

Simple Linear Regression

Question #1: Anatomical Data from Domestic Cats

Load the `cats` dataset from the `MASS` library. This dataset includes the body and heart weights of both male and female adult domestic cats.

1. Create a scatterplot of heart weight versus body weight. From this plot alone, do you think simple linear regression would be a good fit for the data? Why?
2. Regress heart weight onto body weight. For this model:
 - a. Write out the regression equation.
 - b. Interpret the meaning of the coefficients in context of the problem.
 - c. Are the coefficients significant? How can you tell?
 - d. Is the overall regression significant? How can you tell? How does the answer to part c. relate?
 - e. Find and interpret the RSE.
 - f. Find and interpret the coefficient of determination.
3. Add the regression line to your plot from part 1.
4. Add a visualization of the residuals to your plot from part 3. Do any of the residuals seem abnormally large?
5. Construct 95% confidence intervals for the model coefficients. Interpret the intervals in context of the problem.
6. Assess each of the assumptions of the model.
7. Redraw the scatterplot and regression line from part 3 and add both confidence and prediction bands.
 - a. Why is the prediction band wider than the confidence band?
 - b. Why does the confidence band widen as it travels away from the center of the regression line?
8. Construct confidence and prediction intervals for body weights of 2.8 kg, 5 kg, and 10 kg. Do you foresee any issues with reporting any of these intervals?

Question #2: Considering Transformations

Continue with the `cats` dataset from the `MASS` library.

1. Create a Box-Cox plot for transforming the `cats` regression you created in question 1 above.
2. Determine the best value of λ for a Box-Cox transformation on the `cats` regression. (Hint: Try to balance interpretability and accuracy; when taking this perspective, there isn't really a completely "correct" answer.)
3. Transform your data based on your answer to part 2.
4. Construct a new regression now using the transformed data.
5. Create a scatterplot of the transformed data and overlay the new regression line.
6. Inspect the summary information and validate the assumptions of the linear regression model. Is there anything to be concerned about in the new model?
7. Compare the models you created:
 - a. Give one reason why you might use the original model instead of the Box-Cox transformed model.
 - b. Give one reason why you might use the Box-Cox transformed model instead of the original model.
8. Attempt to apply a Box-Cox transformation on the model on which you already applied a Box-Cox transformation. What happens?