

## Revision:

### 1. Laplace table revision:

Time domain	Freq dom
$u(t)$	$1/s$
$t^n$	$n! / s^{n+1}$
$e^{-t} f(t)$	$F(s + \alpha)$
$\cos(\alpha t)$	$\frac{s}{s^2 + \alpha^2}$
$\sin(\alpha t)$	$\frac{\alpha}{s^2 + \alpha^2}$
$f(t \pm t_0)$	$e^{\pm st_0} F(s)$
$f'(t)$	$sF(s) - f(0)$
$f''(t)$	$s^2 F(s) - f(0)s - f'(0)$
$\int f(t) dt$	$F(s)/s$
$t f(t)$	$\frac{dF(s)}{ds}$

### Simple Cases:

1- 2<sup>nd</sup> order:  
check all coefficients are  $> 0$

### 2- 3<sup>rd</sup> order:

$$a_3 s^3 + a_2 s^2 + a_1 s + a_0$$

$$a_1 > 0 \quad \forall i \in \{1, 2, 3\}$$

$$a_2 a_1 > a_0 a_3$$

## 2. Routh stability rev

الزوال إلى بيجهل راحة  
لأن system ويقول من stable  
و لا

### خطوات الحل:

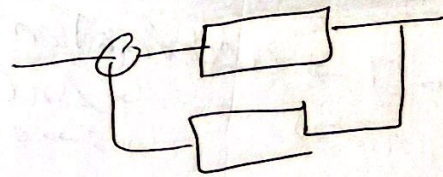
1- بنجيب ال Transfer function

2- نأخذ ال denominator  $C(s)$

characteristic equation

3- نأوليه بـ

4- نأخذ الجدول مثال  
نأكد إن هيفيش أي -ve  
موجود في أول column.



### Special cases:

1- Case zero exist

اعتبارنا انت بخط  $\infty$   
مكان الارق وتجب  $\lim_{s \rightarrow \infty}$   
وغالبا هتلا في ال system  
بقى unstable لو مش كذا  
بقى critically stable

### 2. Row of zeros:

نأخذ ال Row ال فوقه و  
نعمل ال Differential



### 3. Steady state:

$$E(s) = \frac{R(s)}{1 + G(s)}$$

$$e_{ss} = \lim_{s \rightarrow 0} (s E(s))$$

$$G(s) = \frac{P(s)}{s^n Q(s)}$$

### Static error coefficients:

1.  $K_P \rightarrow \square \rightarrow \text{Position} \rightarrow \lim_{s \rightarrow 0} (G(s))$   
(@  $n=1$ )

2.  $K_V \rightarrow \square \rightarrow \text{Velocity} \rightarrow \lim_{s \rightarrow 0} (s G(s))$   
(@  $n=2$ )

3.  $K_A \rightarrow \square \rightarrow \text{Acceleration} \rightarrow \lim_{s \rightarrow 0} (s^2 G(s))$   
(@  $n=3$ )

### Evaluation table:

Type	Step	ramp	Parabola
zero	Const	$\infty$	$\infty$
1	0	Const	$\infty$
2	0	0	Const

For  $H(s) \neq 1$ :

$$TF = \frac{G(s)}{1 + H(s)G(s) - G(s)}$$

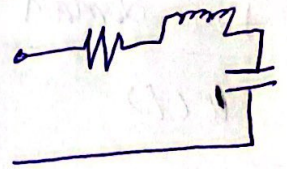
### 4. Mathematical Modeling:

#### 1- Electric systems:

$$R \rightarrow R \dots$$

$$L \rightarrow sL$$

$$C \rightarrow \frac{1}{sC}$$



#### 2. Mechanical systems:

1.  $F = ma$  & 2- For every action there is a reaction which is equal in magnitude & opposite in direction  $F \rightarrow F$

3- Spring  $K \rightarrow \text{spring constant}$

$$F = X_t K = X(s) K$$

$\hookrightarrow \text{Displacement}$

#### 4. Piston



$$P = B \dot{X}(t) = s B X(s)$$

#### 5. Fluids:

$$Q_0 = H/R$$



$$Q_{in} - Q_{out} = A \frac{dh}{dt}$$