# Pattern Classification 07. Classifiers Combination

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#### **Classifiers Combination**

Classifier 1 Classifier 2 Classifier 3

P<sub>correct</sub> 93% 92% 90%

- Robust approach
- Best classifier for the training set might not be the best for the test set
- It is risky to choose the best in training

#### **Classifiers Combination**

 Diversity is a favorable feature we would like to have in the classifiers we choose to combine

- Ways to combine:
  - Majority vote
  - Average the class posterior probabilities, i.e.,  $P(C_i|\underline{X})$
  - Average some sort of score function
  - Can also choose median instead of average

#### **AdaBoost Classifier**

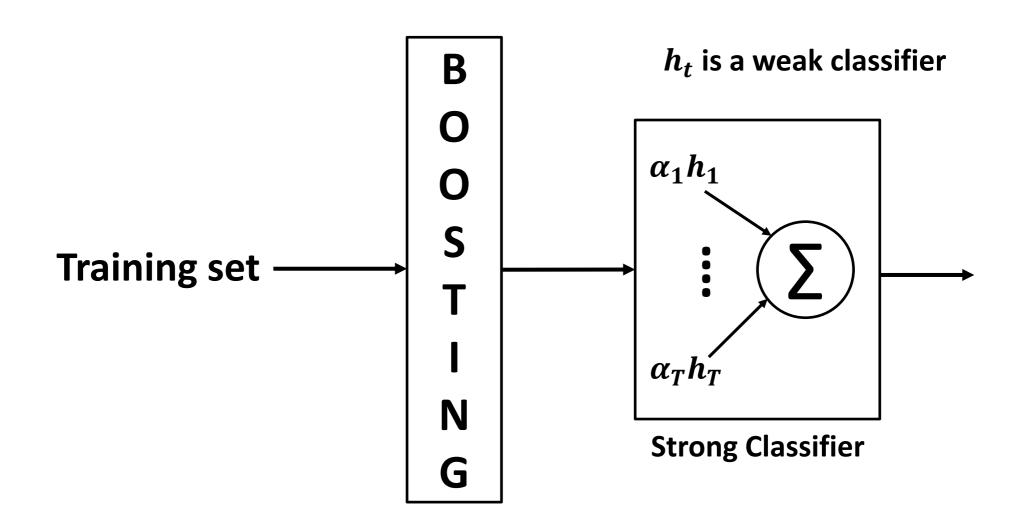
The AdaBoost algorithm is an iterative procedure

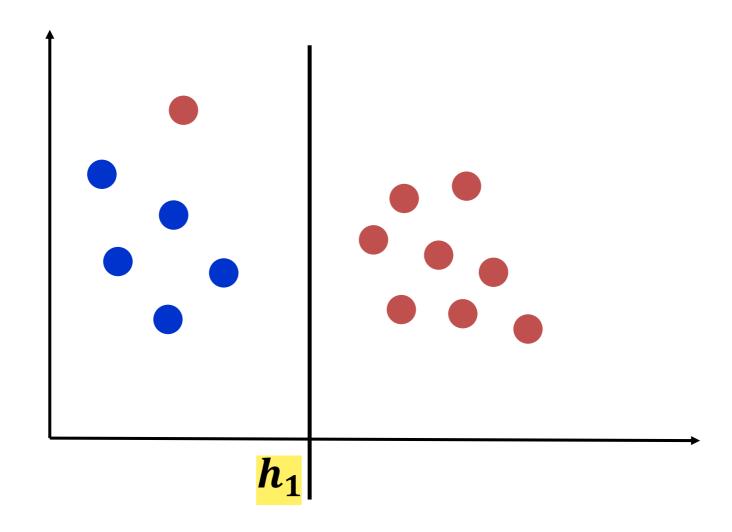
AdaBoost tries to approximate the Bayes classifier by combining many weak classifiers

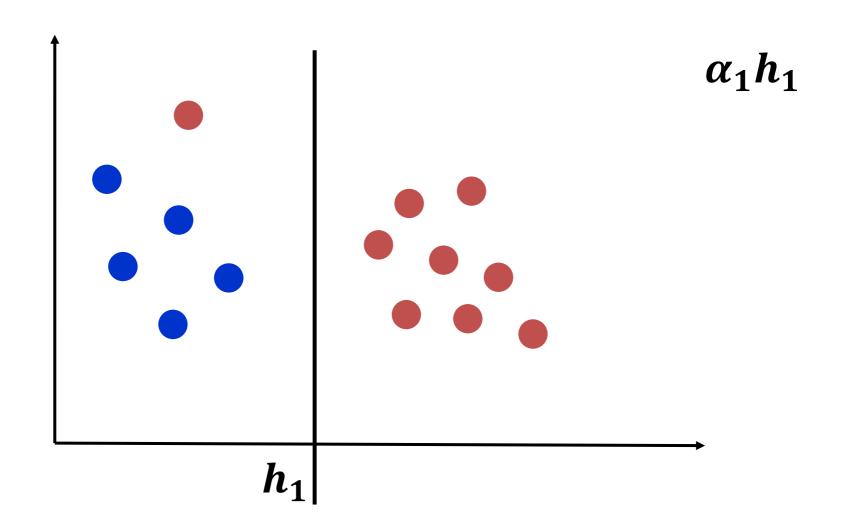
 AdaBoost selects the best weak classifiers to create a strong classifier

#### **AdaBoost Classifier**

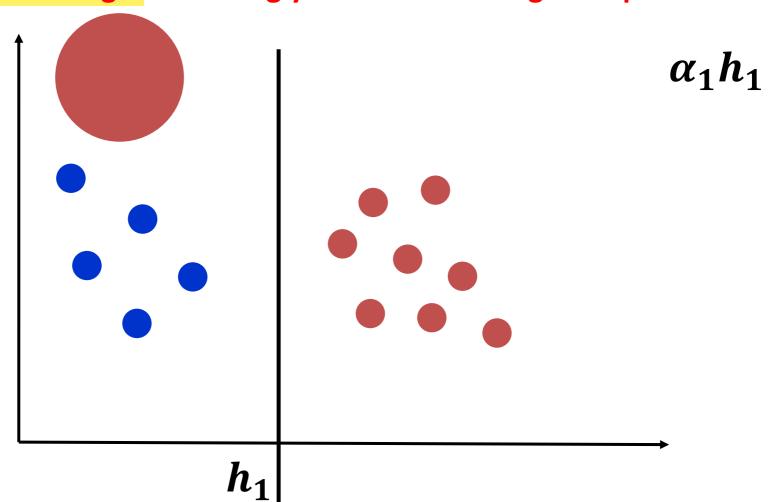
- A weak classifier is able to guess the right class with a percentage slightly bigger than random guessing
  - E.g., random guessing acc. is 50% in case of binary classification
  - So, a weak binary classifier's acc. is 51%  $\rightarrow$  close to random
- A strong classifier is usually correct > 80%

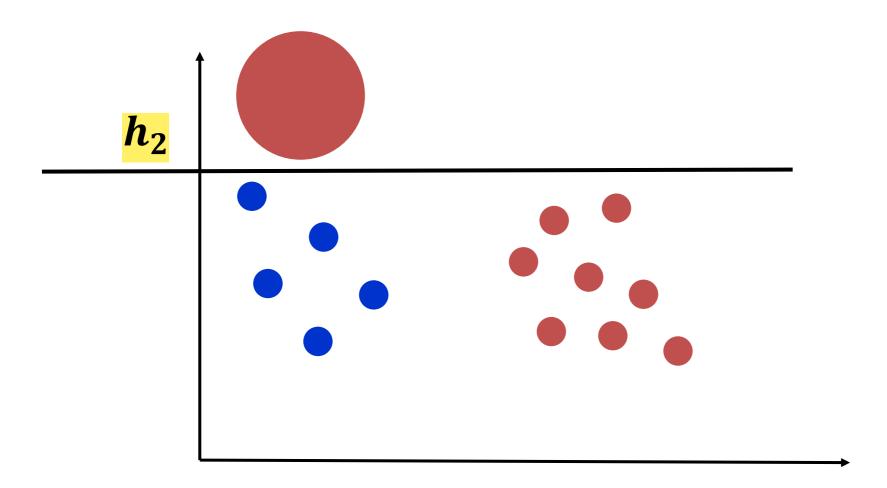


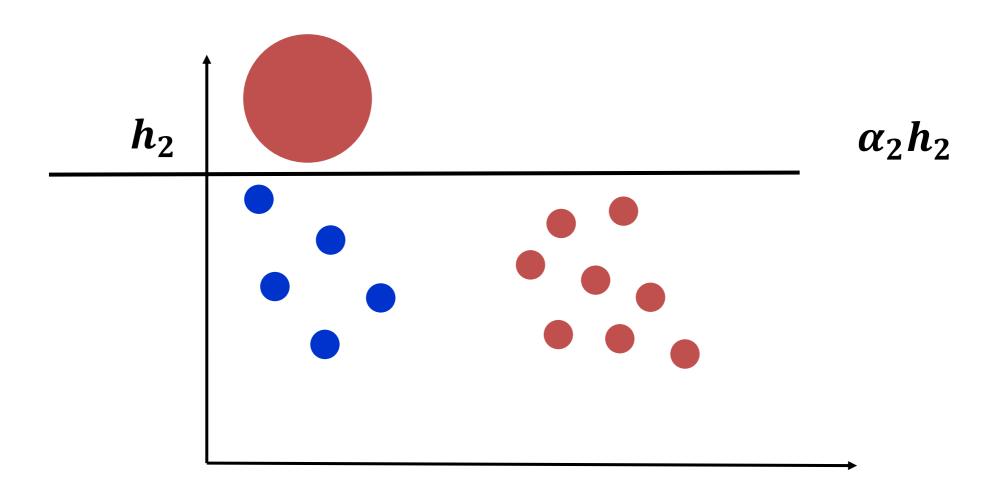


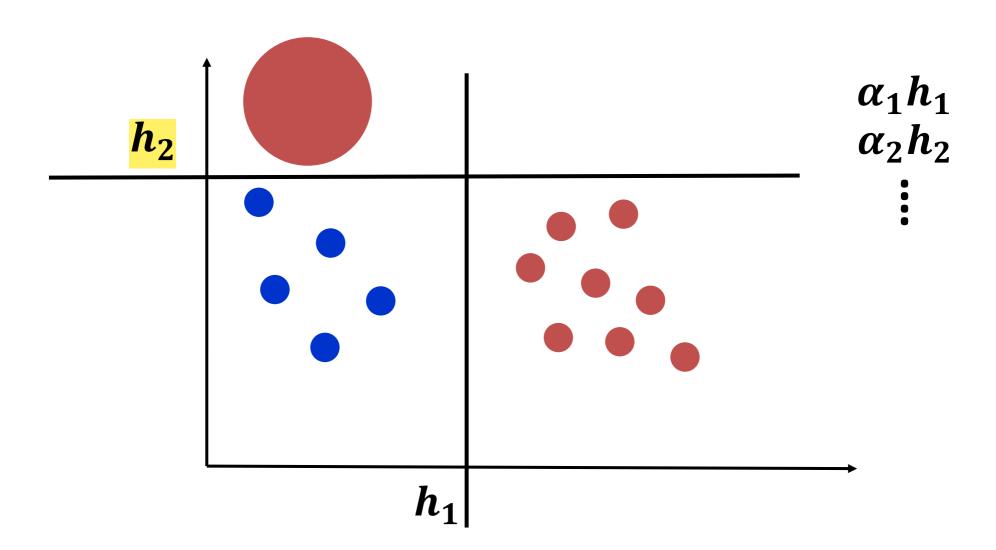


**More weight** for wrongly classified training examples









## **AdaBoost Algorithm**

$$\mathbb{I}(y) = \begin{cases} 1 & y = True \\ 0 & y = False \end{cases}$$

 ${f 1.}$  Initialize weights of the training examples:

$$w_m = \frac{1}{M}$$
 ,  $m = 1, 2, ..., M$ 

- 2. For t=1 to T:
  - a) Select a classifier  $h_t$  that best fits to the training data using weights  $w_m$  of the training examples
  - b) Compute error of  $h_t$  as:  $err_t = \frac{\sum_{m=1}^{M} w_m \mathbb{I}(c_m \neq h_t(x_m))}{\sum_{m=1}^{M} w_m}$
  - C) Compute weight of classifier:  $\alpha_t = \log\left(\frac{1 err_t}{err_t}\right)$
  - d) Update weights of wrongly classified examples:

$$w_m \leftarrow w_m \frac{e^{\alpha_t \mathbb{I}(c_m \neq h_t(x_m))}}{e^{\alpha_t \mathbb{I}(c_m \neq h_t(x_m))}}$$
 for  $m = 1 \dots M$ 

- e) Renormalize weights  $w_m$
- 3. Output:  $C(x) = \underset{k}{\operatorname{argmax}} \sum_{t=1}^{T} \alpha_t \mathbb{I}(h_t(x) = k)$

#### **AdaBoost Classifier**

- AdaBoost works well only in case of binary classification
- However, it is not the case for multi-class classification
- AdaBoost assumes that the error of each weak classifier is less than 0.5
  - $-\alpha_t$  is negative if error is greater than 0.5
  - The error of random guessing in case of two classes is 0.5
  - In case of K multi-classes the random guessing error rate is  $\frac{K-1}{K}$

#### **Multi-Class AdaBoost**

 Same as AdaBoost algorithm except for step (2.c):

$$\alpha_t = log\left(\frac{1 - err_t}{err_t}\right) + log(K - 1)$$

•  $\alpha_t$  is positive if only:

$$(1 - err_t) > \frac{1}{K}$$

## **Overfitting**

 AdaBoost is <u>robust</u> to <u>overfitting</u> given that select the best **weak classifiers**

 However, relying on complex classifiers will be more prone to overfitting

## Acknowledgment

 These slides have been created relying on lecture notes of Amir Atiya and Sven Behnke

• J. Zhu, H. Zou, S. Rosset, T. Hastie, "Multiclass AdaBoost", 2009