

## Sheet 1

1-Determine the power value for each of the following signals:

(a)  $10 \cos \left( 100t + \frac{\pi}{3} \right)$

(b)  $10 \cos \left( 100t + \frac{\pi}{3} \right) + 16 \sin \left( 150t + \frac{\pi}{5} \right)$

(c)  $(10 + 2 \sin 3t) \cos 10t$

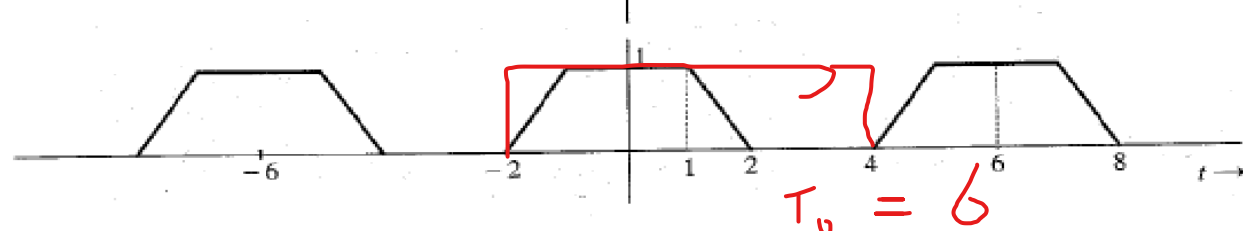
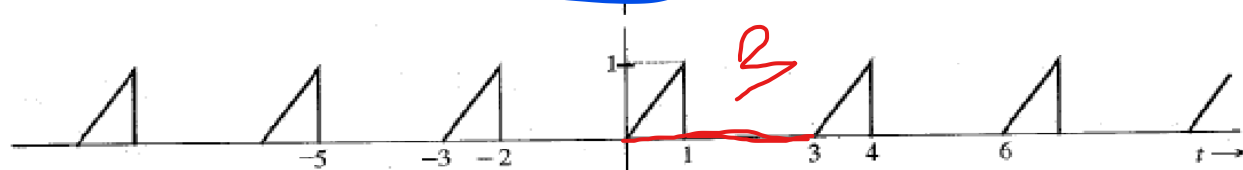
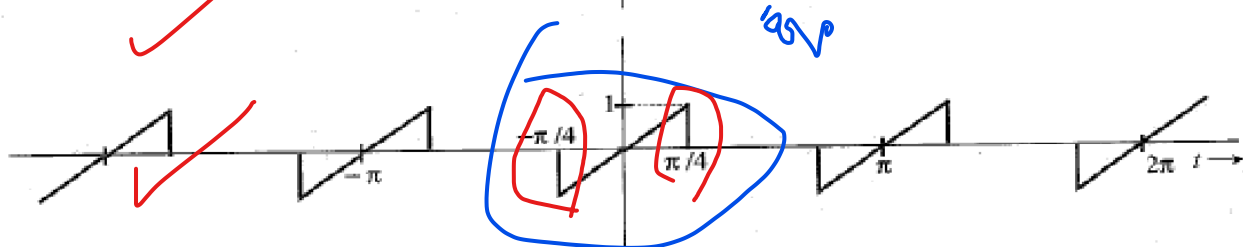
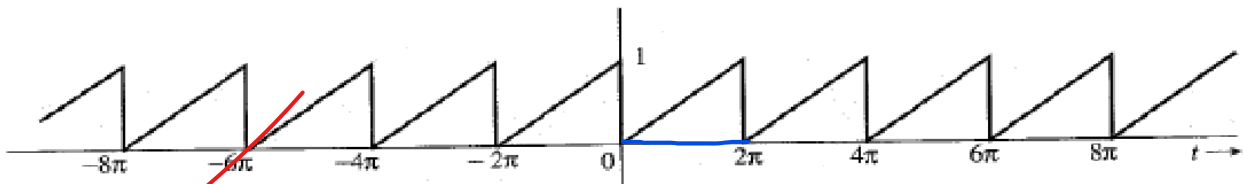
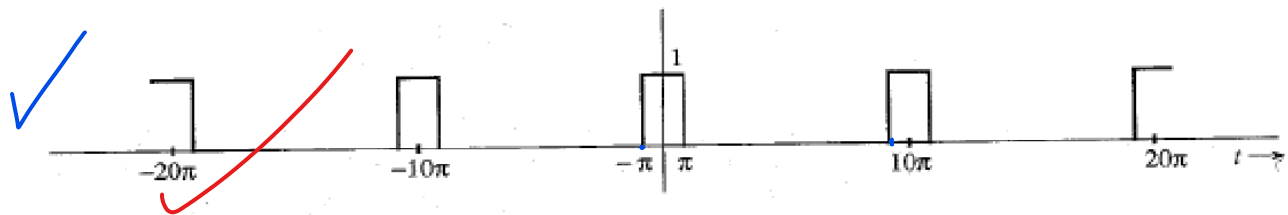
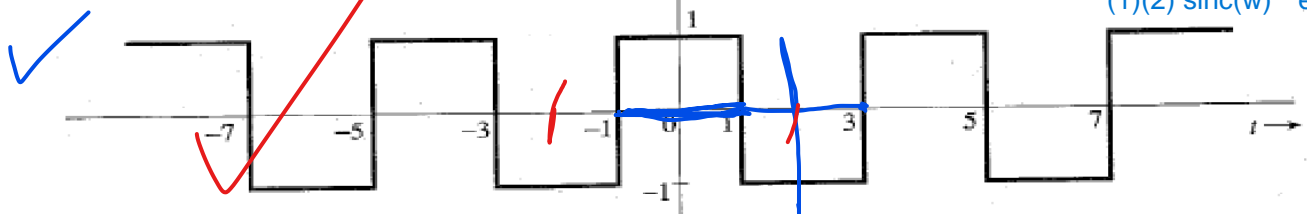
(d)  $10 \cos 5t \cos 10t$

(e)  $10 \sin 5t \cos 10t$

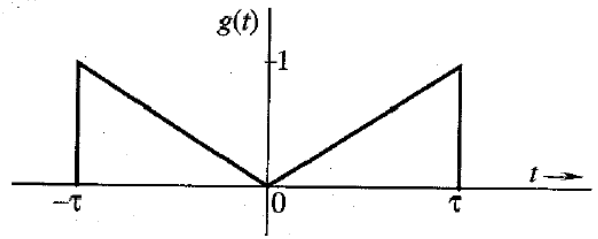
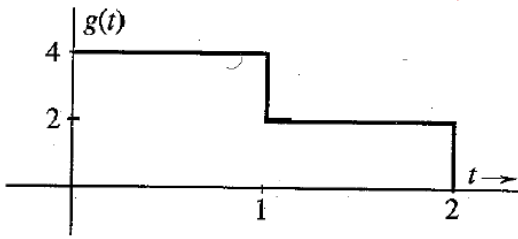
(f)  $e^{j\omega t} \cos \omega_0 t$

2-For each of the shown periodic signals, find exponential Fourier series and sketch the corresponding spectra.

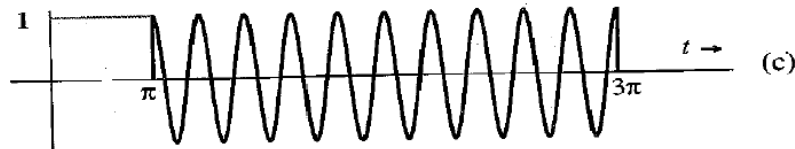
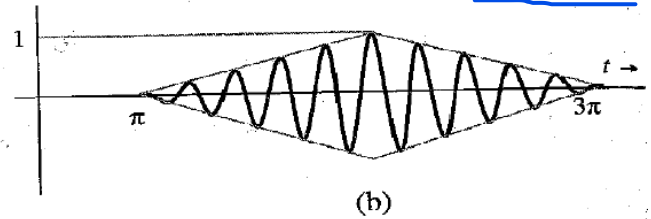
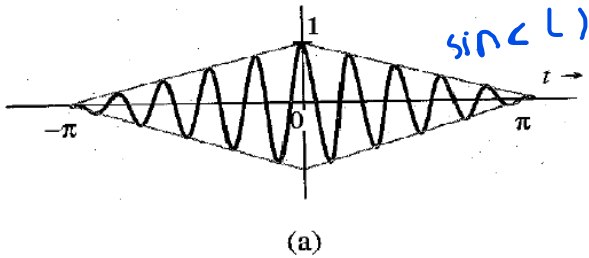
(1)  $\text{rect}(t/2) - (1)\text{rect}(t/2 - 2)$   $\checkmark = (1)(2) \text{sinc}(w) - (1)(2) \text{sinc}(w) * e^{-(jwot)}$



3- Find the Fourier transform of the signals shown:



4- Find Fourier transform of the shown signals using the appropriate properties of the Fourier transform. Sketch the amplitude and phase Spectra. *Hint: These functions can be expressed in the form  $g(t)\cos(\omega_0 t)$*



5-Signals  $g_1(t)=10^4 \text{rect}(10^4 t)$  and  $g_2(t)=\delta(t)$  are applied at the inputs of the ideal low-pass filter  $H_1(\omega)=\text{rect}(\omega/40000\pi)$  and  $H_2(\omega)=\text{rect}(\omega/20000\pi)$  as shown. The output  $y_1(t)$  and  $y_2(t)$  of these filters are multiplied to obtain the signal  $y(t)=y_1(t)y_2(t)$

- Sketch  $G_1(\omega)$  and  $G_2(\omega)$ .
- Sketch  $H_1(\omega)$  and  $H_2(\omega)$ .
- Sketch  $Y_1(\omega)$  and  $Y_2(\omega)$ .
- Find the bandwidths of  $y_1(t)$ ,  $y_2(t)$  and  $y(t)$ .

