Statistics in Data science

Data science involve the analysis and interpretation of complex datasets to extract valuable insights and support decision-making. Statistics plays a crucial role in data science, providing the foundation for various methods and techniques used in the field.

statistical concepts and techniques in data science

1. Descriptive Statistics (normal distribution)

task 4

2. Inferential Statistics

task 5

3. Data Exploration and Visualization

task 6

1- Descriptive Statistics

Descriptive Statistics -> Descriptive statistics are a set of techniques used to summarize and describe the main features of a dataset.

Descriptive statistics divided into:

1- central tendency -> Mean, Median, Mode

2- measures of dispersion" variability" -> Range, Variance, Standard

Deviation

1. **central tendency** -> aim to identify a representative or central value around which the data points cluster. They provide a single value that summarizes the central location of the data.

- 1. Mean -> the sum of all values divided by the number of observations. It represents the central point of a dataset.
- 2. Median -> The middle value of a dataset when arranged in ascending or descending order. It is less sensitive to extreme values than the mean.
- 3. Mode -> The value or values that appear most frequently in a dataset.

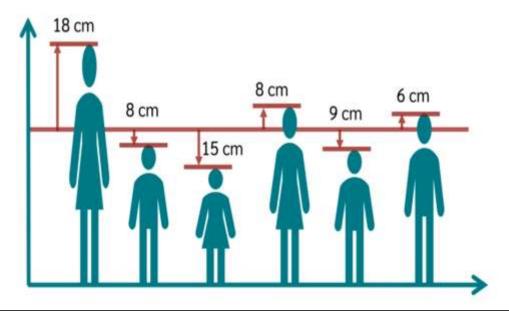
- 2. measures of dispersion" variability"=>quantify the spread, variability, or extent to which data points deviate from the central tendency. They provide information about how "spread out" the values are.
 - 1. Range -> The difference between the maximum and minimum values in a dataset.
 - 2. Variance -> A measure of how spread out the values in a dataset are from the mean "the unit is the square of original unit => cm "so the variance difficult to interpret.
 - 3. Standard Deviation -> The square root of the variance. It provides a more Population Sample ic mean".

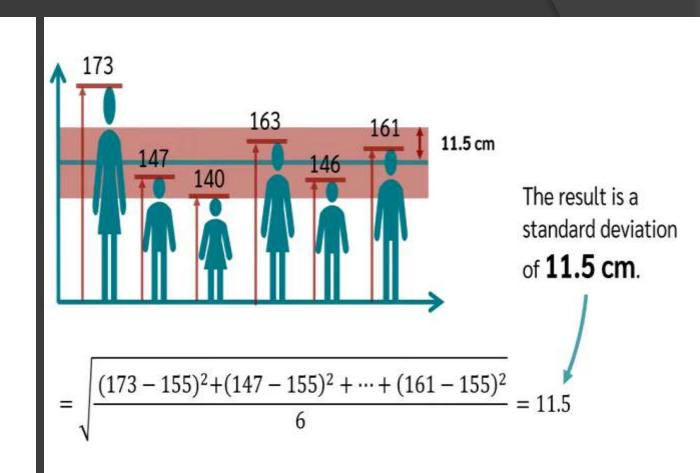
$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})^2} \qquad s = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

 Dispersion measures provide information about the variability or spread of values in a dataset.

Ex:

we want to know how much the persons deviate from the mean value on average.





central tendency vs measures of dispersion

central tendency => describe the center or average of a
dataset,

dispersion => provide information about how the individual data points are spread around that center.

In data analysis => understanding not only the average income (mean) but also the spread of incomes (standard deviation) provides a more complete picture of the economic situation.

Two type of data:

- 1. Qualitative → non-numerical data but words descriptive by observation.
 - Involve 5 sense like (seeing feeling test hear smell)
- 2. Quantitative → numerical data
 - Numerical data :
 - 1. Discrete (counting): integer number.
 - 2. Continues (measurement): decimal number.

Scales of Measurement

Type of scaling -> Nominal Scale, Ordinal Scale, Interval Scale, Ratio Scale.

Scales of Measurement

Data	Nominal	Ordinal	Interval	Ratio
Labeled	1	1		
Meaningful Order	×	2		
Measurable Difference	X	×	1	
True Zero Starting Point	X	X	X	1

2- inferential statistics

inferential statistics => is predictions about a population based on a sample of data drawn from that population.

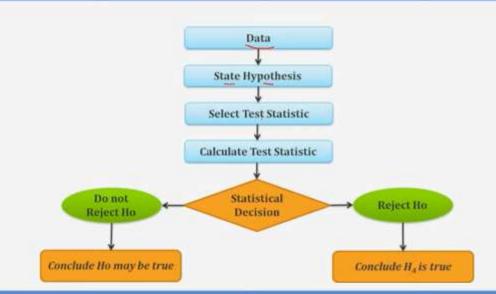
techniques in inferential statistics

- 1. Hypothesis Testing => is an idea that can be tested.
 - Null Hypothesis (H0): A statement that there is no effect or no difference.
 - Alternative Hypothesis (H1 or Ha): A statement expressing the presence of an effect or difference.
 - P-value => The probability of obtaining results as extreme as the observed results, assuming the null hypothesis is true.
- 2. Linear regression Analysis => used in data science to explore the relationship between a dependent variable and one or more independent variables.
 - Simple Linear regression => Involves one independent variable.
 - Multiple Linear Regression => Involves more than one independent variable.

1. Hypothesis Testing

1

Hypotheses Testing Process



Statistical Decision (z)

Level α Rejection Regions for Testing $\mu=\mu_0$ (normal population and σ known)

Alternative hypothesis Reject null hypothesis if: $\mu<\mu_0 \qquad \qquad Z<-z_\alpha$ $\mu>\mu_0 \qquad \qquad Z>z_\alpha$ $\mu\neq\mu_0 \qquad \qquad Z<-z_{\alpha/2}$ $\sigma r Z>z_{\alpha/2}$

2

Test Statistic Calculation

z-distribution

• t-distribution

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$$

$$t = \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}}$$

Test Statistic Selection

Case	Data	Statistic
1	Normal population (σ Known)	Z
2	Not-Normal population (n \geq 30)	z
3	Normal population (σ Unknown)	t

Example of hypothesis

Example 4

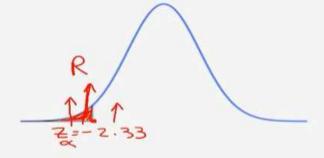
 A manufacturer of a pizza measures the amount of cheese used per run. Suppose that a consumer agency wishes to establish that the population mean is less than 71 pounds, the target amount established for this product. There are n = 80 observations and a computer calculation gives $\bar{x} =$ 68.45 and s = 9.583. What can it conclude if the probability of a Type I error is to be at most 0.01? -> Ha: M< 71 -> claim

Solution

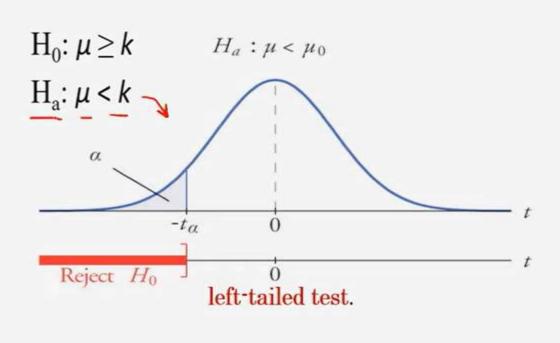
Ho: M > 71

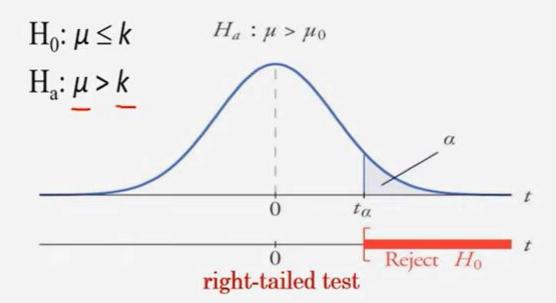
- Null hypothesis: μ ≥ 71 pounds
- Alternative hypothesis: μ < 71 pounds
- Level of significance: $\alpha \le 0.01$ (Z = -2.33)

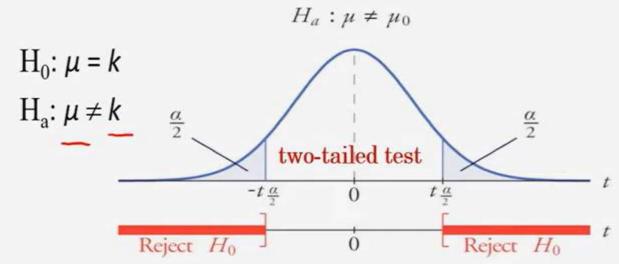
$$Z = \frac{68.45 - 71}{9.583/\sqrt{80}} = -2.38$$



 Decision: Since Z = −2.38 is less than −2.33, the null hypothesis must be rejected at level of significance 0.01. In other words, the suspicion that μ < 71 pounds is confirmed.



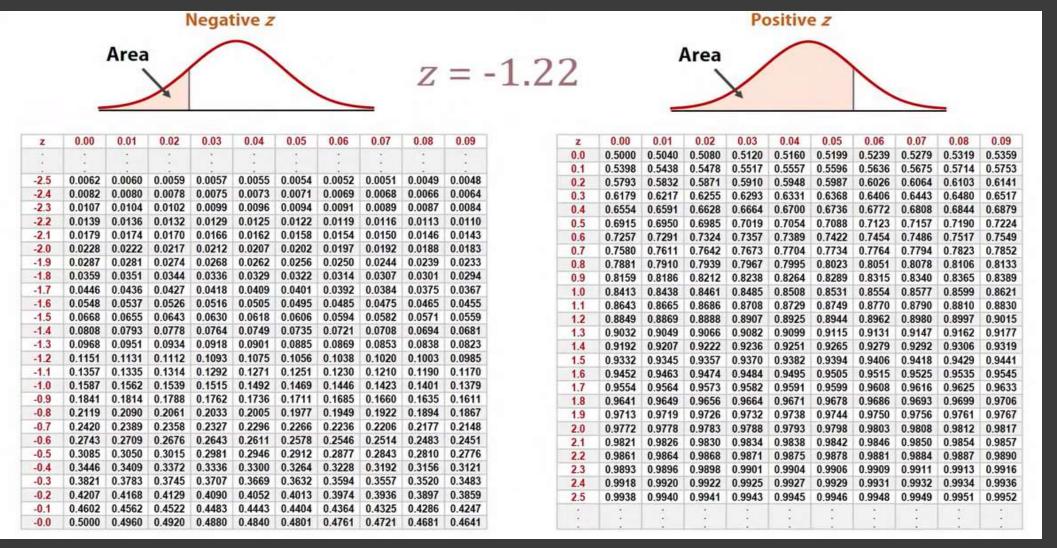




To calc $Z\alpha$

Significance Level (α): This is the predetermined threshold used to determine statistical significance. Common choices are 0.05, 0.01, or 0.10. " start of reject "





P-value

Z/t-Value vs P-value

Z or t-Value

 \succeq • Level of significance (α).



- Sample (Z or t-Value).
- Convert α to Zc or tc-Value
- Compare Z and Zc
- · Take the Decision

P-value

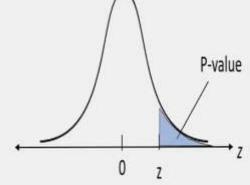
• Level of significance (α).



- Sample (Z or t-Value)
- · Convert Z or t-Value to P-Value
- Compare P-Value and α
- Take the Decision

Decision Rule Based on P-value

- To use a P-value to make a conclusion in a hypothesis test, compare the P-value with α .
- 1. If P-value $\leq \alpha$, then reject H_0 .
- 2. If P-value > α , then fail to reject Ho.



Way to calc p-value

Finding the P-value

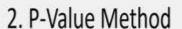
- After determining the hypothesis test's standardized test statistic and the test statistic's corresponding area, do one of the following to find the Pvalue.
 - 1) For a left-tailed test, P = (Area in left tail).
 - 2) For a right-tailed test, P = (Area in right tail).
 - 3) For a two-tailed test, P = 2 * (Area in tail of test statistic).

ex:

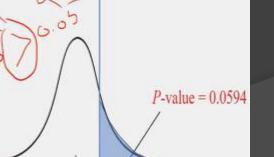
Z-Value vs P-value



$$\alpha$$
 = 0.05 means Z_{α} = Z_{c} = 1.96



$$\alpha = 0.05$$



0 1.56

 $\alpha = 0.05$

2- Linear regression → is a statistical method used to model the relationship between a dependent variable (outcome) and one or more independent variables (predictor)

Have two type:

- Simple linear regression: Involves one independent variable.
 - Equ: $y = b.x + a + \epsilon$

- Multiple linear regression: Involves more than independent variable.
 - Equ: $y = b_1.x_1 + b_2.x_2 + ... + b_k.x_k + a$

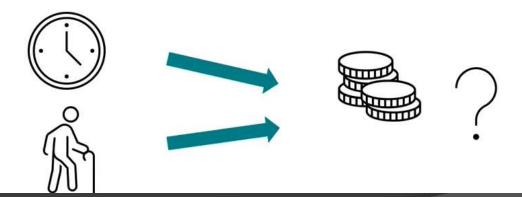
Simple linear regression

Does the weekly working time have an influence on the hourly salary of employees?

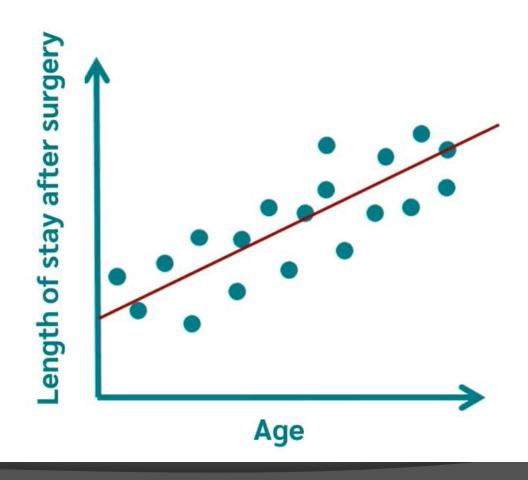


Multiple linear regression

Do the weekly working hours and the age of employees have an influence on their hourly salary?



Simple Linear Regression



Estimated length $\hat{y} = b \cdot x + a$

$$\hat{y} = 0.14 \cdot x + 1.2$$

$$5.82 = 0.14 \cdot 33 + 1.2$$

Calculation of a and b

$$b = r rac{s_y}{s_x} \qquad a = ar{y} - b \cdot ar{x}$$

3- Data Exploration and Visualization

Data Exploration and Visualization

- Histograms, Box Plots: Visualization of the distribution of data.
- Correlation Analysis: Understanding relationships between variables.

 Histogram -> A histogram is a graphical representation of the distribution of a dataset.

click to learn more histogram -> https://n9.cl/7rpfv click to learn more box plots -> https://n9.cl/jixa7

2. Correlation Analysis -> Understanding relationships between variables. click to learn more -> https://n9.cl/1a9ru

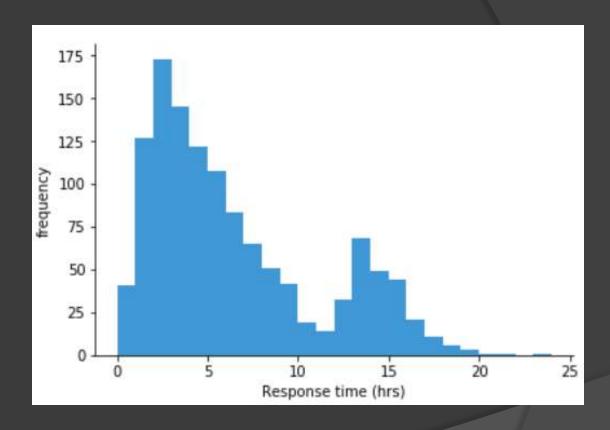
Histogram → A histogram is a chart that plots the distribution of a numeric variable's values as a series of bars. Each bar typically covers a range of numeric values called a bin, each bar describe afreq of data points.

When you should use a histogram?

Histograms are good for showing general distributional features of dataset variables.

Adv:

You can see roughly where the peaks of the distribution are, whether the distribution is skewed or symmetric, and if there are any outliers.



Histograms are good at showing the distribution of a single variable, but it's somewhat tricky to make comparisons between histograms if we want to compare that variable between different groups

Then using box plots

Bar chart → if the variable is not continuous and numeric, but instead discrete or categorical then using bar chart.

Purchases by User Type

6K

4K

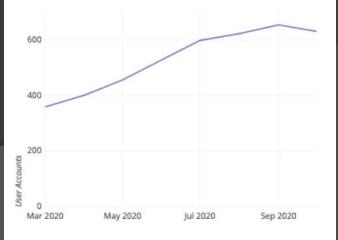
2K

Guest New User Existing User

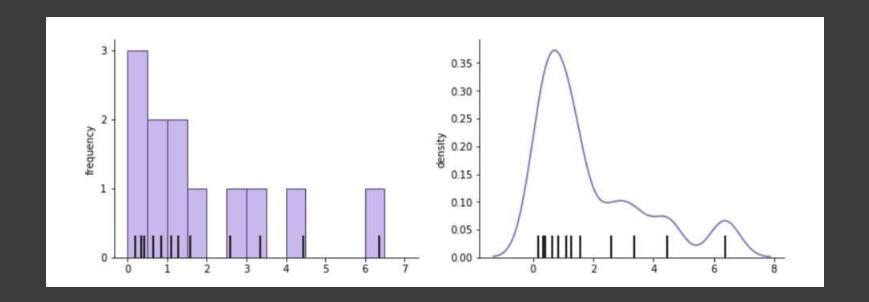
User Type

Line chart -> If you have binned numeric data but want the vertical axis of your plot to convey something other than

frequency information, then use line chart



Density curve → is an alternative to the histogram that gives each data point a continuous contribution to the distribution.



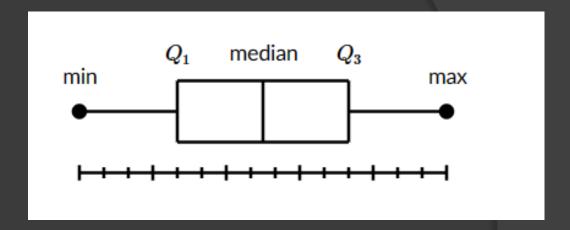
Box plots → In a box plot, we draw a box from the first quartile to the third quartile. A vertical line goes through the box at the median. The whiskers go from each quartile to the minimum or maximum.

To make box plot in data:

Step 1: Order the data from smallest to largest.

Step 2: Find the median.

Step 3: Find the quartiles.



Step 4: Complete the five-number summary by finding the min and the max.

End