

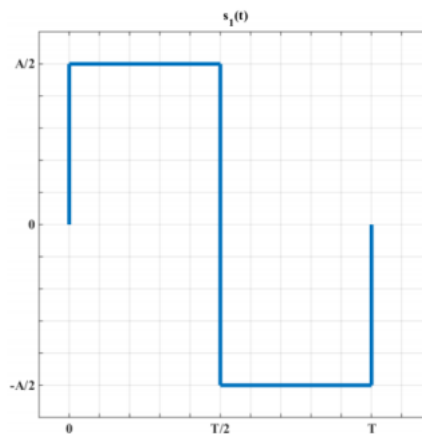
Sheet 1

Matched Filters

Problem 1

Consider the signal $s_1(t)$ as shown in Fig

- 1) Determine the impulse response of the matched filter (write an expression)
- 2) Draw the matched filter as function of time
- 3) Plot the matched filter output as function of time
- 4) Determine the peak value of the output



Problem 2

Consider the signals $s(t)$ defined as

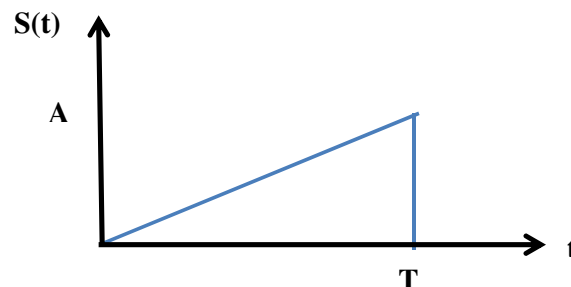
$$s(t) = \frac{A}{T} \cos(2\pi f_0 t), \quad 0 \leq t \leq T$$

- 1) Determine the impulse response of the Matched Filter for this signal.
- 2) Draw the Matched Filter as function of time.
- 3) Determine the output of the Matched Filter at $t = T$.
- 4) Suppose the signal $s(t)$ passes through a correlator that correlates $s(t)$ with $s(t)$. Determine the correlator's output at $t=T$, and compare it with the result of part (3).

Problem 3

Consider the signal $s(t)$

- 1) Determine the impulse response of the matched filter (write an expression)
- 2) Draw the matched filter as function of time
- 3) Determine the time at which the output of the matched filter is maximized
- 4) Determine the peak value of the matched filter's output.



Problem 4

Consider the signals $s(t)$ defined as

$$s(t) = A, \quad 0 \leq t \leq T$$

It is required to approximate the Matched Filter of $s(t)$ by an ideal Low Pass Filter of bandwidth B , such that the peak pulse SNR is maximized.

- 1) Determine the optimum value of B such that the LPF provides the best approximation to the Matched Filter.
- 2) Describe the relative performance of the LPF compared to the Matched Filter.

Hint: You may use the approximation $\text{sinc}(x) \approx \cos\left(\frac{\pi}{2}x\right)$.

Problem 5

In this problem we explore another method for the approximate realization of a matched filter, this time using the simple resistance-capacitance (RC) low-pass filter shown in Figure P4.4. The frequency response of this filter is

$$H(f) = \frac{1}{1 + jf/f_0}$$

where $f_0 = 1/2\pi RC$. The input signal $g(t)$ is a rectangular pulse of amplitude A and duration T . The requirement is to optimize the selection of the 3-dB cutoff frequency f_0 of the filter so that the peak pulse signal-to-noise ratio at the filter output is maximized. With this objective in mind, show that the optimum value of f_0 is $0.2/T$, for which the loss in signal-to-noise ratio compared to the matched filter is about 1 dB.

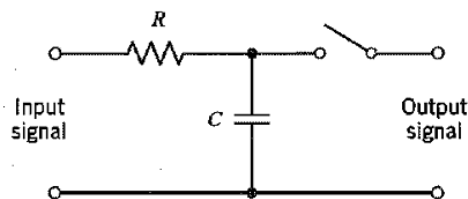


FIGURE P4.4