

**DM HOMEWORK 2** (29 января 2016 г.)*Tropin Andrew**e-mail: [andrewtropin@gmail.com](mailto:andrewtropin@gmail.com)**github: [abcdw](#)***Problem 1.**

Let  $M = (8, 15)$ ,  $N = (9, 20)$  on real axis, then  $K = M \cup N$  will be  $(8, 20)$

**Problem 2.**

$A = \{a, b, \{a, b\}\}$ . How many elements does this set have:  $P(A)$ .

$$\begin{aligned} N(A) &= 3 \\ N(P(A)) &= 2^{N(A)} = 2^3 = 8 \end{aligned}$$

**Problem 3.**

- For every  $x$  in  $\mathbb{R}$   $x$  in power of two not equal to minus one. It's true.
- Exists such  $x$  in  $\mathbb{Z}$ , that  $x$  in power of two equal to 2. It's false.

**Problem 4.**

Let  $A = \{1, 2, 3, 4, 5\}$  and  $B = \{0, 3, 6\}$ . Find

- $A \cup B = \{0, 1, 2, 3, 4, 5, 6\}$
- $A \cap B = \{3\}$
- $A - B = \{1, 2, 4, 5\}$
- $B - A = \{0, 6\}$

**Problem 5.**

$$A - B = A \cap B^c$$

$$x \in (A - B) \Rightarrow x \in A \& x \notin B \Rightarrow x \in A \& x \in B^c \Rightarrow x \in (A \cap B^c)$$

$$x \in (A \cap B^c) \Rightarrow x \in A \& x \in B^c \Rightarrow x \in A \& x \notin B \Rightarrow x \in (A - B)$$

**Problem 6.**

- $A \cap B \cap C = \{4, 6\}$
- $(A \cup B) \cap C = \{4, 5, 6, 8, 10\}$

**Problem 7.**

It's hard enough to draw them with LaTeX.

- $A \cap (B - C)$  will look like three circles and only one small part, that belongs to A and B, but not C will be filled.
- All universe will be filled, except circles related to  $A, B, C$ .

**Problem 8.**

$$A^c \cup (A \cup B^c \cup C^c)^c \cup (B \cap (A \cup C)^c) = A^c \cup (B - (A \cup C)) = A^c$$