

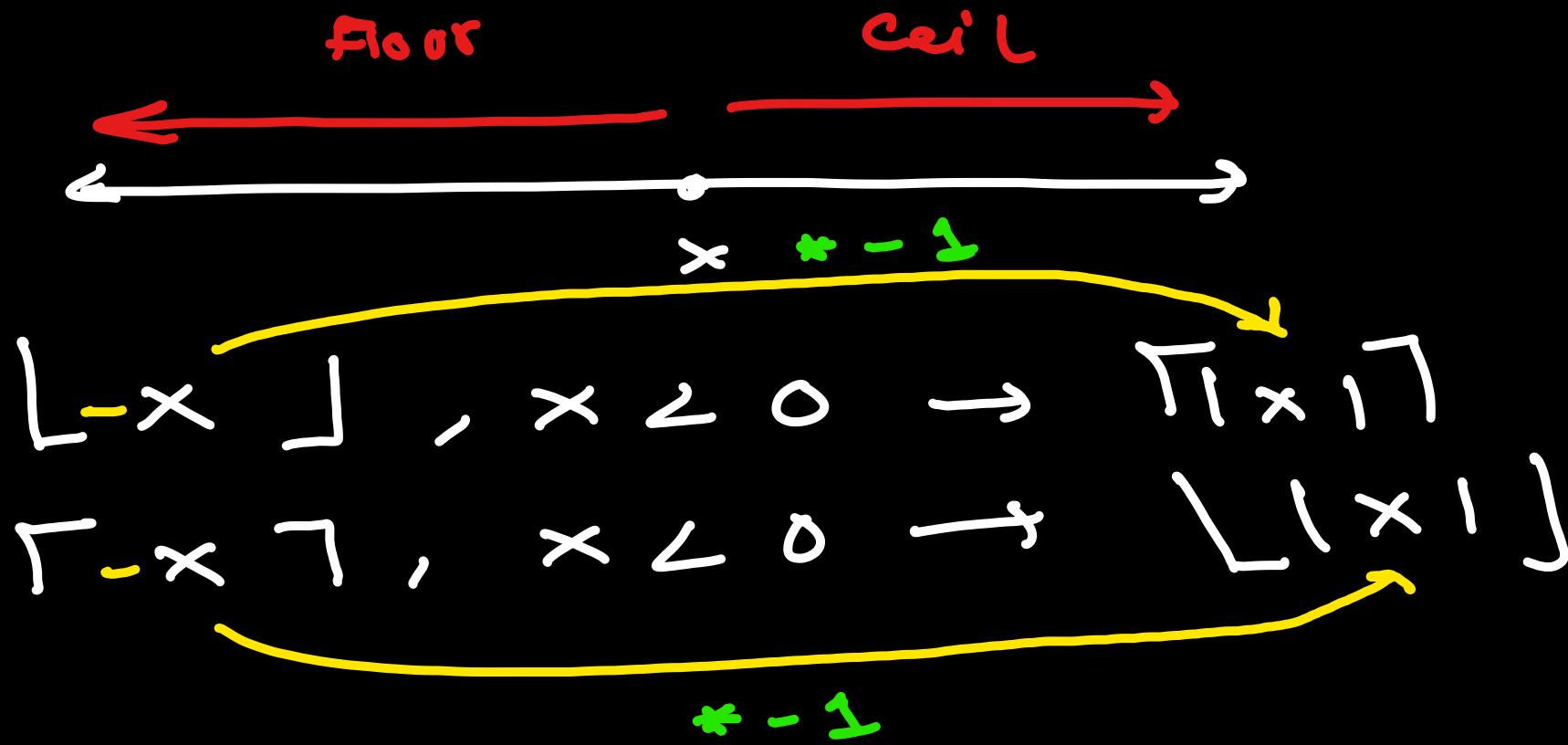
$x \in \mathbb{R}$

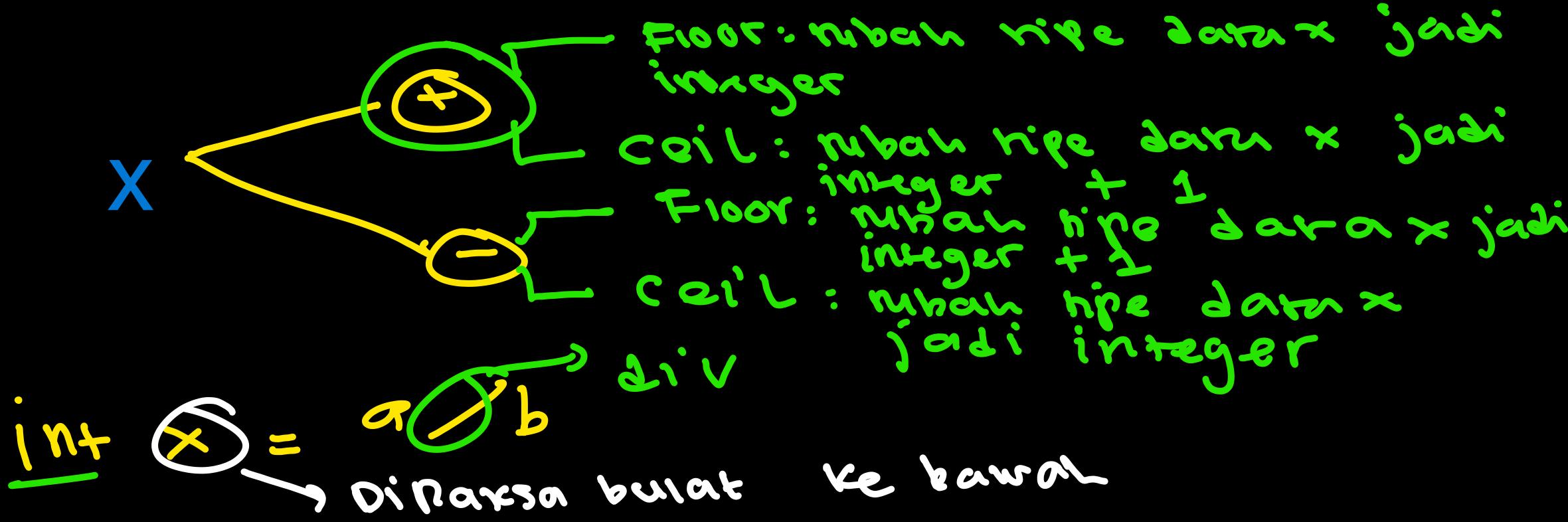
FLOOR =  $\lfloor x \rfloor$  → membulatkan  $x$  ke bawah

ceil =  $\lceil x \rceil$  → membulatkan  $x$  ke atas

$$\begin{aligned}\lfloor 3,5 \rfloor &= 3 \\ \lceil 3,2 \rceil &= 4\end{aligned} \quad \begin{array}{c} \xleftarrow{\text{---}} \xrightarrow{\text{---}} \\ -3 \qquad \qquad -2 \end{array} \quad \begin{array}{c} \lfloor -3,5 \rfloor = -4 \\ \xleftarrow{\text{---}} \xrightarrow{\text{---}} \\ -3 \qquad \qquad -2 \end{array}$$

$$\begin{aligned}-2 > -3 \\ \lceil -2,4 \rceil &= -2 \\ -2 > -2,4\end{aligned}$$





$$n = \underline{3,5}$$

$$x = \text{trunc}(3,5)$$
$$= 3$$

$3,5 \neq 3 \rightarrow$  n decimal

$$n = 3,0$$

$$x = \text{trunc}(3,0)$$
$$= 3$$

$3,0 = 3 \rightarrow$  n buat

## Analisis Kompleksitas :

- ① Jumlah proses di exec . program
- ② Time process

int  $x = y + 1 ; \rightarrow$  (1 operasi)  $\gamma_0(1)$   
 $y = x + 2 ; \rightarrow$  (1 operasi)  $\gamma_0(1)$

for (int i = 1 ;  $i \leq N ; i++ \{$   
    Cout << i << endl;  
    akan menyimpan sebanyak N

$N = 5 \rightarrow$

cout << 1 << endl  
cout << 2 << endl  
cout << 3 << endl  
cout << 4 << endl  
cout << 5 << endl

} permutations

$N \rightarrow$

cout << 1 << endl  
cout << 2 << endl  
-----  
cout << N << endl

}  $N \times$

Complexity :  $O(N)$

```
for (int i = 1 ; i<= N; i++){
    for(int j = 1; j<= M; j++){
        cout<<i<<endl;
    }
}
```

Setiap i dia akan  
ceruk j sebanyak M.  
i sebanyak N, operasi  
sebanyak N x M

$N$   $O(NM)$

$i = 1$   
 $j = 1$   
 $j = 2$   
 $j = 3$   
- - -  
 $j = m$   
 $i = 2$   
 $j = 1$   
 $j = 2$   
 $j = \dots$   
 $j = m$

$$f(n) = n \times f(n-1)$$

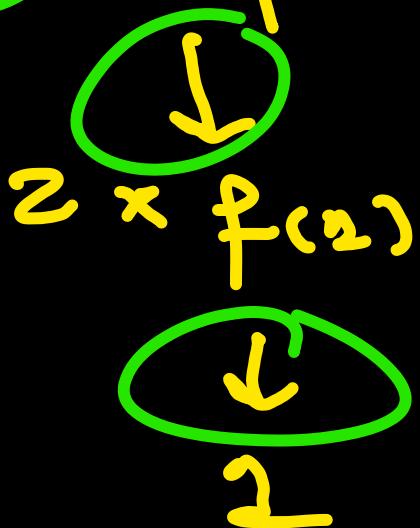
$$f(5) \rightarrow 5 \times f(4) \rightarrow 4 \times f(3) \rightarrow 3 \times f(2)$$

$$\begin{aligned}f(n) &= n \times (n-1) \times (n-2) \times \dots \times 1 \\&= 1 \times 2 \times 3 \times \dots \times n\end{aligned}$$

Banyak operasinya :  $n$

$\Theta(n)$

---



$$O(N) \xleftarrow{\rightarrow 1 \leq N \leq 10^{10}}$$

$$1 \text{ detik} \rightarrow \underline{N = 10^8}$$

$$O(10^8 \cdot 10^2) = 1 \text{ detik}, \dots$$

```
for (int i = 0; i < x; i++){ → × operasi  
    cin >> y;  
    cout << faktor(y) << endl;  
}  
→ operasi.
```

unik sebab ; operasi ada  
y operasi ; sebanyak  $O(Cxy)$   
karena ;

$$x = T, \quad n = 7$$
$$x = 10^7; \quad y = 10^3$$

$$O(x \cdot y) = O(10^{10})$$

$$10^8 = 1 \text{ Sek}$$

$$10^{10} = 1 \text{ Sek und mehr}$$

TLE · Time limit  
Exceeded

$$T = 5$$

- 4 →  $4! = 1 \times 3 \times 2 \times 1 = 24$  } sama aj'a
- 4 →  $\frac{4!}{4} = \frac{1 \times 3 \times 2 \times 1}{4} = 24$  } kurang efisien
- 4 →  $4! = 1 \times 3 \times 2 \times 1 = 24$
- 4 →  $4! = 4 \times 3 = 24$
- 4 → dsb.

$$3! = 6$$

$$T = 5$$

$$\underline{3} \rightarrow = 3 \times 2 \times 1 = 6$$

$$\underline{4} \rightarrow 4! = \underline{4 \cdot 3!} = \underline{4 \times 6} = \underline{24}$$

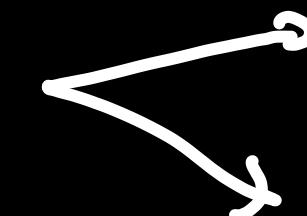
$$\underline{5} \rightarrow 5 \times 4! = \underline{5 \times 24} = \underline{120}$$

$$\underline{6} \rightarrow 6 \times 5! = \underline{6 \times 120} = \underline{720}$$

7

Memoisation → Dynamic Programming  
(D.P.)

Memoization DP



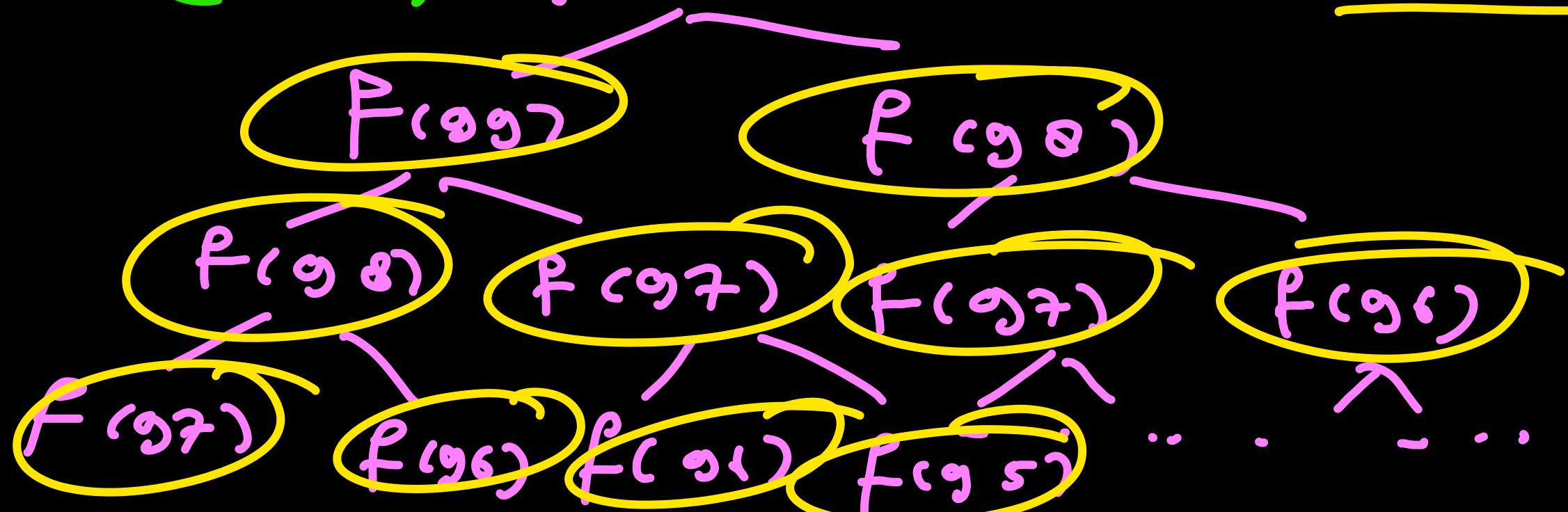
$O(N)$   
 $O(\log N)$

$$\begin{aligned} O(\log N) &\rightarrow \frac{2 \log N}{2} \\ O(\log 10^{10}) &\rightarrow \underline{\frac{2 \log (10^{10}) \leq 10^8}{}} \end{aligned}$$

# Problem solving

Greedy  
Dnc  
Dp

Fibonacci without Memo  
 $O(C2^n)$   $F(100) \rightarrow 2^{100}$  "children



# Fibonacci with memo

O( $\log n$ )  $f(100)$

$f(99)$

$f(98)$

memo[98]

$f(97)$

memo[97]

$f(98)$

$f(97)$

$f(96)$

...

memo[98]

~~$f(95)$~~

memo[95]

memo[98]

memo

$f(96)$

memo

$f(95)$

memo

without memo:  $O(2^n)$

$N = 100 \rightarrow 2^{100} \rightarrow 10^{30} \dots 1e30$

without memo:  $O(\log n)$

$N = 100 \rightarrow (2^{\log 100}) = \lceil \log_2 100 \rceil = 7$

$$O(NP) \leq 256 \text{ MB} \quad 25 \rightarrow 10^{16}$$

$$N \times M \rightarrow 1 \leq N, M \leq 10^5$$

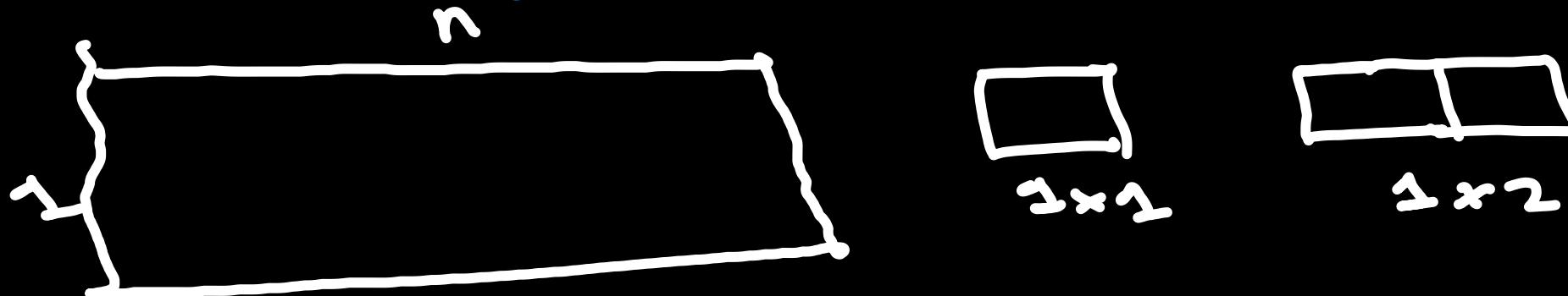
$$\rightarrow O(NM)$$

$$\rightarrow O(10^5 \cdot 10^5) = 10^{10} (\forall) \\ = 1, \dots \leq 21$$

int jawaban = N / M  $\rightarrow$  O(1)

# Dynamic Programming

Misalkan kamu punya lantai berukuran  $1 \times N$ . Kamu punya ubin berukuran  $1 \times 1$  dan  $1 \times 2$ . Berapa banyak cara memasang ubin (jika tidak boleh tumpang tindih dan semua lantai tertutupi ubin)



misalkan fungsi  $dp(n)$  = menyatakan banyak cara mengisi lantai berukuran  $1 \times n$  dengan ubin  $1 \times 1$  dan  $1 \times 2$



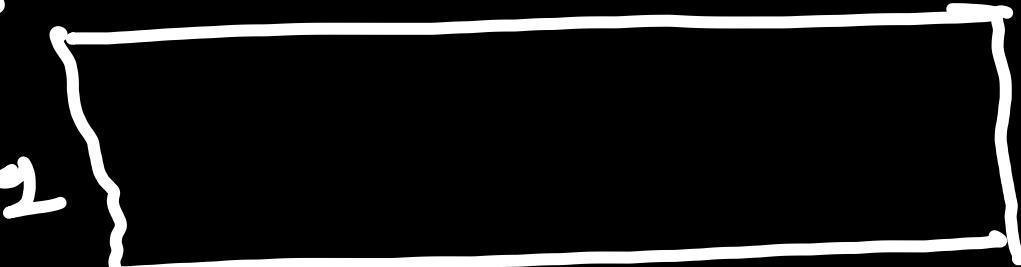
$1 \times 1$   $2 \times 2$

~~1x1~~

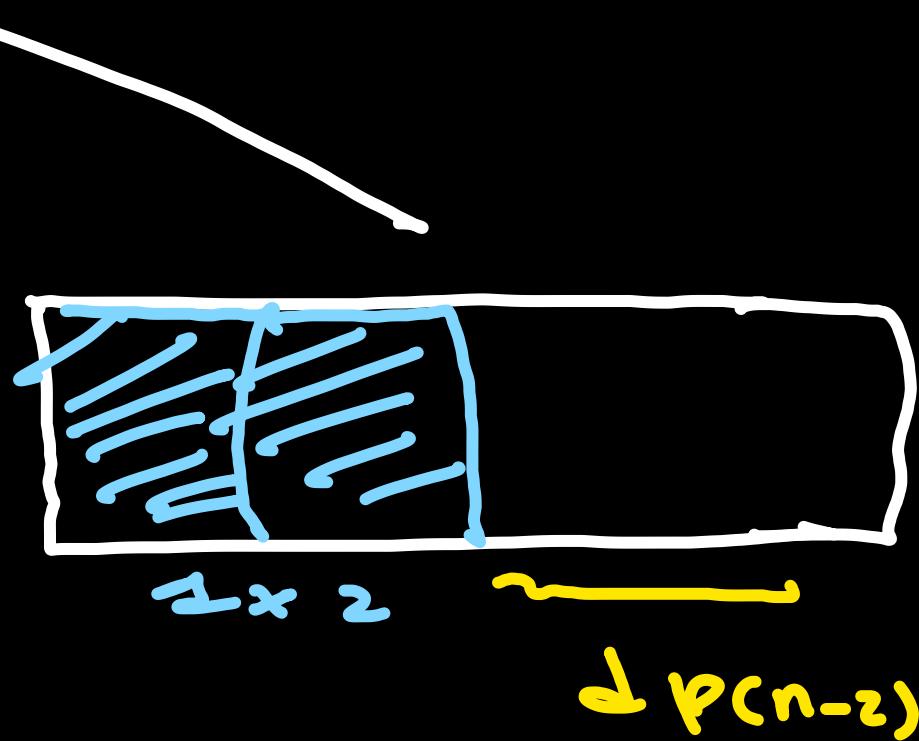
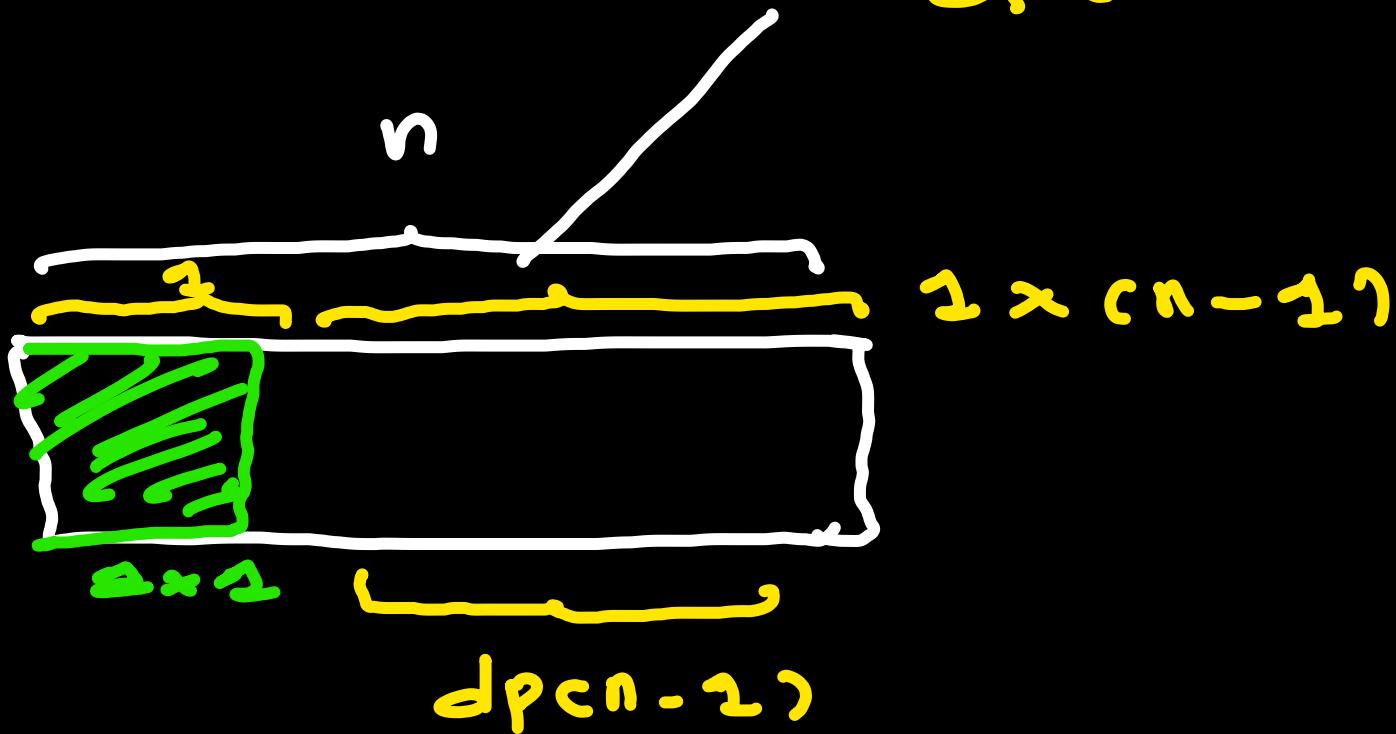
2 cara  $\rightarrow dP(2) = 2$

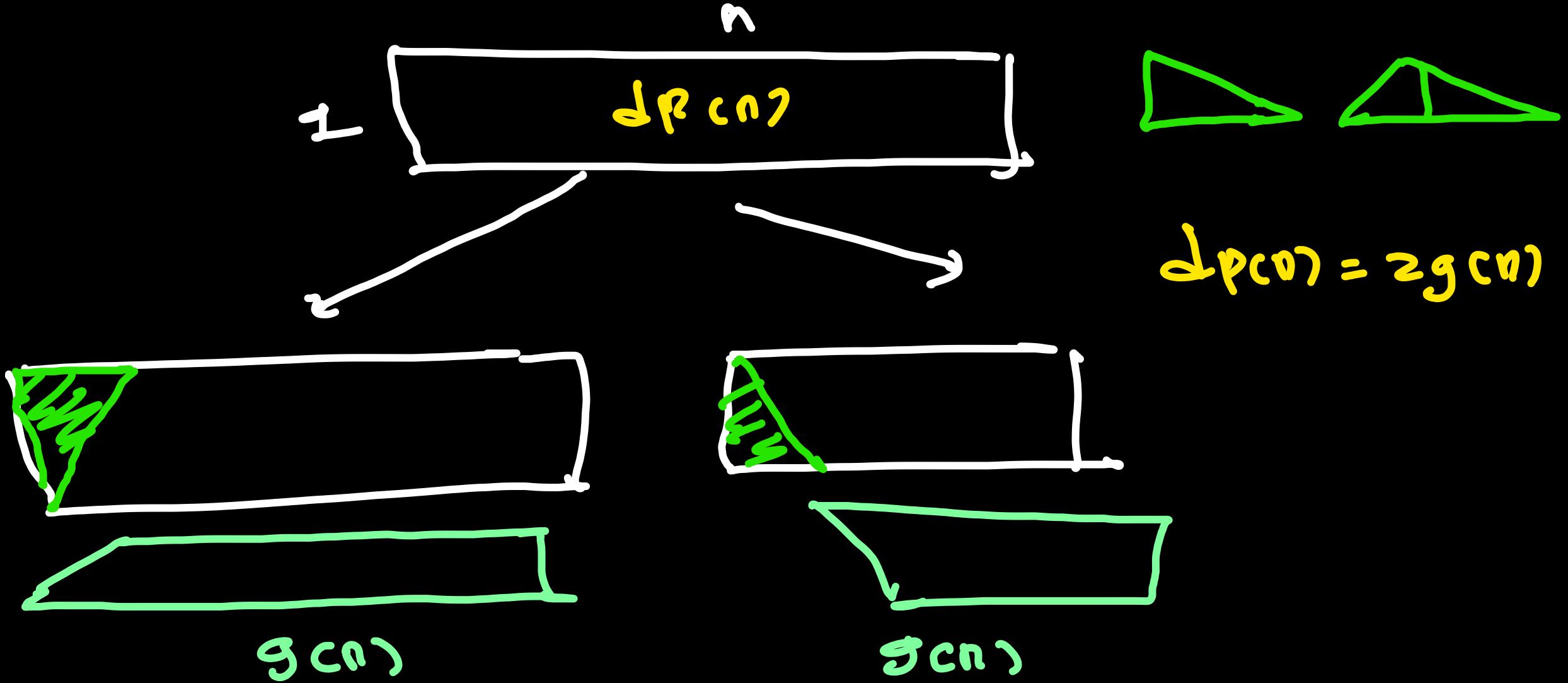
~~1x2~~

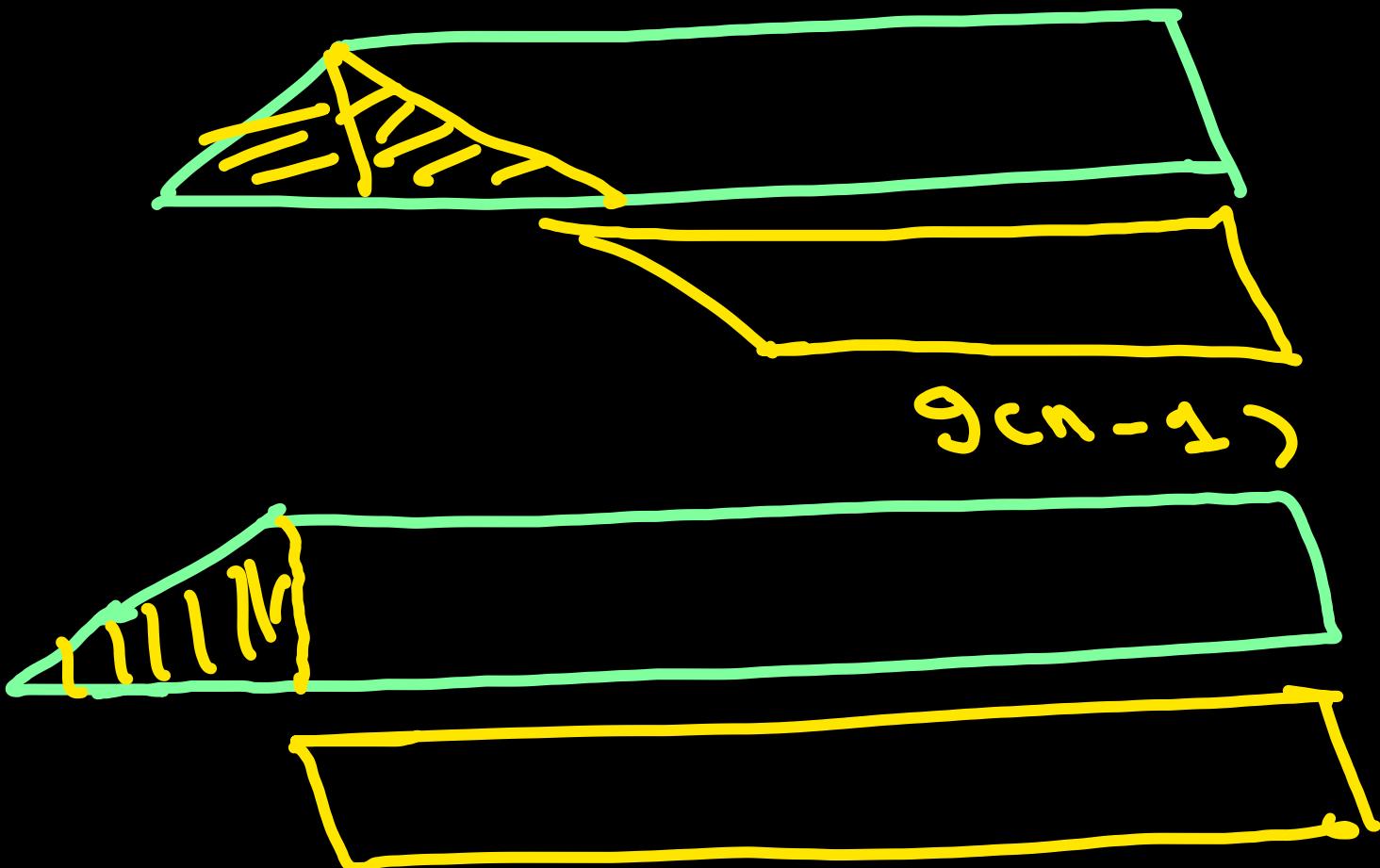
$1 \times 2$



$$dP(n) = dP(n-1) + dP(0)$$
$$dP(0) = 1$$
$$dP(1) = 1$$
$$dP(2) = 2$$







$$dp(n) = 2g(n)$$

$$g(n) = g(n-1) + dp(n-1)$$

$$dp(n-1) = 2g(n-1)$$

$$g(n) = g(n-1) + 2g(n-1)$$

$$g(n) = 3g(n-1)$$

$$dp(n-1)$$

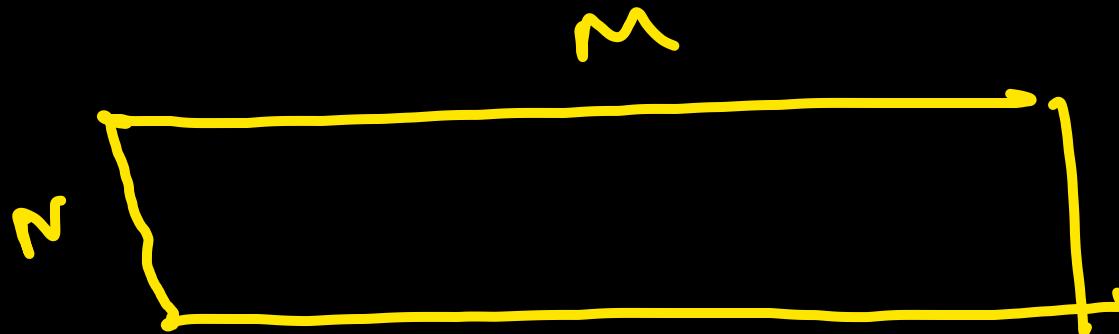
$$\begin{aligned} dp(n) &= 2 \cdot 3g(n-1) \\ &= 6g(n-1) \end{aligned}$$

$$dp(n) = 2g(n)$$

$$dp(n-1) = 2g(n-1) \rightarrow 6g(n-1) = 3$$

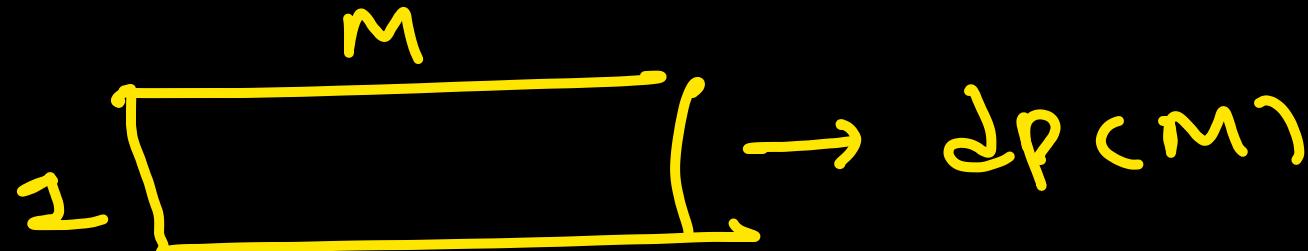
$$dp(n) = 3 dp(n-1)$$

lantai dengan ukuran  $N \times M$



$$dp(n) = 3dp(n-1)$$

$$dp(M) = 3dp(M-1) \rightarrow \text{karang } N=1$$



```
cin>>N>>M;  
if(N == 1){
```

```
cout<<dp(M)<<endl;
```

```
}
```

$$dp(1) = 2$$

$$dp(2) = 3 \quad dp(2-1) = 3dp(1) \rightarrow 3 \cdot 2 \\ = 6$$

$$dp(3) = 3 \cdot 6 \rightarrow 3 \cdot (3 \cdot 2) \\ = 18$$

$$dp(4) = 3 \cdot 18 \rightarrow 3 \cdot (3 \cdot (3 \cdot 2)) \\ = 54$$

$$dp(m) = \underbrace{3 \times 3 \times 3 \times 3 \times \dots \times 3}_{m-1} \times 2$$

$$\text{LPCM} = \frac{3^{n-2}}{2}$$

$$A = [5 \ 6 \ 3 \ 92 \ 7 \ 95 \ 3]$$

$$B = [7 \ 5 \ 5 \ 7 \ 3 \ 9 \ 3 \ 65 \ 3]$$

$$R_A = \frac{36}{8} \\ = 4,5$$

~~R<sub>A</sub> > R<sub>B</sub>~~

R<sub>A</sub> > R<sub>B</sub>

$$R_B = \frac{48}{10} \\ = 4,8$$

sesuaikan pemindahan

$$R_A' = \frac{36+3}{9} = 4,3$$

$$\begin{aligned}
 R_B' &= 28 - 3 / 9 \\
 &= 25 / 9 \\
 &= 5
 \end{aligned}$$

~~R<sub>A</sub>~~ ~~R<sub>B</sub>~~

Kalau kita mindahin kentang yang bobot kecil di truk B ke truk A maka rata rata A akan berkurang dan rata B bertambah

Bagaimana caranya kita bikin rata rata A bertambah dan rata - rata B berkurang? sehingga tercapai rata rata A > rata rata B

-> Pindahkan kentang dengan bobot bobot yang besar ke truk A

$$A = \lfloor N_{\text{kentang}} \rfloor$$

$$B = \lfloor M_{\text{kentang}} \rfloor$$

$$A = \lfloor N+1 \rfloor$$

$$B = \lfloor M-1 \rfloor$$

$B \lceil 1_{\text{kentang}} \rceil \rightarrow$  udah pindahin

$B \lceil M_{\text{kentang}} \rceil \rightarrow B \lceil 1_{\text{kentang}} \rceil$

$$N+1 - (M-1) = 1$$

Pindahin tuuk A

$$A = \lfloor N+M+1 \rfloor$$

B.sort( )

B = [ 7 7 6 5 5 5 4 3 3 3 ]

for ( i=0 ; i < B.length ; i++ ) {  
 B[i] }

}