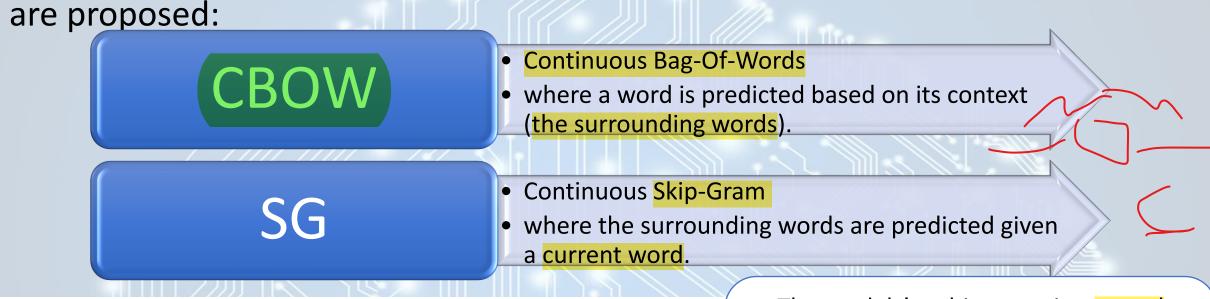


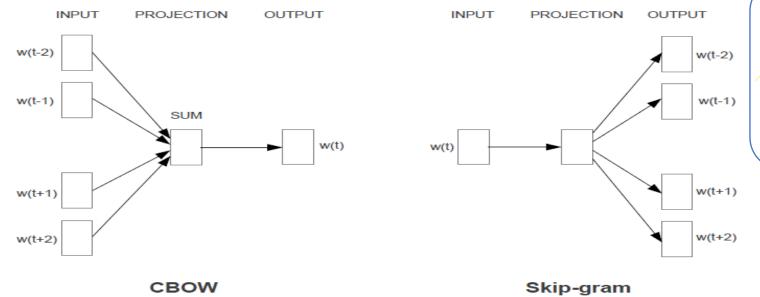
## **Word Embeddings**

- Previously, we saw how to represent a word as a sparse, long vector with dimensions corresponding to words in the vocabulary or documents in a collection.
- We now introduce a more powerful word representation: embeddings, short dense vectors.
  - With number of dimensions *d* ranging from 50-1000.
  - The vectors are dense: instead of vector entries being sparse, mostly-zero counts or functions of counts, the values will be real-valued numbers that can be negative.
- It turns out that dense vectors work better in every NLP task than sparse vectors.
- One method for computing embeddings is Word2vec where embeddings are static: meaning that the method learns one fixed embedding for each word in the vocabulary.
- Other methods such as BERT, are for learning dynamic contextual embeddings in which the vector for each word is different in different contexts.

## Word2vec

• Word2vec is developed by *Tomas Mikolov et al. at Google* where two models are proposed:





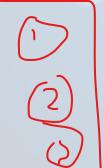
The models' architecture is a neural network with three layers: an input layer, a hidden layer and an output layer.

The models are trained using huge text corpora

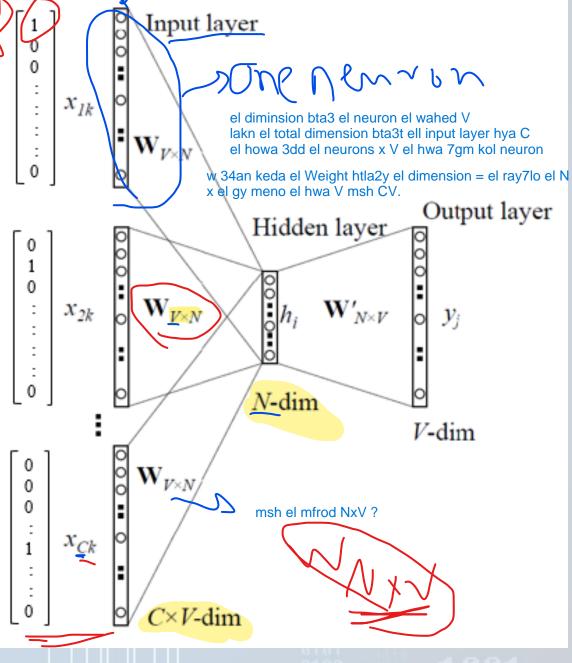
Though, we won't use the neural network after training!!!

### **Input Layer:**

- Its size is CV
  - C=number of context words
  - V=number of words in the vocabulary
- The inputs are C context vectors:
  - Each context vector is one-hot
     encoded vector of size V (it is a vector
     having 1 in the position encoding the word,
     and 0 otherwise).

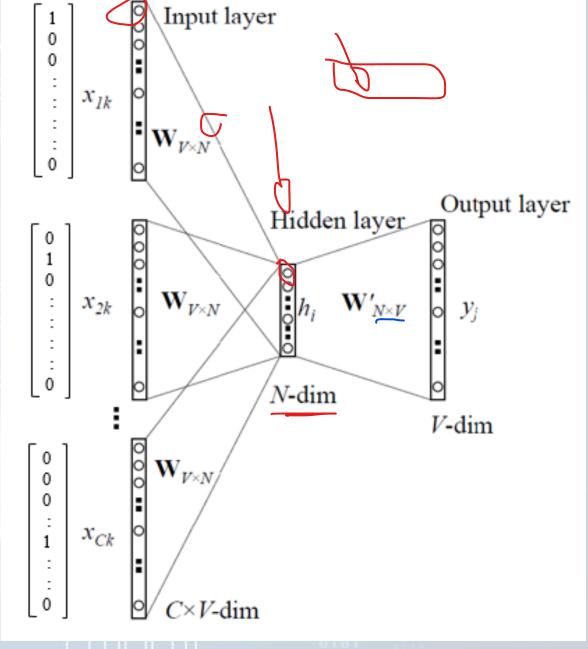


 $V = \{ahmed, salah, mohammed\}$  |V| = 3  $ahmed = \{1, 0, 0\}$   $salah = \{0, 1, 0\}$   $mohmaeed = \{0.0, 1\}$ 



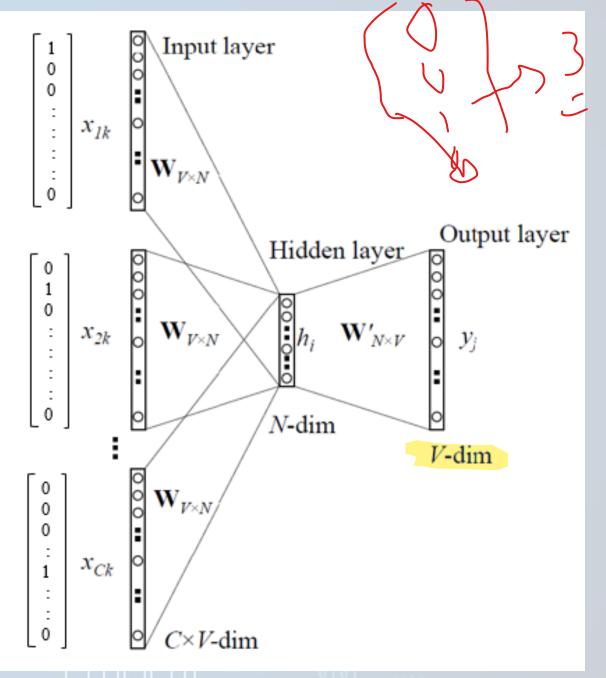
#### **Hidden Layer:**

- Its size is N
  - N=number of neurons in the hidden layer
     =the dimension of embeddings
     (it is a hyper parameter)
- Fully-connected (dense) layer whose weights are the word embeddings.



### **Output layer:**

- Its size is **V** 
  - Where the gold output is the one-hot vector encoding the "middle/target word".
- It is a softmax layer which is designed so that the sum of the probabilities obtained in the output layer equals 1.
  - The network is going to tell us the probability for every word in our vocabulary of being the "target word" for the given input(s) "context word(s)"

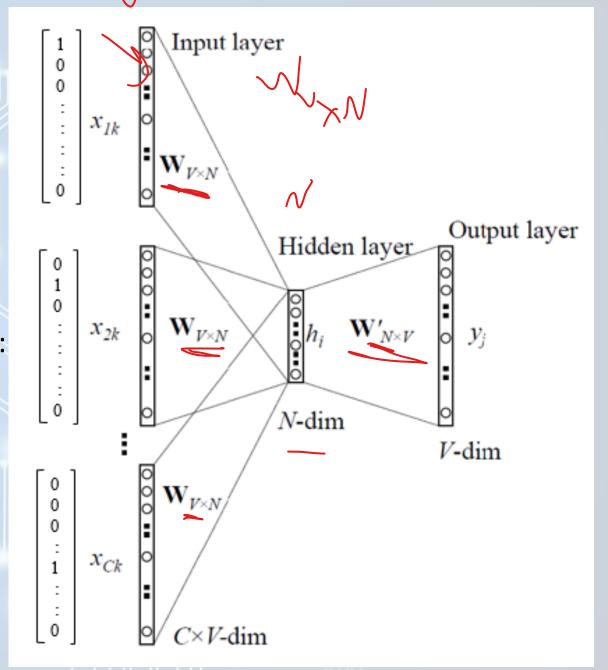


#### Weights:

- There are two sets of weights:
  - one is between the input and the hidden layer:

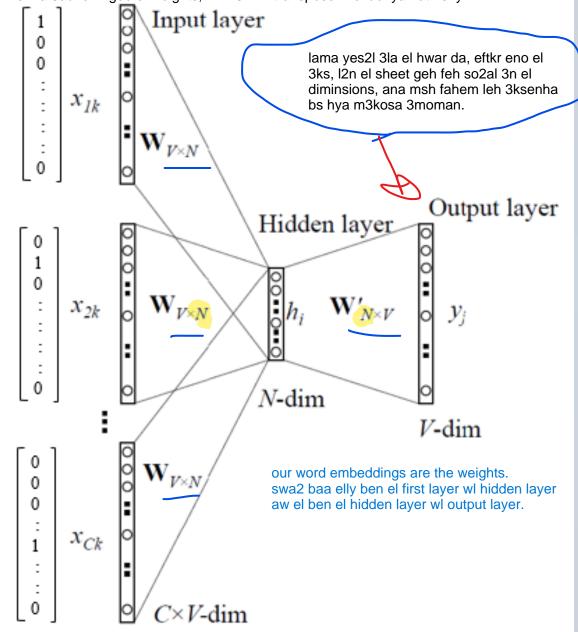
Input-Hidden layer matrix
consisting of CW[V × N] matrices

second is between hidden and output layer:
 Hidden-Output layer matrix size = [N × V]



- There is a no activation function between any layers (linear activation):
  - Linear network except for the softmax at the output layer.
- The input-to-hidden-layer weight matrix is multiplied with the input vector to produce the hidden layer output.
- The hidden input gets multiplied by hidden-output weights to produce the output then pass it to softmax.
- Error between output and target is calculated and back propagated to re-adjust the weights.
- The weights between the input layer and the hidden layer are taken as the word vectors after training.

h3na homa m3kosen, w la adry lmaza ya haza, wlaken lama kont bdwr 3la el youtube l2et enha zy ma ehna kona mt3wden, fa azon enha msh htfr2 tlama 3aksna kol haga, l2n fl akher ehna 3auzen ngeb el weights, w hn3mml transpose w el donya hatmshy



- Let the available corpus be this one sentence "word vectors are widely used".
- The unique words in the vocabulary are 5 words (V = 5) as follows:

["word", "vectors", "are", "widely", "used"].

Training data for C=1 (context words)

training sample	context word	target word
1	word	vectors
2	vectors	are
3	are	widely
4	widely	used

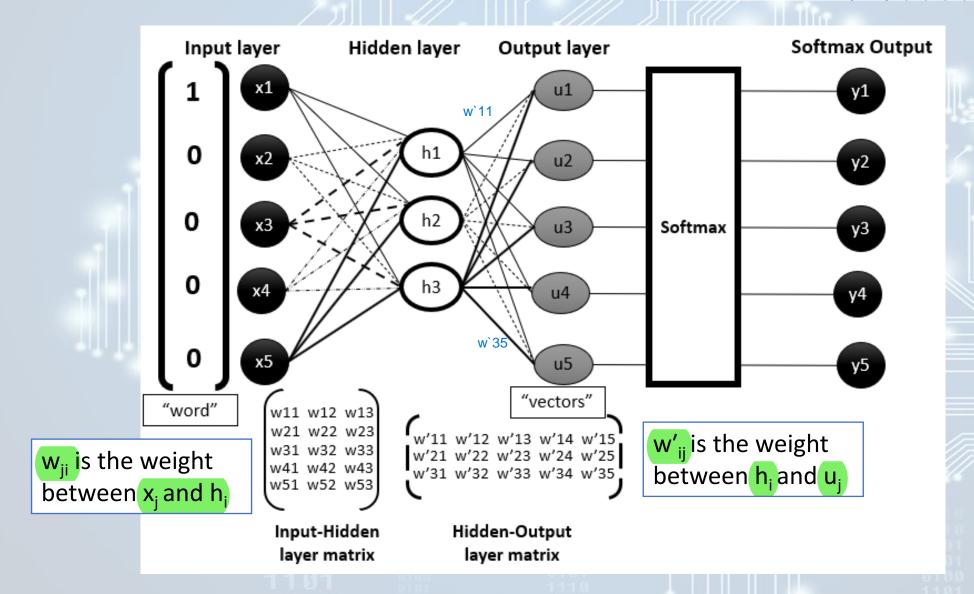
Encoded training data:

training sample	context word	target word
1	[1,0,0,0,0]	[0,1,0,0,0]
2	[0,1,0,0,0]	[0,0,1,0,0]
3	[0,0,1,0,0]	[0,0,0,1,0]
4	[0,0,0,1,0]	[0,0,0,0,1]

commonly used 300 & 100

• Let N = 3, consider the first training sample:

training sample	context word	target word
1	[1,0,0,0,0]	[0,1,0,0,0]



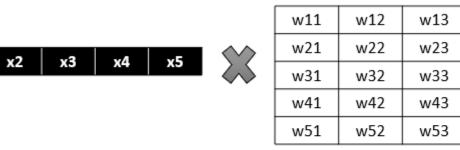
#### • Equations:

$$h_i = \sum_i w_{ji} * x_j \text{ where } i = 1, 2, 3 \text{ and } j = 1, 2, 3, 4, 5$$
 (1)

$$u_j = \sum_i w'_{ij} * h_i \text{ where } i = 1, 2, 3 \text{ and } j = 1, 2, 3, 4, 5$$
 (2)

$$y_j = Softmax(u_j) \text{ where } j = 1, 2, 3, 4, 5$$
 (3)

#### Matrix Forms:



****	***25	1.4						
w32	w33	h1	h2	h3		The outpu	it of the hidde	en laver
w42	w43					•	"word vector"	•
w52	w53				• ]		nput word.	101 1110
						<u>'</u>	npat wora.	

 $\begin{bmatrix} 0 & 0 & 0 & 1 & 0 \end{bmatrix} \times \begin{bmatrix} 17 & 24 & 1 \\ 23 & 5 & 7 \\ 4 & 6 & 13 \\ 10 & 12 & 19 \\ 11 & 18 & 25 \end{bmatrix} = \begin{bmatrix} 10 & 12 & 19 \end{bmatrix}$ 

h1	h2	h3	$\langle \rangle$	w′11	w′12	w'13	w′14	w′15					
112	112	113		w'21	w'22	w'23	w'24	w'25	u1	u2	u3	u4	u5
				w'31	w'32	w'33	w'34	w'35					

- The error calculations are performed given the target vector: [0,1,0,0,0] through back propagation where the weight values (w and w') are updated.
- The training continues for many iterations until the weights are adjusted for all the training samples.
- Finally, the vectors of the words in the vocabulary are weights in the Input-Hidden layer matrix such that each row in the matrix is the word vector representation of the equivalent word.

The word in the vocabulary	The equivalent word vector
word	[w11 w12 w13]
vectors	[w21 w22 w23]
are	[w31 w32 w33]
widely	[w41 w42 w43]
used	[w51 w52 w53]

- For C>1 (context words), the only difference will be in handling the C input vectors.
  - Each vector will be multiplied with the input-hidden layer matrix W[V ×N] returning C [1 × N] vectors.
  - Finally, to obtain a single vector → all C [1 × N] vectors will be averaged element-wise.
- This computation is equivalent to initially computing a **mean vector** for the C input one-hot encoded vectors then proceeding as in the case of C = 1.
- For C=2 → window size=1

training sample context word target word

1 (word,are) vectors
2 (vectors,widely) are
3 (are,used) widely
4 widely used

Word Vectors are widely used C = 2

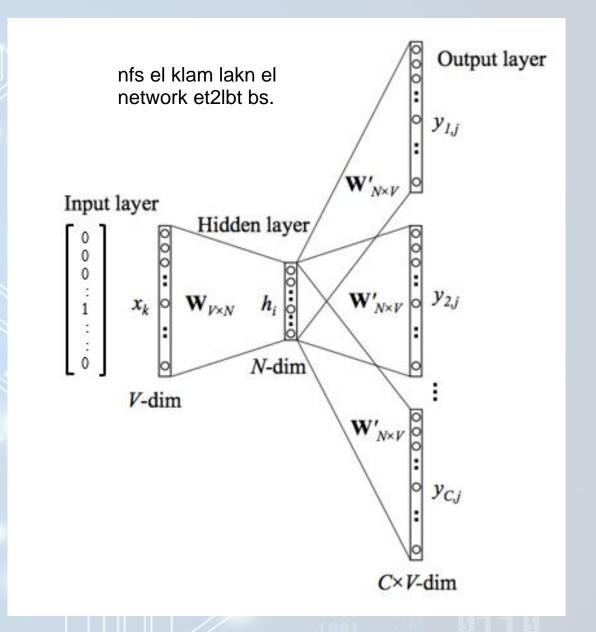
Word + are => Vectors

training sample	context words	mean context word	target word
1	([1,0,0,0,0],[0,0,1,0,0])	$[0.5,0,0.5,0,0]$ $\bigcirc$	[0,1,0,0,0]
2	([0,1,0,0,0],[0,0,0,1,0])	[0, 0.5, 0, 0.5, 0]	[0,0,1,0,0]
3	([0,0,1,0,0],[0,0,0,0,1])	[0,0,0.5,0,0.5]	[0,0,0,1,0]
4	[0,0,0,1,0]	[0,0,0,1,0]	[0,0,0,0,1]



#### **Input Layer:**

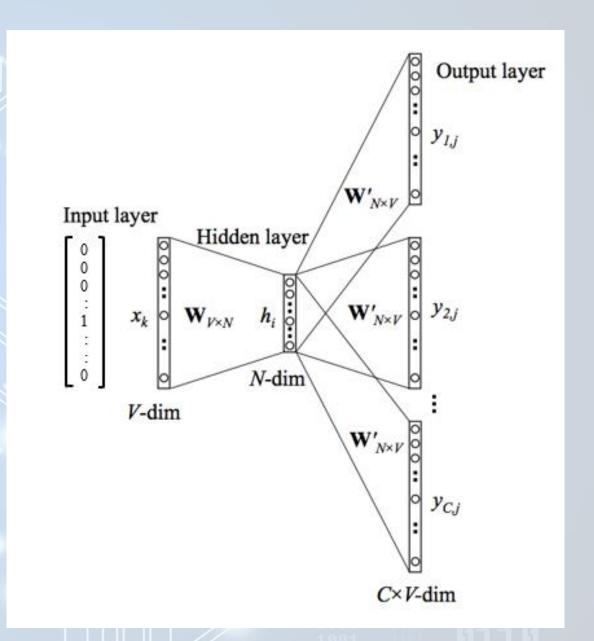
- Its size is V
  - V=number of words in the vocabulary
- The input is 1 middle/target vector:
  - the target vector is a one-hot encoded vector (a vector having 1 in the position encoding the word, and 0 otherwise).





#### **Hidden Layer:**

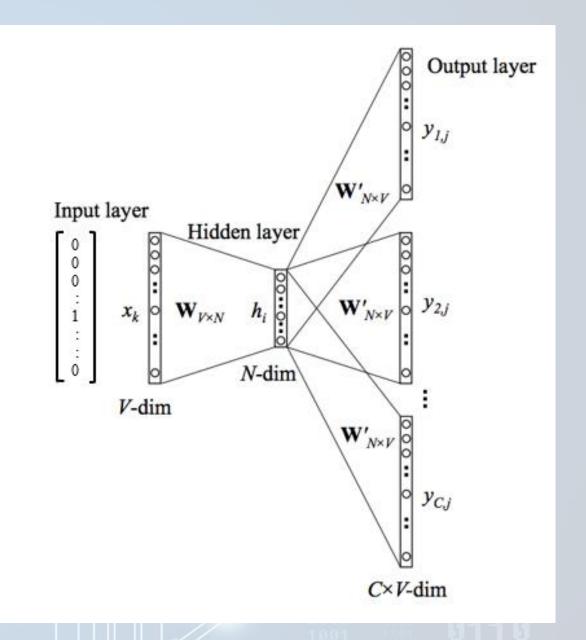
- Its size is N
  - N=number of neurons in the hidden layer
     =the dimension of embeddings
     (it is a hyper parameter)
- Fully-connected (dense) layer whose weights are the word embeddings.





#### **Output Layer:**

- Its size is CV
  - C=number of context words
  - V=number of words in the vocabulary
  - Where the gold outputs are C one-hot vectors each encoding one of the "context words".
- It is a softmax layer which is designed so that the sum of the probabilities obtained in the output layer equals 1.
  - The network is going to tell us the probability for every word in our vocabulary of being the "context word" for the given input "target word"
- C separate errors are calculated and are added element-wise to obtain a final error vector which is back propagated to update the weights.



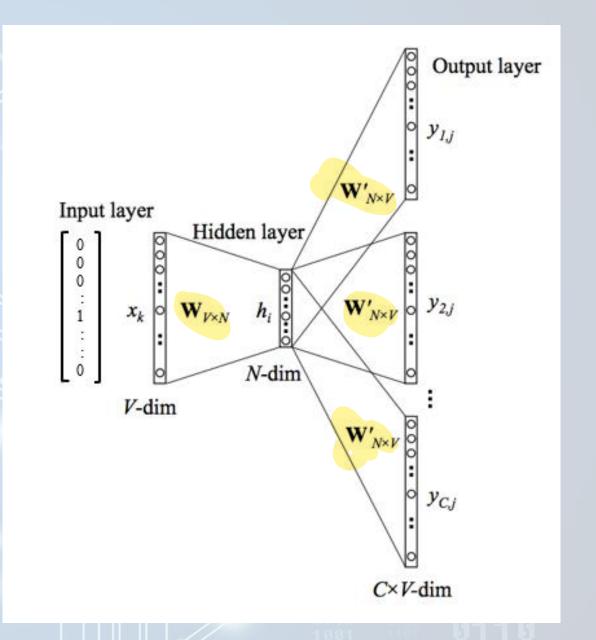
#### **Weights:**

- There are two sets of weights:
  - one is between the input and the hidden layer:

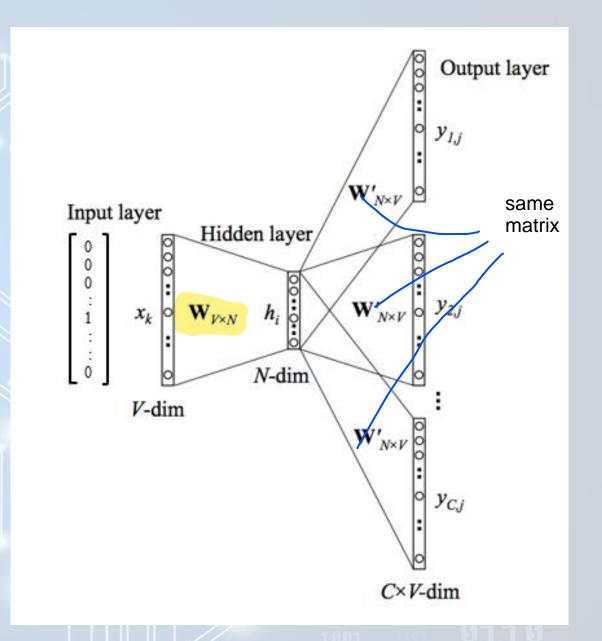
Input-Hidden layer matrix size  $= [V \times N]$ 

second is between hidden and output layer:
 Hidden-Output layer matrix

consisting of C W'[N ×V] matrices



- There is a no activation function between any layers (linear activation):
  - Linear network except for the softmax at the output layer.
- The weights between the input layer and the hidden layer are taken as the word vectors after training.



- Let the available corpus be this one sentence "word vectors are widely used".
- The unique words in the vocabulary are 5 words (V = 5) as follows:

["word", "vectors", "are", "widely", "used"].

Training data for C=2 (context words) > window size=1

training sample	context words	target word
1	(word, are)	vectors
2	(vectors, widely)	are
3	(are,used)	widely
4	(widely)	used

hena el 7aga mt3akstsh bs lazm teb2a fahem en el target 3ndna hena howa el input, lakn el context word howa el output.

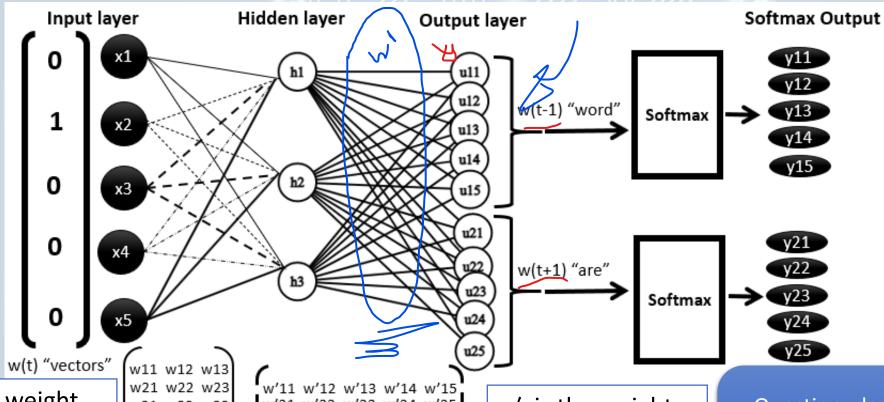
Encoded training data:

	1 U	
training sample	context words	target word
1	([1,0,0,0,0],[0,0,1,0,0])	[0,1,0,0,0]
2	([0,1,0,0,0],[0,0,0,1,0])	[0,0,1,0,0]
3	([0,0,1,0,0],[0,0,0,0,1])	[0,0,0,1,0]
4	([0,0,0,1,0])	[0,0,0,0,1]

we need to predict these.

Let N = 3, consider the first training sample:

training sample	context words	target word
1	([1,0,0,0,0],[0,0,1,0,0])	[0,1,0,0,0]



kol el outputs henaa hayb2o nfs el outputs, 34an enta el hidden layers sabta, w el matrix elly btdrb feha wa7da, fa el output aked msh hy5tlf, lakn el error hwa elly hyt8yr.

w<sub>ji</sub> is the weight between x<sub>j</sub> and h<sub>i</sub>

w21 w22 w23 w31 w32 w33 w41 w42 w43 w51 w52 w53

w33 w43 w'31 w'32 w'33 w'34 w'35 w53

w'<sub>ij</sub> is the weight between h<sub>i</sub> and u<sub>ci</sub> Question: do values u11->u15 differ from values u21 → u25 (and consequently the y) i.e. do we have one output vector or C vectors???

Input-Hidden Hidden-Output layer matrix layer matrix

Only **one** since **W'** matrix is the same

• The training process is similar to CBOW except that the error calculation differs as there are C gold outputs. Therefore, the final error is computed as the summation of the error for each context word as follows:

$$E = \sum_{c=1}^{C} E_c$$

• Finally, the vectors of the words in the vocabulary are weights in the Input-Hidden layer matrix such that each row in the matrix is the word vector representation of the equivalent word.

100000000000000000000000000000000000000	
The word in the vocabulary	The equivalent word vector
word	[w11 w12 w13]
vectors	$[w21 \ w22 \ w23]$
are	[w31 w32 w33]
widely	[w41 w42 w43]
used	[w51 w52 w53]

## **SG** Calculations

- For input x with xk=1 and xk'=0 for all  $k'\neq k$ , the outputs of the hidden layer will be row k in  $\underline{W}$ :  $\mathbf{h} = \mathbf{x}^T \mathbf{W} = \mathbf{W}_{(k,.)} := \mathbf{v}_{w_I}$
- The input to the jth node of the cth output word is:  $u_{c,j} = \mathbf{v'}_{w_j}^T \mathbf{h}$  jth column in W' matrix
- Since the output layers for each output word share the same weights so  $u_{c,j} = u_j$
- Computing the jth node of the cth output word via softmax function:

$$p(w_{c,j} = w_{O,c}|w_I) = y_{c,j} = \frac{\sum_{exp(u_{c,j})} exp(u_{c,j})}{\sum_{j'=1}^{V} exp(u_{j'})}$$
 This is the probability that the output of the jth output is equal to the actual value of the jth index of the cth output vector (one-hot encoded)

• This way the forward pass is done so next the weights W and W' need to be learned with backpropagation and stochastic gradient descent.

## **SG Calculations**

• First, a loss function is defined as:  $E = -\log p(w_{O,1}, w_{O,2}, \dots, w_{O,C}|w_I)$ 

 $egin{align} E = -\log p(w_{O,1}, w_{O,2}, \dots, w_{O,C}|w_I) \ = -\log \prod^C exp(u_{c,j_c^*}) \ \hline \end{array}$ 

The probability of the output words (context words) given the input (target/middle) word

Negative log likelihood

→ objective is to minimize it

Take the derivative w.r.t. uc,j:

 $-\sum_{c=1}^{C} log = -\log\prod_{c=1}^{C} \frac{exp(u_{c,j_c^*})}{\sum_{j'=1}^{V} exp(u_j')}$ 

jc\* is the index of the cth output

de htl3 -1, 3nd el j el s7, gher keda 0

 $rac{\partial E}{\partial u_{c,j}} = y_{c,j} - t_{c,j}$ 

tc,j=1 if the jth node of the cth true output word is equal to 1 and 0 other wise.

How is this computed??

Compute the derivative w.r.t. W':

$$rac{\partial E}{\partial w_{ij}'} = \sum_{c=1}^C rac{\partial E}{\partial u_{c,j}} \cdot rac{\partial u_{c,j}}{\partial w_{ij}'} \quad \text{Using the chain rule}$$
 $= \sum_{c=1}^C (y_{c,j} - t_{c,j}) \cdot h_i$ 

The gradient descent update equation for W':

$$w_{ij}^{\prime (new)} = w_{ij}^{\prime (old)} - \eta \cdot \sum_{c=1}^{C} (y_{c,j} - t_{c,j}) \cdot h_i$$

## **SG Calculations**

Computing for W, begin with taking the derivative of the error w.r.t. hi:

$$rac{\partial E}{\partial h_i} = \sum_{j=1}^V rac{\partial E}{\partial u_j} \cdot rac{\partial u_j}{\partial h_i}$$
 Using the chain rule  $=\sum_{j=1}^V \sum_{c=1}^C (y_{c,j} - t_{c,j}) \cdot w_{ij}'$ 

• Compute the derivative w.r.t. W: 
$$\frac{\partial E}{\partial w_{ki}} = \frac{\partial E}{\partial h_i} \cdot \frac{\partial h_i}{\partial w_{ki}} \longrightarrow \text{Using the chain rule}$$
$$= \sum_{j=1}^V \sum_{c=1}^C (y_{c,j} - t_{c,j}) \cdot w'_{ij} \cdot x_k$$

The gradient descent update equation for W:

$$w_{\;\mathsf{ji}}^{(new)} = w_{\;\mathsf{ji}}^{(old)} - \eta \cdot \sum_{i=1}^{V} \sum_{c=1}^{C} (y_{c,j} - t_{c,j}) \cdot w_{ij}' \cdot x_{j}$$

 $[V*N]=[V*N]-[V*1]([N*V][V*1])^T$ 

$$W_{input}^{(new)} = W_{input}^{(old)} - \eta \cdot x \cdot \left(W_{output} \sum_{c=1}^{C} e_c 
ight)^{\!\mathsf{T}}$$

Matrix forms:

$$extstyle extstyle ext$$

Each gradient descent update requires a summation over the entire vocabulary  $\rightarrow$ Computationally expensive. So techniques such as hierarchical softmax and negative sampling are used to make this computation more efficient.

# Other Kinds of Static Embeddings



## **FastText**

- An extension of word2vec developed by Piotr Bojanowski et al. at Facebook.
- Addresses a problem with word2vec "unknown words"—words that appear in a test corpus but were unseen in the training corpus.
- A related problem is word sparsity, such as in languages with rich morphology, where some
  of the many forms for each noun and verb may only occur rarely.
- FastText deals with these problems by using subword models, representing each word as itself plus a bag of constituent n-grams, with special boundary symbols < and > added to each word.
- For example, with n = 3 the word where would be represented by the sequence <where>
  plus the character n-grams: <wh, whe, her, ere, re>
  - Note that the sequence <her>, corresponding to the word her is different from the tri-gram her from the word where.
- Now, the vocabulary is the union of the subwords of all words (subwords refer to the words themselves + n-grams). Then a skip-gram/cbow embedding is learned for each subword.
- The vector of a word is the sum of the whole word vector in addition to the sum of its subwords' vectors.
- Unknown words can then be presented only by the sum of the constituent n-grams.

## GloVe

• Short for Global Vectors, because the model is based on capturing global corpus statistics developed by Jeffrey Pennington et al. at Stanford University.

- Unlike word2vec that captures local statistics of a corpus, GloVe captures both local and global statistics of a corpus.
  - In word2vec, the vector learnt for a certain word is only affected by the surrounding context words.
  - In GloVe, the global statistics of the corpus are considered as it operates on cooccurrence matrices that are built across the entire corpus.
- GloVe is based on ratios of probabilities from the word-word co-occurrence matrix.

GloVe is a global log-bilinear regression model.

## Sphere

- The approaches such as word2vec, fastText and GloVe are distributional approaches:
  - Antonyms (good, bad) can lie in close proximity (cosine similarity close to 1)
    - → as antonyms can often occur in similar contexts.
  - Synonyms (happiness, joy) lie in close proximity (cosine similarity close to 1).
  - Unrelated words (car, apple) lie far away (cosine similarity close to 0).
  - Other antonyms can lie far away (cosine similarity close to 0).

There is **no clear distinction** between the different semantic relations among words such as synonyms, antonyms and unrelated words.

## Sphere

• Sphere approach developed by Sandra Rizkallah et al. at Cairo University solves this problem by embedding the vectors of opposite or antonyms words at opposite poles of the sphere (cosine similarity close to -1).

• Sphere is a semi-supervised relaxation algorithm that optimizes a devised error

function. At closer distance **Happiness** "joy" and "happiness" lie at a Good close distance → Synonyms "good" and "bad" lie at two opposite poles of the sphere  $\rightarrow$ Radius=1 unit **Antonyms** At two opposite sphere poles Question "ask" and "question" lie at a close distance → Synonyms At close distance

## **Evaluating Vector Models**

- The most important evaluation metric for vector models is extrinsic evaluation on tasks.
- It is also useful to have intrinsic evaluations:
  - 1. Similarity: computing the correlation between an algorithm's word similarity scores and word similarity ratings assigned by humans.
  - 2. Semantic Textual Similarity: evaluates the performance of sentence-level similarity algorithms, consisting of a set of pairs of sentences, each pair with human-labeled similarity scores.
  - 3. Analogy: the system has to solve problems of the form "a is to b as c is to \_\_\_\_" e.g.: "Cairo is to Egypt as Rome is to \_\_\_\_" → "Italy". Need to find d such that the associated word vectors va, vb, vc, vd are related to each other in the following relationship: "vb − va = vd − vc" where the vd is obtained to be the vector with highest cosine similarity to the vector (vb-va+vc).

