Mock exam answers for part ii paper 1 a

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Exercise 1

- **A** T and L are strictly dominated, and there aren't any pure strategy Nash equilibrium. There is a unique mixed strategy Nash equilibrium, given by Pr(M) = 2/3, Pr(B) = 1/3, Pr(C) = 1/2, and Pr(R) = 1/2.
- **B** 1 minmax's 2 with T. 2 minmax's 1 with L. By Fudenberg and Maskin (1986), V^* is the set of feasible payoffs that strictly dominate (1,1), the minmax point.¹
- C Take a one-shot correlated strategy profile (s_1, s_2) with payoffs (v_1, v_2) . Phase (A): play s_i each period as long as (s_1, s_2) was played in the previous period. After any deviation from phase (A) go to phase (B): both players minmax for $n(\delta)$ rounds. If there are any deviations while in phase (B), then begin phase (B) again.

Exercise 2

- 1 Ignore two of the three events. Undesirable for those wanting a triathalon. (Although, randomization over the dictating event seems to work, and seems much more reasonable.)
- **2** Maybe sum rankings across the three events. Satisfies α , β , and not a dictatorship so doesn't satisfy γ .

Exercise 3

a Player 1's strategies are U or D. Player 2's strategies are LL, LR, RL, RR. There are two proper subgames, one for each move of 1.

 $^{^1\}mathrm{Given}$ that this result was not directly in the notes, it's fine if you used Friedman (1971,77) and said V^* is the set of feasible payoffs that Pareto dominate the static Nash equilibrium payoffs via a suitably described Nash-reversion strategy.

- **b** Via backward induction, 2,1.
- ${f c}$ Subgame-perfect equilibrium are Nash equilibrium, so 2,1 is one. For others, draw out the normal form

- 1,1 is the other.
- **d** Yes, 2 can mix between L and R off the path of play. (By Kuhn's theorem there exists a corresponding mixed strategy.)
- **e** There are no proper sub-games, so sub-game perfect and Nash equilibrium are the same.
- **f** The normal form is given by the 2-by-2 payoff matrix. The unique Nash equilibrium outcome is 1,1.
- **g** We recover game A.²

Exercise 4, excluded from exam

- i Consider a two-player non-zero sum game in normal form. Player 1 gets a new strategy that can be played, that is, we add a new row to the payoff matrix. Give an example to show that player 1's equilibrium payoff can decrease as a result of this increased flexibility in strategic choice.
- ii Consider a two-player zero sum game. Again assume that Player 1 gets a new strategy that can be played. What can happen to player 1's equilibrium payoff? Can it decrease? Why or why not?

 $^{^2{\}rm This}$ question demonstrates a fragility of Nash and sub-game perfect equilibrium to small changes in a game's information structure. A solution concept called $sequential\ equilibrium,$ proposed by Kreps and Wilson (1982), helps deal with this.