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1 Basic

1.1 Compiler Shell

```
if [ $# -ne 2 ] ; then
    g++ -std=c++17 -DABS -Wall -Wextra -Wshadow $1.cpp -o
    $1
else
    g++ -std=c++17 -DABS -Wall -Wextra -Wshadow $1.cpp -o
    $1 -fsanitize=address
fi
./$1
chmod +x ./run.sh
./run.sh main [1]
```

1.2 Testing Todo List

0. choose editor
1. shell script
2. __int128, __lg, __builtin_popcount
3. judge speed v.s. local speed
4. CE penalty?

1.3 Debug Macro

```
void db() {cout << endl;}
template <typename T, typename ...U> void db(T i, U ...
    j) {
    cout << i << ' ', db(j...);
}
#define tes(x...) db("[ " + string(x) + " ]", x)
```

1.4 Stress Test Shell

```
g++ main.cpp -o main
g++ gen.cpp -o gen
g++ good.cpp -o good
for i in {1..100} ; do
    ./gen > input.txt
    ./main < input.txt > output1.txt
    ./good < input.txt > output2.txt
    if cmp --silent -- "output1.txt" "output2.txt" ; then
        continue
    fi
    echo Input:
    cat input.txt
    echo Your Output:
    cat output1.txt
    echo Correct Output:
    cat output2.txt
    break
done
echo OK!
```

1.5 Fast IO

```
#include<unistd.h>
char OB[65536]; int OP;
inline char RC() {
    static char buf[65536], *p = buf, *q = buf;
    return p == q && (q = (p = buf) + read(0, buf, 65536)
        ) == buf ? -1 : *p++;
}
inline int R() {
    static char c;
    while((c = RC()) < '0'); int a = c ^ '0';
    while((c = RC()) >= '0') a *= 10, a += c ^ '0';
    return a;
}
inline void W(int n) {
    static char buf[12], p;
    if (n == 0) OB[OP++] = '0'; p = 0;
    while (n) buf[p++] = '0' + (n % 10), n /= 10;
    for (--p; p >= 0; --p) OB[OP++] = buf[p];
    if (OP > 65520) write(1, OB, OP), OP = 0;
}
```

2 Data Structure

2.1 Leftist Tree

```
struct node {
    ll rk, data, sz, sum;
    node *l, *r;
    node(ll k) : rk(0), data(k), sz(1), l(0), r(0), sum(k)
    {}
};
ll sz(node *p) { return p ? p->sz : 0; }
ll rk(node *p) { return p ? p->rk : -1; }
ll sum(node *p) { return p ? p->sum : 0; }
node *merge(node *a, node *b) {
    if (!a || !b) return a ? a : b;
    if (a->data < b->data) swap(a, b);
    a->r = merge(a->r, b);
    if (rk(a->r) > rk(a->l)) swap(a->r, a->l);
    a->rk = rk(a->r) + 1, a->sz = sz(a->l) + sz(a->r) +
    1;
    a->sum = sum(a->l) + sum(a->r) + a->data;
    return a;
}
void pop(node *&o) {
    node *tmp = o;
    o = merge(o->l, o->r);
    delete tmp;
}
```

2.2 Splay Tree

```

struct Splay {
    int pa[N], ch[N][2], sz[N], rt, _id;
    ll v[N];
    Splay() {}
    void init() {
        rt = 0, pa[0] = ch[0][0] = ch[0][1] = -1;
        sz[0] = 1, v[0] = inf;
    }
    int newnode(int p, int x) {
        int id = _id++;
        v[id] = x, pa[id] = p;
        ch[id][0] = ch[id][1] = -1, sz[id] = 1;
        return id;
    }
    void rotate(int i) {
        int p = pa[i], x = ch[p][1] == i, gp = pa[p], c =
            ch[i][!x];
        sz[p] -= sz[i], sz[i] += sz[p];
        if (~c) sz[p] += sz[c], pa[c] = p;
        ch[p][x] = c, pa[p] = i;
        pa[i] = gp, ch[i][!x] = p;
        if (~gp) ch[gp][ch[gp][1] == p] = i;
    }
    void splay(int i) {
        while (~pa[i]) {
            int p = pa[i];
            if (~pa[p]) rotate(ch[pa[p]][1] == p ^ ch[p][1]
                == i ? i : p);
            rotate(i);
        }
        rt = i;
    }
    int lower_bound(int x) {
        int i = rt, last = -1;
        while (true) {
            if (v[i] == x) return splay(i), i;
            if (v[i] > x) {
                last = i;
                if (ch[i][0] == -1) break;
                i = ch[i][0];
            }
            else {
                if (ch[i][1] == -1) break;
                i = ch[i][1];
            }
        }
        splay(i);
        return last; // -1 if not found
    }
    void insert(int x) {
        int i = lower_bound(x);
        if (i == -1) {
            // assert(ch[rt][1] == -1);
            int id = newnode(rt, x);
            ch[rt][1] = id, ++sz[rt];
            splay(id);
        }
        else if (v[i] != x) {
            splay(i);
            int id = newnode(rt, x), c = ch[rt][0];
            ch[rt][0] = id;
            ch[id][0] = c;
            if (~c) pa[c] = id, sz[id] += sz[c];
            ++sz[rt];
            splay(id);
        }
    }
};

```

2.3 Link Cut Tree

```

// vertex-weighted, path add, path multiply, path query
sum
struct LCT {
    int ch[N][2], pa[N], sz[N], _id;
    ll v[N], lz_mul[N], lz_add[N], sum[N];
    bool rev[N];
    LCT() : _id(1) {}
    int newnode() {
        int x = _id++;

```

```

        ch[x][0] = ch[x][1] = pa[x] = 0, sz[x] = 1;
        v[x] = lz_add[x] = sum[x] = 0, lz_mul[x] = 1;
        rev[x] = false;
        return x;
    }
    void pull(int i) {
        sum[i] = v[i], sz[i] = 1;
        if (ch[i][0]) sum[i] += sum[ch[i][0]], sz[i] += sz[
            ch[i][0]];
        if (ch[i][1]) sum[i] += sum[ch[i][1]], sz[i] += sz[
            ch[i][1]];
    }
    void push(int i) {
        if (lz_mul[i] != 1) mul(ch[i][0], lz_mul[i]), mul(
            ch[i][1], lz_mul[i]), lz_mul[i] = 1;
        if (lz_add[i]) add(ch[i][0], lz_add[i]), add(ch[i
            ][1], lz_add[i]), lz_add[i] = 0;
        if (rev[i]) reverse(ch[i][0]), reverse(ch[i][1]),
            rev[i] = false;
    }
    void reverse(int i) {
        if (!i) return;
        swap(ch[i][0], ch[i][1]);
        rev[i] ^= true;
    }
    bool isrt(int i) { // rt of splay
        if (!pa[i]) return true;
        return ch[pa[i]][0] != i && ch[pa[i]][1] != i;
    }
    void rotate(int i) {
        int p = pa[i], x = ch[p][1] == i, c = ch[i][!x], gp
            = pa[p];
        if (ch[gp][0] == p) ch[gp][0] = i;
        else if (ch[gp][1] == p) ch[gp][1] = i;
        pa[i] = gp, ch[i][!x] = p, pa[p] = i;
        ch[p][x] = c, pa[c] = p;
        pull(p), pull(i);
    }
    void splay(int i) {
        vector<int> anc;
        anc.push_back(i);
        while (!isrt(anc.back())) anc.push_back(pa[anc.back
            ]());
        while (!anc.empty()) push(anc.back()), anc.pop_back
            ();
        while (!isrt(i)) {
            int p = pa[i];
            if (!isrt(p)) rotate(ch[p][1] == i ^ ch[pa[p]][1]
                == p ? i : p);
            rotate(i);
        }
    }
    void access(int i) {
        int last = 0;
        while (i) {
            splay(i), ch[i][1] = last;
            pull(i), last = i, i = pa[i];
        }
    }
    void makert(int i) {
        access(i), splay(i), reverse(i);
    }
    void link(int i, int j) {
        // assert(findrt(i) != findrt(j));
        makert(i), pa[i] = j;
    }
    void cut(int i, int j) {
        makert(i), access(j), splay(i);
        // assert(sz[i] == 2 && ch[i][1] == j);
        ch[i][1] = pa[j] = 0, pull(i);
    }
    int findrt(int i) {
        access(i), splay(i);
        while (ch[i][0]) push(i), i = ch[i][0];
        splay(i);
        return i;
    }
    // custom functions
    void mul(int i, ll d) {
        if (!i)
            return;
        v[i] *= d, lz_mul[i] *= d;

```

```

    lz_add[i] *= d, sum[i] *= d;
}
void add(int i, ll d) {
    if (!i) return;
    v[i] += d, lz_add[i] += d, sum[i] += d * sz[i];
}
void mul_path(int i, int j, ll d) {
    // assert(findrt(i) == findrt(j));
    makert(i), access(j);
    splay(i), mul(i, d);
}
void add_path(int i, int j, ll d) {
    // assert(findrt(i) == findrt(j));
    makert(i), access(j), splay(i), add(i, d);
}
ll query_path(int i, int j) {
    // assert(findrt(i) == findrt(j));
    makert(i), access(j), splay(i);
    return sum[i];
}
}
};

```

2.4 Treap

```

struct node {
    int data, sz;
    node *l, *r;
    node(int k) : data(k), sz(1), l(0), r(0) {}
    void up() {
        sz = 1;
        if (l) sz += l->sz;
        if (r) sz += r->sz;
    }
    void down() {}
};
int sz(node *a) { return a ? a->sz : 0; }
node *merge(node *a, node *b) {
    if (!a || !b) return a ? a : b;
    if (rand() % (sz(a) + sz(b)) < sz(a))
        return a->down(), a->r = merge(a->r, b), a->up(), a;
    return b->down(), b->l = merge(a, b->l), b->up(), b;
}
void split(node *o, node *&a, node *&b, int k) {
    if (!o) return a = b = 0, void();
    o->down();
    if (o->data <= k)
        a = o, split(o->r, a->r, b, k), a->up();
    else b = o, split(o->l, a, b->l, k), b->up();
}
void split2(node *o, node *&a, node *&b, int k) {
    if (sz(o) <= k) return a = o, b = 0, void();
    o->down();
    if (sz(o->l) + 1 <= k)
        a = o, split2(o->r, a->r, b, k - sz(o->l) - 1);
    else b = o, split2(o->l, a, b->l, k);
    o->up();
}
node *kth(node *o, int k) {
    if (k <= sz(o->l)) return kth(o->l, k);
    if (k == sz(o->l) + 1) return o;
    return kth(o->r, k - sz(o->l) - 1);
}
int Rank(node *o, int key) {
    if (!o) return 0;
    if (o->data < key)
        return sz(o->l) + 1 + Rank(o->r, key);
    else return Rank(o->l, key);
}
bool erase(node *o, int k) {
    if (!o) return 0;
    if (o->data == k) {
        node *t = o;
        o->down(), o = merge(o->l, o->r);
        delete t;
        return 1;
    }
    node *&t = k < o->data ? o->l : o->r;
    return erase(t, k) ? o->up(), 1 : 0;
}
void insert(node *&o, int k) {
    node *a, *b;

```

```

    split(o, a, b, k),
    o = merge(a, merge(new node(k), b));
}
void interval(node *&o, int l, int r) {
    node *a, *b, *c;
    split2(o, a, b, l - 1), split2(b, b, c, r);
    // operate
    o = merge(a, merge(b, c));
}

```

2.5 2D Segment Tree

```

// 2D range add, range sum in  $\log^2$ 
struct seg {
    int l, r;
    ll sum, lz;
    seg *ch[2]{};
    seg(int _l, int _r) : l(_l), r(_r), sum(0), lz(0) {}
    void push() {
        if (lz) ch[0]->add(l, r, lz), ch[1]->modify(l, r, lz), lz = 0;
    }
    void pull() {sum = ch[0]->sum + ch[1]->sum;}
    void add(int _l, int _r, ll d) {
        if (_l <= l && r <= _r) {
            sum += d * (r - l + 1);
            lz += d;
            return;
        }
        if (!ch[0]) ch[0] = new seg(l, l + r >> 1), ch[1] = new seg(l + r >> 1, r);
        push();
        if (_l < l + r >> 1) ch[0]->add(_l, _r, d);
        if (l + r >> 1 < _r) ch[1]->add(_l, _r, d);
        pull();
    }
    ll qsum(int _l, int _r) {
        if (_l <= l && r <= _r) return sum;
        if (!ch[0]) return lz * (min(r, _r) - max(l, _l) + 1);
        push();
        ll res = 0;
        if (_l < l + r >> 1) res += ch[0]->qsum(_l, _r);
        if (l + r >> 1 < _r) res += ch[1]->qsum(_l, _r);
        return res;
    }
};
struct seg2 {
    int l, r;
    seg v, lz;
    seg2 *ch[2]{};
    seg2(int _l, int _r) : l(_l), r(_r), v(0, N), lz(0, N) {}
    if (l < r - 1) ch[0] = new seg2(l, l + r >> 1), ch[1] = new seg2(l + r >> 1, r);
    void add(int _l, int _r, int _l2, int _r2, ll d) {
        v.add(_l2, _r2, d * (min(r, _r) - max(l, _l) + 1));
        if (_l <= l && r <= _r) {
            lz.add(_l2, _r2, d);
            return;
        }
        if (_l < l + r >> 1) ch[0]->add(_l, _r, _l2, _r2, d);
        if (l + r >> 1 < _r) ch[1]->add(_l, _r, _l2, _r2, d);
    }
    ll qsum(int _l, int _r, int _l2, int _r2) {
        ll res = v.qsum(_l2, _r2);
        if (_l <= l && r <= _r) return res;
        res += lz.qsum(_l2, _r2) * (min(r, _r) - max(l, _l) + 1);
        if (_l < l + r >> 1) res += ch[0]->query(_l, _r, _l2, _r2);
        if (l + r >> 1 < _r) res += ch[1]->query(_l, _r, _l2, _r2);
        return res;
    }
};

```

2.6 Zkw

```

ll mx[N << 1], sum[N << 1], lz[N << 1];

```

```

void add(int l, int r, ll d) { // [l, r), 0-based
    int len = 1, cntl = 0, cntr = 0;
    for (l += N, r += N + 1; l ^ r ^ 1; l >>= 1, r >>= 1,
        len <= 1) {
        sum[l] += cntl * d, sum[r] += cnt[r] * d;
        if (len > 1) {
            mx[l] = max(mx[l << 1], mx[l << 1 | 1]) + lz[l];
            mx[r] = max(mx[r << 1], mx[r << 1 | 1]) + lz[r];
        }
        if (~l & 1)
            sum[l ^ 1] += d * len, mx[l ^ 1] += d, lz[l ^ 1]
                += d, cntl += len;
        if (r & 1)
            sum[r ^ 1] += d * len, mx[r ^ 1] += d, lz[r ^ 1]
                += d, cntr += len;
    }
    sum[l] += cntl * d, sum[r] += cntr * d;
    if (len > 1) {
        mx[l] = max(mx[l << 1], mx[l << 1 | 1]) + lz[l];
        mx[r] = max(mx[r << 1], mx[r << 1 | 1]) + lz[r];
    }
    cntl += cntr;
    for (l >>= 1; l; l >>= 1) {
        sum[l] += cntl * d;
        mx[l] = max(mx[l << 1], mx[l << 1 | 1]) + lz[l];
    }
}

ll qsum(int l, int r) {
    ll res = 0, len = 1, cntl = 0, cntr = 0;
    for (l += N, r += N + 1; l ^ r ^ 1; l >>= 1, r >>= 1,
        len <= 1) {
        res += cntl * lz[l] + cntr * lz[r];
        if (~l & 1) res += sum[l ^ 1], cntl += len;
        if (r & 1) res += sum[r ^ 1], cntr += len;
    }
    res += cntl * lz[l] + cntr * lz[r];
    cntl += cntr;
    for (l >>= 1; l; l >>= 1) res += cntl * lz[l];
    return res;
}

ll qmax(int l, int r) {
    ll maxl = -INF, maxr = -INF;
    for (l += N, r += N + 1; l ^ r ^ 1; l >>= 1, r >>= 1)
        {
            maxl += lz[l], max[r] += lz[r];
            if (~l & 1) maxl = max(maxl, mx[l ^ 1]);
            if (r & 1) maxr = max(maxr, mx[r ^ 1]);
        }
    maxl = max(maxl + lz[l], maxr + lz[r]);
    for (l >>= 1; l; l >>= 1) maxl += lz[l];
    return maxl;
}

```

3 Flow / Matching

3.1 Dinic

```

struct Dinic {
    const int INF = 1 << 30;
    struct edge {
        int v, f;
        edge(int _v, int _f) : v(_v), f(_f) {}
    };
    vector<vector<int>> adj;
    vector<edge> E;
    vector<int> level;
    int n, s, t;
    Dinic(int _n, int _s, int _t) : n(_n), s(_s), t(_t)
        { adj.resize(n); }
    void add_edge(int u, int v, int f) {
        adj[u].pb(E.size(), E.pb(edge(v, f)));
        adj[v].pb(E.size(), E.pb(edge(u, 0)));
    }
    bool bfs() {
        level.assign(n, -1);
        queue<int> q;
        level[s] = 0, q.push(s);
        while (!q.empty()) {
            int v = q.front(); q.pop();
            for (int id : adj[v]) if (E[id].f > 0 && level[E[
                id].v] == -1) {

```

```

                level[E[id].v] = level[v] + 1;
                q.push(E[id].v);
            }
        }
        return level[t] != -1;
    }
    int dfs(int v, int minf) {
        if (v == t) return minf;
        int ans = 0;
        for (int id : adj[v]) if (E[id].f > 0 && level[E[id]
            ].v == level[v] + 1) {
            int nxtf = dfs(E[id].v, min(minf, E[id].f));
            minf -= nxtf, E[id].f -= nxtf;
            ans += nxtf, E[id ^ 1].f += nxtf;
            if (!minf) return ans;
        }
        if (!ans) level[v] = -1;
        return ans;
    }
    int solve() {
        int ans = 0;
        while (bfs()) ans += dfs(s, INF);
        return ans;
    }
};

```

3.2 Min Cost Max Flow

```

template <typename T>
struct MCMF {
    const T INF = 111 << 60;
    struct edge {
        int v;
        T f, c;
        edge(int _v, T _f, T _c) : v(_v), f(_f), c(_c) {}
    };
    vector<edge> E;
    vector<vector<int>> adj;
    vector<T> dis, pot;
    vector<int> rt;
    int n, s, t;
    MCMF(int _n, int _s, int _t) : n(_n), s(_s), t(_t) {
        adj.resize(n);
    }
    void add_edge(int u, int v, T f, T c) {
        adj[u].pb(E.size(), E.pb(edge(v, f, c)));
        adj[v].pb(E.size(), E.pb(edge(u, 0, -c)));
    }
    bool SPFA() {
        rt.assign(n, -1), dis.assign(n, INF);
        vector<bool> vis(n, false);
        queue<int> q;
        q.push(s), dis[s] = 0, vis[s] = true;
        while (!q.empty()) {
            int v = q.front(); q.pop();
            vis[v] = false;
            for (int id : adj[v]) if (E[id].f > 0 && dis[E[id]
                ].v > dis[v] + E[id].c + pot[v] - pot[E[id].
                v]) {
                dis[E[id].v] = dis[v] + E[id].c + pot[v] -
                    pot[E[id].v], rt[E[id].v] = id;
                if (!vis[E[id].v]) vis[E[id].v] = true, q.
                    push(E[id].v);
            }
        }
        return dis[t] != INF;
    }
    bool dijkstra() {
        rt.assign(n, -1), dis.assign(n, INF);
        priority_queue<pair<T, int>, vector<pair<T, int>
            >>, greater<pair<T, int>>> pq;
        dis[s] = 0, pq.emplace(dis[s], s);
        while (!pq.empty()) {
            int d, v; tie(d, v) = pq.top(); pq.pop();
            if (dis[v] < d) continue;
            for (int id : adj[v]) if (E[id].f > 0 && dis[E[id]
                ].v > dis[v] + E[id].c + pot[v] - pot[E[id].
                v]) {
                dis[E[id].v] = dis[v] + E[id].c + pot[v] -
                    pot[E[id].v], rt[E[id].v] = id;
                pq.emplace(dis[E[id].v], E[id].v);
            }
        }
    }
};

```

```

    }
    return dis[t] != INF;
}
pair <T, T> solve() {
    pot.assign(n, 0);
    T cost = 0, flow = 0;
    bool fr = true;
    while ((fr ? SPFA() : dijkstra())) {
        for (int i = 0; i < n; ++i) {
            dis[i] += pot[i] - pot[s];
        }
        T add = INF;
        for (int i = t; i != s; i = E[rt[i] ^ 1].v) {
            add = min(add, E[rt[i]].f);
        }
        for (int i = t; i != s; i = E[rt[i] ^ 1].v) {
            E[rt[i]].f -= add, E[rt[i] ^ 1].f += add;
        }
        flow += add, cost += add * dis[t];
        fr = false;
        swap(dis, pot);
    }
    return make_pair(flow, cost);
}
};

```

3.3 Kuhn Munkres

```

template <typename T>
struct KM { // 0-based
    T w[N][N], hl[N], hr[N], slk[N];
    T fl[N], fr[N], pre[N]; int n;
    bool vl[N], vr[N];
    const T INF = 1e9;
    queue <int> q;
    KM (int _n) : n(_n) {
        for (int i = 0; i < n; ++i) for (int j = 0; j < n; ++j)
            w[i][j] = -INF;
    }
    void add_edge(int a, int b, int wei) {
        w[a][b] = wei;
    }
    bool check(int x) {
        if (vl[x] = 1, ~fl[x]) return q.push(fl[x]), vr[fl[x]] = 1;
        while (~x) swap(x, fr[fl[x] = pre[x]]);
        return 0;
    }
    void bfs(int s) {
        fill(slk, slk + n, INF), fill(vl, vl + n, 0), fill(vr, vr + n, 0);
        q.push(s), vr[s] = 1;
        while (1) {
            T d;
            while (!q.empty()) {
                int y = q.front(); q.pop();
                for (int x = 0; x < n; ++x)
                    if (!vl[x] && slk[x] >= (d = hl[x] + hr[y] - w[x][y]))
                        if (pre[x] = y, d) slk[x] = d;
                        else if (!check(x)) return;
            }
            d = INF;
            for (int x = 0; x < n; ++x)
                if (!vl[x] && d > slk[x]) d = slk[x];
            for (int x = 0; x < n; ++x) {
                if (vl[x]) hl[x] += d;
                else slk[x] -= d;
                if (vr[x]) hr[x] -= d;
            }
            for (int x = 0; x < n; ++x) if (!vl[x] && !slk[x] && !check(x)) return;
        }
    }
    T solve() {
        fill(fl, fl + n, -1), fill(fr, fr + n, -1), fill(hr, hr + n, 0);
        for (int i = 0; i < n; ++i) hl[i] = *max_element(w[i], w[i] + n);
        for (int i = 0; i < n; ++i) bfs(i);
        T res = 0;
    }
};

```

```

        for (int i = 0; i < n; ++i) res += w[i][fl[i]];
        return res;
    }
};

```

3.4 SW Min Cut

```

template <typename T>
struct SW { // 0-based
    T g[N][N], sum[N]; int n;
    bool vis[N], dead[N];
    void init(int _n) {
        n = _n;
        for (int i = 0; i < n; ++i) fill(g[i], g[i] + n, 0);
        fill(dead, dead + n, false);
    }
    void add_edge(int u, int v, T w) {
        g[u][v] += w, g[v][u] += w;
    }
    T solve() {
        T ans = 1 << 30;
        for (int round = 0; round + 1 < n; ++round) {
            fill(vis, vis + n, false), fill(sum, sum + n, 0);
            int num = 0, s = -1, t = -1;
            while (num < n - round) {
                int now = -1;
                for (int i = 0; i < n; ++i) if (!vis[i] && !dead[i]) {
                    if (now == -1 || sum[now] < sum[i]) now = i;
                }
                s = t, t = now;
                vis[now] = true, num++;
                for (int i = 0; i < n; ++i) if (!vis[i] && !dead[i]) {
                    sum[i] += g[now][i];
                }
            }
            ans = min(ans, sum[t]);
            for (int i = 0; i < n; ++i) {
                g[i][s] += g[i][t];
                g[s][i] += g[t][i];
            }
            dead[t] = true;
        }
        return ans;
    }
};

```

3.5 Gomory Hu Tree

```

vector <array <int, 3>> GomoryHu(vector <vector <pii>>
    adj, int n) {
    // Tree edge min -> mincut (0-based)
    Dinic flow(n);
    for (int i = 0; i < n; ++i) for (auto [j, w] : adj[i])
        flow.add_edge(i, j, w);
    flow.record();
    vector <array <int, 3>> ans;
    vector <int> rt(n);
    for (int i = 0; i < n; ++i) rt[i] = 0;
    for (int i = 1; i < n; ++i) {
        int t = rt[i];
        flow.reset(); // clear flows on all edge
        ans.push_back({i, t, flow.solve(i, t)});
        flow.runbfs(i);
        for (int j = i + 1; j < n; ++j) if (rt[j] == t && flow.vis[j]) {
            rt[j] = i;
        }
    }
    return ans;
}

```

3.6 Blossom

```

struct Matching { // 0-based
    int fa[N], pre[N], match[N], s[N], v[N], n, tk;
    vector <int> g[N];
    queue <int> q;
};

```

```

Matching (int _n) : n(_n), tk(0) {
    for (int i = 0; i <= n; ++i) match[i] = pre[i] = n;
    for (int i = 0; i < n; ++i) g[i].clear();
}
void add_edge(int u, int v) {
    g[u].push_back(v), g[v].push_back(u);
}
int Find(int u) {
    return u == fa[u] ? u : fa[u] = Find(fa[u]);
}
int lca(int x, int y) {
    tk++;
    x = Find(x), y = Find(y);
    for (; ; swap(x, y)) {
        if (x != n) {
            if (v[x] == tk) return x;
            v[x] = tk;
            x = Find(pre[match[x]]);
        }
    }
}
void blossom(int x, int y, int l) {
    while (Find(x) != l) {
        pre[x] = y, y = match[x];
        if (s[y] == 1) q.push(y), s[y] = 0;
        if (fa[x] == x) fa[x] = 1;
        if (fa[y] == y) fa[y] = 1;
        x = pre[y];
    }
}
bool bfs(int r) {
    for (int i = 0; i <= n; ++i) fa[i] = i, s[i] = -1;
    while (!q.empty()) q.pop();
    q.push(r);
    s[r] = 0;
    while (!q.empty()) {
        int x = q.front(); q.pop();
        for (int u : g[x]) {
            if (s[u] == -1) {
                pre[u] = x, s[u] = 1;
                if (match[u] == n) {
                    for (int a = u, b = x, last; b != n; a = last, b = pre[a])
                        last = match[b], match[b] = a, match[a] = b;
                    return true;
                }
                q.push(match[u]);
                s[match[u]] = 0;
            } else if (!s[u] && Find(u) != Find(x)) {
                int l = lca(u, x);
                blossom(x, u, l);
                blossom(u, x, l);
            }
        }
    }
    return false;
}
int solve() {
    int res = 0;
    for (int x = 0; x < n; ++x) {
        if (match[x] == n) res += bfs(x);
    }
    return res;
}
};

```

3.7 Weighted Blossom

```

struct WeightGraph { // 1-based
    static const int inf = INT_MAX;
    static const int maxn = 514;
    struct edge {
        int u, v, w;
        edge() {}
        edge(int u, int v, int w) : u(u), v(v), w(w) {}
    };
    int n, n_x;
    edge g[maxn * 2][maxn * 2];
    int lab[maxn * 2];
    int match[maxn * 2], slack[maxn * 2], st[maxn * 2],
        pa[maxn * 2];

```

```

    int flo_from[maxn * 2][maxn + 1], S[maxn * 2], vis[
        maxn * 2];
    vector<int> flo[maxn * 2];
    queue<int> q;
    int e_delta(const edge &e) { return lab[e.u] + lab[e.
        v] - g[e.u][e.v].w * 2; }
    void update_slack(int u, int x) { if (!slack[x] ||
        e_delta(g[u][x]) < e_delta(g[slack[x]][x])) slack
        [x] = u; }
    void set_slack(int x) {
        slack[x] = 0;
        for (int u = 1; u <= n; ++u)
            if (g[u][x].w > 0 && st[u] != x && S[st[u]] == 0)
                update_slack(u, x);
    }
    void q_push(int x) {
        if (x <= n) q.push(x);
        else for (size_t i = 0; i < flo[x].size(); i++)
            q_push(flo[x][i]);
    }
    void set_st(int x, int b) {
        st[x] = b;
        if (x > n) for (size_t i = 0; i < flo[x].size(); ++
            i) set_st(flo[x][i], b);
    }
    int get_pr(int b, int xr) {
        int pr = find(flo[b].begin(), flo[b].end(), xr) -
            flo[b].begin();
        if (pr % 2 == 1) {
            reverse(flo[b].begin() + 1, flo[b].end());
            return (int)flo[b].size() - pr;
        }
        return pr;
    }
    void set_match(int u, int v) {
        match[u] = g[u][v].v;
        if (u <= n) return;
        edge e = g[u][v];
        int xr = flo_from[u][e.u], pr = get_pr(u, xr);
        for (int i = 0; i < pr; ++i) set_match(flo[u][i],
            flo[u][i ^ 1]);
        set_match(xr, v);
        rotate(flo[u].begin(), flo[u].begin() + pr, flo[u].
            end());
    }
    void augment(int u, int v) {
        for (; ) {
            int xnv = st[match[u]];
            set_match(u, v);
            if (!xnv) return;
            set_match(xnv, st[pa[xnv]]);
            u = st[pa[xnv]], v = xnv;
        }
    }
    int get_lca(int u, int v) {
        static int t = 0;
        for (++t; u || v; swap(u, v)) {
            if (u == 0) continue;
            if (vis[u] == t) return u;
            vis[u] = t;
            u = st[match[u]];
            if (u) u = st[pa[u]];
        }
        return 0;
    }
    void add_blossom(int u, int lca, int v) {
        int b = n + 1;
        while (b <= n_x && st[b]) ++b;
        if (b > n_x) ++n_x;
        lab[b] = 0, S[b] = 0;
        match[b] = match[lca];
        flo[b].clear();
        flo[b].push_back(lca);
        for (int x = u, y; x != lca; x = st[pa[y]])
            flo[b].push_back(x), flo[b].push_back(y = st[
                match[x]]), q_push(y);
        reverse(flo[b].begin() + 1, flo[b].end());
        for (int x = v, y; x != lca; x = st[pa[y]])
            flo[b].push_back(x), flo[b].push_back(y = st[
                match[x]]), q_push(y);
        set_st(b, b);
        for (int x = 1; x <= n_x; ++x) g[b][x].w = g[x][b].

```



```

    w = 0;
    for (int x = 1; x <= n; ++x) flo_from[b][x] = 0;
    for (size_t i = 0; i < flo[b].size(); ++i) {
        int xs = flo[b][i];
        for (int x = 1; x <= n_x; ++x)
            if (g[b][x].w == 0 || e_delta(g[xs][x]) <
                e_delta(g[b][x]))
                g[b][x] = g[xs][x], g[x][b] = g[x][xs];
        for (int x = 1; x <= n; ++x)
            if (flo_from[xs][x]) flo_from[b][x] = xs;
    }
    set_slack(b);
}

void expand_blossom(int b) {
    for (size_t i = 0; i < flo[b].size(); ++i)
        set_st(flo[b][i], flo[b][i]);
    int xr = flo_from[b][g[b][pa[b]].u], pr = get_pr(b, xr);
    for (int i = 0; i < pr; i += 2) {
        int xs = flo[b][i], xns = flo[b][i + 1];
        pa[xs] = g[xns][xs].u;
        S[xs] = 1, S[xns] = 0;
        slack[xs] = 0, set_slack(xns);
        q_push(xns);
    }
    S[xr] = 1, pa[xr] = pa[b];
    for (size_t i = pr + 1; i < flo[b].size(); ++i) {
        int xs = flo[b][i];
        S[xs] = -1, set_slack(xs);
    }
    st[b] = 0;
}

bool on_found_edge(const edge &e) {
    int u = st[e.u], v = st[e.v];
    if (S[v] == -1) {
        pa[v] = e.u, S[v] = 1;
        int nu = st[match[v]];
        slack[v] = slack[nu] = 0;
        S[nu] = 0, q_push(nu);
    } else if (S[v] == 0) {
        int lca = get_lca(u, v);
        if (!lca) return augment(u, v), augment(v, u), true;
        else add_blossom(u, lca, v);
    }
    return false;
}

bool matching() {
    memset(S + 1, -1, sizeof(int) * n_x);
    memset(slack + 1, 0, sizeof(int) * n_x);
    q = queue<int>();
    for (int x = 1; x <= n_x; ++x)
        if (st[x] == x && !match[x]) pa[x] = 0, S[x] = 0,
            q_push(x);
    if (q.empty()) return false;
    for (; ; ) {
        while (q.size()) {
            int u = q.front(); q.pop();
            if (S[st[u]] == 1) continue;
            for (int v = 1; v <= n; ++v)
                if (g[u][v].w > 0 && st[u] != st[v]) {
                    if (e_delta(g[u][v]) == 0) {
                        if (on_found_edge(g[u][v])) return true;
                    } else update_slack(u, st[v]);
                }
        }
        int d = inf;
        for (int b = n + 1; b <= n_x; ++b)
            if (st[b] == b && S[b] == 1) d = min(d, lab[b] / 2);
        for (int x = 1; x <= n_x; ++x)
            if (st[x] == x && slack[x]) {
                if (S[x] == -1) d = min(d, e_delta(g[slack[x]][x]));
                else if (S[x] == 0) d = min(d, e_delta(g[slack[x]][x]) / 2);
            }
        for (int u = 1; u <= n; ++u) {
            if (S[st[u]] == 0) {
                if (lab[u] <= d) return 0;
                lab[u] -= d;
            } else if (S[st[u]] == 1) lab[u] += d;
        }
    }
}

```

```

    }
    for (int b = n + 1; b <= n_x; ++b)
        if (st[b] == b) {
            if (S[st[b]] == 0) lab[b] += d * 2;
            else if (S[st[b]] == 1) lab[b] -= d * 2;
        }
    q = queue<int>();
    for (int x = 1; x <= n_x; ++x)
        if (st[x] == x && slack[x] && st[slack[x]] != x
            && e_delta(g[slack[x]][x]) == 0)
            if (on_found_edge(g[slack[x]][x])) return true;
        for (int b = n + 1; b <= n_x; ++b)
            if (st[b] == b && S[b] == 1 && lab[b] == 0)
                expand_blossom(b);
    }
    return false;
}

pair<long long, int> solve() {
    memset(match + 1, 0, sizeof(int) * n);
    n_x = n;
    int n_matches = 0;
    long long tot_weight = 0;
    for (int u = 0; u <= n; ++u) st[u] = u, flo[u].clear();
    int w_max = 0;
    for (int u = 1; u <= n; ++u)
        for (int v = 1; v <= n; ++v) {
            flo_from[u][v] = (u == v ? u : 0);
            w_max = max(w_max, g[u][v].w);
        }
    for (int u = 1; u <= n; ++u) lab[u] = w_max;
    while (matching()) ++n_matches;
    for (int u = 1; u <= n; ++u)
        if (match[u] && match[u] < u)
            tot_weight += g[u][match[u]].w;
    return make_pair(tot_weight, n_matches);
}

void add_edge(int ui, int vi, int wi) { g[ui][vi].w = g[vi][ui].w = wi; }
void init(int _n) {
    n = _n;
    for (int u = 1; u <= n; ++u)
        for (int v = 1; v <= n; ++v)
            g[u][v] = edge(u, v, 0);
}
};

```

3.8 Flow Model

- Maximum/Minimum flow with lower bound / Circulation problem
 - Construct super source S and sink T .
 - For each edge (x, y, l, u) , connect $x \rightarrow y$ with capacity $u - l$.
 - For each vertex v , denote by $in(v)$ the difference between the sum of incoming lower bounds and the sum of outgoing lower bounds.
 - If $in(v) > 0$, connect $S \rightarrow v$ with capacity $in(v)$, otherwise, connect $v \rightarrow T$ with capacity $-in(v)$.
 - To maximize, connect $t \rightarrow s$ with capacity ∞ (skip this in circulation problem), and let f be the maximum flow from S to T . If $f \neq \sum_{v \in V, in(v) > 0} in(v)$, there's no solution. Otherwise, the maximum flow from s to t is the answer.
 - To minimize, let f be the maximum flow from S to T . Connect $t \rightarrow s$ with capacity ∞ and let the flow from S to T be f' . If $f + f' \neq \sum_{v \in V, in(v) > 0} in(v)$, there's no solution. Otherwise, f' is the answer.
 - The solution of each edge e is $l_e + f_e$, where f_e corresponds to the flow of edge e on the graph.
- Construct minimum vertex cover from maximum matching M on bipartite graph (X, Y)
 - Redirect every edge: $y \rightarrow x$ if $(x, y) \in M$, $x \rightarrow y$ otherwise.
 - DFS from unmatched vertices in X .
 - $x \in X$ is chosen iff x is unvisited.
 - $y \in Y$ is chosen iff y is visited.
- Maximum density induced subgraph
 - Binary search on answer, suppose we're checking answer T
 - Construct a max flow model, let K be the sum of all weights
 - Connect source $s \rightarrow v$, $v \in G$ with capacity K
 - For each edge (u, v, w) in G , connect $u \rightarrow v$ and $v \rightarrow u$ with capacity w
 - For $v \in G$, connect it with sink $v \rightarrow t$ with capacity $K + 2T - (\sum_{e \in E(v)} w(e)) - 2w(v)$
 - T is a valid answer if the maximum flow $f < K|V|$
- Minimum weight edge cover

1. For each $v \in V$ create a copy v' , and connect $u' \rightarrow v'$ with weight $w(u, v)$.
 2. Connect $v \rightarrow v'$ with weight $2\mu(v)$, where $\mu(v)$ is the cost of the cheapest edge incident to v .
 3. Find the minimum weight perfect matching on G' .
- Project selection problem
 1. If $p_v > 0$, create edge (s, v) with capacity p_v ; otherwise, create edge (v, t) with capacity $-p_v$.
 2. Create edge (u, v) with capacity w with w being the cost of choosing u without choosing v .
 3. The mincut is equivalent to the maximum profit of a subset of projects.
 - 0/1 quadratic programming

$$\sum_x c_x x + \sum_y c_y \bar{y} + \sum_{xy} c_{xy} x \bar{y} + \sum_{xyx'y'} c_{xyx'y'} (x \bar{y} + x' \bar{y}')$$

can be minimized by the mincut of the following graph:

 1. Create edge (x, t) with capacity c_x and create edge (s, y) with capacity c_y .
 2. Create edge (x, y) with capacity c_{xy} .
 3. Create edge (x, y) and edge (x', y') with capacity $c_{xyx'y'}$.

4 Graph

4.1 Heavy-Light Decomposition

```
vector<int> dep, pa, sz, ch, hd, id;
int _id;
void dfs(int i, int p) {
    dep[i] = ~p ? dep[p] + 1 : 0;
    pa[i] = p, sz[i] = 1, ch[i] = -1;
    for (int j : g[i])
        if (j != p) {
            dfs(j, i);
            if (ch[i] == -1 || sz[ch[i]] < sz[j]) ch[i] = j;
            sz[i] += sz[j];
        }
}
void hld(int i, int p, int h) {
    hd[i] = h;
    id[i] = _id++;
    if (~ch[i]) hld(ch[i], i, h);
    for (int j : g[i]) if (j != p && j != ch[i])
        hld(j, i, j);
}
void query(int i, int j) {
    while (hd[i] != hd[j]) {
        if (dep[hd[i]] < dep[hd[j]]) swap(i, j);
        query2(id[hd[i]], id[i] + 1, i = pa[hd[i]]);
    }
    if (dep[i] < dep[j]) swap(i, j);
    query2(id[j], id[i] + 1);
}
```

4.2 Centroid Decomposition

```
vector<vector<int>> dis;
vector<int> pa, sz;
vector<bool> vis;
void dfs_sz(int i, int p) {
    sz[i] = 1;
    for (int j : g[i]) if (j != p && !vis[j])
        dfs_sz(j, i), sz[i] += sz[j];
}
void cen(int i, int p, int _n) {
    for (int j : g[i]) if (j != p && !vis[j] && sz[j] > _n / 2)
        return cen(j, i, _n);
    return i;
}
void dfs_dis(int i, int p, int d) { // from i to
    ancestor with depth d
    dis[i][d] = ~p ? dis[p][d] + 1 : 0;
    for (int j : g[i]) if (j != p && !vis[j])
        dfs_dis(j, i, d);
}
void cd(int i, int p, int d) {
    dfs_sz(i), i = cen(i);
    vis[i] = true, pa[i] = p;
    dfs_dis(i, -1, d);
    for (int j : g[i]) if (!vis[j])
        cd(j, i, d + 1);
}
```

4.3 Edge BCC

```
vector<int> low, dep, bcc_id, stk;
vector<bool> vis;
int _id;
void dfs(int i, int p) {
    low[i] = dep[i] = ~p ? dep[p] + 1 : 0;
    stk.push_back(i);
    vis[i] = true;
    for (int j : g[i])
        if (j != p) {
            if (!vis[j])
                dfs(j, i), low[i] = min(low[i], low[j]);
            else
                low[i] = min(low[i], dep[j]);
        }
    if (low[i] == dep[i]) {
        int id = _id++;
        while (stk.back() != i) {
            int x = stk.back();
            stk.pop_back();
            bcc_id[x] = id;
        }
        stk.pop_back();
        bcc_id[i] = id;
    }
}
```

4.4 Block Cut Tree

```
vector<vector<int>> g, _g;
vector<int> dep, low, stk;
void dfs(int i, int p) {
    dep[i] = low[i] = ~p ? dep[p] + 1 : 0;
    stk.push_back(i);
    for (int j : g[i]) if (j != p) {
        if (dep[j] == -1) {
            dfs(j, i), low[i] = min(low[i], low[j]);
            if (low[j] >= dep[i]) {
                int id = _g.size();
                _g.emplace_back();
                while (stk.back() != j) {
                    int x = stk.back();
                    stk.pop_back();
                    _g[x].push_back(id), _g[id].push_back(x);
                }
                stk.pop_back();
                _g[j].push_back(id), _g[id].push_back(j);
                _g[i].push_back(id), _g[id].push_back(i);
            }
        } else low[i] = min(low[i], dep[j]);
    }
}
```

4.5 SCC / 2SAT

```
struct SAT {
    vector<vector<int>> g;
    vector<int> dep, low, scc_id;
    vector<bool> is;
    vector<int> stk;
    int n, _id;
    SAT() {}
    void init(int _n) {
        n = _n, _id = 0;
        g.assign(2 * n, vector<int>());
        dep.assign(2 * n, -1), low.assign(2 * n, -1);
        scc_id.assign(2 * n, -1), is.assign(2 * n, false);
        stk.clear();
    }
    void add_edge(int x, int y) {g[x].push_back(y);}
    int rev(int i) {return i < n ? i + n : i - n;}
    void add_ifthen(int x, int y) {add_clause(rev(x), y);}
    void add_clause(int x, int y) {
        add_edge(rev(x), y);
        add_edge(rev(y), x);
    }
    void dfs(int i, int p) {
        dep[i] = low[i] = ~p ? dep[p] + 1 : 0;
        stk.push_back(i);
        for (int j : g[i])
```



```

    if (j != p && scc_id[j] == -1) {
        if (dep[j] == -1)
            dfs(j, i);
        low[i] = min(low[i], low[j]);
    }
    if (low[i] == dep[i]) {
        int id = _id++;
        while (stk.back() != i) {
            int x = stk.back();
            stk.pop_back();
            scc_id[x] = id;
        }
        stk.pop_back();
        scc_id[i] = id;
    }
}
bool solve() {
    for (int i = 0; i < 2 * n; ++i)
        if (dep[i] == -1)
            dfs(i, -1);
    for (int i = 0; i < n; ++i) {
        if (scc_id[i] == scc_id[i + n]) return false;
        if (scc_id[i] < scc_id[i + n])
            is[i] = true;
        else
            is[i + n] = true;
    }
    return true;
}
};

```

4.6 Virtual Tree

```

vector<vector<int>> _g;
vector<int> st, ed, stk;
void solve(vector<int> v) {
    sort(all(v), [&](int x, int y) {return st[x] < st[y];});
    int sz = v.size();
    for (int i = 0; i < sz - 1; ++i)
        v.push_back(lca(v[i], v[i + 1]));
    sort(all(v), [&](int x, int y) {return st[x] < st[y];});
    v.resize(unique(all(v)) - v.begin());
    stk.clear(); stk.push_back(v[0]);
    for (int i = 1; i < v.size(); ++i) {
        int x = v[i];
        while (ed[stk.back()] < ed[x]) stk.pop_back();
        _g[stk.back()].push_back(x), stk.push_back(x);
    }
    // do something
    for (int i : v) _g[i].clear();
}

```

4.7 Directed MST

```

template <typename T> struct DMST { // 1-based
    T g[maxn][maxn], fw[maxn];
    int n, fr[maxn];
    bool vis[maxn], inc[maxn];
    void clear() {
        for (int i = 0; i < maxn; ++i) {
            for (int j = 0; j < maxn; ++j) g[i][j] = inf;
            vis[i] = inc[i] = false;
        }
    }
    void addedge(int u, int v, T w) {
        g[u][v] = min(g[u][v], w);
    }
    T query(int root, int _n) {
        n = _n;
        if (dfs(root) != n) return -1;
        T ans = 0;
        while (true) {
            for (int i = 1; i <= n; ++i) fw[i] = inf, fr[i] = i;
            for (int i = 1; i <= n; ++i) if (!inc[i]) {
                for (int j = 1; j <= n; ++j) {
                    if (!inc[j] && i != j && g[j][i] < fw[i]) {
                        fw[i] = g[j][i];
                        fr[i] = j;
                    }
                }
            }
        }
    }
};

```

```

    }
    int x = -1;
    for (int i = 1; i <= n; ++i) if (i != root && !inc[i]) {
        int j = i, c = 0;
        while (j != root && fr[j] != i && c <= n) ++c, j = fr[j];
        if (j == root || c > n) continue;
        else { x = i; break; }
    }
    if (!~x) {
        for (int i = 1; i <= n; ++i) if (i != root && !inc[i]) ans += fw[i];
        return ans;
    }
    int y = x;
    for (int i = 1; i <= n; ++i) vis[i] = false;
    do { ans += fw[y]; y = fr[y]; vis[y] = inc[y] = true; } while (y != x);
    inc[x] = false;
    for (int k = 1; k <= n; ++k) if (vis[k]) {
        for (int j = 1; j <= n; ++j) if (!vis[j]) {
            if (g[x][j] > g[k][j]) g[x][j] = g[k][j];
            if (g[j][k] < inf && g[j][k] - fw[k] < g[j][x]) g[j][x] = g[j][k] - fw[k];
        }
    }
    return ans;
}
int dfs(int now) {
    int r = 1;
    vis[now] = true;
    for (int i = 1; i <= n; ++i) if (g[now][i] < inf && !vis[i]) r += dfs(i);
    return r;
}
};

```

4.8 Dominator Tree

```

struct Dominator_tree {
    int n, id;
    vector <vector <int>> adj, radj, bucket;
    vector <int> sdом, dom, vis, rev, par, rt, mn;
    Dominator_tree (int _n) : n(_n), id(0) {
        adj.resize(n), radj.resize(n), bucket.resize(n);
        sdом.resize(n), dom.resize(n, -1), vis.resize(n, -1);
        rev.resize(n), rt.resize(n), mn.resize(n), par.resize(n);
    }
    void add_edge(int u, int v) {adj[u].pb(v);}
    int query(int v, bool x) {
        if (rt[v] == v) return x ? -1 : v;
        int p = query(rt[v], true);
        if (p == -1) return x ? rt[v] : mn[v];
        if (sdом[mn[v]] > sdом[mn[rt[v]]]) mn[v] = mn[rt[v]];
        rt[v] = p;
        return x ? p : mn[v];
    }
    void dfs(int v) {
        vis[v] = id, rev[id] = v;
        rt[id] = mn[id] = sdом[id] = id, id++;
        for (int u : adj[v]) {
            if (vis[u] == -1) dfs(u), par[vis[u]] = vis[v];
            radj[vis[u]].pb(vis[v]);
        }
    }
    void build(int s) {
        dfs(s);
        for (int i = id - 1; ~i; --i) {
            for (int u : radj[i]) {
                sdом[i] = min(sdом[i], sdом[query(u, false)]);
            }
            if (i) bucket[sdом[i]].pb(i);
            for (int u : bucket[i]) {
                int p = query(u, false);
                dom[u] = sdом[p] == i ? i : p;
            }
        }
    }
};

```

```

    if (i) rt[i] = par[i];
}
vector<int> res(n, -1);
for (int i = 1; i < id; ++i) {
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
}
for (int i = 1; i < id; ++i) res[rev[i]] = rev[dom[i]];
res[s] = s;
dom = res;
}
};

```

5 String

5.1 Aho-Corasick Automaton

```

struct AC {
    int ch[N][26], to[N][26], fail[N], sz;
    vector<int> g[N];
    int cnt[N];
    AC () {sz = 0; extend();}
    void extend() {fill(ch[sz], ch[sz] + 26, 0), sz++;}
    int nxt(int u, int v) {
        if (!ch[u][v]) ch[u][v] = sz, extend();
        return ch[u][v];
    }
    int insert(string s) {
        int now = 0;
        for (char c : s) now = nxt(now, c - 'a');
        cnt[now]++;
        return now;
    }
    void build_fail() {
        queue<int> q;
        for (int i = 0; i < 26; ++i) if (ch[0][i]) {
            to[0][i] = ch[0][i];
            q.push(ch[0][i]);
            g[0].push_back(ch[0][i]);
        }
        while (!q.empty()) {
            int v = q.front(); q.pop();
            for (int j = 0; j < 26; ++j) {
                to[v][j] = ch[v][j] ? ch[v][j] : to[fail[v]][j];
            }
            for (int i = 0; i < 26; ++i) if (ch[v][i]) {
                int u = ch[v][i], k = fail[v];
                while (k && !ch[k][i]) k = fail[k];
                if (ch[k][i]) k = ch[k][i];
                fail[u] = k;
                cnt[u] += cnt[k], g[k].push_back(u);
                q.push(u);
            }
        }
    }
    int match(string &s) {
        int now = 0, ans = 0;
        for (char c : s) {
            now = to[now][c - 'a'];
            if (ch[now][c - 'a']) now = ch[now][c - 'a'];
            ans += cnt[now];
        }
        return ans;
    }
};

```

5.2 KMP Algorithm

```

vector<int> build_fail(string s) {
    vector<int> f(s.length() + 1, 0);
    int k = 0;
    for (int i = 1; i < s.length(); ++i) {
        while (k && s[k] != s[i]) k = f[k];
        if (s[k] == s[i]) k++;
        f[i + 1] = k;
    }
    return f;
}
int match(string s, string t) {
    vector<int> f = build_fail(t);

```

```

    int k = 0, ans = 0;
    for (int i = 0; i < s.length(); ++i) {
        while (k && s[i] != t[k]) k = f[k];
        if (s[i] == t[k]) k++;
        if (k == t.length()) ans++, k = f[k];
    }
    return ans;
}

```

5.3 Z Algorithm

```

vector<int> build(string s) {
    int n = s.length();
    vector<int> Z(n);
    int l = 0, r = 0;
    for (int i = 0; i < n; ++i) {
        Z[i] = max(min(Z[i - 1], r - i), 0);
        while (i + Z[i] < s.size() && s[Z[i]] == s[i + Z[i]]) {
            l = i, r = i + Z[i], Z[i]++;
        }
    }
    return Z;
}

```

5.4 Manacher

```

vector<int> manacher(string &s) {
    string t = "^#";
    for (char c : s) t += c, t += '#';
    t += '&';
    int n = t.length();
    vector<int> r(n, 0);
    int C = 0, R = 0;
    for (int i = 1; i < n - 1; ++i) {
        int mirror = 2 * C - i;
        r[i] = (i < R ? min(r[mirror], R - i) : 0);
        while (t[i - 1 - r[i]] == t[i + 1 + r[i]]) r[i]++;
        if (i + r[i] > R) R = i + r[i], C = i;
    }
    return r;
}

```

5.5 Suffix Array

```

int sa[N], tmp[2][N], c[N], rk[N], lcp[N];
void buildSA(string s) {
    int *x = tmp[0], *y = tmp[1], m = 256, n = s.length();
    for (int i = 0; i < m; ++i) c[i] = 0;
    for (int i = 0; i < n; ++i) c[x[i] = s[i]]++;
    for (int i = 1; i < m; ++i) c[i] += c[i - 1];
    for (int i = n - 1; ~i; --i) sa[--c[x[i]]] = i;
    for (int k = 1; k < n; k <= 1) {
        for (int i = 0; i < m; ++i) c[i] = 0;
        for (int i = 0; i < n; ++i) c[x[i]]++;
        for (int i = 1; i < m; ++i) c[i] += c[i - 1];
        int p = 0;
        for (int i = n - k; i < n; ++i) y[p++] = i;
        for (int i = 0; i < n; ++i) if (sa[i] >= k) y[p++] = sa[i] - k;
        for (int i = n - 1; ~i; --i) sa[--c[x[y[i]]]] = y[i];
        y[sa[0]] = p = 0;
        for (int i = 1; i < n; ++i) {
            int a = sa[i], b = sa[i - 1];
            if (!(x[a] == x[b] && a + k < n && b + k < n && x[a + k] == x[b + k])) p++;
            y[sa[i]] = p;
        }
        if (n == p + 1) break;
        swap(x, y), m = p + 1;
    }
}
void buildLCP(string s) {
    // lcp[i] = LCP(sa[i - 1], sa[i])
    // lcp(i, j) = min(lcp[rk[i] + 1], lcp[rk[i] + 2], ..., lcp[rk[j]])
    int n = s.length(), val = 0;
    for (int i = 0; i < n; ++i) rk[sa[i]] = i;
    for (int i = 0; i < n; ++i) {
        if (!rk[i]) lcp[rk[i]] = 0;

```

```

else {
    if (val) val--;
    int p = sa[rk[i] - 1];
    while (val + i < n && val + p < n && s[val + i]
        == s[val + p]) val++;
    lcp[rk[i]] = val;
}
}
}

```

5.6 Suffix Automaton

```

struct SAM {
    int ch[N][26], len[N], link[N], cnt[N], sz;
    SAM () {len[0] = 0, link[0] = -1, sz = 1;}
    void build(string s) {
        int last = 0;
        for (char c : s) {
            int cur = sz++;
            len[cur] = len[last] + 1;
            int p = last;
            while (~p && !ch[p][c - 'a']) ch[p][c - 'a'] =
                cur, p = link[p];
            if (p == -1) {
                link[cur] = 0;
            } else {
                int q = ch[p][c - 'a'];
                if (len[p] + 1 == len[q]) {
                    link[cur] = q;
                } else {
                    int nxt = sz++;
                    len[nxt] = len[p] + 1, link[nxt] = link[q];
                    for (int j = 0; j < 26; ++j) ch[nxt][j] = ch[
                        q][j];
                    while (~p && ch[p][c - 'a'] == q) ch[p][c -
                        'a'] = nxt, p = link[p];
                    link[q] = link[cur] = nxt;
                }
            }
            cnt[cur]++;
            last = cur;
        }
        vector<int> p(sz);
        iota(all(p), 0);
        sort(all(p), [&](int i, int j) {return len[i] > len[
            j]});
        for (int i = 0; i < sz; ++i) cnt[link[p[i]]] += cnt[
            p[i]];
    }
};

```

5.7 Minimum Rotation

```

string rotate(const string &s) {
    int n = s.length();
    string t = s + s;
    int i = 0, j = 1;
    while (i < n && j < n) {
        int k = 0;
        while (k < n && t[i + k] == t[j + k]) ++k;
        if (t[i + k] <= t[j + k]) j += k + 1;
        else i += k + 1;
        if (i == j) ++j;
    }
    int pos = (i < n ? i : j);
    return t.substr(pos, n);
}

```

5.8 Palindrome Tree

```

struct PAM {
    int ch[N][26], cnt[N], fail[N], len[N], sz;
    string s;
    // 0 -> even root, 1 -> odd root
    PAM (string _s) : s(_s) {
        sz = 0;
        extend(), extend();
        len[0] = 0, fail[0] = 1, len[1] = -1;
        int lst = 1;
        for (int i = 0; i < s.length(); ++i) {
            while (s[i - len[lst] - 1] != s[i]) lst = fail[
                lst];

```

```

            if (!ch[lst][s[i] - 'a']) {
                int idx = extend();
                len[idx] = len[lst] + 2;
                int now = fail[lst];
                while (s[i - len[now] - 1] != s[i]) now = fail[
                    now];
                fail[idx] = ch[now][s[i] - 'a'];
                ch[lst][s[i] - 'a'] = idx;
            }
            lst = ch[lst][s[i] - 'a'], cnt[lst]++;
        }
    }
    void build_count() {
        for (int i = sz - 1; i > 1; --i)
            cnt[fail[i]] += cnt[i];
    }
    int extend() {
        fill(ch[sz], ch[sz] + 26, 0), sz++;
        return sz - 1;
    }
};

```

6 Math

7 Geometry

7.1 Basic

```

int sign(double x) {return abs(x) <= eps ? 0 : (x > 0 ?
    1 : -1);}
struct Pt {
    double x, y;
    Pt (double _x, double _y) : x(_x), y(_y) {}
    Pt operator + (Pt o) {return Pt(x + o.x, y + o.y);}
    Pt operator - (Pt o) {return Pt(x - o.x, y - o.y);}
    Pt operator * (double k) {return Pt(x * k, y * k);}
    Pt operator / (double k) {return Pt(x / k, y / k);}
    double operator * (Pt o) {return x * o.x + y * o.y;}
    double operator ^ (Pt o) {return x * o.y - y * o.x;}
    double abs() {return hypot(x, y);}
};
int ori(Pt o, Pt a, Pt b) {return sign((o - a) ^ (o - b
));}
bool btw(Pt a, Pt b, Pt c) { // c on segment ab?
    return ori(a, b, c) == 0 && sign((c - a) * (c - b))
        <= 0;
}
double area(Pt a, Pt b, Pt c) {return abs((a - b) ^ (a
- c)) / 2;}
Pt proj_vector(Pt a, Pt b, Pt c) { // vector ac proj to
    ab
    return (b - a) * ((c - a) * (b - a)) / ((b - a) * (b
        - a));
}
Pt proj_pt(Pt a, Pt b, Pt c) { // point c proj to ab
    return proj_vector(a, b, c) + a;
}

```

7.2 Segment Intersection

```

bool banana(Pt a, Pt b, Pt c, Pt d) { // segment ab and
    cd
    if (btw(a, b, c) || btw(a, b, d) || btw(c, d, a) ||
        btw(c, d, b)) return true;
    return ori(a, b, c) * ori(a, b, d) == -1 && ori(c, d,
        a) * ori(c, d, b) == -1;
}
Pt intersect(Pt a, Pt b, Pt c, Pt d) { // segment ab
    and cd
    double abc = (b - a) ^ (c - a);
    double abd = (b - a) ^ (d - a);
    if (sign(abc - abd) == 0) return d;
    return (d * abc - c * abd) / (abc - abd);
}

```

7.3 Convex Hull

```

vector<Pt> ConvexHull(vector<Pt> pt) {
    int n = pt.size();

```

```

sort(all(pt), [&](Pt a, Pt b) {return a.x == b.x ? a.
    y < b.y : a.x < b.x;});
vector<Pt> ans = {pt[0]};
for (int t : {0, 1}) {
    int m = ans.size();
    for (int i = 1; i < n; ++i) {
        while (ans.size() > m && ori(ans[ans.size() - 2],
            ans.back(), pt[i]) <= 0)
            ans.pop_back();
        ans.push_back(pt[i]);
    }
    reverse(all(pt));
}
ans.pop_back();
return ans;
}

```

7.4 PolarAngle Sort

```

void PolarAngleSort(vector<Pt> &pts) {
    auto pos = [&](Pt a) {return sign(a.y) == 0 ? sign(a
        .x) < 0 : sign(a.y) > 0;};
    sort(all(pts), [&](Pt a, Pt b) {return pos(a) == pos(
        b) ? sign(a ^ b) > 0 : pos(a) < pos(b);});
}

```

7.5 Rotating Caliper

```

void RotatingCaliper(vector<Pt> &pts) {
    int n = pts.size();
    for (int i = 0, j = 2; i < n; ++i) {
        int ni = (i + 1) % n;
        while (true) {
            int nj = (j + 1) % n;
            if (area(pts[j], pts[i], pts[ni]) < area(pts[nj],
                pts[i], pts[ni])) {
                j = nj;
            } else {
                break;
            }
        }
        // do something
    }
}

```

7.6 Rotating SweepLine

```

void RotatingSweepLine(vector<Pt> &pt) {
    int n = pt.size();
    vector<int> id(n), pos(n);
    vector<pair<int, int>> line;
    for (int i = 0; i < n; ++i) for (int j = 0; j < n; ++
        j) if (i ^ j) line.emplace_back(i, j);
    sort(line.begin(), line.end(), [&](pair<int, int> i,
        pair<int, int> j) {
        Pt a = pt[i.second] - pt[i.first], b = pt[j.second]
            - pt[j.first];
        return (a.pos() == b.pos() ? sign(a ^ b) > 0 : a.
            pos() < b.pos());
    });
    iota(id.begin(), id.end(), 0);
    sort(id.begin(), id.end(), [&](int i, int j) {
        return (sign(pt[i].y - pt[j].y) == 0 ? pt[i].x < pt
            [j].x : pt[i].y < pt[j].y);
    });
    for (int i = 0; i < n; ++i)
        pos[id[i]] = i;
    for (auto [i, j] : line) {
        // point sort by the distance to line(i, j)
        // do something.
        tie(pos[i], pos[j], id[pos[i]], id[pos[j]]) =
            make_tuple(pos[j], pos[i], j, i);
    }
}

```

8 Polynomial

9 Else

9.1 Bit Hack

```

long long next_perm(long long v) {
    long long t = v | (v - 1);
    return (t + 1) | (((~t & -~t) - 1) >> (__builtin_ctz(
        v) + 1));
}
void subset(long long s) {
    long long sub = s;
    while (sub) sub = (sub - 1) & s;
}

```

9.2 Hilbert Curve

```

long long hilbertOrder(int x, int y, int pow, int
    rotate) {
    if (pow == 0) return 0;
    int hpow = 1 << (pow - 1);
    int seg = (x < hpow) ? ((y < hpow) ? 0 : 3) : ((y <
        hpow) ? 1 : 2);
    seg = (seg + rotate) & 3;
    const int rotateDelta[4] = {3, 0, 0, 1};
    int nx = x & (x ^ hpow), ny = y & (y ^ hpow);
    int nrot = (rotate + rotateDelta[seg]) & 3;
    long long subSquareSize = 1ll << (pow * 2 - 2);
    long long ans = seg * subSquareSize;
    long long add = hilbertOrder(nx, ny, pow - 1, nrot);
    ans += (seg == 1 || seg == 2) ? add : (subSquareSize
        - add - 1);
    return ans;
}

```

9.3 Pbds

```

#include <ext/pb_ds/priority_queue.hpp>
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
#include <ext/rope>
using namespace __gnu_cxx;
int main () {
    __gnu_pbds::priority_queue<int> pq1, pq2;
    pq1.join(pq2); // pq1 += pq2, pq2 = {}
    cc_hash_table<int, int> m1;
    tree<int, null_type, less<int>, rb_tree_tag,
        tree_order_statistics_node_update> oset;
    oset.insert(2), oset.insert(4);
    cout << *oset.find_by_order(1) << ' ' << oset.
        order_of_key(1) << '\n'; // 4 0
    bitset<100> BS;
    BS.flip(3), BS.flip(5);
    cout << BS._Find_first() << ' ' << BS._Find_next(3)
        << '\n'; // 3 5
    rope<int> rp1, rp2;
    rp1.push_back(1), rp1.push_back(3);
    rp1.insert(0, 2); // pos, num
    rp1.erase(0, 2); // pos, len
    rp1.substr(0, 2); // pos, len
    rp2.push_back(4);
    rp1 += rp2, rp2 = rp1;
    cout << rp2[0] << ' ' << rp2[1] << '\n'; // 3 4
}

```

9.4 Random

```

struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }
    size_t operator()(uint64_t a) const {
        static const uint64_t FIXED_RANDOM = chrono::
            steady_clock::now().time_since_epoch().count();
        return splitmix64(i + FIXED_RANDOM);
    }
};
unordered_map<int, int, custom_hash> m1;
random_device rd; mt19937 rng(rd());

```

9.5 Matroid Intersection

Start from $S = \emptyset$. In each iteration, let

- $Y_1 = \{x \notin S \mid S \cup \{x\} \in I_1\}$
- $Y_2 = \{x \notin S \mid S \cup \{x\} \in I_2\}$

If there exists $x \in Y_1 \cap Y_2$, insert x into S . Otherwise for each $x \in S, y \notin S$, create edges

- $x \rightarrow y$ if $S - \{x\} \cup \{y\} \in I_1$.
- $y \rightarrow x$ if $S - \{x\} \cup \{y\} \in I_2$.

Find a *shortest* path (with BFS) starting from a vertex in Y_1 and ending at a vertex in Y_2 which doesn't pass through any other vertices in Y_2 , and alternate the path. The size of S will be incremented by 1 in each iteration. For the weighted case, assign weight $w(x)$ to vertex x if $x \in S$ and $-w(x)$ if $x \notin S$. Find the path with the minimum number of edges among all minimum length paths and alternate it.