ECSE 420 - Assignment 1 Report

Q1:

1.1

Implemented a method for calculating the product of two matrices sequentially using 3 nested for loops. This algorithm is quite slow at $O(n^3)$. This method also checks if both matrices have valid dimensions for multiplication, and throws an exception if not.

1.2

Our parallel method employs the same algorithm as the sequential method, however for the innermost for loop we create a new thread for each iteration. This means that each dot product operation takes place in its own thread. We are using a fixed thread pool for this case and the maximum number of threads is by default set to the number of available processor threads on the host machine.

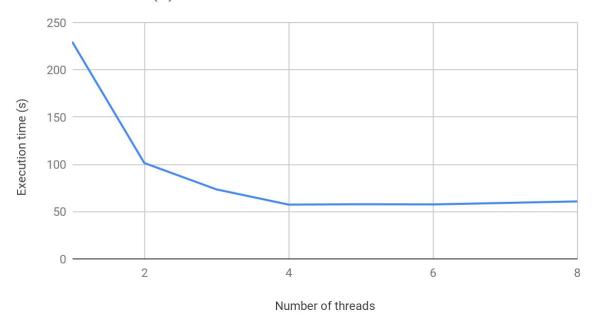
1.3

Here we get the current system time in milliseconds before and after executing the method. We then take the difference of the two to get the method's execution time.

1.4For a matrix size of 2000 x 2000 and a host machine with 4 processor threads:

Number of threads	Execution time (s)	
1	229.7	
2	101.4	
3	73.5	
4	57.4	
5	57.8	
6	57.6	
8	60.8	

Execution time (s) vs. Number of threads

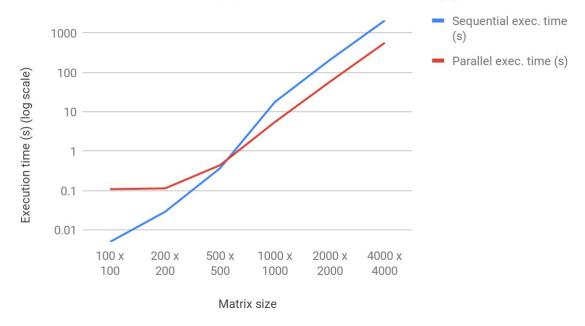


As we can see, there is a clear advantage to increasing the number of threads the pool can use. However, creating more threads than the host machine's processor can handle (exceeding the numbers of processor cores/threads) can lead to diminishing returns or even performance degradation.

1.5
Using 4 threads:

Matrix size	Sequential exec. time (s)	Parallel exec. time (s)
100 x 100	0.005	0.109
200 x 200	0.029	0.114
500 x 500	0.369	0.441
1000 x 1000	17.8	5.52
2000 x 2000	207.7	57.9
4000 x 4000	2081.7	566.5

Sequential exec. time (s) vs Parallel exec. time (s)



1.6

For 1.4, we can see that improvement in execution begins to plateau as we approach the number of physical processor threads on the host machine, for our case 4. We can also see that as we continue to increase the number of threads beyond this the execution actually begins to increase. We believe this is because it gets more complicated for the host OS scheduler to process the increased number of threads.

As for 1.5, we can see that for small matrix sizes the sequential method is actually much faster than the parallel method. This is because of the time needed to create the threads for the parallel method. However, once we get to matrix sizes above 500x500, the parallel method starts to become significantly faster than the sequential method since the overhead caused by creating threads becomes negligible compared to the overall computation time.

<u>Q2:</u>

2.1

Deadlock can occur only if all the following conditions are met:

- Mutual exclusion: prevents simultaneous access to a shared resource.
- Hold and wait: A process is holding one resource while requesting other resources which are held by other processes.
- No preemption: Resources can only be released by the process holding it.
- Circular wait: Each process is waiting for a resource held by another process in the list, with the last process waiting for resources from the first.

2.2

There are multiple different strategies to avoiding deadlock. For example:

- Resource ordering: Each object that needs to be locked is assigned an order and we
 ensure that all threads can only acquire the locks in that order. This helps to avoid
 the circular wait condition for deadlock.
- Deadlock detection: Detect deadlocks when they happen and either terminate the offending process or preempt the resource allocated to break the deadlock.
- Require processes to request all resources needed before executing. However, it is difficult to predict what the process will need and this can often lead to starvation.

Q3:

3.1

To cause deadlock in our Dining Philosopher program, every philosopher needs to grab the chopstick to his right (without releasing it until after eating), then grab the chopstick to his left. It will inevitably cause a deadlock since at some point all philosophers will be holding the chopstick to their right, while waiting for the chopstick to their left which will never be available.

3.2

To solve the imminent deadlock from the initial Dining Philosopher program, we forced at least one philosopher (the first in our case) to wait for the left chopstick to be available before grabbing the right chopstick. What this does is eliminate the circular wait condition that is a key element in causing deadlock.

We used ReentrantLock with the fair policy set to True instead of the synchronized() block in order to prevent starvation. This method always gives priority to the thread that has been waiting the longest so no thread ever starves. At the same time, when a philosopher picks up the right chopstick but can't pick up the left chopstick (due to it already being in use), we force him to drop his right chopstick to allow other philosophers to dine.

```
Connected to the target VM, address: '127.0.6.1:41897', transport: 'socket' Philosopher 4 ate 438 times and waited for 0.956193565 seconds Philosopher 2 ate 416 times and waited for 0.956193565 seconds Philosopher 2 ate 416 times and waited for 0.940622594 seconds Philosopher 2 ate 464 times and waited for 0.97855131 seconds Philosopher 11 ate 442 times and waited for 0.97855131 seconds Philosopher 2 ate 424 times and waited for 0.97284261 seconds Philosopher 2 ate 424 times and waited for 0.97284261 seconds Philosopher 2 ate 452 times and waited for 1.082296633 seconds Philosopher 12 ate 432 times and waited for 1.083496633 seconds Philosopher 12 ate 432 times and waited for 1.083496633 seconds Philosopher 7 ate 456 times and waited for 1.0834964701 seconds Philosopher 7 ate 456 times and waited for 1.08349684 seconds Philosopher 31 ate 454 times and waited for 1.08349684 seconds Philosopher 31 ate 454 times and waited for 1.085967611 seconds Philosopher 30 ate 478 times and waited for 1.14366652 seconds Philosopher 20 ate 478 times and waited for 1.084968844 seconds Philosopher 20 ate 478 times and waited for 1.078861408 seconds Philosopher 20 ate 478 times and waited for 1.078861408 seconds Philosopher 42 ate 413 times and waited for 1.0816861652 seconds Philosopher 45 ate 425 times and waited for 0.96664192 seconds Philosopher 45 ate 425 times and waited for 0.96664192 seconds Philosopher 45 ate 470 times and waited for 1.081922048 seconds Philosopher 45 ate 454 times and waited for 1.081922048 seconds Philosopher 5 ate 454 times and waited for 1.087921819 seconds Philosopher 19 ate 457 times and waited for 1.087921819 seconds Philosopher 19 ate 457 times and waited for 1.087921819 seconds Philosopher 19 ate 456 times and waited for 1.087921819 seconds Philosopher 19 ate 456 times and waited for 1.087921819 seconds Philosopher 19 ate 457 times and waited for 1.087921819 seconds Philosopher 24 ate 460 times and waited for 1.087921808 seconds Philosopher 25 ate 451 times and waited for 1.087936661 seconds Phi
```

```
Connected to the target VM, address: '127.0.0.1:42683', transport: 'socket' Philosopher 50 ate 1000 times and waited for 2.936154593 seconds Philosopher 48 ate 1000 times and waited for 5.366449549 seconds Philosopher 48 ate 1000 times and waited for 5.384278745 seconds Philosopher 48 ate 1000 times and waited for 5.3684278745 seconds Philosopher 48 ate 1000 times and waited for 6.35597814 seconds Philosopher 48 ate 1000 times and waited for 7.11264779 seconds Philosopher 43 ate 1000 times and waited for 7.69285394 seconds Philosopher 43 ate 1000 times and waited for 7.758811561 seconds Philosopher 43 ate 1000 times and waited for 8.366088324 seconds Philosopher 42 ate 1000 times and waited for 8.366088324 seconds Philosopher 40 ate 1000 times and waited for 8.383048842 seconds Philosopher 38 ate 1000 times and waited for 9.3429495 seconds Philosopher 39 ate 1000 times and waited for 9.3429495 seconds Philosopher 37 ate 1000 times and waited for 9.828706847 seconds Philosopher 35 ate 1000 times and waited for 9.828706847 seconds Philosopher 35 ate 1000 times and waited for 10.3912732296 seconds Philosopher 35 ate 1000 times and waited for 10.3912732296 seconds Philosopher 35 ate 1000 times and waited for 10.39163922 seconds Philosopher 33 ate 1000 times and waited for 10.39163922 seconds Philosopher 30 ate 1000 times and waited for 11.05865825 seconds Philosopher 30 ate 1000 times and waited for 11.474042842 seconds Philosopher 30 ate 1000 times and waited for 11.474042842 seconds Philosopher 30 ate 1000 times and waited for 11.474042842 seconds Philosopher 23 ate 1000 times and waited for 11.474042842 seconds Philosopher 23 ate 1000 times and waited for 11.474042842 seconds Philosopher 23 ate 1000 times and waited for 12.765693485 seconds Philosopher 24 ate 1000 times and waited for 12.765693485 seconds Philosopher 24 ate 1000 times and waited for 12.765693485 seconds Philosopher 24 ate 1000 times and waited for 12.765693485 seconds Philosopher 14 ate 1000 times and waited for 12.7656936564 seconds Philosopher
```

We can see from the above images that the program using ReentrantLocks (on the left) has much lower and more consistent total wait times for each philosopher than the synchronized block method on the right.

<u>Q4:</u>

4.1

$$S = \frac{1}{1 - p + \frac{p}{n}} = \frac{1}{1 - 0.6 + \frac{0.6}{n}} = \frac{1}{0.4 + \frac{0.6}{n}}, \text{ where } n = \text{# of cores}$$

$$S_{max} = \lim_{n \to \infty} \frac{1}{0.4 + \frac{0.6}{n}} = 2.5$$

4.2

$$S_n = \frac{1}{1 - p + \frac{p}{n}} = \frac{1}{1 - 0.8 + \frac{0.8}{n}} = \frac{1}{0.2 + \frac{0.8}{n}}$$

$$S_n' > 2 * S_n \Rightarrow \frac{1}{0.2k + \frac{1 - 0.2k}{n}} > 2 * \frac{1}{0.2 + \frac{0.8}{n}}$$

$$\frac{1}{0.2kn + 1 - 0.2k} > 2 * \frac{1}{0.2n + 0.8}$$

$$0.2n + 0.8 > 0.4kn + 2 - 0.4k$$

$$k < \frac{0.5n - 3}{n - 1}$$

4.3

$$S_n = \frac{1}{s + \frac{1-s}{n}}$$

$$S_n' = 0.5 * S_n = \frac{1}{\frac{s}{3} + \frac{1-\frac{s}{3}}{n}} = 0.5 * \frac{1}{s + \frac{1-s}{n}}$$

$$\frac{sn}{3} + 1 - \frac{s}{3} = \frac{sn + 1 - s}{2}$$

$$2sn + 6 - 2s = 3sn + 3 - 3s$$

$$s = \frac{3}{n-1}$$

Appendix:

Matrix multiplication:

```
package ca.mcgill.ecse420.a1;
import java.util.Arrays;
import java.util.concurrent.ExecutorService;
import java.util.concurrent.Executors;
import java.util.concurrent.TimeUnit;
public class MatrixMultiplication {
 // private static final int NUMBER THREADS =
 private static final int NUMBER_THREADS = 4;
 private static final int MATRIX_SIZE = 2000;
 private static final int NUM ITERATIONS = 1;
 public static void main(String[] args) {
   boolean success = true;
    for (int i = 0; i < NUM ITERATIONS; i++) {</pre>
     System.out.println("\n=== ITERATION " + (i + 1) + "/" + NUM ITERATIONS +
" ====\n");
     // Generate two random matrices, same size
     double[][] a = generateRandomMatrix(MATRIX_SIZE, MATRIX_SIZE);
     double[][] b = generateRandomMatrix(MATRIX SIZE, MATRIX SIZE);
     long start;
     long stop;
     System.out.println("###### Sequential Multiplication #####");
     start = System.currentTimeMillis();
     double[][] seqResult = sequentialMultiplyMatrix(a, b);
     stop = System.currentTimeMillis();
     System.out.println("Sequential exec time(ms): " + (stop - start));
     System.out.println("###### Parallel Multiplication #####");
      start = System.currentTimeMillis();
     double[][] paraResult = parallelMultiplyMatrix(a, b);
     stop = System.currentTimeMillis();
     System.out.println("Parallel exec time(ms): " + (stop - start));
     // Check if results from parallel and sequential are the same
     if (!Arrays.deepEquals(seqResult, paraResult)) {
       success = false;
       break;
```

```
if (!success) {
     System.out.println("Sequential and parallel results did not match");
 }
  * @return the result of the multiplication
 public static double[][] sequentialMultiplyMatrix(double[][] a, double[][] b)
{
   int aRows = a.length;
   int bRows = b.length;
   int bColumns = b[0].length;
    int aColumns = a[0].length;
    double[][] c = new double[aRows][bColumns];
   if (aColumns != bRows) {
     throw new ArithmeticException("Invalid matrix dimensions");
    }
   for (int i = 0; i < aRows; i++) {</pre>
      for (int j = 0; j < bColumns; j++) {</pre>
        for (int k = 0; k < aColumns; k++) {</pre>
          c[i][j] += a[i][k] * b[k][j];
        }
      }
   return c;
 public static double[][] parallelMultiplyMatrix(double[][] a, double[][] b) {
```

```
int aRows = a.length;
    int bRows = b.length;
    int bColumns = b[∅].length;
    int aColumns = a[0].length;
    double[][] c = new double[aRows][bColumns];
   // Throw exception if matrix dimensions are invalid
   if (aColumns != bRows) {
      throw new ArithmeticException("Invalid matrix dimensions");
   try {
      ExecutorService executor = Executors.newFixedThreadPool(NUMBER_THREADS);
      for (int i = 0; i < aRows; i++) {</pre>
       for (int j = 0; j < bColumns; j++) {
          executor.execute(new ParallelMultiply(i, j, a, b, c));
      executor.shutdown();
      executor.awaitTermination(MATRIX_SIZE, TimeUnit.SECONDS);
      System.out.println("Terminated successfully: " + executor.isTerminated());
    } catch (Exception e) {
      e.printStackTrace();
   return c;
 static class ParallelMultiply implements Runnable {
   private int row;
   private int column;
   private double[][] a;
   private double[][] b;
   private double[][] c;
    ParallelMultiply(final int row, final int column, final double[][] a, final
double[][] b, final double[][] c) {
      this.row = row;
      this.column = column;
      this.a = a;
      this.b = b;
      this.c = c;
```

```
}
  public void run() {
    for (int k = 0; k < a.length; k++) {
      c[row][column] += a[row][k] * b[k][column];
 }
}
 * @param numCols number of cols
 * @return matrix
private static double[][] generateRandomMatrix(int numRows, int numCols) {
  double matrix[][] = new double[numRows][numCols];
 for (int row = 0; row < numRows; row++) {</pre>
    for (int col = 0; col < numCols; col++) {</pre>
      matrix[row][col] = (double) ((int) (Math.random() * 10.0));
    }
 return matrix;
}
```

Deadlock:

```
package ca.mcgill.ecse420.a1;

public class Deadlock {

  public static Object lock1 = new Object();
  public static Object lock2 = new Object();

  public static void main(String[] args) {
    DeadlockThread thread1 = new DeadlockThread(lock1, lock2);
    DeadlockThread thread2 = new DeadlockThread(lock2, lock1);
    thread1.start();
    thread2.start();
  }

  public static class DeadlockThread extends Thread {
    final Object lock1;
    final Object lock2;
```

Dining philosophers (with deadlock):

```
package ca.mcgill.ecse420.a1;
import java.util.concurrent.ExecutorService;
import java.util.concurrent.Executors;
public class DiningPhilosophersDeadlock {
 public static void main(String[] args) {
    int numberOfPhilosophers = 50;
   Object[] chopsticks = new Object[numberOfPhilosophers];
    Philosopher[] philosophers = new Philosopher[numberOfPhilosophers];
    ExecutorService executor =
Executors.newFixedThreadPool(numberOfPhilosophers);
   for (int i = 0; i < numberOfPhilosophers; i++) {</pre>
      chopsticks[i] = new Object();
   for (int i = 0; i < numberOfPhilosophers; i++) {</pre>
      philosophers[i] = new Philosopher(chopsticks, i, numberOfPhilosophers);
      executor.execute((philosophers[i]));
      try {
```

```
Thread.sleep((long) (Math.random() * 10));
     } catch (Exception e) {
        e.printStackTrace();
    executor.shutdown();
 public static class Philosopher implements Runnable {
    final Object rightChopstick;
    final Object leftChopstick;
   public Philosopher(Object[] chopsticks, int position, int
numberOfPhilosophers) {
     this.rightChopstick = chopsticks[(position + 1) % numberOfPhilosophers];
     this.leftChopstick = chopsticks[position];
   @Override
   public void run() {
     while (true) {
        String name = Thread.currentThread().getName();
        try {
         synchronized (rightChopstick) {
            System.out.println(name + " - Holding Right Chopstick");
            Thread.sleep((long) (Math.random() * 5));
            synchronized (leftChopstick) {
              System.out.println(name + " - Holding Left Chopstick");
              System.out.println(name + " - Eating");
             Thread.sleep((long) (Math.random() * 5));
            System.out.println(name + " - Released Left Chopstick");
          }
         System.out.println(name + " - Released Right Chopstick");
         Thread.sleep((long) (Math.random() * 10));
        } catch (Exception e) {
         e.printStackTrace();
        }
     }
```

Dining philosophers (no deadlock):

```
package ca.mcgill.ecse420.a1;
import java.util.concurrent.ExecutorService;
import java.util.concurrent.Executors;
public class DiningPhilosophersNoDeadlock {
 public static void main(String[] args) {
    int numberOfPhilosophers = 50;
   Object[] chopsticks = new Object[numberOfPhilosophers];
    Philosopher[] philosophers = new Philosopher[numberOfPhilosophers];
    ExecutorService executor =
Executors.newFixedThreadPool(numberOfPhilosophers);
   for (int i = 0; i < numberOfPhilosophers; i++) {</pre>
      chopsticks[i] = new Object();
   // Initialize Philosophers and execute the Thread
   for (int i = 0; i < numberOfPhilosophers; i++) {</pre>
      philosophers[i] = new Philosopher(chopsticks, i, numberOfPhilosophers);
      executor.execute((philosophers[i]));
      try {
        Thread.sleep((long) (Math.random() * 10));
      } catch (Exception e) {
        e.printStackTrace();
    executor.shutdown();
 public static class Philosopher implements Runnable {
   int ate = 0;
   final int id;
   final Object rightChopstick;
   final Object leftChopstick;
   Philosopher(Object[] chopsticks, int position, int numberOfPhilosophers) {
      this.id = position + 1;
      // Force the first philosopher to grab the chopstick to his left first
philosopher
      if (position != 0) {
       this.rightChopstick = chopsticks[position];
```

```
this.leftChopstick = chopsticks[(position + 1) % numberOfPhilosophers];
     } else {
        this.rightChopstick = chopsticks[(position + 1) % numberOfPhilosophers];
        this.leftChopstick = chopsticks[position];
   @Override
    public void run() {
     long start;
     long totalWait = 0;
     for (int x = 0; x < 1000; x++) {
        start = System.nanoTime();
        try {
          synchronized (rightChopstick) {
            Thread.sleep((long) (Math.random() * 5));
            // If chopstick is already locked, wait until available
            synchronized (leftChopstick) {
              totalWait += System.nanoTime() - start;
              ate++;
              Thread.sleep((long) (Math.random() * 5));
         Thread.sleep((long) (Math.random() * 10));
        } catch (Exception e) {
         e.printStackTrace();
        }
     System.out.println("Philosopher " + id + " ate " + ate + " times and
waited for " + totalWait/1000000000.0 + " seconds");
   }
 }
```

Dining philosophers (no starvation):

```
package ca.mcgill.ecse420.a1;
import java.util.concurrent.ExecutorService;
import java.util.concurrent.Executors;
import java.util.concurrent.locks.ReentrantLock;
public class DiningPhilosophersNoStarvation {
 public static void main(String[] args) {
   int numberOfPhilosophers = 50;
    Chopstick[] chopsticks = new Chopstick[numberOfPhilosophers];
    Philosopher[] philosophers = new Philosopher[numberOfPhilosophers];
    ExecutorService executor =
Executors.newFixedThreadPool(numberOfPhilosophers);
   for (int i = 0; i < numberOfPhilosophers; i++) {</pre>
      chopsticks[i] = new Chopstick();
   for (int i = 0; i < numberOfPhilosophers; i++) {</pre>
      philosophers[i] = new Philosopher(i, i > 0 ? chopsticks[i - 1] :
chopsticks[chopsticks.length - 1], chopsticks[i]);
      executor.execute((philosophers[i]));
     try {
        Thread.sleep((long) (Math.random() * 10));
      } catch (Exception e) {
        e.printStackTrace();
    executor.shutdown();
 public static class Chopstick {
    private ReentrantLock reLock = new ReentrantLock(true);
   public Chopstick() {
   public boolean grabStick() {
      return reLock.tryLock();
```

```
public void dropStick() {
     reLock.unlock();
   }
 public static class Philosopher implements Runnable {
   int ate = 0;
   final int id;
   final Chopstick rightChopstick;
    final Chopstick leftChopstick;
   public Philosopher(int position, Chopstick rightChopstick, Chopstick
leftChopstick) {
     this.id = position + 1;
     this.rightChopstick = rightChopstick;
     this.leftChopstick = leftChopstick;
   @Override
    public void run() {
     long start;
     long totalWait = 0;
     for (int x = 0; x < 1000; x++) {
        start = System.nanoTime();
       try {
         if (rightChopstick.grabStick()) {
            Thread.sleep((long) (Math.random() * 5));
            if (leftChopstick.grabStick()) {
              totalWait += System.nanoTime() - start;
              Thread.sleep((long) (Math.random() * 5));
              leftChopstick.dropStick();
            rightChopstick.dropStick();
         Thread.sleep((long) (Math.random() * 10));
        } catch (Exception e) {
         e.printStackTrace();
```

```
// To see # of times each philosopher ate, comment out the other
System.out.println() lines
    System.out.println("Philosopher " + id + " ate " + ate + " times and
waited for " + totalWait/1000000000.0 + " seconds");
    }
}
```