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1.assignment / 6.task

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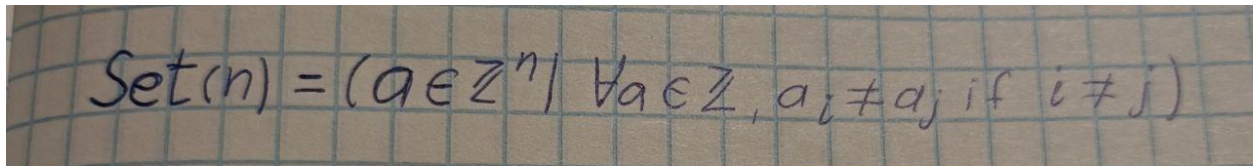
Group 10

Task

Implement the set type which contains integers. Represent the set as a sequence of its elements. Implement as methods: inserting an element, removing an element, returning whether the set is empty, returning whether the set contains an element, returning a random element without removing it from the set, returning the number of even numbers in the set (suggestion: store the number of even numbers and update it when the set changes), printing the set. A set can store every element only once.

Set type

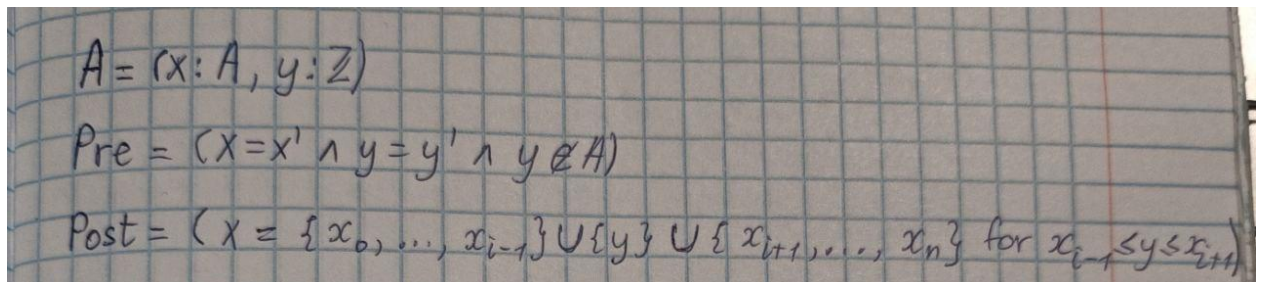
Set of values


$$\text{Set}(n) = (a \in \mathbb{Z}^n \mid \forall a \in \mathbb{Z}, a_i \neq a_j \text{ if } i \neq j)$$

*For later usage, I will shortly denote it as $\text{Set}(n) = A$

Operations

1. Insert an element


$$\begin{aligned} A &= (x: A, y: \mathbb{Z}) \\ \text{Pre} &= (x = x' \wedge y = y' \wedge y \notin A) \\ \text{Post} &= (x = \{x_0, \dots, x_{i-1}\} \cup \{y\} \cup \{x_{i+1}, \dots, x_n\} \text{ for } x_{i-1} \leq y \leq x_{i+1}) \end{aligned}$$

2. Remove an element

$$A = (x:A, y:\mathbb{Z})$$

$$\text{Pre} = (x = x' \wedge y = y' \wedge |x| \neq 0)$$

$$\text{Post} = (x = x \setminus \{y\})$$

3. Check if the set is empty

$$A = (x:A, l:\mathbb{N})$$

$$\text{Pre} = (x = x')$$

$$\text{Post} = (\text{Pre} \wedge l = (|x| == 0))$$

4. Check if an element is in the set

$$A = (x:A, y:\mathbb{Z}, l:\mathbb{N})$$

$$\text{Pre} = (x = x' \wedge y = y' \wedge |x| \neq 0)$$

$$\text{Post} = (\text{Pre} \wedge l = \forall_{i=1}^{|x|} \text{SEARCH } x[i] == y)$$

5. Returning the random element of a set

$$\begin{aligned}
 A &= (x: A, y: \mathbb{Z}, r: \mathbb{N}) \\
 \text{Pre} &= (x = x' \wedge |x| \neq 0) \\
 \text{Post} &= (\text{Pre} \wedge (r = \text{RANDOM}() \bmod (|x| + 1)) \wedge y = x[r])
 \end{aligned}$$

6. Returning the number of even numbers

$$\begin{aligned}
 A &= (x: A, y: \mathbb{Z}) \\
 \text{Pre} &= (x = x' \wedge |x| \neq 0) \\
 \text{Post} &= (\text{Pre} \wedge y = \sum_{i=1}^{|x|} 1)
 \end{aligned}$$

7. Print all the element of a set

$$\begin{aligned}
 A &= (x: A) \\
 \text{Pre} &= (x = x' \wedge |x| \neq 0) \\
 \text{Post} &= (\text{Pre} \wedge \text{PRINT } x[i])
 \end{aligned}$$

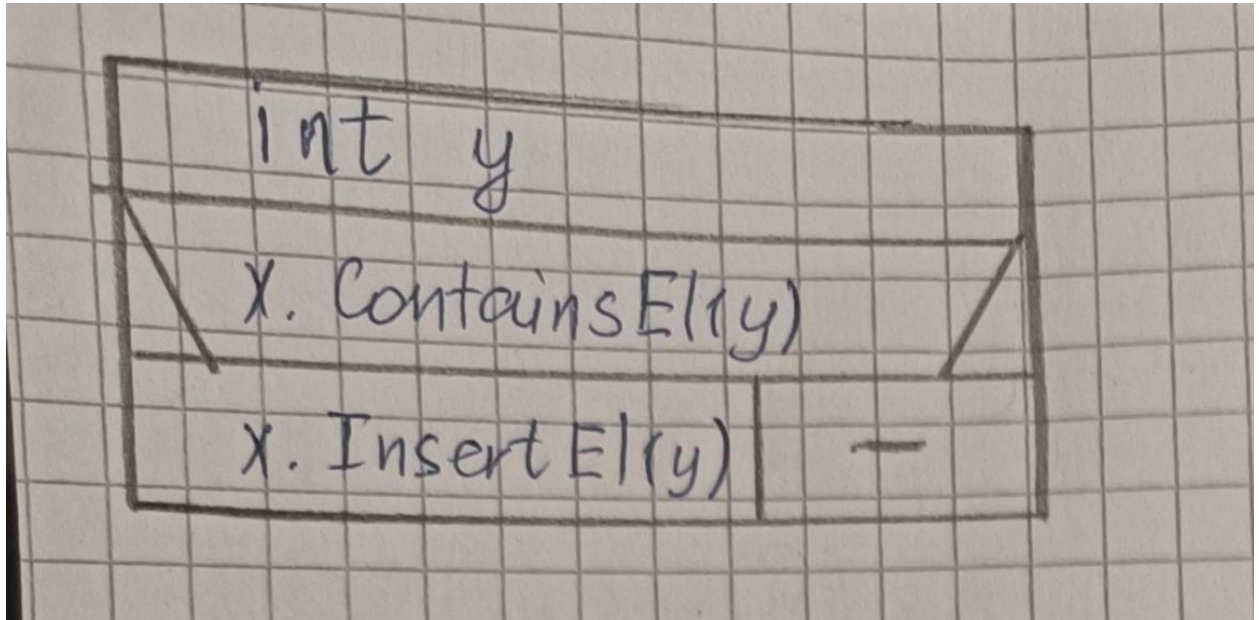
Representation

Integers in the set are inserted in the sequence in ascending order

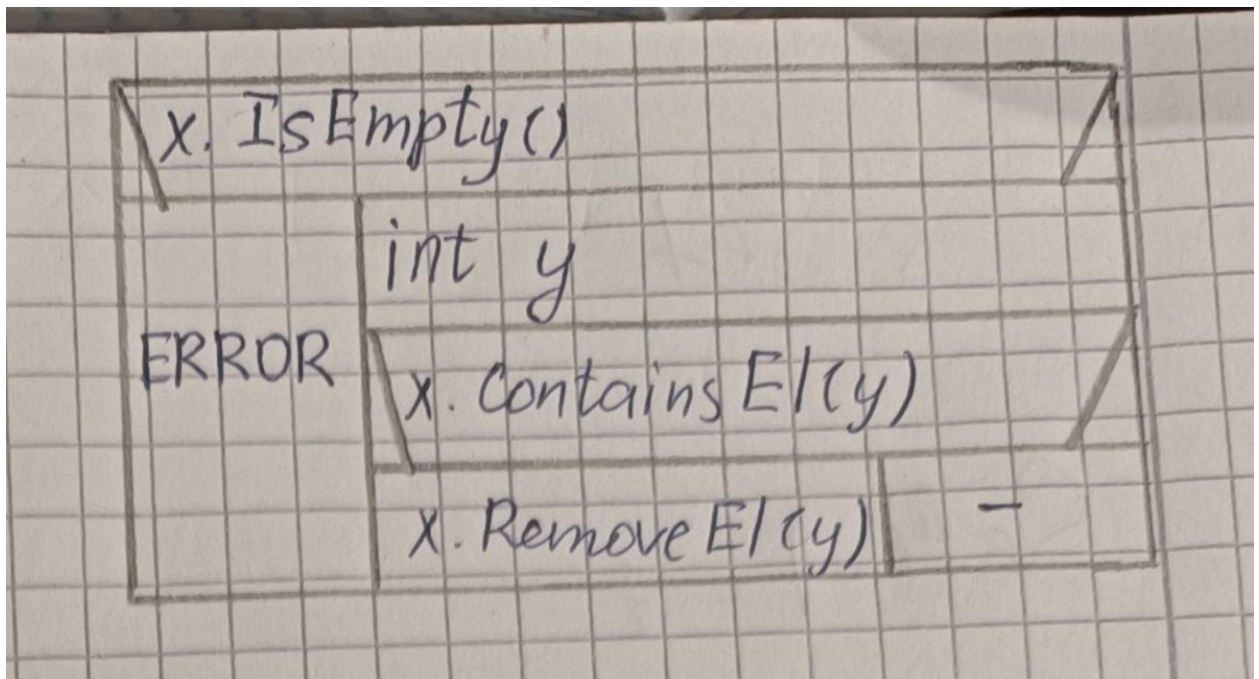
E.g. $\text{Set}(n) = 1\ 3\ 5\ 6\ 7\ 10$

Implementation

1. Inserting an element



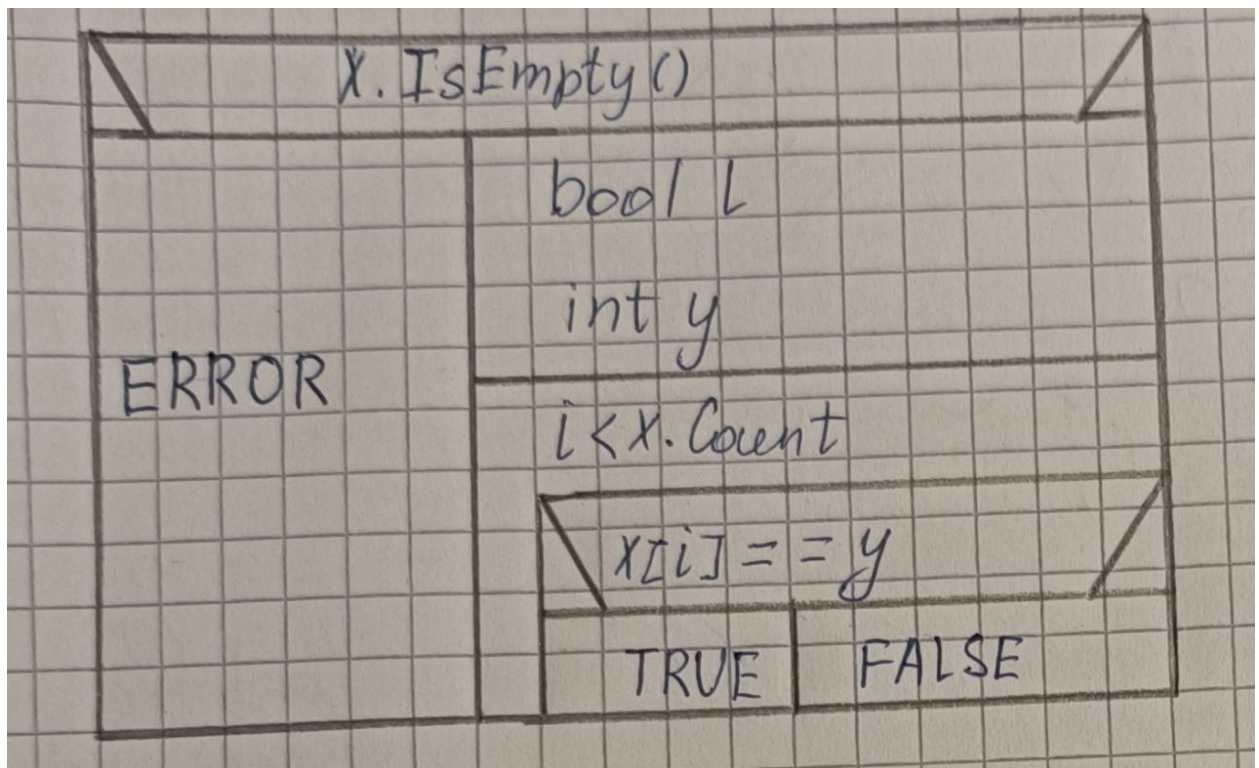
2. Removing an element



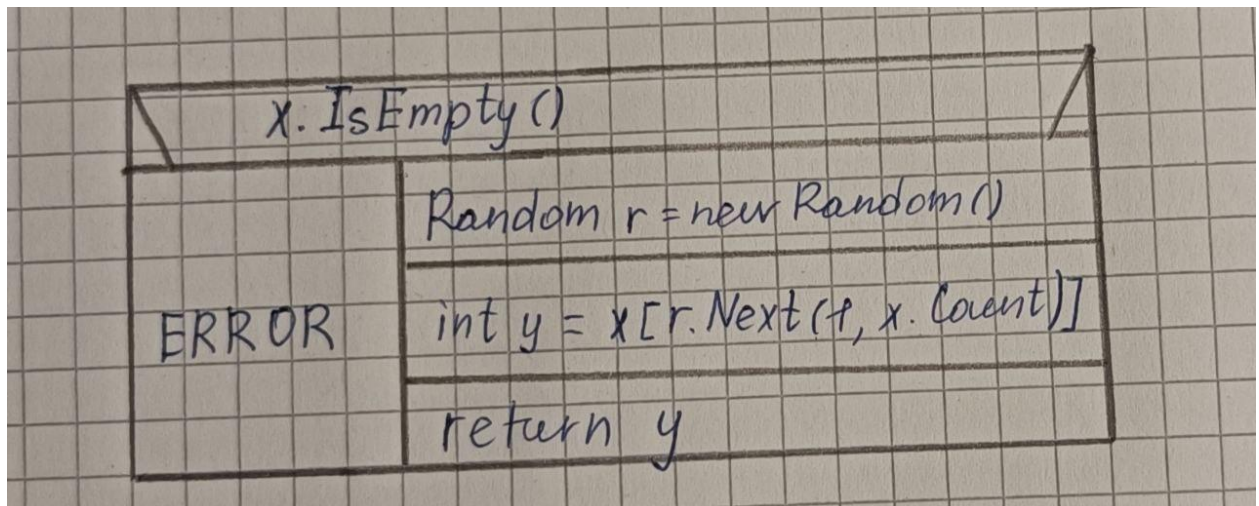
3. Check if the set is empty

`x.IsEmpty()`

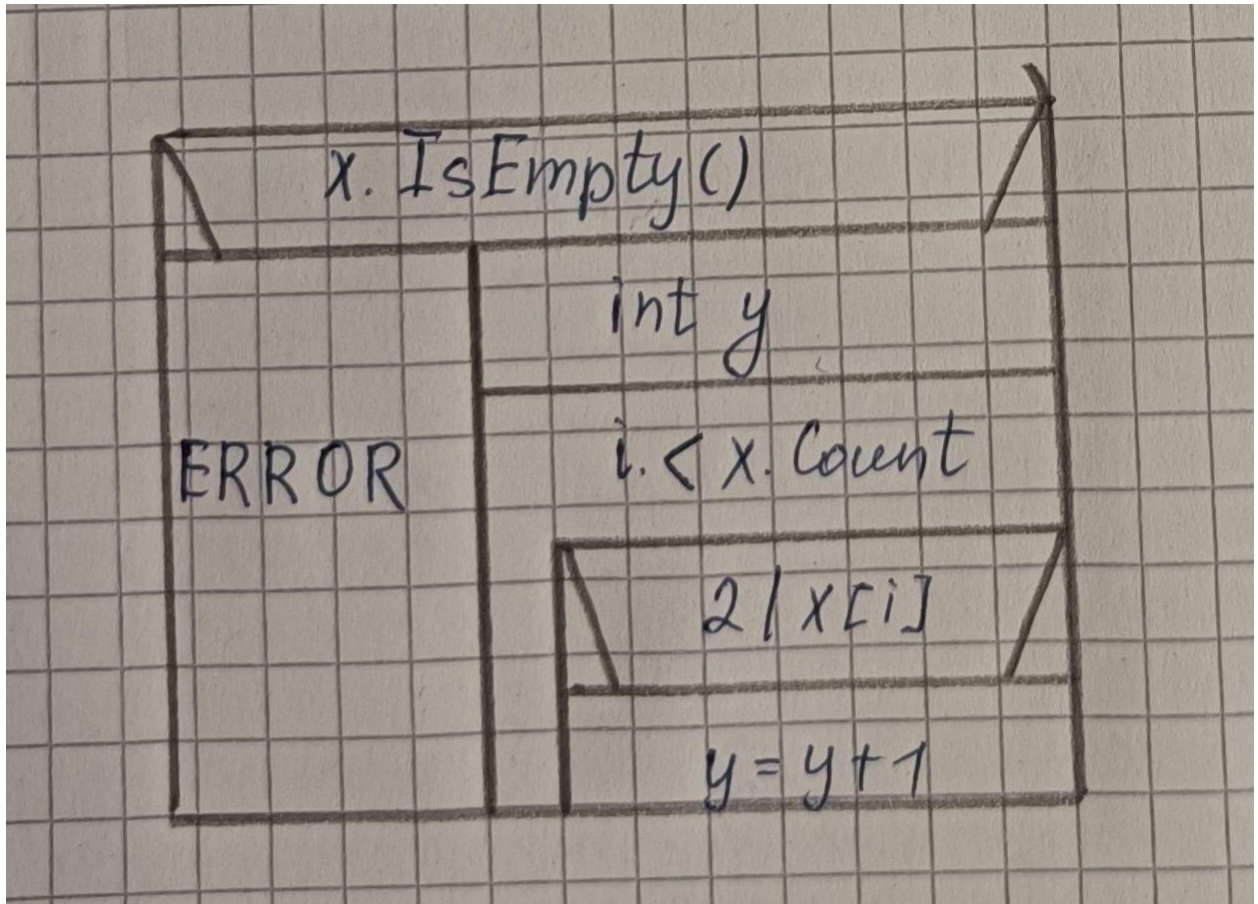
4. Check if the element is in the set



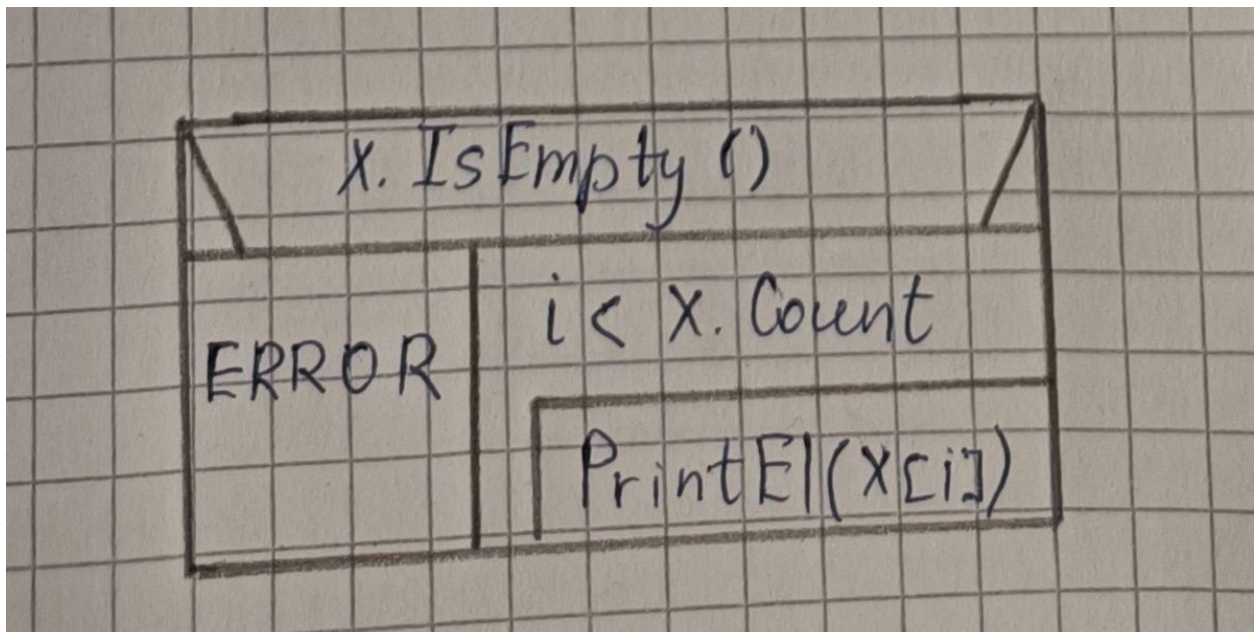
5. Returning random element



6. Returning the number of even elements



7. Printing the set



Testing

Testing operations

1. Testing InsertEl()
 - Check the size to see that new Set is empty
 - Insert 5 and check that the size of the set has changed to 1
 - Insert 3 and check that it's at position 0, because it's a sorted set
 - Try to insert 3 again, check if the size of the set is 2, containing (3, 5), then check that the element at position 0 is 3 and the element at position 1 is 5
2. Testing RemoveEl()
 - Insert 2, insert 3, then check if the set contains element 2
 - Remove 2, check if the set does not contain 2
3. Testing IsEmpty()
 - Instantiate new Set and check that is it empty
 - Insert 1, check that the set has an element
 - Remove 1, check if the set is empty now
4. Testing ContainsEl()
 - Insert 3, 4 and check if the set contains both of them
 - Check if the set contains element 5, which was not inserted
5. Testing ReturnRandomEl()
 - Insert 5, 6, 7, then return any random element and check that set contains the returned element
 - Check if the random element equals 4, which is not in the set
6. Testing EvenNums()
 - Insert 5, 6 and 4 and check if the number of even numbers equals 2
 - Remove 4 and check if the number of even numbers is 1 now

Testing exceptions

1. Check if the EmptySetException is thrown when the set is empty for operations:
 - RemoveEl()
 - ContainsEl()
 - ReturnRandomEl()
 - EvenNums()