

Abigail Nervo
400170276

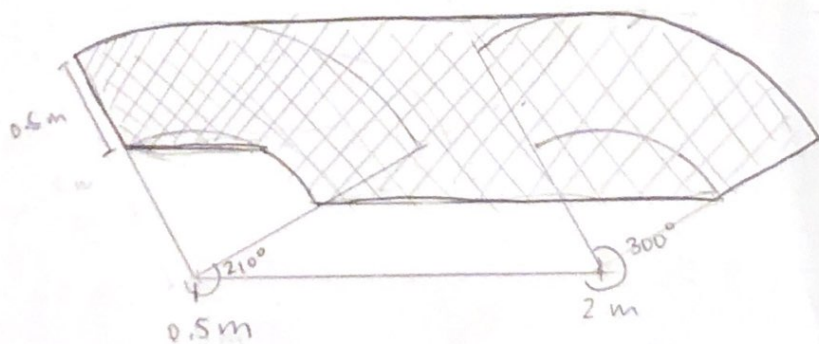
ME 4K03 TEST 1

Q1

1. End effector: the part of the robot that interacts with the environment attached to the last joint of the robot.
2. Repeatability: precision - how well the robot can be positioned in the same place repeatedly
3. Dextrous workspace: the volume of space the end-effector can reach with any orientation
4. Major axes: the first 3 joints of the robot.

Q2

$0.5 \text{ m} = 2 \text{ cm}$



Q3

a) let transformation matrix $T = I$

$$T = \text{Rot}(60^\circ, X) * \text{Rot}(Y, -45^\circ) * I * \text{Trans}(2, -4, 5)$$

$$T = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0.5 & -0.866 & 0 \\ 0 & 0.866 & 0.5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 0.707 & 0 & -0.707 & 0 \\ 0 & 1 & 0 & 0 \\ 0.707 & 0 & 0.707 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & -4 \\ 0 & 0 & 5 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T = \begin{bmatrix} 0.707 & 0 & -0.707 & -2.12 \\ -0.612 & 0.5 & -0.612 & -6.28 \\ 0.353 & 0.866 & 0.353 & -0.99 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

b) we have $T = \text{Rot}(60^\circ, X) * \text{Rot}(Y, -45^\circ) * I * \text{Trans}(2, -4, 5)$

we want $T = \text{Rot}(Y, -45^\circ) * I * \text{Trans}(2, -4, 5) * X$

$$\text{Trans}(2, -4, 5)^{-1} * \text{Rot}(Y, -45^\circ)^{-1} * T = X$$

So we have:

$$T = \text{Rot}(Y, -45^\circ) * I * \text{Trans}(2, -4, 5) * \underbrace{\text{Trans}(2, -4, 5)^{-1} * \text{Rot}(Y, -45^\circ)^{-1}}_{\text{transformation matrix relative to current frame in step 3}} * T$$