

## **Must Do Searching and sorting problems for Placement**

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# Searching And Sorting

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Ans → First and last occurrence of  $x$

Given a sorted array arr, containing  $n$  elements, with duplicate elements, task is to find out index of first and last occurrence of element

$x$ .  
Example:  $\{1, 2, 3, 5, 5, 5, 5, 8, 10, 16\}$   $x = 5$   
O/P → 2 5

Intuition :-

- we are binary searching given array & array + n for  $x$ .
- if present return  $\{i-1, i\}$
- 2 variable for lower & upper bound  
return them both

Code :-

bool isPresent = binary\_search(arr, arr+n, x);  
③ if (!isPresent) return {-1, -1};

int ind1 = lower\_bound(arr, arr+n, x) - arr;  
ind2 = upper\_bound(arr, arr+n, x) - arr - 1;

return {ind1, ind2};

③

Ques → Value equal to index value

Given arr of type int, find element whose value is equal to that of its index value

Example :

I/P = {15, 2, 45, 12, 63} O/P → 2.

Intuition :

if  $i$  is inside a loop,

if ( $i == \text{arr}[i]$ ) return  $\text{arr}[i]$   
else

Code :-

vector<int> valueEqualIndex(int arr[], int n)

(1)

vector<int> ans;

for (i=1; i <=n)

(2)

if ( $i == \text{arr}[i-1]$ )

ans.push\_back(i);

(3)

return ans;

(4)

Ques → Search in a rotated sorted array

array[], sorted., prior to being passed to your func<sup>n</sup>, nums is possibly rotating at unknown pivot value,  $k$  ( $1 \leq k < \text{length}$ ) such that resulting array  $[\text{num}[k], \text{num}[k+1], \dots, \text{num}[n-1], \text{num}[0], \text{num}[1], \dots, \text{num}[k-1]]$

Example  $\rightarrow [0, 1, 2, 3, 4, 5, 6] \rightarrow \text{rotate} \rightarrow [4, 5, 6, 7, 0, 1, 2]$

I/P -  $[0, 1, 2, 3, 4, 5, 6]$  target = 0

O/P  $\rightarrow 4$  (if not present return -1)

Intuition :- (Binary Search)

Need to modify binary search, plan is to create a recursive func<sup>n</sup> that takes l and r as range in input and the key.

algo :-

- 1) find middle point  $\text{mid} = (l+h)/2$
- 2) If key is present at middle point, return  $\text{mid}$ .
- 3) else if  $\text{arr}[l \dots \text{mid}]$  is sorted
  - ① If key to be searched lies in range from  $\text{arr}[l]$  to  $\text{arr}[\text{mid}]$ , recur for  $[l \dots \text{mid}]$
  - ② else recur for  $\text{arr}[\text{mid}+1 \dots h]$
- 4) Else ( $\text{arr}[\text{mid}+1 \dots h]$  must be sorted)
  - ① if key to be searched lies in range from  $\text{arr}[\text{mid}+1]$  to  $\text{arr}[h]$ , recur for  $\text{arr}[\text{mid}+1 \dots n]$
  - ② else recur for  $\text{arr}[l \dots \text{mid}]$

Ques → Middle of Three

Ques →

Given 3 nos., A, B, C. find the middle no.

In Example? A = 978    B = 518    C = 300

O/P - 518  
since  $518 > 300$  &  $518 < 978$

Intuition :-

$$\text{Sum}(A+B+C) - [\max(A, B, C) - \min(A, B, C)]$$

"", Overall sum = Circular Range.

middle  $\rightarrow$  ( $\max - \min$ ) from sum

Code :-

```
int middle(int A, int B, int C)
{
    return (A+B+C) - max({A,B,C}) - min({A,B,C});
}
```

## Ques → Find missing and repeating

Unsorted array arr of size N of type integers.  
1 number 'A' from set  $\{1, 2, 3, \dots, N\}$  is missing  
and 1 no. 'B' occurs twice in array.

Find these ones.

Example :- arr [] = {2, 2, 3}

O/P :- 2 → 2 is repeating  
no. & 1 is missing no. .

### \* Intuition :- (Using count array)

Create temp array temp[], initial value is 0.

Traverse input array arr[], and do following  
for each arr[i].

- if ( $\text{temp}[arr[i]] == 0$ )  $\text{temp}[arr[i]] = 1$ ;
- if ( $\text{temp}[arr[i]] == 1$ )  $\text{temp}[arr[i]] = 2$   
repeat for this.

Traverse temp[] and output the array element  
having value as 0 (It is the missing element)

(TC - O(N) SC - O(N))

## Ques - Find majority element

Given array A, find majority element in array. (size?)

majority : any element appear more than  $N/2$  times.

Example :  $N=3$ ,  $\{1, 2, 3\}$ ,  $O/P = -1$

$N=5$ ,  $\{3, 1, 3, 3, 2\} \Rightarrow O/P = 3$  (3 times)

Intuition : (using moore Voting Technique).

→ 1<sup>st</sup> step is to check majority elem.

if it is, then definitely return majority element else return candidate for maj. ele.

→ check obtained elem. is maj. or not.

Algo :- ( $Tc - O(N)$ )

- 1) loop through each element & maintain count of majority element, and majority index  $\Rightarrow$  maj index
- 2) If next ele. is same then, inc count if next ele. is not same. then inc count.
- 3) if count reach 0 then. changes maj index to curr element & chang count to 1.
- 4) Again traverse through array & find count of majority element found.
- 5) If count  $>$  than half  $N/2$ , print element
- 6) else print -1.

Snipper :-

Step 1

int findCandidate (int a[], int size)

(1)

int maj\_index = 0; count = 1;

for (i=1; i<size) {

if (a[maj\_index] == a[i])

count++;

else

count--;

if (count == 0) {

maj\_index = i;

count = 1;

(2)

return a[maj\_index]

Step 2

isMajority (int a[], int size, int cand)

{}

int count = 0;

for (i=0; i<size(); i++) {

(3)

if (a[i] == cand) count++;

if (count > size/2)

return 1;

else

return 0;

(4)

Ans → Search in an array where adjacent differ by at most 'k'.

Step array is an array of int where each element has difference of atmost k.

Given a key 'x' find index value of 'x' if xpl. ele. exist to return the 1st occurrence of key.

\* Example :-

$$\text{arr}[] = \{4, 5, 6, 7, 6, 3\} \quad k=1 \quad x=6$$

O/P = 2 // 1st index of 6 is 2.

$$\text{arr}[] = \{20, 40, 50, 70, 70, 60, 3\} \quad k=20 \quad x=60$$

O/P = 5 // 1st index of 60 is 5.

# Intuition :-

The diff. b/w all adj. ele is atmost k. Start compare left most ele. find the difference b/w curr. ele & 'x'.

Let difference be 'diff'.

We know that x atleast 'diff/k' away, so instead of searching 1 by 1, we jump 'diff/k'.

\* Code :- int search(int arr[], int n, int x, int k)

(1)

int i = 0;

while (i < n)

(2) if (arr[i] == x)

return i;

i = i + max (1, abs(arr[i] - x)/k);

(3)

cout < "not present";

return -1;

(4)

Ques :- Find a pair with given difference

Given unsorted array & no. 'n', find if there exist pair of element in array whose difference is n.

Example: arr[ ] = {5, 20, 3, 2, 50, 80} n = 78

$$\text{O/P} \Rightarrow (2, 80) \Rightarrow 80 - 2 = 78 = n.$$

Intuition :-

- Hashing can be used. Create empty hash table as HT. Traverse in array. use array element as hash key & enter in HT.
- Traverse array again. look for value target in HT.

\* Implementation :- bool findPair(int arr[], size, n)

(1)

unordered\_map<int, int> mpp;

for (int i=0; i<size)

    mpp[arr[i]]++;

for (i=0; i<size) (2)

    if (mpp.find(n+arr[i]) != mpp.end())

(3)

        cout << "found " << arr[i] << ", " << n+arr[i];

        return true;

(4)

(5)

    cout << " Not found ";

return false;

(6)

Ques- Find all four sum numbers

Given array int and another number. find all unique quadruple from given array that sums up to given number.

Example :-  $N=5 \quad K=3 \quad A[3] = \{0, 0, 2, 1, 1\}$ .  
O/P - 0 0 1 2 \$ sum of 0, 0, 1, 2 is  $3 = K$ .

Intuition :- (Hashing Based solution ( $O(n^2)$ ))

- 1) Store sums of all pair in hash table.
- 2) Traverse through all pairs again & search for  $x$  (curr pair sum) in hash table.
- 3) If pair is found with required sum, then make sure that all elements are distinct array elements and an element is not considered more than 1.

Pseudo code :- findElement(arr[], int n, int x).

```

{ unordered_map<int, pair<int, int>> mp;
  for (int i=0; i<n-1)
  {
    for (int j=i+1; j<n) mp[arr[i]+arr[j]] = {i, j};
  }
  for (int i=0; i<n-1; i++)
  {
    for (int j=i+1; j<n; j++)
    {
      if (arr[i]+arr[j] == x)
      {
        if (mp.find(x-arr[i]) != mp.end())
        {
          pair<int, int> p = mp[x-arr[i]];
          if (p.first == i && p.second == j || p.first == j && p.second == i)
          {
            cout << arr[i] << ", " << arr[j] << ", " << arr[p.first]
            << ", " << arr[p.second];
          }
        }
      }
    }
  }
}
  
```

Sum = ~~if arr[i]+arr[j]~~

```

if (mp.find(x-sum) != mp.end())
  
```

```

pair<int, int> p = mp[x-sum];
  
```

```

if (p.first == i && p.second == j || p.first == j && p.second == i)
  
```

```

cout << arr[i] << ", " << arr[j] << ", " << arr[p.first]
  
```

```

<< ", " << arr[p.second];
  
```

```

return;
  
```

Ques →

Stickler Thief

Given an array of +ve nos, find max sum of sub sequence with the constraints that no. 2 num. in seq should be adjacent in array.

So, 3 2 7 10 should return 13.

(3+10) for 3 2 5 7 10 (3, 5, 8, 7) return 13. Or  
Answe in most efficient way.

Example : arr[ ] = { 5, 5, 10, 100, 10, 5 } . O/P - 110.

Intuition :-

Loop for all elem. in arr[ ], maintain 2 sums,  
incl & excl where, incl = max-sum including the previous elem. & excl = Max-Sum excluding the previous element.

Max sum excluding the current element will be max(incl, excl) and max-sum including current element will be excl + curr-ele.

At the end loop return max of incl and excl.

Code :- findMaxSum ( Vector<int> arr, int n )

    int incl = arr[0], excl = 0, excl\_new, i;

    For ( i = 1 ; i < n ; i++ )

        excl\_new = ( incl > excl ) ? incl : excl;

        inlc = excl + arr[ i ];

        excl = excl\_new;

    return ( incl > excl ) ? incl : excl;

3

Ques + Count triplet with sum smaller than x.  
 Given array, size, & sum, find the count of triplet  $(i, j, k)$  having  $(i \leq j \leq k)$  with sum of  $(arr[i] + arr[j] + arr[k])$  smaller than given value sum.  
 Example -  $N = 5$ ,  $sum = 12$ .  $arr[ ] = \{ 5, 1, 3, 4, 7 \}$ .  
 O/P - 4.  $\because (1, 3, 4), (1, 3, 5), (1, 3, 7), (1, 4, 5)$ .

Intuition :-

- 1) Sort in rising order, & initialize ans = 0.
- 2) For loop  $i=0$  to  $n-2$ , to find all triplet with  $arr[i]$  as first element.
  - ① Initialize other two element as corner element of subarray  $arr[i+1, \dots, n-1]$ , i.e.,  $j = i+1$  &  $k = n-1$ .
  - ② Move  $j$  &  $k$  toward each other until they meet, i.e., while  $(j < k)$  :- (i) if  $arr[i] + arr[j] + arr[k] \geq sum$  then  $k--$ .
  - else for current  $i$  &  $j$ , there can  $(k-j)$  possible 3<sup>rd</sup> element that satisfy the constraint
  - (ii) else do  $ans += (k-j)$  followed by  $j++$ .

Code :-  $sort(arr, arr+n)$ , int ans = 0;

```
for( i=0 ; i<n-2 ; i++ ) {  
    int j=i+1, k=n-1;  
    while( j < k ) {  
        if ( arr[i] + arr[j] + arr[k] >= sum )  
            k--;  
        else  
            ans += (k-j);  
        j++;  
    }  
}
```

else {

    ans += (k-j);  
    j++;

}

③

③

return ans;

③

Ques -

Merge 2 sorted array, without extra space

Gives sorted arrays  $\text{arr1}[ ]$  &  $\text{arr2}[ ]$ , of  $N, M$  each  
merge 2 array into 1 sorted array without  
using extra space.

Example:  $N = 4, M = 5$

$\text{arr1}[ ] = \{1, 3, 5, 7\}$ ,  $\text{arr2}[ ] = \{0, 2, 6, 8, 9\}$

O/P  $\rightarrow [0, 1, 2, 3, 5, 6, 7, 8, 9]$

Intuition :-

- 1) Create swap of 2 pointers  $*a$  &  $*b$ .
- 2) while  $j$  while ( $\text{start} \leq \text{end}$  and  $j \leq m$ ).  
then check for  $\text{arr1}[\text{start}] > \text{arr2}[j]$   
  - swap ( $\&\text{arr1}[\text{end}]$ ,  $\&\text{arr2}[j]$ );
  - $\text{end}--$ ;  $j++$ ;
  - else  $\text{start}++$ ;

Now sort both the array till its size

Code :-

```

void swap (int *a, int *b)
{
    int temp;
    temp = *a;
    *a = *b;
    *b = temp;
}

void merge (arr1, arr2, n, m)
{
    start = 0; end = n-1; j = 0;
    while (start <= end and j < m)
    {
        if (arr1[start] > arr2[j])
        {
            swap (&arr1[end], &arr2[j]);
            end--;
            j++;
        }
        else
            start++;
    }
    sort (arr1, arr1+n);
    sort (arr2, arr2+m);
}

```

## Ques + Zero sum subarray

Given array  $[ ]$  of  $N$  size, find total count of sub array having their sum equal 0.

Example :-  $n = 6$  arr $[ ] = [0, 0, 5, 5, 0, 3]$ .

OP  $\rightarrow 6 \rightarrow [0], [0], [0], [0], [0, 0] \& [0, 0, 3]$ .

### # Intuition :-

BF - check for every sub-arr if  $\text{sum} = 0$ , return

Optimal - (i) find prefix sum  $[4, 6, 3, 4, 10]$  4 repeat 2 time, if we are getting any  $K$  value 2 or more time then it is ~~sum~~ sum subarray

using Hash map - maintain sum of element encountered so far in variable say  $\text{curr sum}$ .

if  $\text{sum} = 0$ , found it. starting from 0 index till curr.

Check if current sum exist in hash table or not, if curr sum already exist in hash table, then this sum is subarray.

Subtract array ele. arr $[0]$  to arr $[i]$ . same sum obtain.

Insert current sum into hash table.

### Dry Run :-

6	1	3	-1	-3	4	1	-2	2
---	---	---	----	----	---	---	----	---

$\text{sum} = 0$ , map(empty), vector(empty)

0 1 2 3 4 5 6

Step 1 - arr  $| 6 | 3 | -1 | -3 | 4 | -2 | 2 |$  map  
 $\uparrow$   
 $\text{sum} = 6$   $6 \rightarrow 0$

0	1	2	3	4	5	6
6	3	-1	-3	4	-2	2
i						

map

6 → 0
9 → 1

One to One

0	1	2	3	4	5	6
6	3	-1	-3	4	-2	2
i	2					

map

6 → 0
9 → 1
8 → 2

0	1	2	3	4	5	6
6	3	-1	-3	4	-2	2
i						

map

6 → 0
9 → 1
8 → 2
5 → 3

0	1	2	3	4	5	6
6	0	-1	-3	4	-2	2
i						

map

6 → 0
3 → 1, 4
8 → 2
5 → 3
2 → 5

0	1	2	3	4	5	6
6	3	-1	-3	4	-2	2
i						

map

6 → 0
9 → 1, 4
8 → 2
5 → 3
7 → 5

0	1	2	3	4	5	6
6	3	-1	-3	4	-2	2
i						

vector  $\{2, 4, 5, 6\}$ 

map.

6 → 0
9 → 1, 4, 6
8 → 2
5 → 3
7 → 5

## Ques → Product array puzzle

Given array  $\text{num}[i]$ , construct product array ' $P$ ',  
size is :  $P[i] = \text{product of all elements of num}$   
except  $\text{num}[i]$ .

Example :-  $n=5$

$\text{num}[i] = [10, 3, 5, 6, 2]$  O/P - 180, 600, 360, 300, 900  
 $\Rightarrow 3^* 5^* 6^* 2 = 180 ; 10^* 5^* 6^* 2 = 600$ , and so on..

Intuition :-

2 int i & j for loop. i will track position of our cursor and j will do product calc. as:

$\text{if } (i \neq j) \text{ product} * \text{num}[j]; i$

code :-  $\text{vector<long long int>} v;$

$\text{for } (i=0; i < n)$

(1)  $\text{long long int product} = 1;$

$\text{for } (\text{int } j=0; j < n; j++)$

(2)

$\text{if } (i \neq j)$

$\text{product} * \text{num}[j];$

(3)

$v.\text{push\_back}(\text{product});$

(4)

$\text{return } v;$

Aus → Sort by set bit count

Aus →

given array, sort the array (in descending order)  
acc. to count of set bits in binary representation of array

Example :-

$\text{arr}[7] = \{5, 2, 3, 9, 4, 6, 7, 15, 32\}$

15 - 1111, 7 - 0111, 5 - 0101, 3 - 0011, 9 - 1001, 6 - 0110,

2 - 0010, 4 - 0100, 32 - 100000.

O/P - {15, 7, 3, 5, 9, 6, 2, 4, 32}.

Intuition :-

Create an array and store set-bit count of all int.  
in aux-array.

Simultaneously sort both array acc. to non-increasing  
order of auxiliary array.

Code :-      SortBySetBit (int arr[], int n)

```
int aux[n];
for (int i=0; i<n; i++)
    aux[i] = count Bits (arr[i]);
```

insertionSort (arr, aux, n);

}

in insertion sort ()

for ( $i=1 \rightarrow i < n$ ) { int  $k_1 = \text{aux}[i]$ ;

$k_2 = \text{arr}[i]$ ; int  $j = i-1$ ;

while ( $j >= 0 \& \& \text{aux}[j] < k_1$ ) {

$\text{aux}[j+1] = \text{aux}[j]$ ;  $\text{arr}[j+1] = \text{arr}[j]$ ;

$j = j-1$ ; }

$\text{aux}[j+1] = k_1$ ;  $\text{arr}[j+1] = k_2$ ; ? ?

## Ques → Minimum swap to sort

Given array, find mini. no. swaps to sort in <sup>swap</sup> ~~using order.~~

Example :

num = {2, 8, 5, 4}  $\rightarrow$  8  $\leftrightarrow$  4  $\rightarrow$  2, 4, 5, 8

Intuition :-

- 1) Take an empty vector, & sort it, say b[ ].
- 2) Take a map to track the count, and enter array values in map.
- 3) Iterate a loop in which if (num[i] != b[i])
- 4) swap pos = m[b[i]] with num[i], and increase count for all elements & return count  $\rightarrow$  cnt in end

Code :- minSwap (vector<int> &num) [E]

```
n = size, vector<int> b = num;
sort (b.begin(), b.end());
map<int, int> m; for (int i=0; i < n; i++) m[num[i]] = i;
int cnt = 0;
```

for (i=0; i < n) (E)

if (num[i] != b[i]) (E)

int pos = m[b[i]] i;

m[num[i]] = pos;

num[i] = b[i];

m[num[i]] = i;

cnt ++;

(3)

(3)

(3)

Ques. Max. no. of people that can be killed with strength P

Infinite no. of people standing in row, from 1 to  $\infty$ .  
A person of index  $i$  has strength  $i^2$ . You've strength  $P$ , So you have to tell what is the max. no. of people you can kill with strength  $P$ .

You can kill a person with strength  $x$  if  $P \geq x$ .  
So after kill strength decrease by  $x$ .

Example :-

$$P = 14, \text{ 1st person has str. } 1^2 = 1 \Rightarrow 1 > P$$

$$\Rightarrow 14 - 1 = 13(P) \text{, 2nd person } \Rightarrow 13 - 4 = 9$$

$$\text{Otherwise, 3rd person } \Rightarrow 9 - 9 \leq 0 \text{, can't kill.}$$

Ans.  $\boxed{3}$

\* Intuition :-  $Tc(O(\log n)) - Sc - O(1)$

We can use binary search.

Start binary search by considering low as 0 and high  $10^{15}$ . We will calculate mid value, we will & using mid value we will change position of low and high.

$$O:- \text{mid} = \text{low} + (\text{high} - \text{low})/2$$

$$\text{then, } (n * (n+1) * (2 * n + 1)) / 6$$

Code :-

low = 0; high = 1000000L; ans = 0L;

while (low <= high)

(2) // to calculate mid value

low mid = low + (high - low) / 2;

low value =  $(n * (n+1)) * (2 * n + 1) / 16$ ;

if (value <= n) // compare value with n

(3) ans = mid;

low = mid + 1;

(4)

else

high = mid - 1;

(5)

return ans;

Ques :- Find  $k^{th}$  smallest element in given n range

Given n ranges,  $n = \text{no. of ranges}$  &  $q = \text{no. of queries}$ , find  $k^{th}$  smallest element for each query (let  $k > 1$ )  
print  $k^{th}$  smallest ele if exist else -1.

Example :-

I/P :- arr[ ] = { {1, 4}, {6, 8} } ; Queries = {2, 6, 8}

O/P - 2      7      -1  
 $\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 2 & 3 & 4 & 6 & 7 & 8 \end{matrix} \rightarrow 2^{nd} \text{ element is } 2.$

6<sup>th</sup> element is 7, so not exist so -1.

\* Intuition :- (Merge Overlapping Interval). TC -  $O(n \log(n))$

- 1) First we'll merge overlapping interval & keep all intervals sorted in ascending order of start time.
- 2) after merging in merged[], we use linear search for  $k^{th}$  smallest element.

\* Implementation :- kthSmallest (vector<interval> merge, int k)

(1)  $n = \text{merge.size();}$

for ( $j = 0 \rightarrow j < n$ )

if ( $k \leq \text{abs}(\text{merge}[j].e - \text{merge}[j].s + 1)$ )

return ( $\text{merge}[j].s + k - 1$ )

$k = k - \text{abs}(\text{merge}[j].e - \text{merge}[j].s + 1);$

(2)

if ( $k$ )

return -1.

(3)

Ques → Find minimum element in sorted and rotated array

Sorted array is rotated at unknown point,  
find min. element in it.

Example :-  $\{5, 6, 1, 2, 3, 4\}$  O/P - I

$\{1, 2, 3, 4\}$  O/P - I. ( $\because$  it is minimum)

#### \* Intuition :- (Binary Search - $T.C.(O \log(n))$ )

- Min. element is the element whose prev. ele. is greater than it. If no prev., then no rotation, (then 1<sup>st</sup> element is minimum).
- Check this condn for middle element by comparing with (mid-1)<sup>th</sup> term and (mid+1)<sup>th</sup> term.
- If minimum does not at middle :-
  - Then it lies either left half or right half
    - (1) If the middle element is smaller than last element, the min. lies in LH.
    - (2) Else, lies in Right half (RH).

#### \* Implementation :- Find Min (int arr, low, high)

if (high < low) return arr[0];

if (high == low) return arr[low];

int mid = low + (high - low) / 2;

// to find mid.

// now we check if ele. (mid+1) is mini. elem.

```
if (arr[mid] < arr[mid + 1] && arr[mid + 1] < arr[mid])  
    return arr[mid + 1];
```

// check if mid itself is mini ele.

```
if (arr[mid] > arr[low] && arr[mid] < arr[mid - 1])  
    return arr[mid];
```

// Decide whether we need to go LH or RH

```
if (arr[high] > arr[mid])  
    return findMin(arr, low, mid - 1);  
return findMin(arr, mid + 1, high);
```

## Ques. $k^{\text{th}}$ element of 2 sorted array

Given 2 sorted arrays, need to find  $k^{\text{th}}$  element.

Final element that would be at  $k^{\text{th}}$  position

of final sorted array.

Example :-

Input :- A<sub>1</sub> = 2 3 6 7 9      A<sub>2</sub> = 1 4 8 10      k = 5  
 $k = 5$ , final sorted array :- 1 2 3 4 6 7 8 9 10  
I/P - 6.

Intuition :- (use upper\_bound())

Example - A<sub>1</sub> = 2 3 4 6 7 9 , A<sub>2</sub> = 1 4 8 10  
 $k = 5$       ans = 6 .

→ 5<sup>th</sup> ele. is 6, 8, 1<sup>st</sup> ele. is 1. Notice here that upper\_bound(A) gives 5, upper\_bound(A) gives 4, it is the nos. less than or equal to nos. we are given as input to upper\_bound().

→ using upper\_bound to check what is position of element in sorted array.

upper\_bound func<sup>n</sup> return pointer to elem which is  $\geq$  than the element we searched.

→ To find  $k^{\text{th}}$  element, need to just find upper\_bound().

→ If we have given 2 array, we just need to sum of upper-bound for 2 array.

\* I/P - 1 2 3 6 7 9      2 4 8 10      k=5

Value of upper\_bound pts value(6) in arr1 = 3  
And arr2 is 2.

Total = 5 which is ans.

### Alg0 :-

- 1) we take a mid between  $[L, R]$  using  $\text{mid} = (L, R) / 2$
- 2) check if mid can be  $K^{\text{th}}$  element using  
 $\text{upper bound}()$  funcn.
- 3) Find the sum  $\text{upper bound}()$  for both the array  
and if sum is  $\geq K$ , its possible value of  $K^{\text{th}}$  also.
- 4) if sum is  $\geq K$ , then  $R = \text{mid} - 1$ .
- 5) else if sum  $< K$ , then cur. mid is too small  
so we assign  $L = \text{mid} + 1$ .
- 6) Repeat from top.
- 7) Return smallest value found

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## Ques- Aggressive Cow (Cpobj)

Given array of  $N$  length, which denote pos of stalls. Now  $N = \text{no. of stalls}$  &  $K = \text{no. of aggressive cows}$ . To prevent cow from fighting, you need to assign cow to stall, such that, minimum dist b/w 2 of them is as large as possible.

Find largest minimum dist.

Example :-

arr: ⑦, ②, ⑨, ⑧, 9 &  $K=3$ . Ans - O/P - 3.

1<sup>st</sup> cow @ stall 1, 2<sup>nd</sup> cow at stall 4, 3<sup>rd</sup> cow @ stall 8

\* Intuition :-

We need to define `isPossible()` that check if dist.  $x$  is possible between each of the cow. We use greedy approach, by placing cows at leftmost possible stall such that, atleast  $x$  dist away from last placed cow.

We need to sort given array first, so once we have our sorted array to do greedy task, then we apply Binary Search, on sorted input, & use `isPossible()` to find largest distance.

Binary Search :-

Firstly, consider low & high starting & end pos  
 $\text{low} = 0$  &  $\text{high} = \text{end pos}$ .

Let mid be minimum dist., check in sorted array, how many position available of that min. dist. b/w them is mid.

Try Run over = 1, 2, 4, 8, 9 low = l, high = h, mid.

$$\boxed{1|2|4|8|9} \rightarrow \boxed{1|2|4|8|9} \rightarrow \boxed{1|2|9|8|9}$$

$l=2$ ,  $h=9$ ,  $n=8$ ,  $c_1 \uparrow$ ,  $c_2 \uparrow$ ,  $c_3 \uparrow$ ,  $2-1 \geq 4$  X,  $9-1 \geq 8$  X  
 $mid = \frac{l+h}{2} = 4$

$$\boxed{1|2|9|8|9} \rightarrow \boxed{1|2|7|8|9} \rightarrow$$

$c_1 \uparrow$ ,  $c_2 \uparrow$ ,  $c_3 \uparrow$ ,  $8-1 \geq 9$  ✓,  $9-8 \geq 4$  X

Now we could only place 2 cows not 3, so return false as "4" diet. But cows is not possible, it has to be 1 or from 4  
 $\text{so high} = \text{mid} - 1 = 4 - 1 = 3$

Now, low = 1, high = 3, so mid =  $\frac{l+h}{2} = 2$ .

$$\boxed{1|2|4|8|9} \rightarrow \boxed{\frac{1}{2}|2|4|8|9} \rightarrow \boxed{1|2|4|8|9} \rightarrow$$

$l=1$ ,  $h=3$ ,  $c_1 \uparrow$ ,  $c_2 \uparrow$ ,  $c_3 \uparrow$ ,  $2-1 \geq 2$  X,  $9-1 \geq 2$  ✓  
 $mid = \frac{l+h}{2} = 2$

$$\boxed{1|2|4|8|9} \quad ans = 2$$

$c_1 \uparrow$ ,  $c_2 \uparrow$ ,  $c_3 \uparrow$ ,  $8-1 \geq 2$  ✓

Now, we know, one possible ans is 2. %, we need to maximize mini ans. So try to find for diet > 2.

So, low = mid + 1,  $2+1=3$ .

low = 3, high = 3, mid = 3.

$$\boxed{1|2|4|8|9} \rightarrow \boxed{1|2|9|8|9} \rightarrow \boxed{1|2|4|8|9} \rightarrow$$

$l=3$ ,  $h=3$ ,  $c_1 \uparrow$ ,  $c_2 \uparrow$ ,  $c_3 \uparrow$ ,  $2-1 \geq 3$  X,  $4-1 \geq 3$  ✓  
 $mid = \frac{3+3}{2} = 3$

$$\boxed{1|2|4|8|9} \rightarrow \boxed{1|2|4|8|9}$$

$c_1 \uparrow$ ,  $c_2 \uparrow$ ,  $c_3 \uparrow$ ,  $9-8 \geq 3$  X,  $8-1 \geq 3$  ✓

$$ans = 3, 4, 8 \Rightarrow \textcircled{3}$$

## K is Possible function

bool isPossible() { vector<int> stalls, minDist, k);

① int curr = 1;

// already place 1<sup>st</sup> available slot (greedy)

int lastCustPos = stalls[0];

for (int i=0; i < stalls.size(); i++)

②

if (stalls[i] - lastCustPos >= minDist)

③

curr++;

lastCustPos = stalls[i];

if (curr >= k) return true;

④

return false;

⑤

\* \* Allocates minimum number of pages  
 Given no. of pages, in  $n$  diff. books and  $m$  student. Books arranged in ascending order of no. of pages. Every student assigned to read some consecutive book. Task is to assign book in such a way, max no. of pages assigned to student is minimum.

④ Example 8:- Pages:  $[12, 34, 67, 90]$   $m = 2$

Ans - O/P - 113.

2 no. of students, books can be distributed as:

(1)  $[12]$  and  $[34, 67, 90]$ , max page allocated to student

2 with  $34 + 67 + 90 = 191$  page

(2)  $[12, 34]$  and  $[67, 90]$ , max page allocated to student 2 is,

$67 + 90 = 157$  pages

(3)  $[12, 34, 67]$  and  $[90]$  max page allocated to student 2,

$12 + 34 + 67 = 113$  pages.

minimum no. of pages

⑤ Intuition :- (Binary search)

→ we fix value for no. of pages as mid of current, minimum & maximum.

→ Initialize, minimum=0 & maximum = sum of all pages.

→ If curr mid is sol<sup>n</sup>, then search LH, else High Half (HH)

# How to check mid value is feasible or not

\* Basically, we need to check, if we can assign pages to all student in a way, max no. doesn't exceed curr. value. To do this,

\* we sequentially assign pages to every student until curr. no. of assigned pages doesn't exceed value.

↳ if no. of student > m, sol<sup>n</sup> not possible/feasible  
 else possible/feasible.

Ques -

Job Scheduling Algo.

Given  $N$  jobs, every job is represented by following three elements :-

- 1) Start Time
  - 2) Finish Time
  - 3) Profit or value arrived
- Find max profit subset of jobs such that no two jobs in subset overlap.

\* Example :-  $n = 4$

Job details :- start time, finish time, profit ?

Job 1 :  $\{1, 2, 50\}$  Job 2 :  $\{3, 5, 20\}$

Job 3 :  $\{6, 19, 100\}$  Job 4 :  $\{2, 100, 200\}$

Ans - max profit is 250.

We can get max profit by scheduling job 1 & 4.

$$\rightarrow 50 + 200 \Rightarrow 250 \text{ profit}$$

Intuition :- (Recursion)

$\Rightarrow$  Sort jobs according to finish time.

Now, apply following recursion process.

(i)  $\text{f}[n]$  array  $\Rightarrow$  array of  $n$  jobs.

Find  $\text{maxProfit}(\text{arr}, n)$

$\{$  (a) if ( $n = -1$ ) return arr[ $\{$ ];

b) Return max. of following 2 profit.

i) max profit by excluding curr job, i.e.

$\text{findMaxProfit}(\text{arr}, n-1)$

ii) Maximum profit by including curr job.

3

The idea is to find least latest job before current job in sorted array, that doesn't conflict with curr job, & arr[n-i]

Once we find such a job, we recur from all jobs till that job add profit of current job

so we are using binary search, and dp concept.  
Tc  $O(n \log n)$

## Ques :- Arithmetic Number.

Ques :-

Given 3 integers 'A' denote first term of arithmetic sequence, 'c' denote common difference of arithmetic sequence and an integer 'B'.

Tell me whether 'B' exist in the arithmetic seq. or not.

Example :-

$$A=1, B=3, C=2.$$

Output  $\rightarrow 1$ .

3 is 2<sup>nd</sup> term of seq starting with 1 & having common diff: 2.

Intuition :-

Check if  $C = 0$ , if true then  $B = A$ ,  
true than 1 else 0.

Or  $B-A$  remainder of  $(c_B - A) \% C$  not equal 0,  
 $c > 0$  or  $B-A > 0$  or  $c < 0$ ).

the 0, otherwise 1 (true)

Ques → Smallest factorial number

Given a no.  $N$ , find smallest number whose factorial contain atleast  $n$  trailing zeroes.

Example :-

$n = 1$ .      output -  $5!$

Explanation -  $5! = 120$  which has atleast 1 trailing 0.

\* Intuition :-

Trailing 0's in  $x!$  = count of 5s in prime factor of  $x!$ .

$$= \text{floor}(x/5) + \text{floor}(x/25) + \text{floor}(x/125) + \dots$$

We can notice that max. value whose factorial contain  $n$  trailing zeroes is  $5^* n$

so to find max. value fact. contain in trailing zero, use binary search ranging 0 to  $5^* n$ .

And, find smallest no. whose factorial contain  $n$  trailing zeroes.

## Ques - Subset Sum

given list arr of N, print sums of all subset in it.

Example :-

I/P :- N=2 and arr[ ] = {2, 3, 3}

O/P :- 0, 2, 3, 5

when no element taken sum = 0,

when 1 taken sum = 2.

when 2 taken sum = 3.

when 2 & 3 taken sum = 2 + 3 = 5.

Intuition :-

→ we'll solve this question using recursion, we'll take a vector base[ ]; and if n=1,

→ then push 0 and push arr[0] and return base.

→ take 2 variable s, first and last.

and a vector mkn, sumkn.

① mkn contain (first, last);

② mkn contains subset (arr, s-1);

→ Iterating in loop, i and entire

③ a = mkn[i] + (\*arr[i]) and push a into mkn vector.

→ and in end return mkn;

## Ques → Implement Merge Sort in place

Implementation merge sort is standard implementation keeping sorting algo. as in-place.

In-place means it doesn't occupy extra memory for merge operation as in the standard case.

Example :-

$arr[ ] = \{ 2, 3, 4, 13 \} : O/p \rightarrow 1, 2, 3, 4$

$arr[ ] = \{ 56, 2, 45 \} : O/p \rightarrow 2, 45, 56$

### ④ Intuition :-

→ Let we've a no. A, & want to convert into no. B.

& also a constraint that we can also recover no. A any time without using variable.

→ To achieve this we choose no. N, which is greater than both numbers and add  $B^*N$  in A.

### ⑤ To get B out from $(A+B^*N)$

we divide  $(A+B^*N)$  by N as  $(A+B^*N) \% N = B$

# (By taking modulus, we get old no. back, taking divide we get new no.).

## Algorithms

### # mergeSort() :-

→ Calculate mid & split array into two halves (left-sub-array & right-sub-array)

- Recursively call merge sort on left-subarray and right-subarray to sort them.
- Call merge func<sup>n</sup> to merge left-sub and right sub.

# merge():

- ① firstly find max. ele. in both sub array & increment by 1, to avoid collision by 0. & max. element during mod.
- ② Ideal is to traverse both sub-array from start simultaneously.
- ③ One start from 'l' till 'm'; another start from  $m+1$ , till 'r'. So, we will initialize 3 pointers say  $i, j, k$ .
- ④  $i$  move from  $l$  till  $m$ ;  $j$  will move from  $m+1$  till  $r$ ;  $k$  will move from  $l$  till  $r$ .
- ⑤ Now, update value  $a[k]$  by adding  $\min(a[i], a[j]) * \text{maximum\_element}$ .
- ⑥ Then also update those elements which are left in both sub-array.
- ⑦ After updating all the elements divide all the elements by maximum-element. so we get updated array back.

Ques → How to sort a big array with many repetition

Consider big array where elements are from small set and in any range.  
i.e. there are many repetition. How efficiently sort the array?

Example :- arr[ ] = {100, 12, 100, 1, 1, 12, 100, 1, 12, 100, 1, 1}  
arr[ ] = {1, 1, 1, 1, 1, 1, 12, 12, 12, 100, 100, 100}

Intuition :- (Binary Heap).

We can use Binary Heap to solve in  $O(n \log m)$  time, also use Hashing to solve  $O(n + m \log m)$ .

- (1) Create empty hash table. Input array values are stored as key and their count are stored as value in hash table.
- (2) For every element 'x' of arr[ ], do this :
  - (a) if x is present in hashTab, use its value.
  - (b) else insert x with value equal to 1.
- (3) Consider all keys of hash table & sort them.
- (4) Traverse all sorted keys and print every key its value times.

## Implementation

void sort (int arr[], int n)

②

```
map<int, int> count;  
for (int i=0; i<n; i++)  
    count [arr[i]]++;
```

map<int, int> :: iterator it;

int index = 0;

++it

for (it = count.begin(); it != count.end(); it++)

③

while (it → second --)

arr [index ++] = it → first;

④

⑤

T.C -  $O(n + m \log m)$