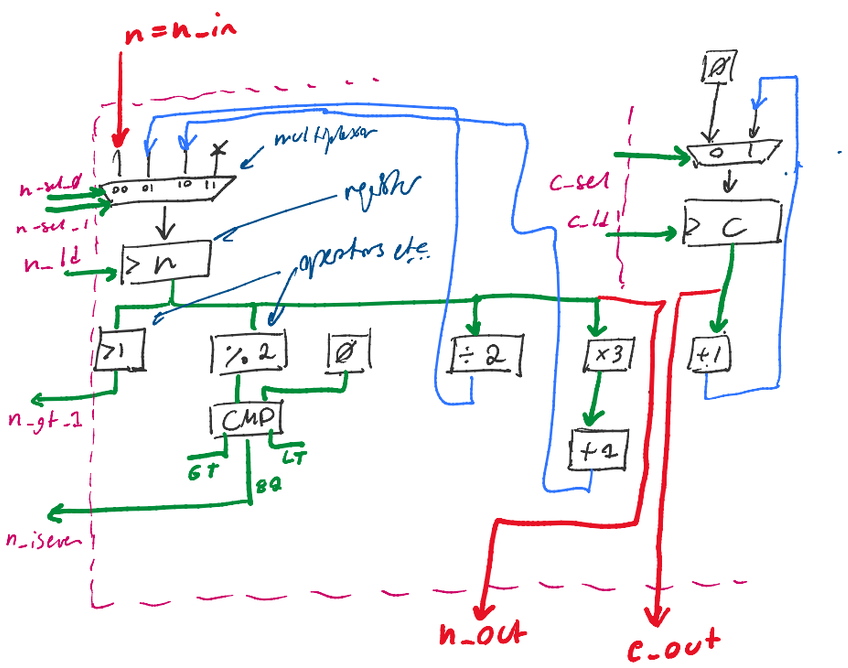
Algorithm design

```
while (1) {
    while (!go_in);
    n = n_in;
    c = 0;
    while (n > 1) {
        if (n % 2 == 0) {
            n = n / 2;
        } else {
            n = 3 * n + 1;
        }
        count++;
    }
    done_out = 1;
}
```

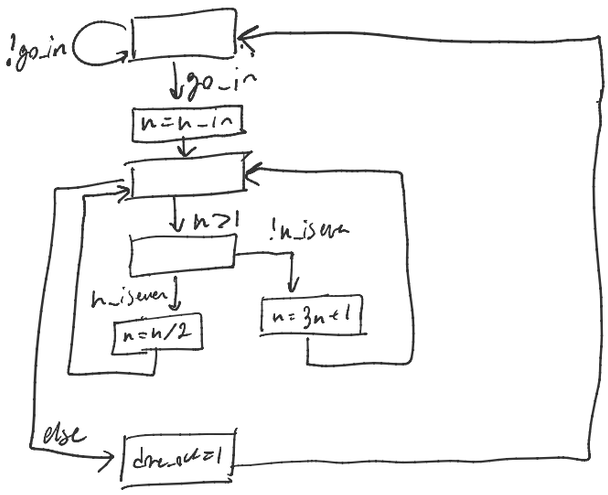
Datapath

optimization

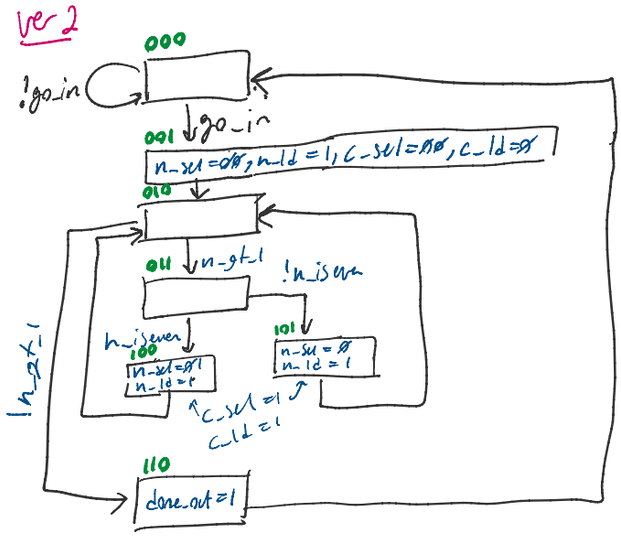
→ typically: boolean signals are control signals
→ ints & floats are data



FSM



ver 2



label states

3-bit state register

State table

X = inputs don't care

☆ = output don't care

needs eqns for these

state register $Q_2Q_1Q_0$	go_in	n_sel	c_sel	n_ld	c_ld	done_out	n_gt_1	n_is_even	new state register values $I_2I_1I_0$
000	0	XX	X	0	0	0	☆	☆	000
000	1	XX	X	0	0	0	☆	☆	001
001	1	00	0	1	1	0	☆	☆	010
010	X	XX	X	0	0	0	0	☆	110
010	X	X X	X	0	0	0	1	☆	011
011	X	X X	X	0	0	0	☆	0	101
011	X	X X	X	0	0	0	☆	1	100
100	X	01	1	1	1	0	☆	☆	010
101	X	10	1	1	1	0	☆	☆	010
110	X	XX	X	0	0	1	☆	☆	000

Eqns

$done\_out = Q_2 Q_1 \overline{Q_0}$

$n\_ld = c\_ld = (Q_2 + Q_0)\overline{Q_1}$

$Q_2Q_1Q_0$: 001, 100, 101

$c\_sel = \overline{Q_2}\,\overline{Q_1}\,Q_0$