Convolutional Neural Networks



Taken by Zach Machcek: https://unsplash.com/@zmachacel

Overall Approach

- Dataset is very large
 - Large number of samples
 - Large size of each sample
 - Large number of classes

 Not practical to learn and explore different models and implementations using the entire dataset

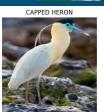
- My approach:
 - Explore and Learn on subset of the data
 - Implement "best" model on full dataset
- Goals:
 - Learn and gain confidence in using and understanding CNNs
 - Strengthen understanding of classification tasks
 - Develop an end to end understanding of a somewhat daunting task

The Dataset: The Ultimate Goal

- 515 bird species/classes
- 82,724 training samples
- 2,586 batches of batch size 32
- Each image of size 224 x 224
- 3rd order tensor (3D array) of 8 bit ints
- 2,575 test images
- 2,575 validation images (5 images per species)

Distribution of data: See Appendix 2











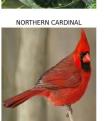














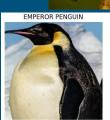


The Dataset: Trimmed

- 100 bird species/classes
- 15,824 training samples
- 495 batches of batch size 32
- Each image of size 224 x 224
- 3rd order tensor (3D array) of 8 bit ints
- 500 test and validation images (5 images per species)

Distribution of data: See Appendix 2









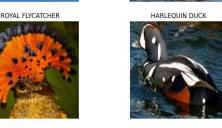








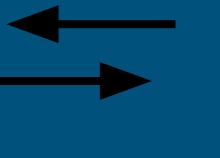


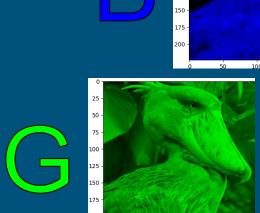


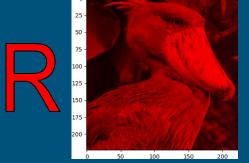


The Images









RGB

CNN for Image Classification

- Convolution
 Layer
- 2. Pooling Layer
- Fully Connected Layer

Some other layers:

- Batch Normalization
- Dropout
- Flattening

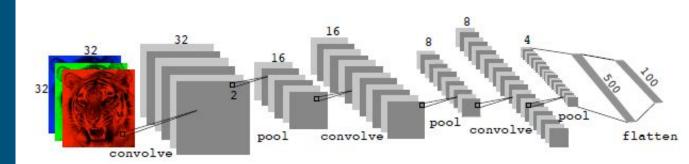


FIGURE 10.8. Architecture of a deep CNN for the CIFAR100 classification task. Convolution layers are interspersed with 2×2 max-pool layers, which reduce the size by a factor of 2 in both dimensions.

Image Source: James, G., Witten, D., et al.. (2022). *An introduction to statistical learning:*With applications in R. Springer.

"Neural Networks are like onions"

Fitting our CNN

- This is an image multi-class classification task
 - Output class probability
- Chose to use categorical cross entropy as loss function

- Output layer is softmax activation for each class
- Very similar ideas to multinomial logistic regression

Definition 6.11. Categorical Cross Entropy Cost Function Given the definition of categorical cross entropy as our loss function, the categorical cross entropy cost of a sample of size *m* is,

$$-\frac{1}{m}\sum_{i=1}^{m}\sum_{k=1}^{K}y_{i,k}\log\hat{y}_{i,k}$$

Parameter Enumeration

4.3.3 Parameter Enumeration in CNNs

In order to calculate the number of parameters of a convolution layer we apply the equation

$$((h \times w \times p) + 1) \times d$$

where h - height of filters in current layer, w - width of filters in current layer, p - number of filters in the previous layer, d - number of filters in the current layer.

Optimization Algorithms

- Recall gradient descent
- Stochastic gradient descent
 - Mini-batch gradient descent
- Improvements on SGD
 - Momentum
 - Nesterov Momentum
 - Adaptive Learning Rates

- Some examples of adaptive learning rate algorithms
 - AdaGrad
 - RMSprop
 - Adam
 - The adaptive method we use

Regularization

- Dataset Augmentation
 - To the right is an example
 - Original (top left)
 - Increase Contrast (top right)
 - Flip horizontally (bottom left)
 - Rotate cw 10 degrees (bottom right)
- Dropout
- Early Stopping









Transfer Learning

What is Transfer Learning?

- Benefits and Obstacles
 - Train less parameters
 - But: Your Data != Their Data

- The models we used for Transfer
 Learning are both trained on ImageNet
 - Pretrained VGG16
 - Pretrained ResNet50

 ImageNet - dataset of over 14 million images in 1000 classes

VGG16

- VGG16 is a 16 layer
 Convolutional Neural
 Network
- Output is shape (7, 7, 512)

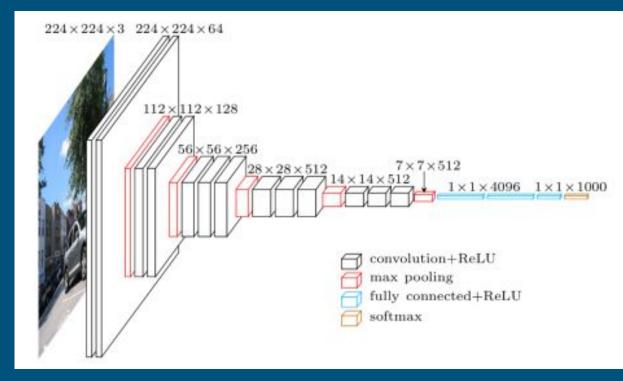


Image Source: https://neurohive.io/en/popular-networks/vgg16/

ResNet50

- 50 Layer Residual CNN
- Similar to ResNet34 but with more layers and instead of stacks of 2 layers, it consists of stacks of 3
- Output of shape (7, 7, 2048)

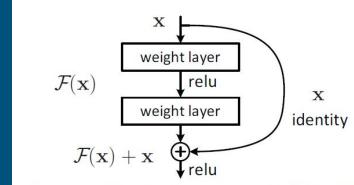
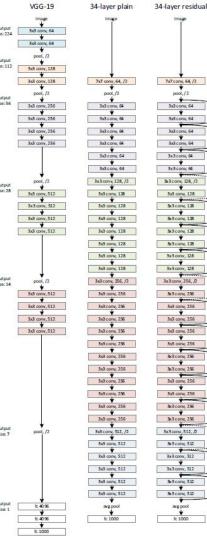


Figure 2. Residual learning: a building block.

2 layer stack example of residual learning

Image Citations:

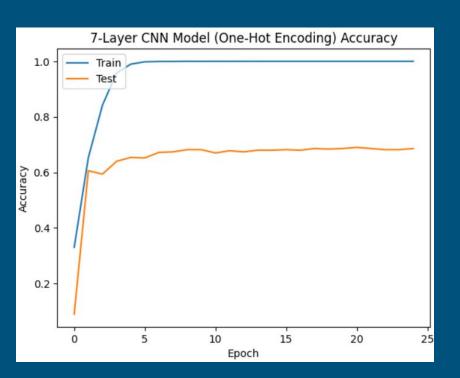
He, K., Zhang, X., Ren, S., & Sun, J. (2015). Deep Residual Learning for Image Recognition. 2016 IEEE Conference on Computer Vision and Pattern Recognition (CVPR). https://doi.org/10.1109/cvpr.2016.90

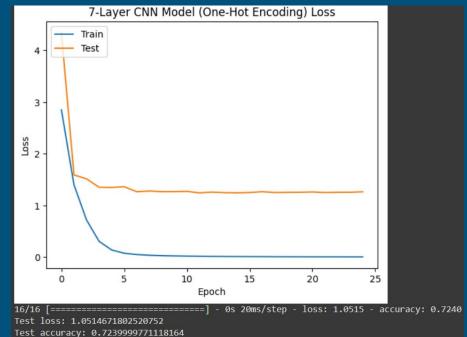


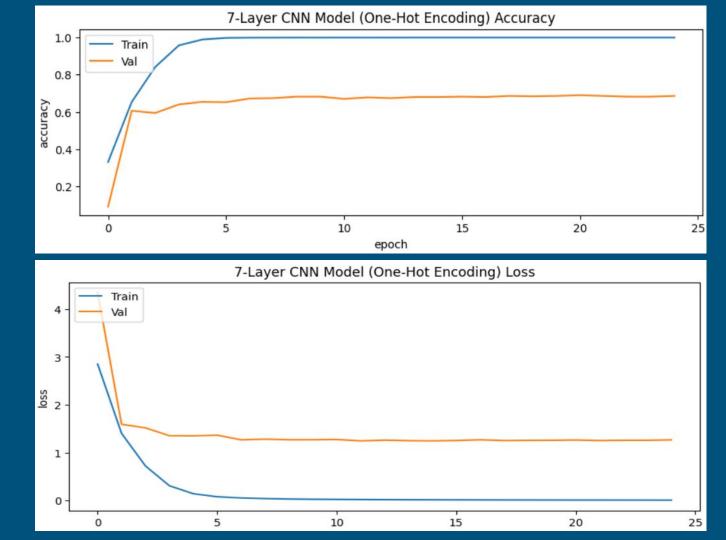
7-Layer CNN

- 7-Layer CNN
- SGD with learning rate = 0.001
- Total Params: 95,754,468
- Loss and Accuracy Curves

Test Accuracy ~ 72.4% Test Loss ~ 1.052



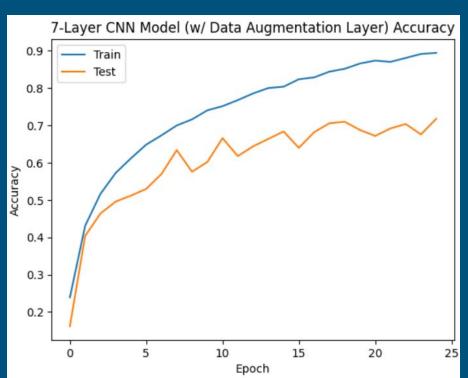


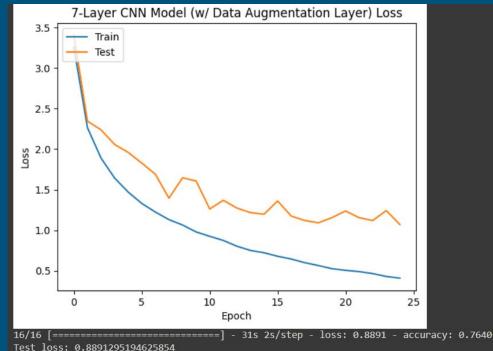


7-Layer CNN w/ Data Augmentation Layer

- 7-Layer CNN
- Added Data Augmentation Layer
- SGD with learning rate = 0.001
- Total Params: 95,754,468
- Loss and Accuracy Curves

Test Accuracy ~ 76.4% Test Loss ~ 0.889

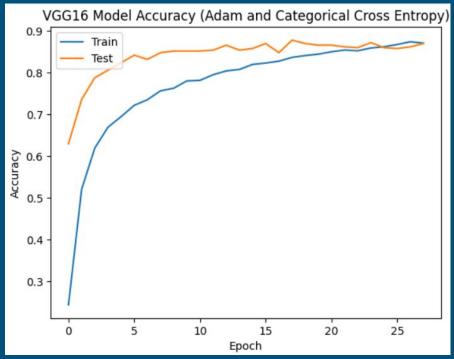


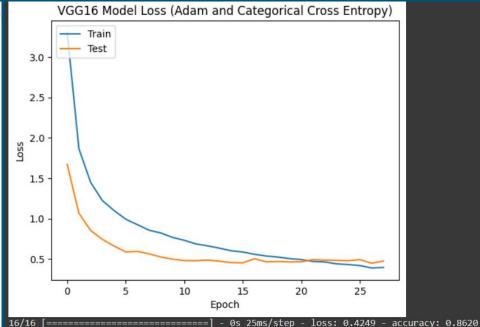


VGG16 Transfer Learning w/ Adam

- Transfer Learning, VGG16
- Adam with learning rate = 0.001
- Total Params: 15,028,644
- Trainable Params: 313,956
- Loss and Accuracy Curves

Test Accuracy ~ 86.2% Test Loss ~ 0.425



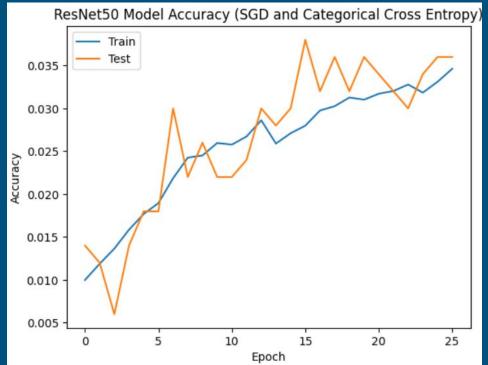


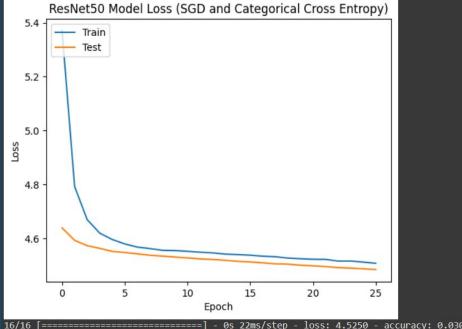
Test loss: 0.4248928427696228
Test accuracy: 0.8619999885559082

ResNet50 Transfer Learning w/ SGD

- Transfer Learning, ResNet50
- SGD with learning rate = 0.0001
- Total Params: 24,688,100
- Trainable Params: 1,100,388
- Loss and Accuracy Curves

Test Accuracy ~ 3.0% Test Loss ~ 4.525



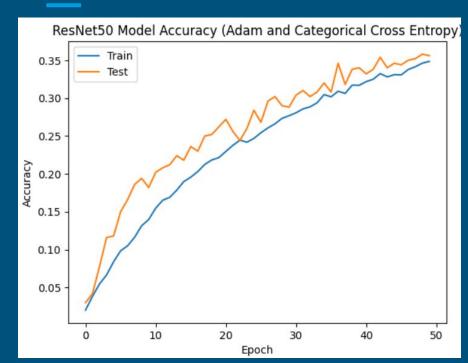


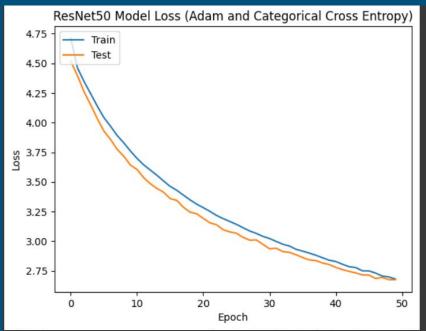
Test loss: 4.525031566619873 Test accuracy: 0.029999999329447746

ResNet50 Transfer Learning w/ Adam

- Transfer Learning, ResNet50
- Adam with learning rate = 0.0001
- Loss and Accuracy Curves

Test Accuracy ~ 38.8% Test Loss ~ 2.521

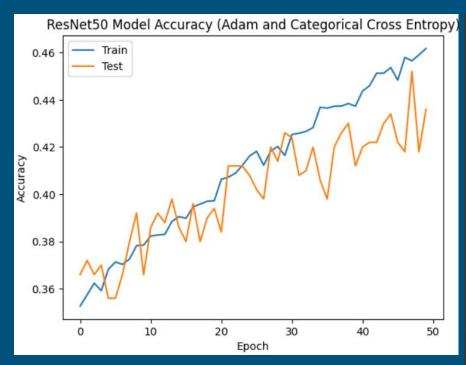


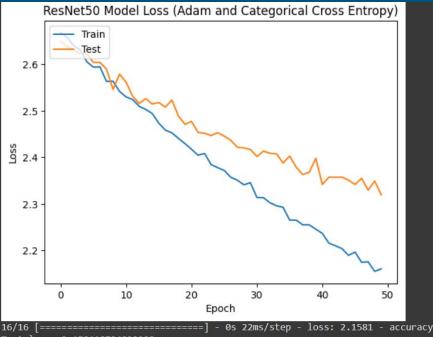


16/16 [=========================] - 0s 23ms/step - loss: 2.5213 - accuracy: 0.3880 Test loss: 2.5213265419006348

- 50 more epochs
- Adam with learning rate = 0.0001

Test Accuracy ~ 43.4% **Test Loss ~ 2.158**



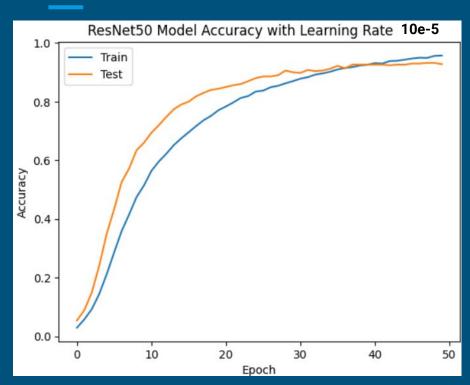


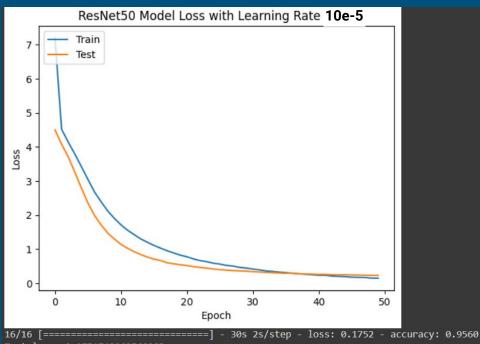
loss: 2.158118724822998

ResNet50 Transfer Learning w/ Adam

- Transfer Learning, ResNet50
- Adam with learning rate = 10e-5
- Loss and Accuracy Curves

Test Accuracy ~ 95.6% Test Loss ~ 0.175





ResNet50 Transfer Learning A Sample of the Results

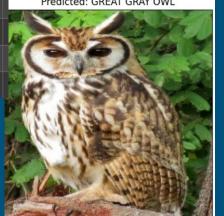
Bird Name Precision Recall 1.0 0.2 STRIATED CARACARA 1.0 0.8 STRIPED OWL 0.83333333333333334 TIT MOUSE 1.0 TOUCHAN 1.0 1.0 TURKEY VULTURE 0.625 WHITE EARED HUMMINGBIRD 1.0 1.0 WHITE NECKED RAVEN 1.0 0.6

Misclassification Examples

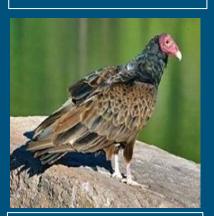
True: WILD TURKEY
Predicted: TURKEY VULTURE



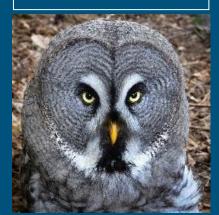
True: STRIPED OWL Predicted: GREAT GRAY OWL



Turkey Vulture



Great Gray Owl



Other methods and Techniques

- Multinomial Logistic Regression
 - ~ 12.5 % Test Accuracy Rate
- Linear Support Vector Classifier
 - ~ 18% Test Accuracy Rate
 - Computationally extremely expensive and very slow to fit
 - Fitting SVC with non-linear kernels is especially slow

 Other methods will potentially benefit from a method of dimensionality reduction such as PCA unlike the CNN which often does not

Computing power is a huge restriction

Choice of Final Model and Hyperparameters for Full Dataset

- ResNet50 Transfer Learning
- Adam w/ learning rate of 10e-5
- Added Data Augmentation Layer
 - Random Horizontal Flipping
 - Random Rotation of 10 deg
 - Random Contrast by 10%
 - Random Zoom In by 10%

- Why this one?
 - Performed well
 - ~96% Test Accuracy
 - Trained fairly quick,w.r.t. the number of epochs
 - 50 epochs
 - Less parameters to train and computationally (more) feasible

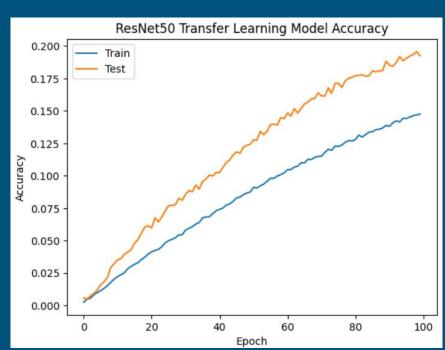
515 Birds Classification Results - Not great

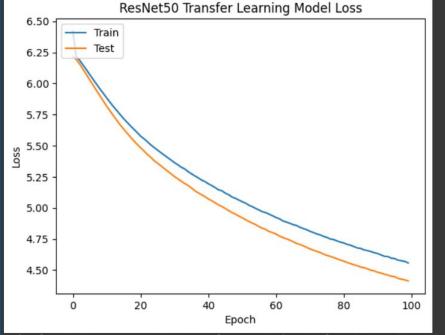
- Transfer Learning, ResNet50
- Adam with learning rate = 10e-5

Test accuracy: 0.20077669620513916

Loss and Accuracy Curves

Test Loss ~ 4.341 Test Accuracy ~ 20.08%





1/81 [========================] - 396s 5s/step - loss: 4.3408 - accuracy: 0.2008 est loss: 4.340805530548096

Discussion of Final Model

- Transfer Learning is quite restrictive
 - Its benefit is computing power but will generally always perform worse than a fully trained model
 - Could add more layers to top
 - Could train part of the pretrained model
 - May need more similar dataset for pretrained model
- Attempted a decrease and increase in learning rate and did not improve results
- The ResNet50 Transfer Learning model seems to be at its limits, but not for certain

Works Cited

- 1. Goodfellow, I., Bengio, Y., & Courville, A. (2017). *Deep learning*. The MIT Press.
- 2. James, G., Witten, D., Hastie, T., & Tibshirani, R. (2022). *An introduction to statistical learning: With applications in R.* Springer.
- 3. Nielsen, M. A. (1970, January 1). Neural networks and deep learning. Retrieved February 22, 2023, from http://neuralnetworksanddeeplearning.com/index.html
- 4. *Deep Learning Tutorial*. Unsupervised feature learning and Deep Learning Tutorial. (n.d.). Retrieved February 22, 2023, from http://ufldl.stanford.edu/tutorial/
- 5. Bagheri, R. (2020, August 28). *An introduction to Deep Feedforward Neural Networks*. Medium. Retrieved February 22, 2023, from https://towardsdatascience.com/an-introduction-to-deep-feedforward-neural-networks-1af281e306cd
- 6. https://www.analyticsvidhya.com/blog/2020/12/mlp-multilayer-perceptron-simple-overview/

Data and Implementation Sources

Dataset 1:

Crash Course Al Letters: https://github.com/crash-course-ai/lab1-neural-networks/tree/master/letters_mod

Dataset 2:

The Bird Image dataset source: https://www.kaggle.com/datasets/gpiosenka/100-bird-species

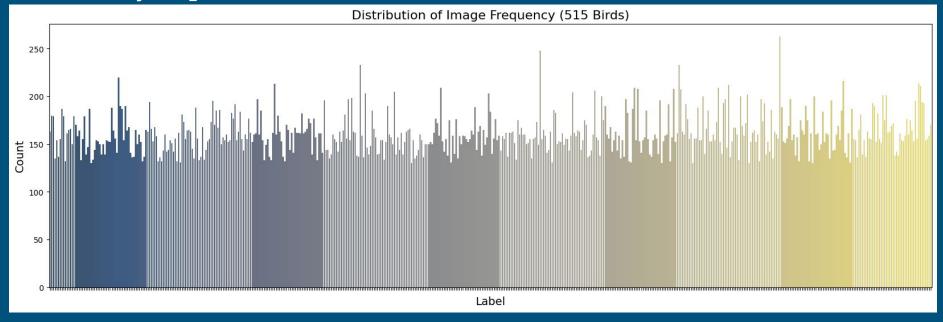
Inspiration behind implementation:

https://www.kaggle.com/code/vencerlanz09/bird-classification-using-cnn-efficientnetb0

Appendix

Distribution of Data for Full Dataset by Alphabetical Order

Average Image Count: 160



Most Common: Rufous Treepie Image Count: 263

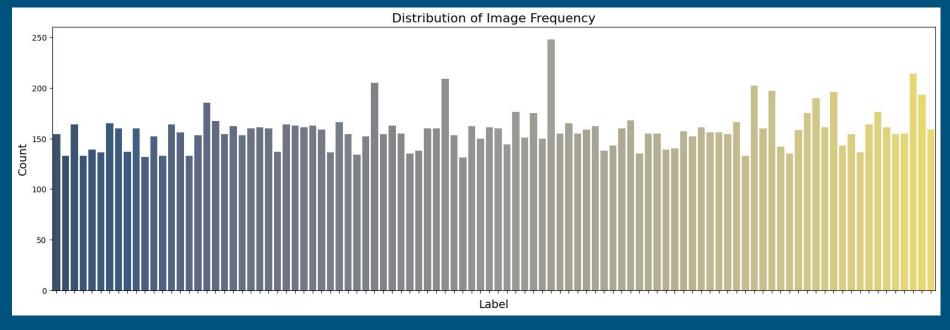


Least Common: Red Tailed Thrush Image Count: 130



Distribution of Data Frequency by Alphabetical Order

Average Image Count: 158



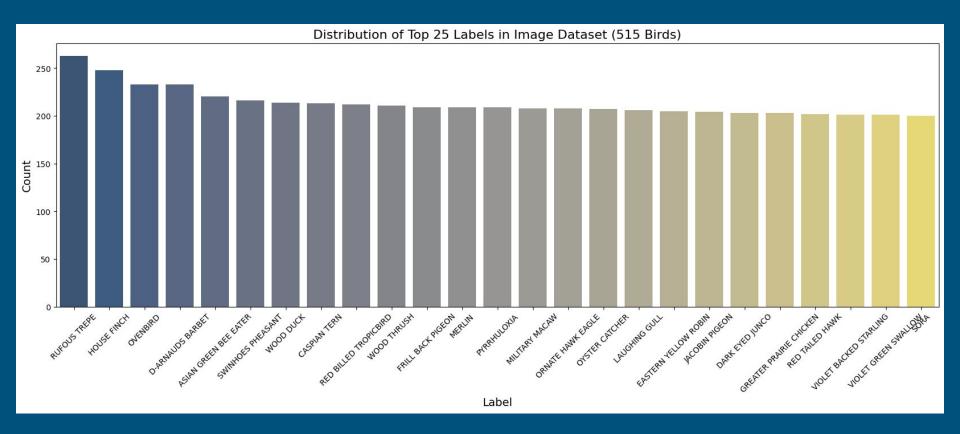
Most Common: House Finch Image Count: 248



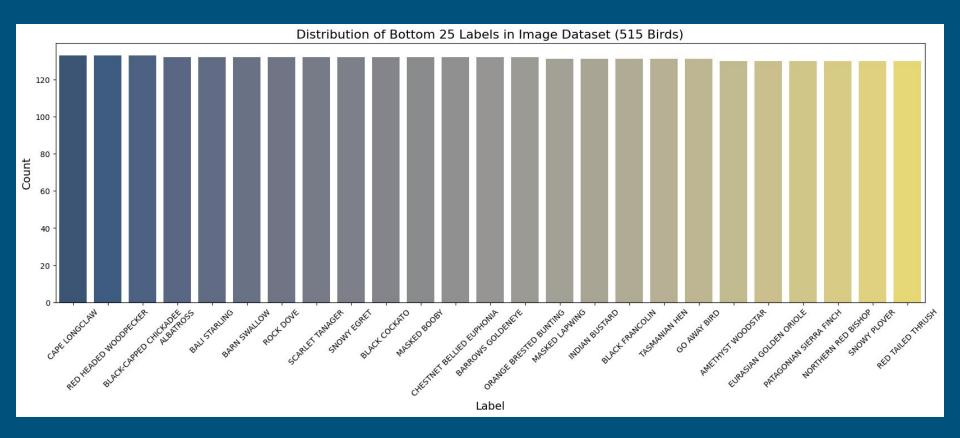
Least Common: Go Away Bird Image Count: 131



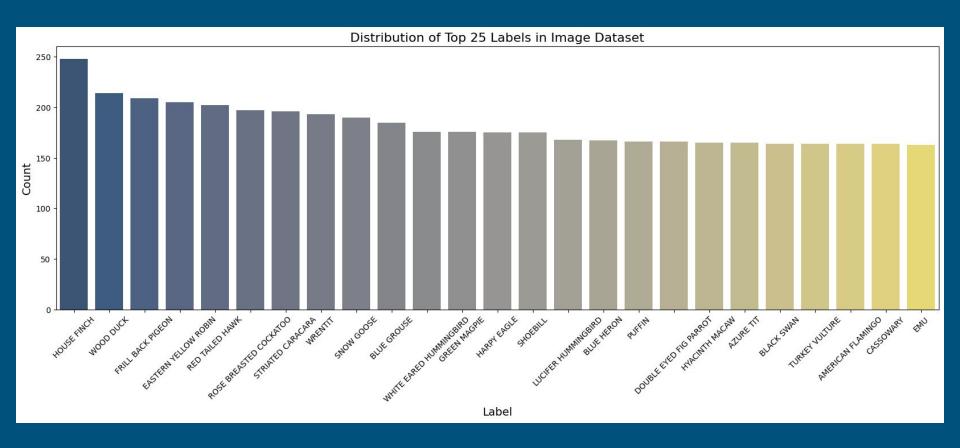
Distribution of Data for Full Dataset



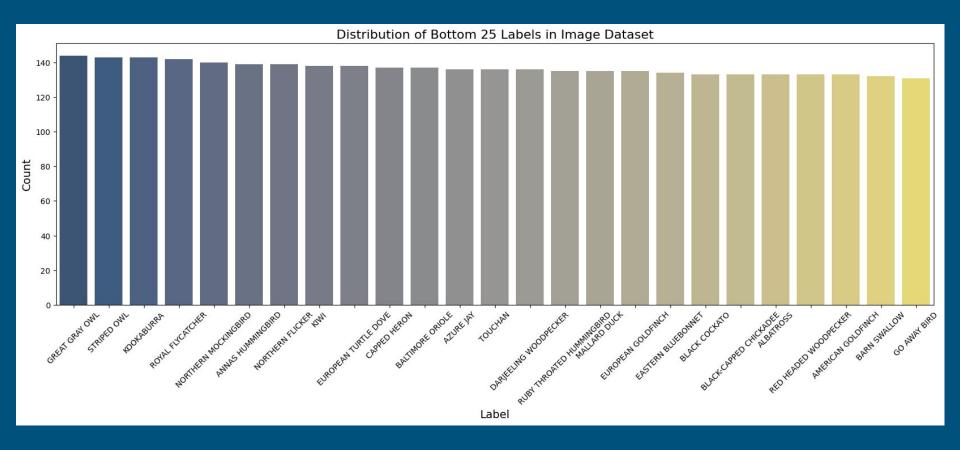
Distribution of Data for Full Dataset



Distribution of Data

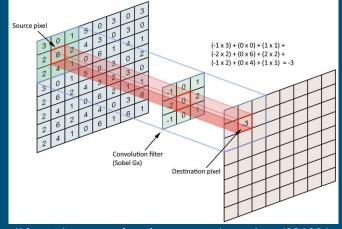


Distribution of Data

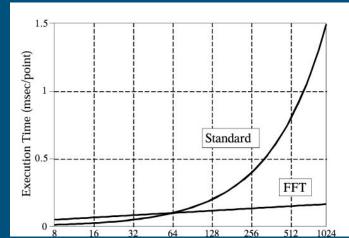


Implementing Convolution

- Our kernel is a sub-matrix of our input matrix consisting of weights
- Kernels form the "filter" which is essentially an entire layer of kernels
- Transforms the input into a convolved output
- Linear transformation. Therefore, we add a non-linear activation function onto the output of the convolution to add non-linearity - we use ReLU
- Sliding method Center square of the filter "slides" over the pixel values, transforms, and replaces center pixel
- DFT method Calculate DFT utilizing FFT algorithm



https://datascience.stackexchange.com/questions/23183/why-convolutions-always-use-odd-numbers-as-filter-size



Smith, S. W. (1997). The scientist and engineer's Guide to Digital Signal Processing. California Technical Pub.

Convolution

Definition 4.1. The Convolution Operator Consider two functions x and w where $x: T \to T'$ where $T, T' \subseteq \mathbb{R}$ and $w: S \to S'$ where $S, S' \subseteq \mathbb{R}$. Let $t \in T$ and $a \in S$. Convolution is then a linear operator denoted as * that is defined as

$$x * w = s(t) = (x * w)(t) = \int x(a)w(t - a)da$$

where x(t) and w(a) take on values of 0 for inputs outside of their domain.

The convolution operator essentially flips *w* around the "y-axis" at point *a* and sums the products evaluated at each point from left to right.

We call *x* the input and *w* the kernel. In our convolutional neural network, the data is the input and the kernel is our filter.

Fitting our CNN - Loss

- We are dealing with a multi-class classification task
- Need a way to denote a measure of "distance" between our predictions and the actual value
 - One Possible Answer: Cross Entropy

Definition 6.6. Cross-Entropy. The cross-entropy of the probability mass function p with respect to the probability mass function q (or the cross-entropy of q from p) is defined as,

$$CE(p,q) = -\mathbb{E}_p[\log q(x)] = -\sum_{x \in \mathcal{X}} p(x)\log q(x)$$

Remark. Note that cross-entropy is part of the relative entropy of p with respect to q. Specifically, CE(p,q) = H(X) + D(p||q).

Fitting our CNN - Our Loss and Cost

- The loss function we used
- The cost function is the sample mean of losses

Definition 6.10. Categorical Cross Entropy In a classification setting, the classification of a data point is typically deterministic given an input.

Let $y_k = \mathbb{P}(Y = k|X) = I(Y = k|X)$ where I is the indicator function and Y is a deterministic random variable supported on the set of classes $C = \{1, ..., k\}$. Let $\hat{y}_k = \Pr(\hat{Y} = k|X)$ where \hat{Y} is a random variable. The categorical cross entropy of y_k with respect to \hat{y}_k is

$$-\sum_{k=1}^{K} y_k \log \hat{y}_k$$

Typically the softmax function is used for our class probability estimate.

Definition 6.11. Categorical Cross Entropy Cost Function Given the definition of categorical cross entropy as our loss function, the categorical cross entropy cost of a sample of size *m* is,

$$-\frac{1}{m}\sum_{i=1}^{m}\sum_{k=1}^{K}y_{i,k}\log\hat{y}_{i,k}$$

Fitting our CNN - Some Information Theory

Definition 6.2. Entropy. If X is a discrete random variable supported on χ with probability mass function p, then the entropy of X is defined as

$$H(X) = -\sum_{x \in \chi} p(x) \log p(x)$$

Note that $H(X) = -\mathbb{E}[\log(p(X))]$

Definition 6.4. Relative Entropy/Kullback-Leichler Divergence. Let X be a discrete random variable supported on χ . The *relative entropy* D(p||q) of the probability mass function p with respect to q is defined by

$$D(p||q) = \sum_{x \in \chi} p(x) \log \frac{p(x)}{q(x)}$$

Note that it is equivalently defined as $D(p||q) = -\mathbb{E}[\log \frac{p(X)}{q(X)}].$

Automatic Differentiation

 Recall the backpropagation algorithm we discussed in class

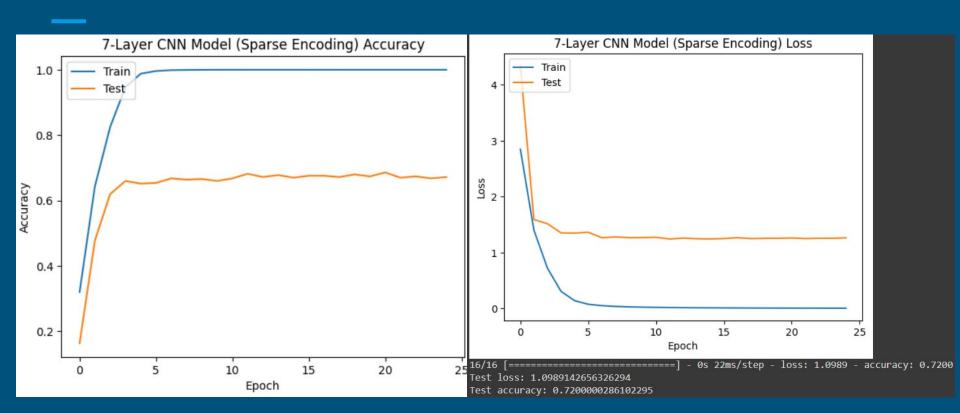
 We worked through an example with MSE as our cost function. For our classification problem, Mean Cross Entropy loss is our cost function and our output function is the softmax activation function • Backpropagation is generalized to tensors

- Backpropagation works essentially the same in CNNs as it does FFNs
 - The parameters it tunes in convolution layers are the weights in filters

7-Layer CNN with Sparse Encoding

- 7-Layer CNN with Sparse Encoding
- SGD with learning rate = 0.001
 - Loss and Accuracy Curves
 - Test Loss and Accuracy

Test Accuracy ~ 72.0% Test Loss ~ 1.100



Fitting our CNN

- How do we actually fit it to our data?
 - We use back propagation!
 - Back propagation is generalized for tensors
- The only essential differences lies in where our trainable parameters are from that we would like to adjust in order to fit our training data
- In the fully connected layer, it is the same as a feedforward NN. However, in the convolution layers, our parameters are the weights in each filter (kernel)
- Notice how sparse the number of parameters compared to fully connected layers

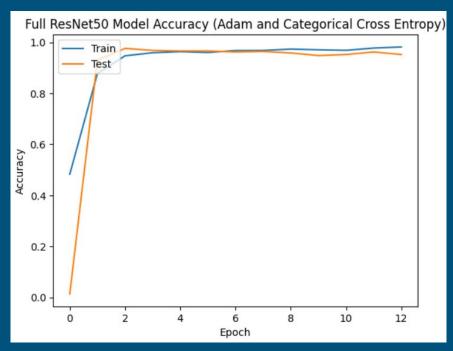
About the Implementations

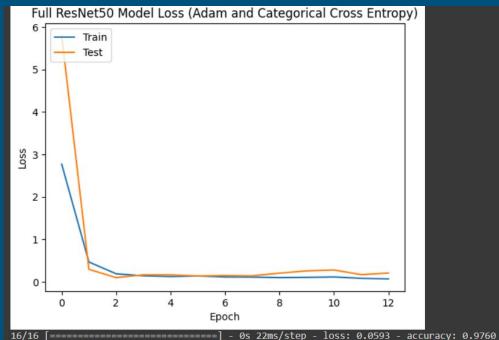
- Compare SGD to Adam to explore optimizer effectiveness and speed
- Explore data augmentation effects on results and learning rate
- Utilize TensorFlow and the Keras library for processing data and building and training the models
- All Transfer Learning use model pre-trained on ImageNet and add one fully connected layer of 512 nodes with ReLU activation function

Fully Trained ResNet50

- Fully Trained ResNet50
- Adam with learning rate = 0.0001
- Total Params: 23,587,712
- Loss and Accuracy Curves

Test Accuracy ~ 97.6% Test Loss ~ 0.059





Test loss: 0.059255003929138184 Test accuracy: 0.9760000109672546