Problem 4. As we don't know our student letter, all the colculations will be held with ay, az.

a) The symbol rate gives 
$$T=2$$
,  $g_{Tx}=I_{6;2}$   
 $g_{c}(t)=a_{1}\delta_{o}(t-1)+a_{2}\delta_{o}(t-2)$   
 $g_{Ry}=I_{C_{0},1}$ 

It gives us the following system. b[n] y gc gc PRX TE T[b] P(4) = 9 + 9 (1)

We have P(t) = 9 x x 9 (t) = IB; 2] \* (a, o(t-1)+ a2 o(t-2))

p(+) = a [ (+-1) + a 2 [ (+-2)

We then can write r[k] = y & grx(k) = Sg(K-t)y(t) dt = 5k-1 g(t) dt sine Ts=1 = SK Ep[n] p(+-2n) dt + w[k] Low \*gex (K Ts)

Then W[K] = W\* gex (t-bis). [[W[K]] = E[W] \* 9 Rx and Cov [w[n], w[n+k3] = on2 Sp g (+) g (+-kts) dt Comain where glit and get - Dis) over lapp

Hence, Cov [W[n], W[nih]] = on on on (b)

So well is white zero mean with varion a on

b) Starting from (1): T[K]= E b[n] ( K a, ][n] (+-2n-1) + a= [n] (+-2n-2) d+ +w[k] Hence as t E [K-1; K] The integral is non negative for:

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So rean take the value: 3 (1+02) blos + vers a, b[n + ] + b[n] + w[H]

and our decision is 
$$\hat{b}[n] = C^{H}U \begin{bmatrix} b[n] \\ b[n] \end{bmatrix} + C^{H}W[n]$$

Then the probability of error, Pe = 1 Pr(Z[n]>01 b[n]=-1) + 1 Pr(Z(n) <01b[n]=+1)

= 1 (Pr ((Hwen3>-CHU[ben13] | ben-13=-1, ben)=1) ben+13=-1 + Pr (chwen3>-chu[ben+13] | ben+13=-1 ben+13=-1 ben+13=-1 ben+13=-1 ben+13=-1 ben+13=-1 ben+13=-1 ben+13=-1 ben+13=-1

As wisGaussian CHuisaloo gaussian with or= CHEWC = ECCHW(CHW)H] = CHECWHIC

if \$\int\_{\colored{1}} \int\_{\colored{1}} \int\_{\co

4+ EE (Q(-CFF"Ug [ b[n+1]) - Q(-CFFUg [ b[n+1]) + 2CFB b[n-1])