

# Mathematics: analysis and approaches Standard level Paper 2

Specimen								
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1 hour 30 minutes								

#### Instructions to candidates

- · Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- · A graphic display calculator is required for this paper.
- Section A: answer all questions. Answers must be written within the answer boxes provided.
- Section B: answer all questions in the answer booklet provided. Fill in your session number
  on the front of the answer booklet, and attach it to this examination paper and your
  cover sheet using the tag provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics: analysis and approaches formula booklet** is required for this paper.
- The maximum mark for this examination paper is [80 marks].





Full marks are not necessarily awarded for a correct answer with no working. Answers must be supported by working and/or explanations. Solutions found from a graphic display calculator should be supported by suitable working. For example, if graphs are used to find a solution, you should sketch these as part of your answer. Where an answer is incorrect, some marks may be given for a correct method, provided this is shown by written working. You are therefore advised to show all working.

## **Section A**

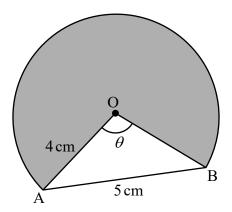
Answer **all** questions. Answers must be written within the answer boxes provided. Working may be continued below the lines, if necessary.

con	tinued	below the lines, if necessary.	
1.	[Max	ximum mark: 6]	
	A m	etal sphere has a radius 12.7 cm.	
	(a)	Find the volume of the sphere expressing your answer in the form $a \times 10^k$ , $1 \le a < 10$ and $k \in \mathbb{Z}$ .	[3]
	The	sphere is to be melted down and remoulded into the shape of a cone with a height of $14.8\mathrm{c}$	cm.
	(b)	Find the radius of the base of the cone, correct to 2 significant figures.	[3]



## 2. [Maximum mark: 6]

The following diagram shows part of a circle with centre  $\,{\rm O}\,$  and radius  $4\,cm$  .



Chord AB has a length of  $5 \, \text{cm}$  and  $A \hat{O} B = \theta$ .

/_\	Find the value of $\theta$ , giving your answer in radians.	[0]
(a)	Find the value of H. diving volit answer in radians	1.51
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(b) Find the area of the shaded region. [3]

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3.	[Max	kimum mark: 6]			
		st January 2020, Laurie invest of $5.5\%$ , compounded <b>quarte</b>		pays a nominal annual interest	
		amount of money in Laurie's a lence with common ratio, $r$ .	account <b>at the end of ea</b>	ch year follows a geometric	
	(a)	Find the value of $r$ , giving yo	our answer to four signific	cant figures.	[3]
	Laur	ie makes no further deposits t	o or withdrawals from the	e account.	
	(b)	Find the year in which the an amount she invested.	nount of money in Laurie	e's account will become double the	[3]



	4.	[Maximum mark:	61
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A six-sided biased die is weighted in such a way that the probability of obtaining a "six" is  $\frac{7}{10}$ .

The die is tossed five times. Find the probability of obtaining

- (a) at most three "sixes". [3]
- (b) the third "six" on the fifth toss. [3]

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## **5.** [Maximum mark: 5]

The following table below shows the marks scored by seven students on two different mathematics tests.

Test 1 ( <i>x</i> )	15	23	25	30	34	34	40
Test 2 ( <i>y</i> )	20	26	27	32	35	37	35

Let  $L_1$  be the regression line of x on y. The equation of the line  $L_1$  can be written in the form x = ay + b.

(a) Find the value of a and the value of b.

[2]

Let  $L_2$  be the regression line of y on x. The lines  $L_1$  and  $L_2$  pass through the same point with coordinates (p,q).

(b)	Find the	value	of p	and	the	value	of	q
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[3]




6.	[Maximum	mark:	7]

The displacement, in centimetres, of a particle from an origin, O, at time t seconds, is given by  $s(t) = t^2 \cos t + 2t \sin t$ ,  $0 \le t \le 5$ .

- (a) Find the maximum distance of the particle from O. [3]
- (b) Find the acceleration of the particle at the instant it first changes direction. [4]




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## **Section B**

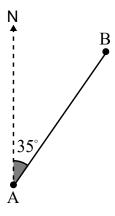
Answer all questions in the answer booklet provided. Please start each question on a new page.

## **7.** [Maximum mark: 16]

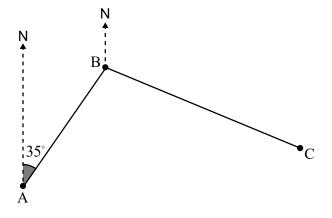
Adam sets out for a hike from his camp at point A. He hikes at an average speed of  $4.2 \, \text{km/h}$  for 45 minutes, on a bearing of  $035^{\circ}$  from the camp, until he stops for a break at point B.

(a) Find the distance from point A to point B.





Adam leaves point B on a bearing of  $114^\circ$  and continues to hike for a distance of  $4.6\,\mathrm{km}$  until he reaches point C .



- (b) (i) Show that  $\angle ABC$  is  $101^{\circ}$ .
  - (ii) Find the distance from the camp to point C.

[5]

(c) Find BĈA.

[3]

Adam's friend Jacob wants to hike directly from the camp to meet Adam at point C.

(d) Find the bearing that Jacob must take to point C.

[3]

Jacob hikes at an average speed of 3.9 km/h.

(e) Find, to the nearest minute, the time it takes for Jacob to reach point C.

[3]



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**8.** [Maximum mark: 15]

The length,  $X\,\mathrm{mm}$ , of a certain species of seashell is normally distributed with mean 25 and variance,  $\sigma^2$ .

The probability that X is less than 24.15 is 0.1446.

(a) Find P(24.15 < X < 25).

[2]

- (b) (i) Find  $\sigma$ , the standard deviation of X.
  - (ii) Hence, find the probability that a seashell selected at random has a length greater than  $26\,\mathrm{mm}$ .

[5]

A random sample of 10 seashells is collected on a beach. Let \it\it{Y} represent the number of seashells with lengths greater than  $26\,\rm mm$  .

(c) Find E(Y).

[3]

(d) Find the probability that exactly three of these seashells have a length greater than  $26\,\mathrm{mm}$  .

[2]

A seashell selected at random has a length less than 26 mm.

(e) Find the probability that its length is between  $24.15\,\mathrm{mm}$  and  $25\,\mathrm{mm}$ .

[3]



9. [Maximum mark: 13]

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Consider a function 
$$f$$
, such that  $f(x) = 5.8 \sin\left(\frac{\pi}{6}(x+1)\right) + b$ ,  $0 \le x \le 10$ ,  $b \in \mathbb{R}$ .

(a) Find the period of f. [2]

The function f has a local maximum at the point (2, 21.8), and a local minimum at (8, 10.2).

- (b) (i) Find the value of b.
  - (ii) Hence, find the value of f(6). [4]

A second function g is given by  $g(x) = p \sin\left(\frac{2\pi}{9}(x - 3.75)\right) + q$ ,  $0 \le x \le 10$ ;  $p, q \in \mathbb{R}$ .

The function g passes through the points (3, 2.5) and (6, 15.1).

- (c) Find the value of p and the value of q. [5]
- (d) Find the value of x for which the functions have the greatest difference. [2]

