

Sheet 1 Laplace Transform

1. Solve the following homogeneous differential equation using:

$$\ddot{y}(t) + 3\dot{y}(t) + 2y(t) = 0$$

- a) Laplace transform
- b) Conventional Techniques



2. Solve the following differential equations:

a) $\ddot{y}(t) + 3\dot{y}(t) + 2y(t) = u(t) = \text{unit step}$, assume the initial conditions:

$$y(0) = -1, \dot{y}(0) = 2$$

b) $\ddot{y}(t) + 3\dot{y}(t) + 2y(t) = \dot{x}(t) + 3x(t)$, assume the initial conditions:

$$y(0) = 1, \dot{y}(0) = 0 \text{ and the input is given by: } x(t) = e^{-4t}.$$

3. Test the linearity of the systems described by the following i/p – o/p relations:

a) $y(t) = au(t)$, where 'a' is a constant.

b) $y(t) = u^3(t)$

c) $y(t) = e^{u(t)}$

e) $\ddot{y}(t) + a\dot{y}(t) + y(t) = u(t)$, $y(0) = \dot{y}(0) = 0$

4. Find the Transfer Function of the following systems: initial conditions = 0

a) $\ddot{y}(t) + 3\dot{y}(t) + 2y(t) = \dot{x}(t) + 3x(t)$

b) $\dot{y}(t) + y(t) = x(t - T)$