

Sheet01: CHAPTER 13: DISK STORAGE, BASIC FILE STRUCTURES, AND HASHING

13.23 Consider a disk with the following: block size $B=512$ bytes, interblock gap size $G=128$ bytes, number of blocks per track=20, number of tracks per surface=400. A disk pack consists of 15 double-sided disks.

(a) What is the total capacity of a track and what is its useful capacity?

Total track size = $20 * (512+128) = 12800$ bytes = 12.8 Kbytes
Useful capacity of a track = $20 * 512 = 10240$ bytes = 10.24 Kbytes

(b) How many cylinders are there?

Number of cylinders = number of tracks = 400

(c) What is the total capacity and the useful capacity of a cylinder?

Total cylinder capacity = $15 * 2 * 20 * (512+128) = 384000$ bytes = 384 Kbytes
Useful cylinder capacity = $15 * 2 * 20 * 512 = 307200$ bytes = 307.2 Kbytes

(d) What is the total capacity and the useful capacity of a disk pack?

Total capacity of a disk pack = $15 * 2 * 400 * 20 * (512+128) = 153600000$ bytes = 153.6 Mbytes
Useful capacity of a disk pack = $15 * 2 * 400 * 20 * 512 = 122.88$ Mbytes

(e) Suppose the disk drive rotates the disk pack at a speed of 2400 rpm (revolutions per minute); what is the transfer rate in bytes/msec and the block transfer time btt in msec? What is the average rotational delay rd in msec? What is the bulk transfer rate?

Transfer rate $tr = (\text{total track size in bytes}) / (\text{time for one disk revolution in msec})$

$tr = (12800) / ((60 * 1000) / (2400)) = (12800) / (25) = 512$ bytes/msec

block transfer time $btt = B / tr = 512 / 512 = 1$ msec

average rotational delay $rd = (\text{time for one disk revolution in msec}) / 2 = 25 / 2 = 12.5$ msec

bulk transfer rate $btr = tr * (B / (B+G)) = 512 * (512 / 640) = 409.6$ bytes/msec

(f) Suppose the average seek time is 30 msec. How much time does it take (on the average) in msec to locate and transfer a single block given its block address?

average time to locate and transfer a block = $s + rd + btt = 30 + 12.5 + 1 = 43.5$ msec

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(g) Calculate the average time it would take to transfer 20 random blocks and compare it with the time it would take to transfer 20 consecutive blocks using double buffering to save seek time and rotational delay.

$$\text{time to transfer 20 random blocks} = 20 * (s + rd + btt) = 20 * 43.5 = 870 \text{ msec}$$

$$\begin{aligned} \text{time to transfer 20 consecutive blocks using double buffering} &= s + rd + 20 * btt \\ &= 30 + 12.5 + (20 * 1) = 62.5 \text{ msec} \end{aligned}$$

13.24 A file has $r=20000$ STUDENT records of fixed-length. Each record has the following fields: NAME (30 bytes), SSN (9 bytes), ADDRESS (40 bytes), PHONE (9 bytes), BIRTHDATE (8 bytes), SEX (1 byte), MAJORDEPTCODE (4 bytes), MINORDEPTCODE (4 bytes), CLASSCODE (4 bytes, integer), and DEGREEPROGRAM (3 bytes). An additional byte is used as a deletion marker. The file is stored on the disk whose parameters are given in previous exercise.

(a) Calculate the record size R in bytes.

$$R = (30 + 9 + 40 + 9 + 8 + 1 + 4 + 4 + 4 + 3) + 1 = 113 \text{ bytes}$$

(b) Calculate the blocking factor bfr and the number of file blocks b assuming an unspanned organization.

$$bfr = \text{floor}(B / R) = \text{floor}(512 / 113) = 4 \text{ records per block}$$

$$b = \text{ceiling}(r / bfr) = \text{ceiling}(20000 / 4) = 5000 \text{ blocks}$$

(c) Calculate the average time it takes to find a record by doing a linear search on the file if (i) the file blocks are stored contiguously and double buffering is used, and (ii) the file blocks are not stored contiguously.

For linear search we search on average half the file blocks = $5000/2 = 2500$ blocks.

i. If the blocks are stored consecutively, and double buffering is used, the time to read 2500 consecutive blocks
 $= s + rd + (2500 * btt) = 30 + 12.5 + 2500 * 1 = 2542.5 \text{ msec}$

ii. If the blocks are scattered over the disk, a seek is needed for each block, so the time is: $2500 * (s + rd + btt) = 2500 * (30 + 12.5 + 1) = 108750 \text{ msec} = 108.75 \text{ sec}$

(d) Assume the file is ordered by SSN; calculate the time it takes to search for a record given its SSN value by doing a binary search.

For binary search, the time to search for a record is estimated as:
 $\text{ceiling}(\log_2 b) * (s + rd + btt)$

$$= \text{ceiling}(\log_2 5000) * (30 + 12.5 + 1) = 13 * 43.5 = 565.5 \text{ msec} = 0.5655 \text{ sec}$$

13.25 Suppose only 80% of the STUDENT records from Exercise 13.24 have a value for PHONE, 85% for MAJORDEPTCODE, 15% for MINORDEPTCODE, and 90% for DEGREEPROGRAM, and we use a variable-length record file. Each record has a 1-byte field type for each field occurring in the record, plus the 1-byte deletion marker and a 1-byte end-of-record marker. Suppose we use a spanned record organization, where each block has a 5-byte pointer to the next block (this space is not used for record storage).

(a) Calculate the average record length R in bytes.

Assuming that every field has a 1-byte field type, and that the fields not mentioned above (NAME, SSN, ADDRESS, BIRTHDATE, SEX, CLASSCODE) have values in every record, we need the following number of bytes for these fields in each record, plus 1 byte for the deletion marker, and 1 byte for the end-of-record marker:

$$R_{\text{fixed}} = (30+1) + (9+1) + (40+1) + (8+1) + (1+1) + (4+1) + 1+1 = 100 \text{ bytes}$$

For the fields (PHONE, MAJORDEPTCODE, MINORDEPTCODE, DEGREEPROGRAM), the average number of bytes per record is:

$$R_{\text{variable}} = ((9+1)*0.8) + ((4+1)*0.85) + ((4+1)*0.15) + ((3+1)*0.9) \\ = 8 + 4.25 + 0.75 + 3.6 = 16.6 \text{ bytes}$$

$$\text{The average record size } R = R_{\text{fixed}} + R_{\text{variable}} = 100 + 16.6 = 116.6 \text{ bytes}$$

$$\text{The total bytes needed for the whole file} = r * R = 20000 * 116.6 = 2332000 \text{ bytes}$$

(b) Calculate the number of blocks needed for the file.

Using a spanned record organization with a 5-byte pointer at the end of each block, the bytes available in each block are $(B-5) = (512 - 5) = 507$ bytes.

The number of blocks needed for the file are:

$$b = \text{ceiling}((r * R) / (B - 5)) = \text{ceiling}(2332000 / 507) = 4600 \text{ blocks}$$

(compare this with the 5000 blocks needed for fixed-length, unspanned records in Problem 4.19(b))

13.26 Suppose that a disk unit has the following parameters: seek time $s=20$ msec; rotational delay $rd=10$ msec; block transfer time $btt=1$ msec; block size $B=2400$ bytes; interblock gap size $G=600$ bytes. An EMPLOYEE file has the following fields: SSN, 9 bytes; LASTNAME, 20 bytes; FIRSTNAME, 20 bytes; MIDDLE INIT, 1 byte; BIRTHDATE, 10 bytes; ADDRESS, 35 bytes; PHONE, 12 bytes; SUPERVISORSSN, 9 bytes; DEPARTMENT, 4 bytes; JOBCODE, 4 bytes; deletion marker, 1 byte. The EMPLOYEE file has $r=30000$ STUDENT records, fixed-length format, and unspanned blocking. Write down appropriate formulas and calculate the following values for the above EMPLOYEE file:

(a) The record size R (including the deletion marker), the blocking factor bfr, and the number of disk blocks b.

$$R = (9 + 20 + 20 + 1 + 10 + 35 + 12 + 9 + 4 + 4) + 1 = 125 \text{ bytes}$$

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$$\text{bfr} = \text{floor}(B / R) = \text{floor}(2400 / 125) = 19 \text{ records per block}$$

$$b = \text{ceiling}(r / \text{bfr}) = \text{ceiling}(30000 / 19) = 1579 \text{ blocks}$$

(b) Calculate the wasted space in each disk block because of the unspanned organization.

$$\text{Wasted space per block} = B - (R * \text{Bfr}) = 2400 - (125 * 19) = 25 \text{ bytes}$$

(c) Calculate the transfer rate t_r and the bulk transfer rate btr for this disk

$$\text{Transfer rate } t_r = B/bt = 2400 / 1 = 2400 \text{ bytes/msec}$$

$$\text{bulk transfer rate } btr = t_r * (B/(B+G))$$

$$= 2400 * (2400/(2400+600)) = 1920 \text{ bytes/msec}$$

(d) Calculate the average number of block accesses needed to search for an arbitrary record in the file, using linear search.

For linear search we have the following cases:

i. search on key field:

if record is found, half the file blocks are searched on average: $b/2 = 1579/2$ blocks

if record is not found, all file blocks are searched: $b = 1579$ blocks

ii. search on non-key field:

all file blocks must be searched: $b = 1579$ blocks

(e) Calculate the average time needed in msec to search for an arbitrary record in the file, using linear search, if the file blocks are stored on consecutive disk blocks and double buffering is used.

If the blocks are stored consecutively, and double buffering is used, the time to read n consecutive blocks = $s + rd + (n * btt)$

$$\text{i. if } n = b/2: \text{ time} = 20 + 10 + ((1579/2) * 1) = 819.5 \text{ msec}$$

$$\text{ii. if } n = b: \text{ time} = s + rd + (n * btt) = 20 + 10 + 1579 * 1 = 1609 \text{ msec}$$

(f) Calculate the average time needed in msec to search for an arbitrary record in the file, using linear search, if the file blocks are not stored on consecutive disk blocks.

If the blocks are scattered over the disk, a seek is needed for each block, so the time to search n blocks is: $n * (s + rd + btt)$

$$\text{i. if } n = b/2: \text{ time} = (1579/2) * (20 + 10 + 1) = 24474.5 \text{ msec} = 24.475 \text{ sec}$$

$$\text{ii. if } n = b: \text{ time} = 1579 * (20 + 10 + 1) = 48949 \text{ msec} = 48.949 \text{ sec}$$

(g) Assume that the records are ordered via some key field. Calculate the average number of block accesses and the average time needed to search for an arbitrary record in the file, using binary search.

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For binary search, the time to search for a record is estimated as:

$$\text{ceiling}(\log_2 b) * (s + rd + btt)$$

$$= \text{ceiling}(\log_2 1579) * (20 + 10 + 1) = 11 * 31 = 341 \text{ msec} = 0.341 \text{ sec}$$

13.27 A PARTS file with Part# as hash key includes records with the following Part# values: 2369, 3760, 4692, 4871, 5659, 1821, 1074, 7115, 1620, 2428, 3943, 4750, 6975, 4981, 9208. The file uses 8 buckets, numbered 0 to 7. Each bucket is one disk block and holds two records. Load these records into the file in the given order using the hash function $h(K) = K \bmod 8$. Calculate the average number of block accesses for a random retrieval on Part#.

Answer:

K h(K) (bucket number)	Bucket	records	overflow
2369 1	0	3760	2428
3760 0		9208	6975
4692 4	1	2369	
4871 7		9209	
5659 3	2	1074	
1821 5			
1074 2	3	5659	
7115 3		7115	
1620 4	4	4692	
2428 4 Overflow		1620	
3943 7	5	1821	
4750 6		4981	
6975 7 Overflow	6	4750	
4981 5			
9208 0	7	4871	
9209 1		3943	

Two records out of 15 are in overflow, which will require an additional block access. The other records require only one block access. Hence, the average time to retrieve a random record is:

$$(1 * (13/15)) + (2 * (2/15)) = 0.867 + 0.266 = 1.133 \text{ block accesses}$$

13.28 Load the records of Exercise 13.27 into expandable hash files based on extendible hashing. Show the structure of the directory at each step. Show the directory at each step, and the global and local depths. Use the has function $h(k) = K \bmod 32$.

Answer:

Hashing the records gives the following result:

	K	h(K) (bucket number)	binary h(K)
record1	2369	1	00001
record2	3760	16	10000
record3	4692	20	10100
record4	4871	7	00111
record5	5659	27	11011
record6	1821	29	11101
record7	1074	18	10010
record8	7115	11	01011
record9	1620	20	10100
record10	2428	28	11100
record11	3943	7	00111
record12	4750	14	01110
record13	6975	31	11111
record14	4981	21	10101
record15	9208	24	11000

Extendible hashing:





