# **EXPERIMENT 2**

### LOGIC GATES AND BOOLEAN ALGEBRA

### **OBJEJTIVE**

Gain experience in truth table and Boolean algebra.

### **THEORY**

### THE AND GATE

The *AND* gate implements the Boolean *AND* function where the output only is logical 1 when all inputs are logical 1. The standard symbol and the truth table for an *AND* gate with two inputs is given below.

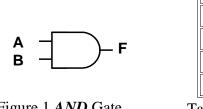


Figure 1 *AND* Gate symbol

Table 1 Truth table of *AND* Gate

В

0

1

0

1

A

 $\frac{0}{0}$ 

1

1

F

0

0

0

1

The Boolean expression for the *AND* gate is F = A.B

# THE OR GATE

The OR gate implements the Boolean OR function where the output is logical 1 when just input is logical 1. The standard symbol and the truth table for an OR gate with two inputs is given below.



Figure 2 OR Gate

Table 2 Truth table of *OR*Gate

The Boolean expression for the OR gate is F = A + B.

### **DIGITAL DESIGN**

### THE NOT GATE

The *NOT* gate implements the Boolean *NOT* function where the output is the inverse of the input. The standard symbol and the truth table for the *NOT* gate is given below.

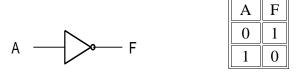


Figure 3 *NOT* Gate Table 3 Truth table of *NOT* Gate

The Boolean expression for the **NOT** gate is  $F = \overline{A}$ 

From these three basic logical gates it's to possible implement any Boolean expression into hardware.

# THE NAND GATE

The *NAND* gate is an *AND* gate followed by a *NOT* gate. The output is logical 1 when one of the inputs is logical 0. The standard symbol and the truth table for the *NAND* gate is given below.

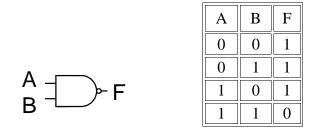


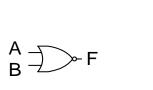
Figure 4 *NAND* Gate Table 4 Truth table of *NAND* Gate

The Boolean expression for the *NAND* gate is  $F = \overline{A \square B}$ .

### **DIGITAL DESIGN**

### THE NOR GATE

The *NOR* is a combination of an *OR* followed by a *NOT* gate. The output is logical 1 when none of the inputs are logical 0. The standard symbol and the truth table for the *NOR* gate is given below.



A B F
0 0 1
0 1 0
1 0 0
1 1 1 0

Figure 5 *NAND* Gate

Table 5 Truth table of *NAND* Gate

The Boolean expression for the *NOR* gate is  $R = \overline{A + B}$ .

### TRUTH TABLE

A truth table is a list of all the possible inputs and the corresponding outputs for a given system. The amount of possible inputs is determined by the amount of input variables. This value can be obtained by the formula  $2^n$ .

**Example:** Determine the truth table for: Y = A'B'C + ABC.

Truth Table			
A	В	C	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

Table 6 Truth Table

### **BUILDING A CIRCUIT**

In order to build a circuit from a truth table, we must first determine the Boolean expression for that particular truth table. Then the circuit can be constructed from multiple *AND* gates who's outputs all tie into one multiple input *OR* gate.

Looking at the truth table, we must first determine the Boolean expression. From the two instances where the output is high we obtain the following Boolean expression.

$$F = A'B'C + ABC$$

To build this circuit we need two 3-input AND gates, two Inverters, and a 2-input OR gate. The completed circuit is shown below:

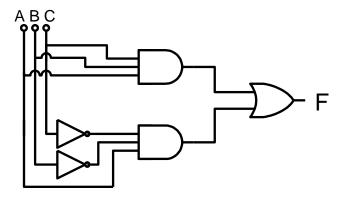


Figure 6 Logic Circuit

# EXPERIMENTAL PROCEDURE

Equation F = (A+B)C'

- 1) Complete the Truth Table of the equation.
- 2) Implement equation by NAND gates.

# **Equipment List:**

- 1) 74LS00 *NAND* GATE
- 2) Standard set equipments

