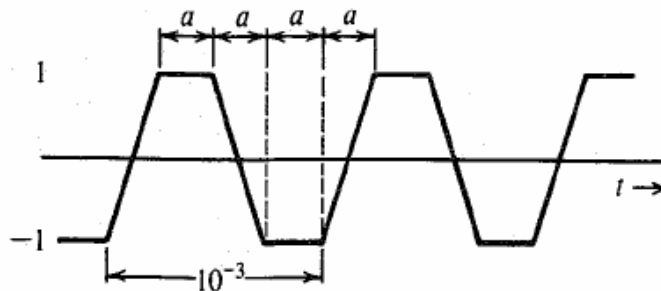


Sheet 3

9. Determine the instantaneous frequency, in hertz, of each of the following waveforms
- $10 \cos (100 \pi t + \pi/3)$
 - $10 \cos (200 \pi t + \sin \pi t)$
 - $2 \exp [j200\pi t (1 + \sqrt{t})]$
 - $\cos (200 \pi t) \cos (5 \sin (2\pi t)) + \sin (200 \pi t) \sin (5 \sin (2\pi t))$
2. Sketch $\phi_{FM}(t)$ and $\phi_{PM}(t)$ for the modulating signal $m(t)$ shown in the figure, given $\omega_c=10^8$, $k_f=10^5$, and $k_p=25$.



3. Over an interval $|t| \leq 1$, an angle modulated signal is given by

$$\phi_{EM} = 10 \cos 13000t$$

It is known that the carrier frequency $\omega_c=10000$

- If this was a PM signal with $k_p=1000$, determine $m(t)$ over the interval $|t| \leq 1$.
- If this was a FM signal with $k_f=1000$, determine $m(t)$ over the interval $|t| \leq 1$.

4. An angle modulated signal with carrier frequency $\omega_c=2\pi \times 10^6$ is described by the equation

$$\phi_{EM} = 10 \cos(\omega_c t + 0.1 \sin 2000\pi t)$$

- Find the power of the modulated signal.
 - Find the frequency deviation Δf .
 - Find the phase deviation $\Delta \phi$.
 - Estimate the bandwidth of $\phi_{EM}(t)$.
5. Given $m(t)=\sin 2000\pi t$, $k_f=200000\pi$, and $k_p=10$.
- Estimate the bandwidths of $\phi_{FM}(t)$ and $\phi_{PM}(t)$.
 - Repeat part (a) if the message amplitude is doubled.
 - Repeat part (a) if the message amplitude is doubled.
 - Comment on the sensitivity of FM and PM bandwidths to the spectrum of $m(t)$.
6. A certain sinusoid at a frequency f_m is used as the modulating signal in both an AM (DSB-LC) and a FM system. When modulated, the peak frequency deviation of the FM system is set to three times the bandwidth of the AM system. The magnitudes of those sidebands spaced $\pm f_m$ Hz from the carrier in both systems are equal and the total average powers are equal in both systems. Determine:
- The modulation index of the FM system.
 - The modulation index of the AM system.

7. The bandwidths of three angle modulated transmitting systems are compared, using the sinusoidal test signal $f(t) = a \cos(2\pi f_m t)$. The resulting approximate bandwidths are tabulated in Table (1) below:

System	$a = 1 \text{ V}$ $f_m = 1 \text{ KHz}$	$a = 2 \text{ V}$ $f_m = 1 \text{ KHz}$	$a = 1 \text{ V}$ $f_m = 2 \text{ KHz}$
A	2 KHz	2 KHz	4 KHz
B	40 KHz	80 KHz	80 KHz
C	50 KHz	100 KHz	50 KHz

Table (1) Test Results of Bandwidth.

Identify the type of angle modulation used (FM or PM / Narrowband or Wideband) for each of these three systems.

8. The sinusoidal signal $f(t) = a \cos(2\pi f_m t)$ is applied to the input of a FM system. The corresponding modulated signal output (in volt) for $a = 1 \text{ V}$, $f_m = 1 \text{ KHz}$, is: $\Phi(t) = 100 \cos[2\pi \cdot 10^7 t + 4 \sin(2000\pi t)]$ across a 50-ohm resistive load.
- What is the peak frequency deviation from carrier?
 - What is the total average power developed by $\Phi(t)$?
 - What percentage of the average power is at 10.000 MHz?
 - What is the approximate bandwidth using Carson's rule?
 - Repeat parts (a) to (d) for the input parameters $a = 75 \text{ V}$, $f_m = 2 \text{ KHz}$; assume all other factors remain unchanged.
9. Design (only the block diagram) an Armstrong indirect FM modulator to generate an FM carrier with a carrier frequency of 98.1 MHz and $\Delta f = 75 \text{ kHz}$. A narrow band FM generator is available at a carrier frequency of 100 kHz and a frequency deviation $\Delta f = 10 \text{ Hz}$. The stock room also has an oscillator with an adjustable frequency in the range of 10 to 100 MHz. There are also plenty of frequency doublers, triplers and quintuplers.
10. A periodic square wave $m(t)$ shown in figure (a) frequency modulates a carrier of frequency $f_c = 10 \text{ kHz}$ with $\Delta f = 1 \text{ kHz}$. The carrier amplitude is A . The resulting FM signal is demodulated, as shown in figure (b). Sketch the waveforms at points b, c, d, and e.

