

Minimum Spanning Trees

Minimum Spanning Trees are data structures that have
the minimum required number of edges to connect all
vertices. Will investigate how to create one using the
Depth First Search.

The major difference between a DFS and a MST is that the
MST must record the edges traveled. You'll know you have
created a MST when the number of edges equals the number
of vertices - 1.

```
class MyStack:
```

```
    def __init__(self, size):
```

```
        self.size = size
```

```
        self.my_stack = [0] * self.size
```

```
        self.top = -1
```

```
    def push(self, val):
```

```
        self.top += 1
```

```
        self.my_stack[self.top] = val
```

```
    def pop(self):
```

```
        self.top -= 1
```

```
        return self.my_stack[self.top + 1]
```

```
    def peek(self):
```

```
        return self.my_stack[self.top]
```

```
    def is_empty(self):
```

```
        return self.top == -1
```

```
class Vertex:
```

```
    def __init__(self, name):
```

```
        self.name = name
```

```
        # Used for searching
```

```
        self.visited = False
```

```
class Graph:
```

```
    def __init__(self):
```

```
        self.max_vertices = 10
```

```
        self.vertex_list = [0]*10
```

```
        self.adjacency_matrix = [[0] * self.max_vertices for i in range(self.max_vertices)]
```

```
        self.vertex_count = 0
```

```
        self.the_stack = MyStack(20)
```

```
    def add_vertex(self, name):
```

```
        self.vertex_list[self.vertex_count] = Vertex(name)
```

```
        self.vertex_count += 1
```

```
    def add_edge(self, first, last):
```

```

self.adjacency_matrix[first][last] = 1
self.adjacency_matrix[last][first] = 1

def print_vertices(self):
    for i in self.vertex_list:
        if isinstance(i, int):
            print(0)
        else:
            print(i.name)

def print_edges(self):
    for row in self.adjacency_matrix:
        for elem in row:
            print(elem, end=' ')
        print()

# NEW print vertex name
def print_vertex(self, index):
    print(self.vertex_list[index].name, end="")

def get_next_unvisited_vertex(self, curr_vertex):
    for i in range(0, self.vertex_count):
        if self.adjacency_matrix[curr_vertex][i] == 1 and self.vertex_list[i].visited is False:
            return i
    return -1

# The Minimum Spanning Tree Function
def min_span_tree(self):
    # Start searching at vertex in index 0
    self.vertex_list[0].visited = True

    # Push 0 in the stack
    self.the_stack.push(0)

    while not self.the_stack.is_empty():
        # Get the current vertex
        curr_vert = self.the_stack.peek()

        # Get the next neighbor vertex
        next_vert = self.get_next_unvisited_vertex(curr_vert)

        # If no more neighbor vertices
        if next_vert == -1:
            # Get rid of it
            self.the_stack.pop()
        else:
            # Visit it
            self.vertex_list[next_vert].visited = True
            self.the_stack.push(next_vert)

    # NEW Major change versus Depth First Search
    # Edge from this vertex
    self.print_vertex(curr_vert)
    # to this vertex

```

```
self.print_vertex(next_vert)
print()
```

```
# Stack is empty so set all vertices back to unvisited
for i in range(0, self.max_vertices):
    if isinstance(i, int):
        pass
    else:
        self.vertex_list[i].visited = False
```

```
# Test the Minimum Spanning Tree
```

```
graph = Graph()
graph.add_vertex('A')
graph.add_vertex('B')
graph.add_vertex('C')
graph.add_vertex('D')
graph.add_vertex('E')
```

```
# Make edges to each vertex
```

```
graph.add_edge(0, 1)
graph.add_edge(0, 2)
graph.add_edge(0, 3)
graph.add_edge(0, 4)
graph.add_edge(1, 2)
graph.add_edge(1, 3)
graph.add_edge(1, 4)
graph.add_edge(2, 3)
graph.add_edge(2, 4)
graph.add_edge(3, 4)
```

```
# Have the algorithm figure out one line that connects
```

```
# from one vertex to the others
```

```
graph.min_span_tree()
```