

Assignment 9, 2023

Decision analysis

Aki Vehtari et al.

1 General information

This is for BDA 2023

The maximum amount of points from this assignment is 3.

We have prepared a **quarto** template specific to this assignment ([html](#), [qmd](#), [pdf](#)) to help you get started.

Setup

We recommend Aalto students use jupyter.cs.aalto.fi, for all others we also provide a [docker container](#).

Tip

Reading instructions:

- [The reading instructions for BDA3 Chapter 9](#) (decision analysis).

Grading instructions:

The grading will be done in peergrade. All grading questions and evaluations for this assignment are contained within this document in the collapsible **Rubric** blocks.

Installing and using CmdStanR:

See the [Stan demos](#) on how to use Stan in R (or Python). [Aalto JupyterHub](#) has working R and CmdStanR/RStan environment and is probably the easiest way to use Stan. * To use CmdStanR in [Aalto JupyterHub](#):
`library(cmdstanr) set_cmdstan_path('/coursedata/cmdstan')`

The Aalto Ubuntu desktops also have the necessary libraries installed.

To install Stan on your laptop, run `install.packages("cmdstanr", repos = c("https://mc-stan.org/r-packages/", getOption("repos")))` in R. If you encounter problems, see additional answers in [FAQ](#). For Aalto students, if you don't succeed in short amount of time, it is probably easier to use [Aalto JupyterHub](#).

If you use [Aalto JupyterHub](#), all necessary packages have been pre-installed. In your laptop, install package `cmdstanr`. Installation instructions on Linux, Mac and Windows can be found at <https://mc-stan.org/cmdstanr/>. Additional useful packages are `loo`, `bayesplot` and `posterior` (but you don't need these in this assignment). For Python users, `PyStan`, `CmdStanPy`, and `ArviZ` packages are useful.

Stan manual can be found at <https://mc-stan.org/users/documentation/>.

From this website, you can also find a lot of other useful material about Stan.

If you edit files ending `.stan` in RStudio, you can click “Check” in the editor toolbar to make syntax check. This can significantly speed-up writing a working Stan model.

! Reporting accuracy

For posterior statistics of interest, only report digits that are not completely random based on the Monte Carlo standard error (MCSE).

Example: If you estimate $E(\mu) \approx 1.234$ with $\text{MCSE}(E(\mu)) = 0.01$, then the true expectation is likely to be between 1.204 and 1.264, it makes sense to report $E(\mu) \approx 1.2$.

See Lecture video 4.1, [the chapter notes](#), and [a case study](#) for more information.

💡 Further information

- The recommended tool in this course is R (with the IDE RStudio).
- Instead of installing R and RStudio on your own computer, see [how to use R and RStudio remotely](#).
- If you want to install R and RStudio locally, download [R and RStudio](#).
- There are tons of tutorials, videos and introductions to R and RStudio online. You can find some initial hints from [RStudio Education pages](#).
- When working with R, we recommend writing the report using `quarto` and the provided template. The template includes the formatting instructions and how to include code and figures.
- Instead of `quarto`, you can use other software to make the PDF report, but the same instructions for formatting should be used.
- Report all results in a single, **anonymous** *.pdf -file and submit it in [peergrade.io](#).
- The course has its own R package `aaltobda` with data and functionality to simplify coding. The package is pre-installed in JupyterHub. To install the package on your own system, run the following code (upgrade="never" skips question about updating other packages):

```
install.packages("aaltobda", repos = c("https://avehtari.github.io/BDA_course_Aalto/", getOption("repos")
```

- Many of the exercises can be checked automatically using the R package `markmyassignment` (pre-installed in JupyterHub). Information on how to install and use the package can be found in [the markmyassignment documentation](#). There is no need to include `markmyassignment` results in the report.
- Recommended additional self study exercises for each chapter in BDA3 are listed in the course web page. These will help to gain deeper understanding of the topic.
- Common questions and answers regarding installation and technical problems can be found in [Frequently Asked Questions \(FAQ\)](#).
- Deadlines for all assignments can be found on the course web page and in Peergrade. You can set email alerts for the deadlines in Peergrade settings.

- You are allowed to discuss assignments with your friends, but it is not allowed to copy solutions directly from other students or from internet.
- You can copy, e.g., plotting code from the course demos, but really try to solve the actual assignment problems with your own code and explanations.
- Do not share your answers publicly.
- Do not copy answers from the internet or from previous years. We compare the answers to the answers from previous years and to the answers from other students this year.
- Use of AI is allowed on the course, but the most of the work needs to be by the student, and you need to report whether you used AI and in which way you used them (See [points 5 and 6 in Aalto guidelines for use of AI in teaching](#)).
- All suspected plagiarism will be reported and investigated. See more about the [Aalto University Code of Academic Integrity and Handling Violations Thereof](#).
- Do not submit empty PDFs, almost empty PDFs, copy of the questions, nonsense generated by yourself or AI, as these are just harming the other students as they can't do peergrading for the empty or nonsense submissions. Violations of this rule will be reported and investigated in the same way as plagiarism.
- If you have any suggestions or improvements to the course material, please post in the course chat feedback channel, create an issue, or submit a pull request to the public repository!

Rubric

- Can you open the PDF and it's not blank nor nonsense? If the pdf is blank, nonsense, or something like only a copy of the questions, 1) report it as problematic in Peergrade-interface to get another report to review, and 2) send a message to TAs.
- Is the report anonymous?

This is the template for [assignment 9](#). You can download the [qmd-file](#) or copy the code from this rendered document after clicking on `</>` Code in the top right corner.

Please replace the instructions in this template by your own text, explaining what you are doing in each exercise.

Setup

The following loads several needed packages:

```
library(bayesplot)
```

This is bayesplot version 1.11.1.9000

- Online documentation and vignettes at mc-stan.org/bayesplot
- bayesplot theme set to `bayesplot::theme_default()`
 - * Does `_not_` affect other ggplot2 plots
 - * See `?bayesplot_theme_set` for details on theme setting

```
library(cmdstanr)
```

This is cmdstanr version 0.8.1.9000

- CmdStanR documentation and vignettes: mc-stan.org/cmdstanr
- CmdStan path: /u/77/ave/unix/.cmdstan/cmdstan-2.35.0-rc3
- CmdStan version: 2.35.0

```
library(dplyr)
```

Attaching package: 'dplyr'

The following objects are masked from 'package:stats':

filter, lag

The following objects are masked from 'package:base':

intersect, setdiff, setequal, union

```
library(ggplot2)
library(ggdist) # for stat_dotsinterval
library(posterior)
```

This is posterior version 1.6.0

Attaching package: 'posterior'

The following object is masked from 'package:bayesplot':

rhat

The following objects are masked from 'package:stats':

mad, sd, var

The following objects are masked from 'package:base':

%in%, match

```
library(brms)
```

Loading required package: Rcpp

Loading 'brms' package (version 2.21.6). Useful instructions can be found by typing `help('brms')`. A more detailed introduction to the package is available through `vignette('brms_overview')`.

Attaching package: 'brms'

The following objects are masked from 'package:ggdist':

dstudent_t, pstudent_t, qstudent_t, rstudent_t

The following object is masked from 'package:bayesplot':

rhat

The following object is masked from 'package:stats':

ar

```
# Globally specify cmdstan backend for brms
options(brms.backend="cmdstanr")
# Tell brms to cache results if possible
options(brms.file_refit="on_change")

# Set more readable themes with bigger font for plotting packages
ggplot2::theme_set(theme_minimal(base_size = 14))
bayesplot::bayesplot_theme_set(theme_minimal(base_size = 14))
```

This exercise is an example of a decision analysis (DA). In a broad context, this means optimizing over different decisions that lead to different outcomes that all have different utilities. In a Bayesian context, this means using posterior distributions to make decisions.

2 Escaping from the chicken coop

You are an adult chicken living in an organic chicken commune, where life is great, if a bit boring. You have settled in comfortably, but you want something more for your offspring. Your traveling corvid friends tell you of places where chickens eat corn all day, get ferried around in [mobile chicken coops to see the world](#) or [get mental stimulation by being trained humanely to perform tricks](#). The chicken elders have gained access to the computers of your human caretakers and have found the results of a complicated statistical analysis of the growth curves of your relatives. Because you are a chicken, you don't care about convergence diagnostics or priors.

Your task is to maximize the chance of escape for your offspring.

Subtask 2.c

Compute and visualize the **expected chicken weight for days 1–40 per diet**, according to the model provided in the template. Do the predictions look reasonable? Why/why not?

Tip

To sample a “new chicken” from the posterior, use [posterior_predict](#) with options `newdata=...`, `allow_new_levels=TRUE`, `sample_new_levels="gaussian"`, where you pass a dataframe as `newdata` which has a “new” chicken ID `Chick` and appropriate values for `Time` and `Diet`.

⚠ A simple GP model

The below fits a GP model to the chicken growth curves. It may take a few minutes to fit, but you can also [download the fit .rds-file](#) and work with that fit object.

```
fit <- brm(  
  weight ~ gp(Time) + (0+Time|Diet) + (0+Time|Chick),  
  data = ChickWeight,  
  family = "lognormal",  
  file="additional_files/assignment9/gp_chicken_fit",  
  cores = parallel::detectCores(),  
  # For the template only, remove the below from your code!  
  iter = 500  
)
```

Start sampling

Running MCMC with 4 chains, at most 12 in parallel...

```
Chain 1 Iteration:    1 / 500 [  0%] (Warmup)  
Chain 2 Iteration:    1 / 500 [  0%] (Warmup)  
Chain 3 Iteration:    1 / 500 [  0%] (Warmup)  
Chain 4 Iteration:    1 / 500 [  0%] (Warmup)  
Chain 3 Iteration: 100 / 500 [ 20%] (Warmup)  
Chain 2 Iteration: 100 / 500 [ 20%] (Warmup)  
Chain 1 Iteration: 100 / 500 [ 20%] (Warmup)  
Chain 4 Iteration: 100 / 500 [ 20%] (Warmup)  
Chain 3 Iteration: 200 / 500 [ 40%] (Warmup)  
Chain 1 Iteration: 200 / 500 [ 40%] (Warmup)  
Chain 2 Iteration: 200 / 500 [ 40%] (Warmup)  
Chain 3 Iteration: 251 / 500 [ 50%] (Sampling)  
Chain 2 Iteration: 251 / 500 [ 50%] (Sampling)  
Chain 1 Iteration: 251 / 500 [ 50%] (Sampling)  
Chain 4 Iteration: 200 / 500 [ 40%] (Warmup)  
Chain 3 Iteration: 350 / 500 [ 70%] (Sampling)  
Chain 2 Iteration: 350 / 500 [ 70%] (Sampling)  
Chain 4 Iteration: 251 / 500 [ 50%] (Sampling)  
Chain 1 Iteration: 350 / 500 [ 70%] (Sampling)  
Chain 3 Iteration: 450 / 500 [ 90%] (Sampling)  
Chain 2 Iteration: 450 / 500 [ 90%] (Sampling)  
Chain 1 Iteration: 450 / 500 [ 90%] (Sampling)  
Chain 3 Iteration: 500 / 500 [100%] (Sampling)  
Chain 3 finished in 17.4 seconds.  
Chain 2 Iteration: 500 / 500 [100%] (Sampling)  
Chain 2 finished in 17.9 seconds.  
Chain 4 Iteration: 350 / 500 [ 70%] (Sampling)  
Chain 1 Iteration: 500 / 500 [100%] (Sampling)  
Chain 1 finished in 19.1 seconds.  
Chain 4 Iteration: 450 / 500 [ 90%] (Sampling)  
Chain 4 Iteration: 500 / 500 [100%] (Sampling)  
Chain 4 finished in 23.0 seconds.
```

All 4 chains finished successfully.

Mean chain execution time: 19.4 seconds.

Total execution time: 23.2 seconds.

Warning: 45 of 1000 (4.0%) transitions ended with a divergence.
See <https://mc-stan.org/misc/warnings> for details.

Warning: 864 of 1000 (86.0%) transitions hit the maximum treedepth limit of 10.
See <https://mc-stan.org/misc/warnings> for details.

Loading required package: rstan

Loading required package: StanHeaders

rstan version 2.35.0.9000 (Stan version 2.35.0)

For execution on a local, multicore CPU with excess RAM we recommend calling
`options(mc.cores = parallel::detectCores())`.

To avoid recompilation of unchanged Stan programs, we recommend calling
`rstan_options(auto_write = TRUE)`

For within-chain threading using ``reduce_sum()`` or ``map_rect()`` Stan functions,
change ``threads_per_chain`` option:

`rstan_options(threads_per_chain = 1)`

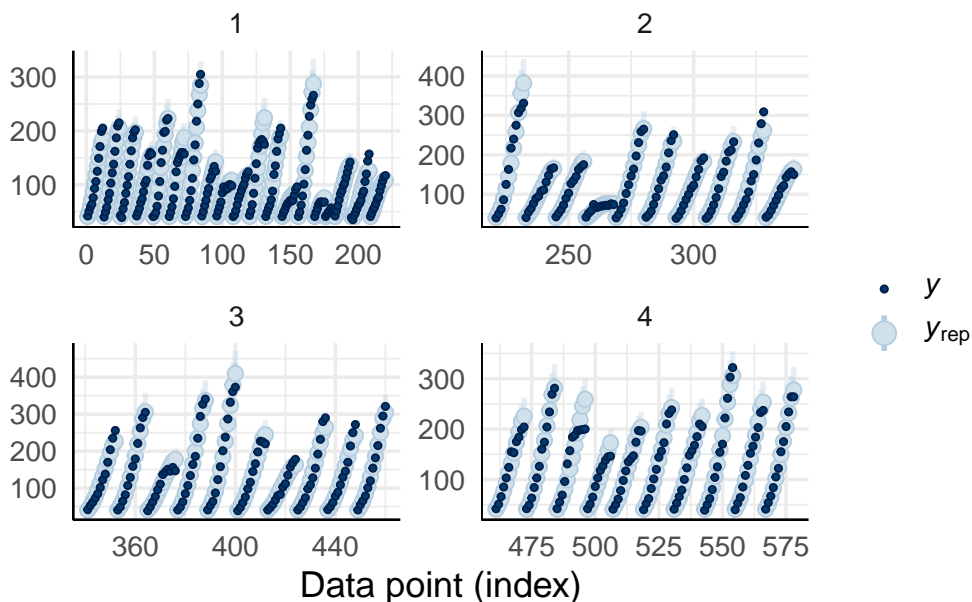
Attaching package: 'rstan'

The following objects are masked from 'package:posterior':

`ess_bulk`, `ess_tail`

```
brms::pp_check(fit, type = "intervals_grouped", group = "Diet")
```

Using all posterior draws for ppc type 'intervals_grouped' by default.



```
# Useful r functions:
```

```
#   rep(..., each=...), cbind, colMeans,
```

```
#   posterior_predict(..., newdata=..., allow_new_levels=TRUE, sample_new_levels="gaussian")
```

```
# ggplot, geom_line, aes(..., group=..., color=...)
```

Rubric

- Does the plot look right and is it readable? It should be quite close to the reference plot below:
- Has it been recognized that the prediction time ?

Your chicken elders have been meticulously collecting data on what kind of characteristics have allowed previous chickens to escape. They have found out that both the age and the weight influence the (daily) probability of escape for a chicken:

- If the chicken is too young, it is not yet mature enough to venture out into the world.
- If the chicken is too old, it will not try to escape anymore.
- If the chicken is small and has just the right size, it can try to squeeze through a tiny crack in the fence.
- If the chicken is big enough, it is strong enough to try to fly over the fence.
- No matter the size, there is always a small residual probability that the chicken can escape.

Every day, chickens will try to escape if they are of the right age. Their daily escape probability $e(\text{day}, \text{weight})$ is implemented in the `daily_probability_of_escape(day, weight)` function. The probability that a chicken with daily weights $w = (w_1, \dots, w_N)$ **has not escaped** after $i + 1$ days can be computed as follows:

$$f_{i+1} = f_i (1 - e(i, w_i))$$

The `chickenwise_probability_of_escape(weights)` computes the probability that a chicken **has escaped** after `length(weights)` days.

💡 Chickenwise probability of escape function

```
bump <- function(x, loc=0, scale=1){
  xi = (x - loc) / scale
  ifelse(abs(xi) < 1, exp(-1/(1-xi^2)), 0.)
}
daily_probability_of_escape <- function(day, weight){
  # Expects a day and a weight and computes the daily probability of escape
  bump(day, 30, 10) * (1e-2 + bump(weight, 200, 150)+bump(weight, 700, 150))
}
chickenwise_probability_of_escape <- function(weights){
  # Expects a vector of daily weights from day 1 to N and computes the probability of
  # escape at the end of the time series
  prob_of_failure = 1
  for(day in 1:length(weights)){
    prob_of_failure = prob_of_failure * (1-daily_probability_of_escape(day, weights[day]))
  }
  return(1 - prob_of_failure)
}
```



```
days = 1:40
weights = 1:900
heatmap_matrix = outer(days, weights, daily_probability_of_escape)
image(days, weights, heatmap_matrix, xlab="day", ylab="weight", main="Daily probability of escape")
```

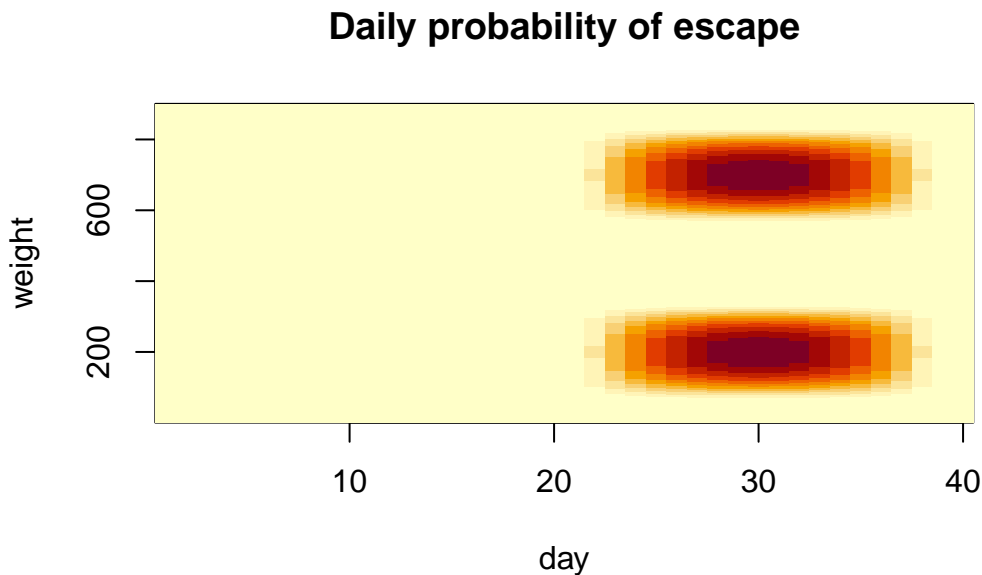


Figure 1: Daily probability of escape for a given day and weight

Subtask 2.a

Compute and visualize the **distribution of the chickenwise probabilities of escape per diet**, according to the model provided in the template.

💡 Tip

You can reuse the predictions you created in the previous subtask. **Work with the draws to compute the chickenwise probability of escape first, and then take the expectation!**

```
# Useful r functions: chickenwise_probability_of_escape (see above)
# rep(..., each=...), apply,
# ggplot, stat_dotsinterval
```

Rubric

- Does the plot look right and is it readable? It should be quite close to the reference plot below:

Subtask 2.b

Compute the **expected probability of escape for each diet**. Why would it be wrong to compute the expected probability of escape by applying the `chickenwise_probability_of_escape` function in the template to the *daily expected chicken weights per diet* computed in subtask 2.a? How does the correctly calculated value compare to the incorrectly calculated value? Why is one higher than the other?

```
# Useful r functions: chickenwise_probability_of_escape (see above)
# apply, aggregate,
```

Rubric

- Do the results look correct and have they been presented in a readable way? They should be roughly the first column below for the correct calculation and the second column below for the wrong calculation: [

```
diet chickenwise_loss meanwise_loss 1 0.55 0.83 2 0.57 0.67 3 0.50 0.10 4
0.52 0.15 ]{.content-hidden when-profile="public"} * Has it been explained
that the expected probability of escape depends on ? * Has it been explained
that
?
```

[AND/OR

for some diets the “incorrect” computation (meanwise_loss) is lower because the mean growth curve (used in the incorrect meanwise_loss) “by chance” passes through the region of low probability of escape, even though due to high within-population variation most chickens’ growth curve won’t pass through that region of low probability of escape?

(Due to a slightly misleading public rubric, either of the above answers would be sufficient)]{.content-hidden when-profile="public"}

3 Overall quality of the report

Rubric

- Does the report include comment on whether AI was used, and if AI was used, explanation on how it was used?
 - No
 - Yes
- Does the report follow the formatting instructions?
 - Not at all
 - Little
 - Mostly
 - Yes
- In case the report doesn’t fully follow the general and formatting instructions, specify the instructions that have not been followed. If applicable, specify the page of the report, where this difference is visible. This will help the other student to improve their reports so that they are easier to read and review. If applicable, specify the page of the report, where this difference in formatting is visible.
- Please also provide feedback on the presentation (e.g. text, layout, flow of the responses, figures, figure captions). Part of the course is practicing making data analysis reports. By providing feedback on the report presentation, other students can learn what they can improve or what they already did well. You should be able to provide constructive or positive feedback for all non-empty and non-nonsense reports. If you think the report is perfect, and you can’t come up with any suggestions

how to improve, you can provide feedback on what you liked and why you think some part of the report is better than yours.