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Research Interest :

Computer vision, image/video processing,
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(You can download lecture notes in my homepage)

Introduction to Algorithm (1)

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Before Starting ... (1/2)

- Algorithm is the heart of AI !
 - How can we make this robot work ?

Artificial Intelligence at CES 2019 The New IoT: The Intelligence of Things

이미지 출처 : CTA

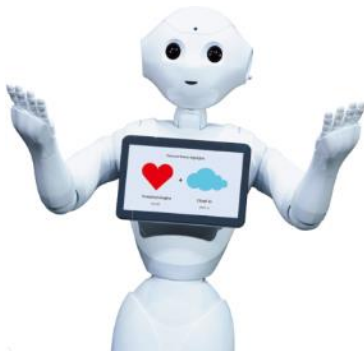


Before Starting ... (2/2)

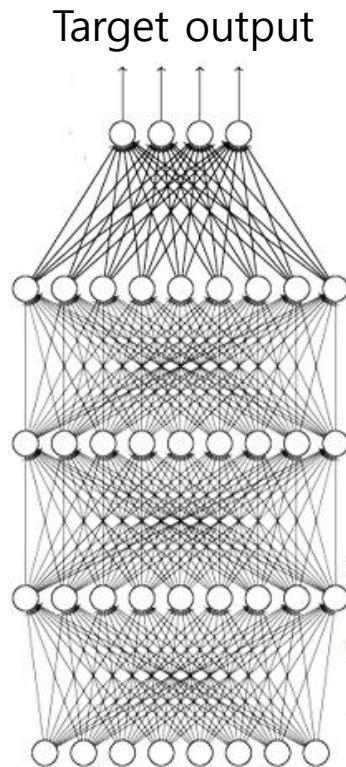
- Algorithm is the heart of AI and computer vision !



Echo (Amazon)



Pepper (Softbank)



Deep learning
structure

What makes it possible ?

"Algorithm"

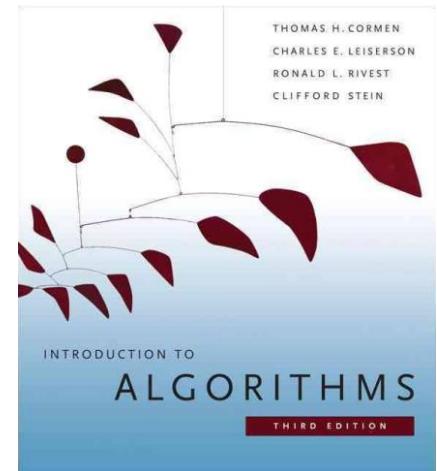


■ What we learn in this class ...

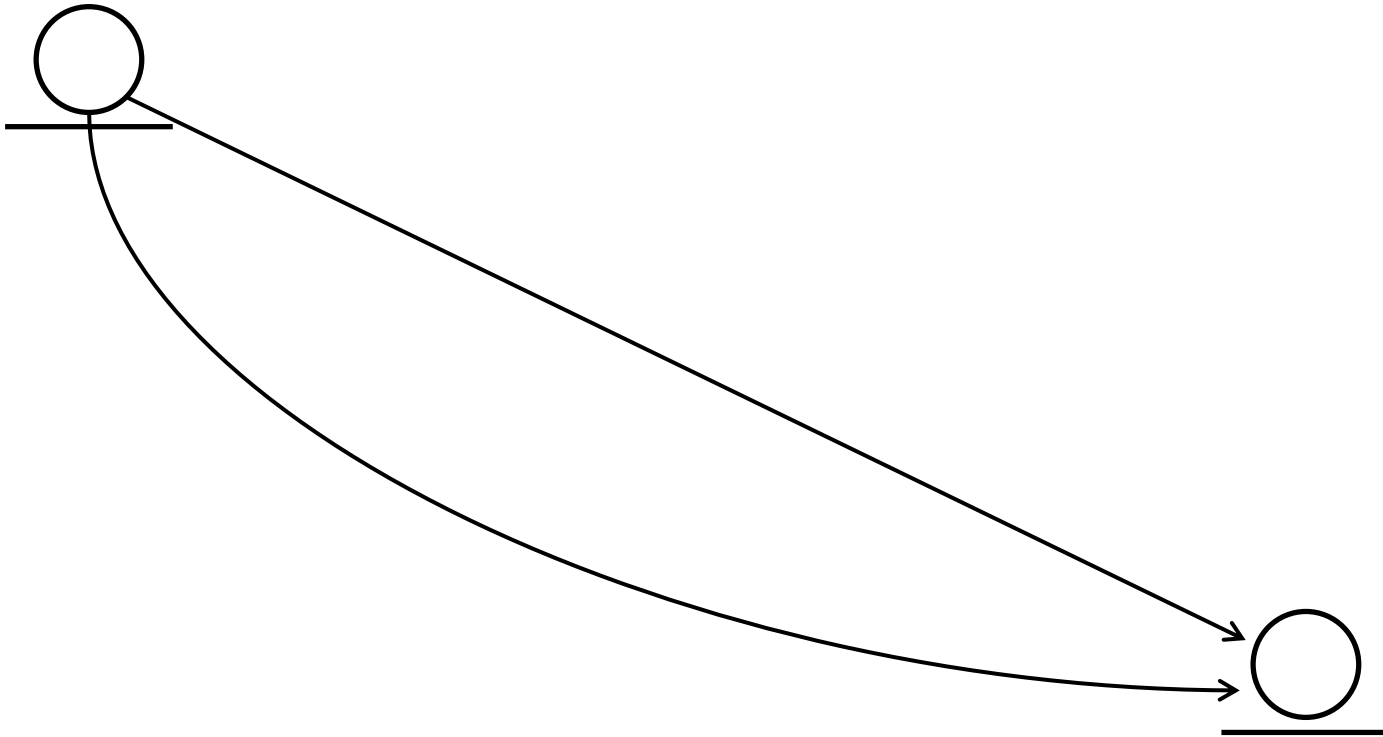
- Introduction to algorithms
- Warming-up : maze algorithm
- Recursion
- Recursion-based algorithms
- Graph theory
- Weighted graph
- Network theory
- Dynamic programming (if possible)
- Practical examples

※ Language : C or (C++)

Lecture Note



Introduction (1/6)



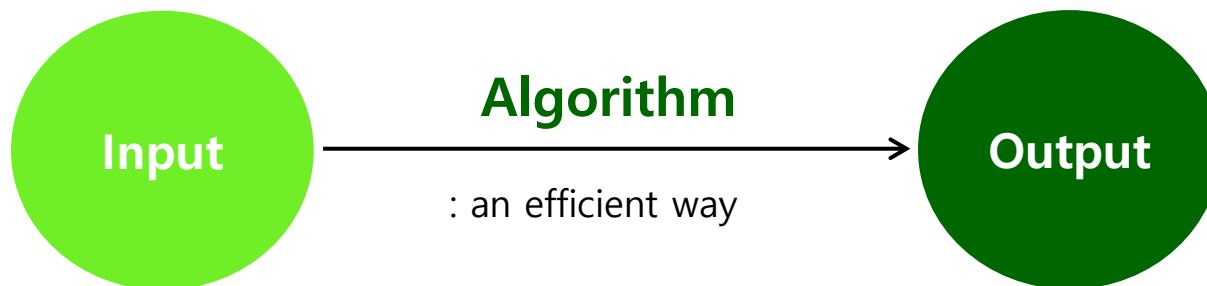
■ What is the Algorithm ?

An algorithm is any well-defined **computational procedure** that takes some values (or a set of values) as **input** and produces some values (or a set of values) as **output**

• Simple example

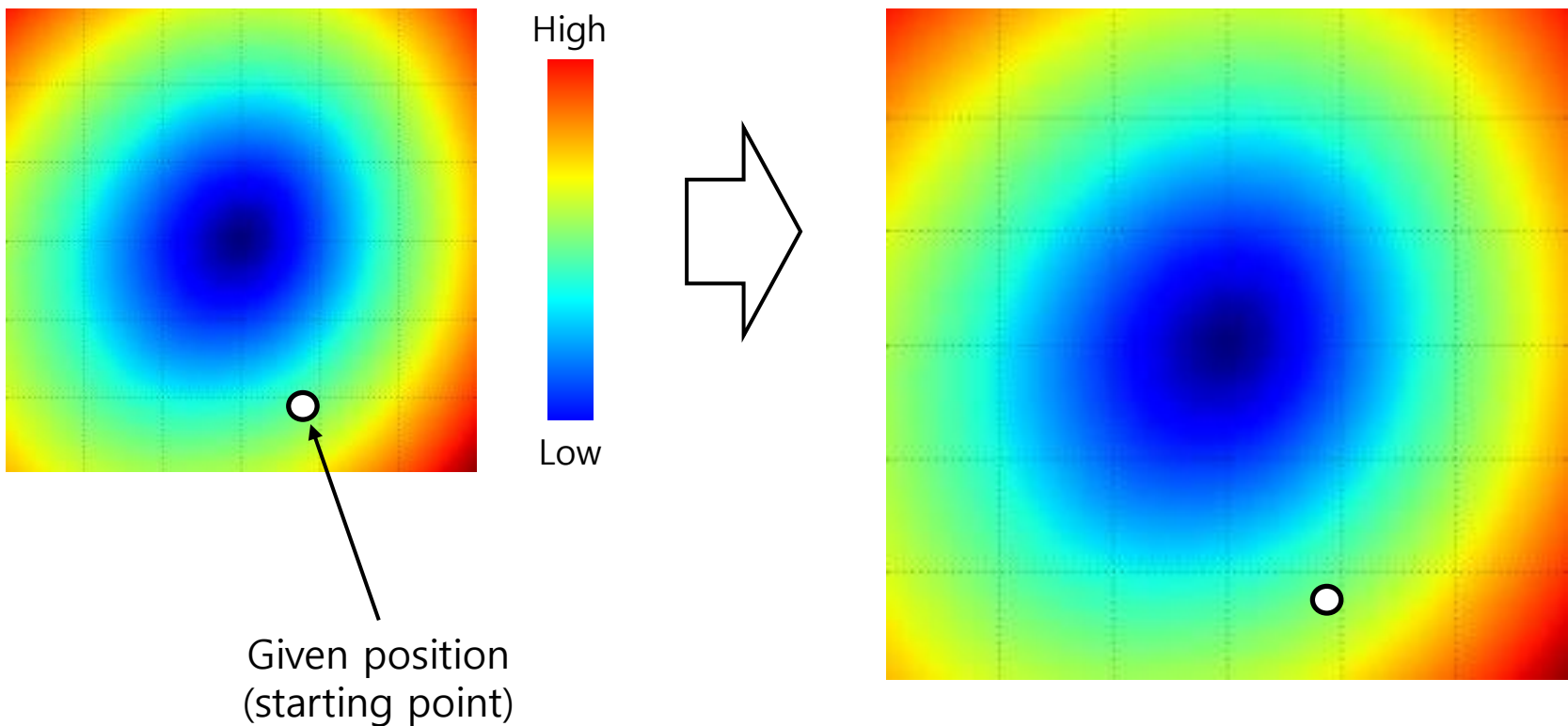
- Task (problem) : compute the average of mid term scores
- Input : mid-term scores
- Output : average score of all the scores

How to compute ?



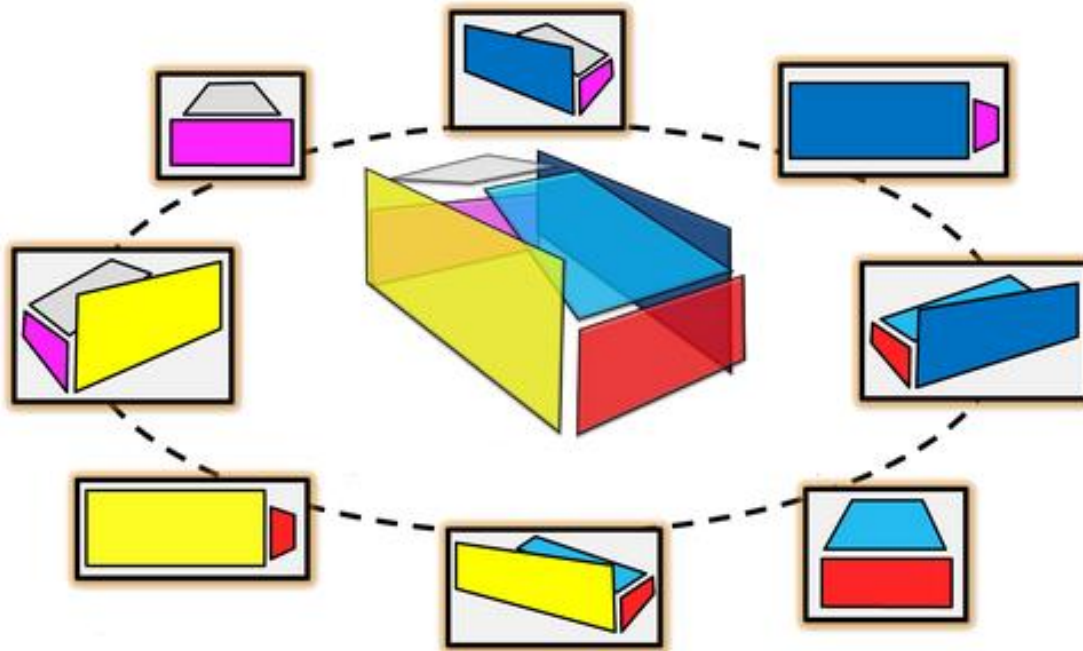
Introduction (3/6)

- Needs for “desirable” algorithms
 - Goal : to find the lowest position on a given 2D space



Draw your algorithm !

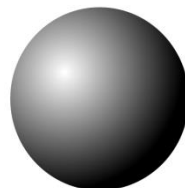
■ Needs for “desirable” algorithms – cont’d



Multiview 3D reconstruction

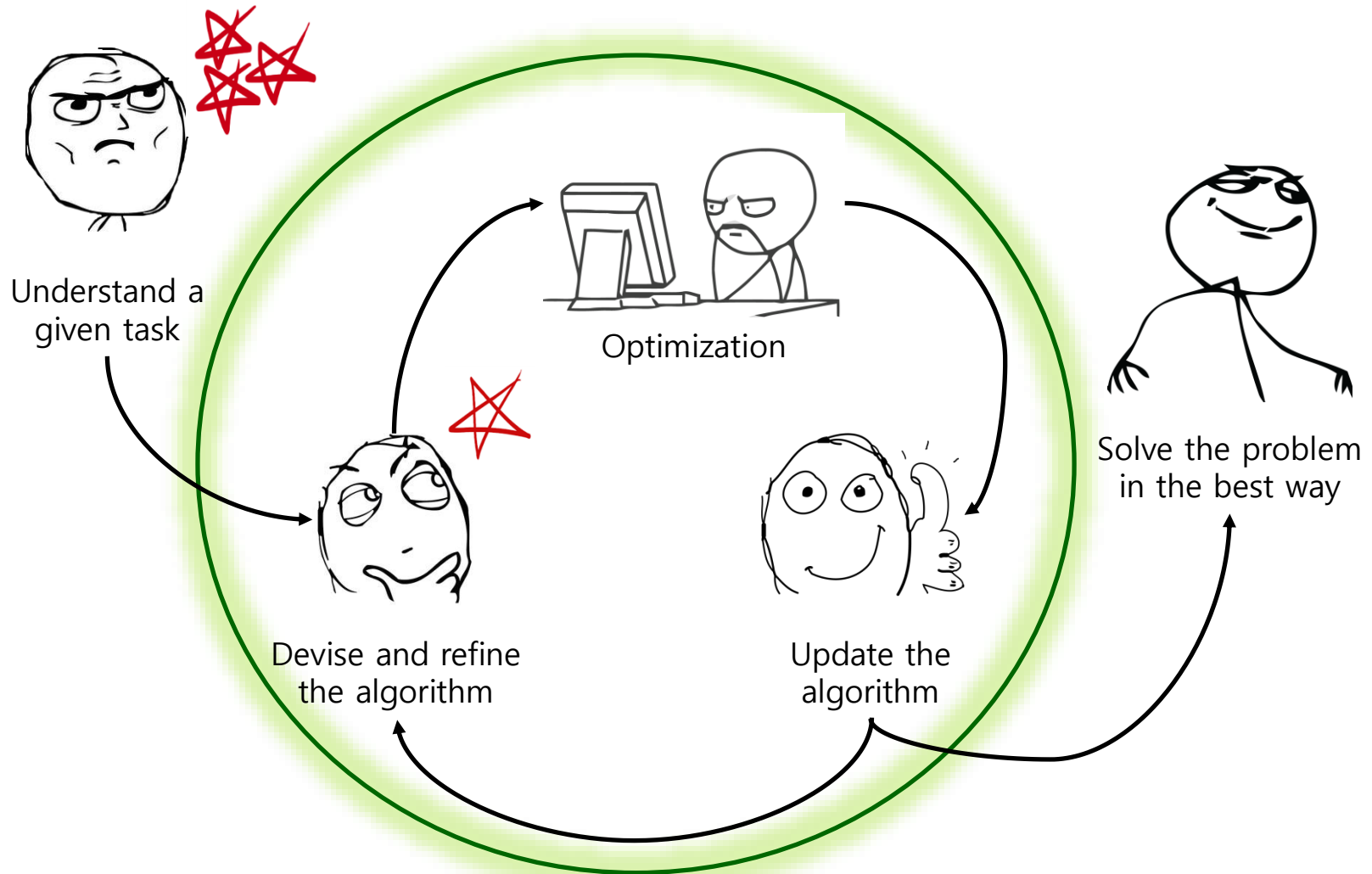
* Image is from Google Image

* Why is infinite-dimensional ?
(Think about a sphere !)



Role of the algorithm ?

■ Procedure to make the algorithm

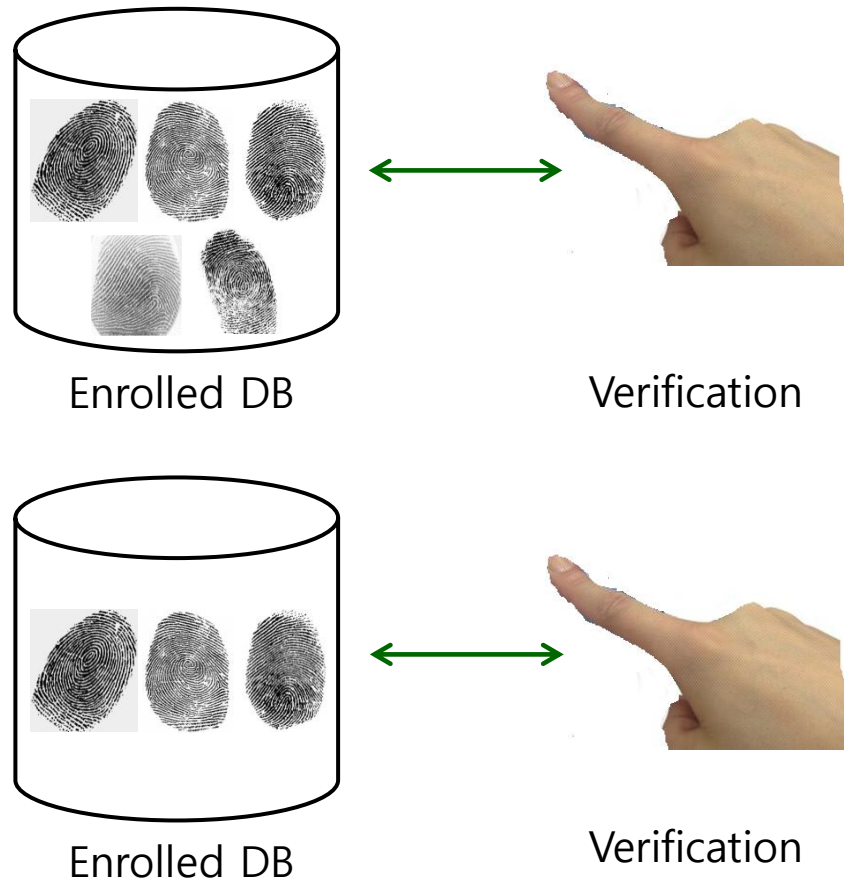


Introduction (6/6)

- For optimization, we always think about () !
- Trade-off between the processing time and the memory



[Fingerprint recognition (S10)]



* Images are from Google Image

■ Integer multiplication

• Normal operation

- (1) Multiplication twice
- (2) Summing up all the values

$$\begin{array}{r} 45 \\ \times 37 \\ \hline 315 \\ 135 \\ \hline 1665 \end{array} \quad \begin{aligned} &= 45 \times (30 + 7) \\ &= (45 \times 30) + (45 \times 7) \\ &= 1350 + 315 \\ &= 1665 \end{aligned}$$

※ Complexity :

Multiplication > addition

• a la russe algorithm

- (1) If A is odd, copy B to C
- (2) $A = A/2$ (integer division), $B = B \times 2$
- (3) Repeat (1)(2) until A becomes 1, summing up all C values

A	B	C
45	37	37
22	74	-
11	148	148
5	296	296
2	592	-
1	1184	1184

$$\rightarrow 37 + 148 + 296 + 1184 = 1665$$

Warming-up Example (2/5)

- Integer multiplication (implementation)
 - Compare the processing time of two cases

Make your C codes !

- **Appendix : time checker**
 - **Compute the processing time as follows :**

```
#include <Windows.h>
```

```
LARGE_INTEGER freq, start, stop;  
double diff;
```

```
QueryPerformanceFrequency(&freq); // computer frequency  
QueryPerformanceCounter(&start); // starting point
```

Algorithm

```
QueryPerformanceCounter(&stop); // stopping point  
diff = (double)(stop.QuadPart - start.QuadPart) / freq.QuadPart;
```

Measuring
time

■ Analysis of previous two approaches for multiplication

- Which algorithm is easy to understand for human ?
- Is it same for the computer ?

➡ A la russe is more efficient for the computer, but not optimal

(x2 or /2) operations can be regarded as **bit shift** in the computer

- `temp[0]>>1` : /2 operation
- `temp[0]<<1` : x2 operation

➡ Even though a la russe requires more lines,
computers can handle this kind of simple operations very fast

✂ Implement it using a bit shift and compare the processing time

- How about multiplication for large numbers ?
 - A la russe algorithm requires quite a lot lines !
 - Karatsuba's algorithm

Given two numbers x and y :

$$x = x_1 B^m + x_0, \quad y = y_1 B^m + y_0$$

$$\begin{aligned} xy &= (x_1 B^m + x_0)(y_1 B^m + y_0) \\ &= z_2 B^{2m} + z_1 B^m + z_0 \end{aligned}$$

$$z_0 = x_0 y_0$$

$$z_1 = x_1 y_0 + x_0 y_1$$

$$z_2 = x_1 y_1$$

$$z_1 = (x_1 + x_0)(y_1 + y_0) - z_2 - z_0$$

Why ?

[Pseudo code for Karatsuba's alg.]

```
procedure karatsuba(num1, num2)
  if (num1 < 10) or (num2 < 10)
    return num1*num2
  /* calculates the size of the numbers */
  m = max(size_base10(num1), size_base10(num2))
  m2 = m/2
  /* split the digit sequences about the middle */
  high1, low1 = split_at(num1, m2)
  high2, low2 = split_at(num2, m2)
  /* 3 calls made to numbers approximately half the size */
  z0 = karatsuba(low1, low2)
  z1 = karatsuba((low1+high1), (low2+high2))
  z2 = karatsuba(high1, high2)
  return (z2*10^(2*m2)) + ((z1-z2-z0)*10^(m2)) + (z0)
```

For example, $12345 \times 6789 = ?$

Try to implement it !

- Algorithm : find the best way to the solution
 - Need to understand a given problem clearly !
- Enjoy thinking with your programming