## CMP N 426 (Computer Security) Problem Set 4 Chapter 4: Number Theory

- **4.6**) For each of the following find x
  - a)  $5 x = 4 \pmod{3}$
  - b)  $7x = 6 \pmod{5}$
- 4.7) Solve the following
  - a) 5 mod 3
  - b) 5 mod -3
  - c) -5 mod 3
- 4.19) Find multiplicative inverse of
  - a) 1234 mod 4321
  - b) 24140 mod 40902
- 4.24) Determine which of the following are reducible over GF(2):
  - a)  $x^3+1$
  - b)  $x^3 + x^2 + 1$
  - c)  $x^4+1$
- 4.25) Determine the gcd of the following pairs of polynomials:
  - a)  $x^3 + x + 1$  and  $x^2 + x + 1$  over GF(2).
  - b)  $x^3 x + 1$  and  $x^2 + 1$  over GF(3).
  - c)  $x^5 + x^4 + x^3 x^3 x + 1$  and  $x^3 + x^2 + x + 1$  over GF(3).
- 4.26) Find the multiplicative inverse of  $(x7 + x + 1) \mod (x8 + x4 + x3 + x + 1)$  over GF(2)
- 4.27) Find the multiplicative inverse of (x3 + x + 1) in  $GF(2^4)$  with m(x) = x4 + x + 1.