

Step v : (Conversion of the string containing terminals and non-terminals to the string of non-terminal. on the RHS) Consider any production of the form

$$NT \rightarrow T_1 T_2 \dots T_n NT_1 \dots NT_n,$$

where $n \geq 1$ For the part $T_1 T_2 \dots T_n$, follow Step III

Check the resultant string by Step II. If not in CNF, follow Step IV.

By this process, the generated new grammar is in CNF.

Example 6.37

Convert the following grammar into CNF.

$$\begin{aligned} S &\rightarrow bA/aB \\ A &\rightarrow bAA/aS/a \\ B &\rightarrow aBB/DS/a \end{aligned}$$

Selation: The productions $S \rightarrow bA, S \rightarrow aB, A \rightarrow bAA, A \rightarrow aS, B \rightarrow aBB, B \rightarrow bS$ are not in CNF. So, we have to convert these into CNF. Let us replace terminal 'a' by a non-terminal C_a and terminal 'b' by a non-terminal C_b . Hence, two new productions will be added to the grammar

$$C_a \rightarrow a \text{ and } C_b \rightarrow b$$

By replacing a and b by new non-terminals and including the two productions, the modified grammar will be

$$\begin{aligned} S &\rightarrow C_b A / C_a B \\ A &\rightarrow C_b A A / C_a S / a \\ B &\rightarrow C_a B B / C_b S / a \\ C_a &\rightarrow a \\ C_b &\rightarrow b \end{aligned}$$

In the modified grammar, all the productions are not in CNF. The productions $A \rightarrow C_b AA$ and $B \rightarrow C_a BB$ are not in CNF, because they contain more than two non-terminals at the RHS. Let us replace AA by a new non-terminal D and BB by another new non-terminal E . Hence, two new productions will be added to the grammar $D \rightarrow AA$ and $E \rightarrow BB$. So, the new modified grammar will be

$$\begin{aligned} S &\rightarrow C_b A / C_a B \\ A &\rightarrow C_b D / C_a S / a \\ B &\rightarrow C_b E / C_a S / a \\ D &\rightarrow AA \\ E &\rightarrow BB \\ C_a &\rightarrow a \\ C_b &\rightarrow b \end{aligned}$$

Example 6.38

Convert the following grammar into CRF.

$$\begin{aligned} S &\rightarrow ABa \\ A &\rightarrow aab \\ B &\rightarrow Ac \end{aligned}$$