Eq. of motion (Itô discretization) in 2D
$$\begin{cases} \vec{r}_{t+dt} = \vec{r}_t + v \hat{u}_t dt + \sqrt{2Ddt} \vec{\xi}_t + \sqrt{F(\vec{r}_t)} dt \end{cases} \qquad \hat{u}_t = (\cos \partial_t, \sin \partial_t)$$

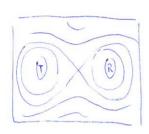
$$\begin{cases} \vec{r}_{t+dt} = \vec{r}_t + \sqrt{2D_{ext}} dt + \sqrt{2Ddt} \vec{\xi}_t + \sqrt{F(\vec{r}_t)} dt \end{cases} \qquad \hat{u}_t = (\cos \partial_t, \sin \partial_t)$$

$$\begin{cases} \vec{r}_{t+dt} = \vec{r}_t + \sqrt{2D_{ext}} dt + \sqrt{2Ddt} \vec{\xi}_t + \sqrt{F(\vec{r}_t)} dt \end{cases} \qquad \hat{v}_t = (\cos \partial_t, \sin \partial_t)$$

$$\begin{cases} \vec{r}_{t+dt} = \vec{r}_t + \sqrt{2D_{ext}} dt + \sqrt{2Ddt} \vec{\xi}_t + \sqrt{F(\vec{r}_t)} dt \end{cases} \qquad \hat{v}_t = (\cos \partial_t, \sin \partial_t)$$

$$\begin{cases} \vec{r}_{t+dt} = \vec{r}_t + \sqrt{2D_{ext}} dt + \sqrt{2Ddt} \vec{\xi}_t + \sqrt{2Ddt} \vec{\xi}_t$$

target-search in heterogeneous environments. Example



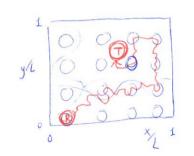
$$U(x,y) = k_x \left(x^{\frac{1}{2}} - x_0^2\right)^2 + \frac{k_y}{2} y^2$$

one can investigate the following observables

- · distribution of termination path times

  (time required to go from R to T without going back to R before reaching T)
- e reactive probability density (probability of being in a given position conditioned to the fact that we consider only the reactive paths)
- · reactive currents
- · cates of going from R to T (or average time to find the target)

 $U(x,y) = k \left[ \sin \left( \frac{8\pi x}{L} \right) + \sin \left( \frac{8\pi y}{L} \right) \right]$ 



Potential: such that a passive particle stay in the minima with race jumps from one

Activity (0): such that it is easier for the particle to travel around in the landscape but still feels the potential.

- . what if target is on a maximum? a minimum? comdomly placed?
- . what happen changing the activity or the posistence of the positiole?
- · chical ABP? (9th 9t + wdt + 12 Dat It 7t)