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Chapter 1

What is EFG

Easy Factor Graph (EFG), is a simple and efficient C++ library for managing undirected graphical models. EFG allows you to build step by step a graphical model made of unary or binary potentials, i.e. factors involving one or two variables. It contains several tools for exporting and importing graphs from textual file. EFG allows you to perform all the probabilistic queries described in Chapter 2, from marginal probabilities computation to learning the tunable parameters of a graph. All the theoretical computations described in the initial Sections of this guide are already implemented inside the library. However, you are strongly encouraged to read this guide to understand how to use such functionalities.

The rest of this guide is structured as follows. Chapter 2 will introduce the main theoretical concepts about factor graphs, with the aim of explaining the capabilities of EFG. Chapter 3 will explain the format of the xml files adopted to represent factor graphs, exploited when importing or exporting the models to or from textual files. Chapter 4 will present the examples adopted for showing how EFG works. All the remaining Chapters, will describe the structure of the classes constituting EFG ¹.

¹A similar guide, but in a html format, is also available at http://www.andreacasalino.altervista.org/__EFG_doxy_quide/index.html.

2 What is EFG

Chapter 2

Theoretical background on factor graphs

This Section will provide the basic concepts about probabilistic models. Moreover, a precise notation will be introduced and used for the rest of this document.

2.1 Preliminaries

This library is intended for managing network of <u>categorical variables</u>. Formally, the generic categorical variable V has a discrete domain Dom:

$$Dom(V) = \{v_0, \cdots, v_n\} \tag{2.1}$$

Essentially, Dom(V) contains all the possible realizations of V. The above notation will be adopted for the rest of the guide: capital letters will refer to variable names, while non capital refer to their realizations. Group of categorical variables can be considered categorical variables too, having a domain that is the Cartesian product of the domains of the variables constituting the group. Suppose X is obtained as the union of variables $V_{1,2,3,4}$, i.e. $X = \bigcup_{i=1}^4 V_i$, then:

$$Dom(X) = Dom(V_1) \times Dom(V_2) \times Dom(V_3) \times Dom(V_4)$$
(2.2)

The generic realization x of X is a set of realizations of the variables $V_{1,2,3,4}$, i.e. $x=\{v_1,v_2,v_3,v_4\}$. Suppose $V_{1,2,3}$ have the domains reported in the tables 2.1. The union $X=\bigcup_{i=1}^3 V_i$ is a categoric variable whose domain is made by the combinations reported in table 2.2.

The entire population of variables contained in a model is a set denoted as $\mathcal{V}=\{V_1,\cdots,V_m\}$. As will be exposed in the following, the probability of $\bigcup_{V_i\in\mathcal{V}}V_i^{-1}$ is computed as the product of a certain number of components called factors.

Knowing the joint probability of $V_{1,\dots,m}$, the probability distribution of a subset $S \subset \{V_{1},\dots,V_{m}\}$ can be in general (not only for graphical models) obtained through marginalization. Assume C is the complement of S:

$$C \cup S = \bigcup_{i=1}^{m} V_i \tag{2.3}$$

¹Which is the joint probability distribution of all the variables in a model

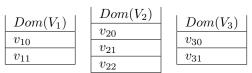


Table 2.1 Example of domains for the group of variables $V_{1,2,3}$.

$Dom(X) = Dom(V_1 \cup V_2 \cup V_3)$
$x_0 = \{v_{10}, v_{20}, v_{30}\}$
$x_1 = \{v_{10}, v_{20}, v_{31}\}$
$x_2 = \{v_{11}, v_{20}, v_{30}\}$
$x_3 = \{v_{11}, v_{20}, v_{31}\}$
$x_4 = \{v_{10}, v_{21}, v_{30}\}$
$x_5 = \{v_{10}, v_{21}, v_{31}\}$
$x_6 = \{v_{11}, v_{21}, v_{30}\}$
$x_7 = \{v_{11}, v_{21}, v_{31}\}$
$x_8 = \{v_{10}, v_{22}, v_{30}\}$
$x_9 = \{v_{10}, v_{22}, v_{31}\}$
$x_{10} = \{v_{11}, v_{22}, v_{30}\}$
$x_{11} = \{v_{11}, v_{22}, v_{31}\}$

Table 2.2 Example of domains for the group of variables $V_{1,2,3}$.

with $C \cap S = \emptyset$, then:

$$\mathbb{P}(S=s) = \sum_{\forall \hat{c} \in Dom(C)} \mathbb{P}(S=s, C=\hat{c})$$
 (2.4)

In the above computation, variables in C were marginalized. Indeed they were in a certain sense eliminated, since the probability of the sub set S was of interest, no matter the realizations of all the variables in C.

A <u>factor</u>, sometimes also called a <u>potential</u>, is a positive real function describing the correlation existing among a subset of variables $D^i \subset \mathcal{V}$. Suppose factor Φ_i involves $\{X,Y,Z\}$, i.e. $D^i = \{X,Y,Z\}$. Then, $\Phi_i(X,Y,Z)$ is a function defined over $Dom(D^i)$. More formally:

$$\Phi_i(D^i) = \Phi_i(X, Y, Z) : \mathsf{Domain}(X) \times \mathsf{Domain}(Y) \times \mathsf{Domain}(Z) \longrightarrow \mathbb{R}^+ \tag{2.5}$$

The aim of Φ_i is to assume 'high' values for those combinations $d^i=\{x,y,z\}$ that are probable to appear together and low values (at least a zero) for those being improbable. The entire population of factors $\{\Phi_1,\cdots\Phi_p\}$ correlating the variables of a model, is considered for computing $\mathbb{P}(V_1,\dots,m)$, i.e. the joint probability distribution of all the variables in the model. The energy function E of a graph is defined as the product of the factors:

$$E(V_{1,\dots,m}) = \Phi_1(D^1) \cdot \dots \cdot \Phi_p(D^p) = \prod_{i=1}^p \Phi_i(D^i)$$
 (2.6)

E is addressed for computing the joint probability distribution of the variables in \mathcal{V} :

$$\mathbb{P}(V_{1,\cdots,m}) = \frac{E(V_{1,\cdots,m})}{\mathcal{Z}} \tag{2.7}$$

where ${\cal Z}$ is a normalization coefficient defined as follows:

$$\mathcal{Z} = \sum_{\forall \tilde{V}_{1,\dots,m} \in Dom(\bigcup_{i=1,\dots,m} V_{i}))} E(\tilde{V}_{1,\dots,m})$$
(2.8)

Although the general theory behind graphical models supports the existance of generic multivaried factors, this library will address only two possible types:

- · Binary potentials: they involve a pair of variables.
- · Unary potentials: they involve a single variable.

We can store the values in the image of a Binary potential in a two dimensional table. For instance, suppose Φ_b involves variables A and B, whose domains contains 3 and 5 possible values respectively:

$$\begin{aligned} \mathsf{DOM}(A) &= \{a_1, a_2, a_3\} \\ \mathsf{DOM}(B) &= \{b_1, b_2, b_3, b_4, b_5\} \end{aligned} \tag{2.9}$$

2.1 Preliminaries 5

	b_0	b_1	b_2	b_3	b_4
a_0	1	4	0	0	0
a_1	0	1	0	0	0
a_2	0	0	5	0	1

Table 2.3 The values in the image of $\Phi_b(A,B)$.

$$\begin{array}{c|cccc} a_0 & a_1 & a_2 \\ \hline 0 & 2 & 0.5 \\ \hline \end{array}$$

Table 2.4 The values in the image of $\Phi_n(A)$.

The values assumed by $\Phi_b(A,B)$ are described by table 2.3. Essentially, $\Phi_b(A,B)$ tells us that the combinations $\{a_0,b_1\},\ \{a_2,b_2\}$ are highly probable; while $\{a_0,b_0\}$, $\{a_1,b_1\}$ and $\{a_2,b_4\}$ are moderately probable. Let be $\Phi_u(A)$ a Unary potential involving variable A. The values characterizing Φ_u can be stored in a simple vector, see table 2.4. If $\Phi_b(A,B)$ would be the only potential in the model, the joint probability density of A and B will assume the following values 2 :

$$\mathbb{P}(a_0, b_1) = \frac{\Phi_b(a_0, b_1)}{\mathcal{Z}} = \frac{4}{\mathcal{Z}} = 0.3333 \tag{2.10}$$

$$\mathbb{P}(a_2, b_2) = \frac{\Phi_b(a_2, b_2)}{\mathcal{Z}} = \frac{5}{\mathcal{Z}} = 0.4167 \tag{2.11}$$

$$\mathbb{P}(a_0, b_0) = \frac{\Phi_b(a_0, b_0)}{\mathcal{Z}} = \mathbb{P}(a_1, b_1) = \mathbb{P}(a_2, b_4) = \frac{1}{\mathcal{Z}} = 0.0833$$
 (2.12)

since \mathcal{Z} is equal to:

$$\mathcal{Z} = \sum_{\forall i = \{0,1,2\}, \forall j = \{0,1,2,3,4\}} \Phi_b(A = a_i, B = b_j) = 12$$
(2.13)

Both Unary and Binary potentials, can be of two possible classes:

- <u>Factors</u>. The potential is simply described by a set of values characterizing the image of the factor. $\Phi_b(A,B)$ and $\Phi_u(A)$ of the previous example are both Simple shapes. Classes EFG::distribution::factor::cnst::Factor and EFG::distribution::factor::modif::Factor handles this kind of potentials.
- Exponential Factors. They are indicated with Ψ_i and their image set is defined as follows:

$$\Psi_i(X) = exp(w \cdot \Phi_i(X)) \tag{2.14}$$

where Φ_i is a Simple shape. Classes EFG::distribution::factor::cnst::FactorExponential and EFG::distribution::factor::modif::Fac handles this kind of potentials. The weight w, can be tunable or not. In the first case, w is a free parameter whose value is decided after training the model (see Section 2.6), otherwise is a constant . Exponential factors with fixed weights will be denoted with $\overline{\Psi}_i$.

Figure 2.1 resumes all the possible categories of factors that can be present in the models handled by this library.

Figure 2.2 reports an example of undirected graph. Set $\mathcal V$ is made of 4 variables: A,B,C,D. There are 5 Binary potentials and 2 Unary ones. The graphical notation adopted for Fig. 2.2 will be adopted for the rest of this guide. Weights α,β,γ and δ are assumed for respectively $\Psi_{AC},\Psi_{AB},\Psi_{CD},\Psi_{B}$. For the sake of clarity, the joint probability of the variables in Fig. 2.2 is computable as follows:

$$\mathbb{P}(A,B,C,D) = \frac{E(A,B,C,D)}{\mathcal{Z}(\alpha,\beta,\gamma,\delta)} = \frac{E(A,B,CD)}{\sum_{\tilde{A},\tilde{B},\tilde{C},\tilde{D}} E(\tilde{A},\tilde{B},\tilde{C},\tilde{D})}$$

$$E(A,B,C,D) = \Phi_{A}(A) \cdot exp(\alpha \Phi_{AC}(A,C)) \cdot exp(\beta \Phi_{AB}(A,B)) \cdots$$

$$\cdots \Phi_{BC}(B,C) \cdot exp(\gamma \Phi_{CD}(C,D)) \cdot \Phi_{BD}(B,D) \cdot exp(\delta \Phi_{B}(B))$$
(2.15)

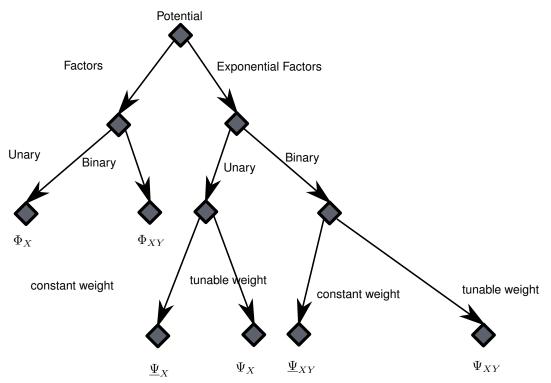


Figure 2.1 All the possible categories of factors, with the corresponding notation.

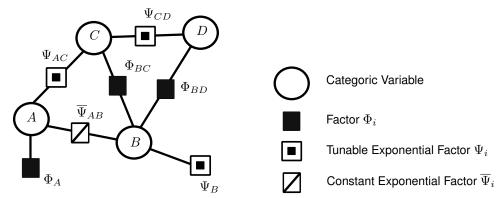


Figure 2.2 Example of graph: the legend of the right applies.

2.2 Message Passing 7

Graphical models are mainly used for performing belief propagation. Subset $\mathcal{O}=\{O_1,\cdots,O_f\}\subset\mathcal{V}$ is adopted for denoting the set of evidences: those variables in the net whose value become known. \mathcal{O} can be dynamical or not. The hidden variables are contained in the complementary set $\mathcal{H}=\{H_1,\cdots,H_t\}$. Clearly $\mathcal{O}\cup\mathcal{H}=\mathcal{V}$ and $\mathcal{O}\cap\mathcal{H}=\emptyset$. \mathcal{H} will be used for referring to the union of all the variables in the hidden set:

$$H = \bigcup_{i=1}^{t} H_i \tag{2.16}$$

while *O* is used for indicating the evidences:

$$O = \bigcup_{i=1}^{f} O_i \tag{2.17}$$

Knowing the joint probability distribution of variables in \mathcal{V} (equation (2.7)) the conditional distribution of H w.r.t. O can be determined as follows:

$$\mathbb{P}(H = h | O = o) = \frac{\mathbb{P}(H = h, O = o)}{\sum_{\forall \hat{h} \in Dom(H)} \mathbb{P}(H = \hat{h}, O = o)}$$

$$= \frac{E(h, o)}{\sum_{\forall \hat{h} \in Dom(H)} E(\hat{h}, o)} = \frac{E(h, o)}{\mathcal{Z}(o)}$$
(2.18)

The above computations are not actually done, since the number of combinations in the domain of $\mathcal H$ is huge also when considering a low-medium size graph. On the opposite, the marginal probability $\mathbb P(H_i=h_i|O=0)$ of a single variable in $H_i\in\mathcal H$ is computationally tractable. Formally $\mathbb P(H_i=h_i|O=0)$ is defined as follows:

$$\mathbb{P}(H_i = h_i | O = o) = \sum_{\forall \tilde{h} \in \{\mathcal{H} \setminus H_i\}} \mathbb{P}(H_i = h_i, \tilde{h} | O = o)$$
(2.19)

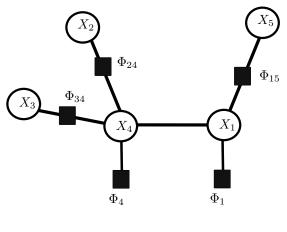
The above marginal distribution is essentially the conditional distribution of H_i w.r.t. O, no matter the other variables in \mathcal{H} .

A generic Random Field is a graphical model for which set \mathcal{O} (and consequently \mathcal{H}) is dynamical: the set of observations as well the values assumed by the evidences may change during time. Random field are handled by class RandomField. Conditional Random Field are Random Field for which set \mathcal{O} must be decided once and cannot change after. Only the values of the evidences during time may change. Class ConditionalRandomField is in charge of handling Conditional Random Field. Both Random Fields and Conditional Random Fields can be learnt knowing a training set, see Section 2.6. On the opposite, class Graph handles constant graphs: they are conceptually similar to Random Fields but learning is not possible. Indeed, all the Exponential Shape involved must be constant.

The rest of this Chapter is structured as follows. Section 2.2.2 will introduce the message passing algorithm, which is the pillar for performing belief propagation. Section 2.3 will expose the concept of maximum a posteriori estimation, useful when querying a graph, while Section 2.4 will address Gibbs sampling for producing a training set of a known model. Section 2.5 will present the concept of subgraph which is a useful way for computing the marginal probabilities of a sub group of variables in \mathcal{H} . Finally, 2.6 will discuss how the learning of a graphical model is done, with the aim of computing the weights of the Exponential shapes that are tunable.

2.2 Message Passing

Message passing is a powerful but conceptually simple algorithm adopted for propagating the belief across a net. Such a propagation is the starting point for performing many important operations, like computing the marginal distributions of single variables or obtaining sub graphs. Before detailing the steps involved in the message passing algorithm, let's start from an example of belief propagation. Without loss of generality we assume all the factors as simple Factors.



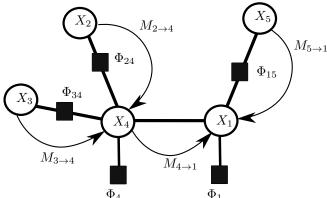


Figure 2.3 Example of graph adopted for explaining the message passing algorithm. Below are reported the messages to compute for obtaining the marginal probability of variable x_1

2.2.1 Belief propagation

Consider the graph reported in Figure 2.3. Supposing for the sake of simplicity that no evidences are available (i.e. $\mathcal{O}=\emptyset$). We are interested in computing $\mathbb{P}(X_1)$, i.e. the marginal probability of X_1 . Recalling the definition introduced in the previous Section, the marginal probability is obtained by the following computation:

$$\mathbb{P}(x_1) = \sum_{\forall \tilde{x}_{2,3,4,5} \in \cup_{i=2}^5 X_i} \mathbb{P}(x_1, \tilde{x}_{2,3,4,5})$$
 (2.20)

Simplifying the notation and getting rid of the normalization coefficient $\mathcal Z$ we can state the following:

$$\mathbb{P}(x_1) \propto \sum_{\tilde{x}_{2,3,4,5}} E(x_1, \tilde{x}_{2,3,4,5}) \tag{2.21}$$

Adopting the algebraic properties of the sums-products we can distribute the computations as follows:

$$\mathbb{P}(x_1) \propto \Phi_1(x_1) \sum_{\tilde{x}_5} \Phi_{15}(x_1, \tilde{x}_5) \sum_{\tilde{x}_4} \Phi_{14}(x_1, \tilde{x}_4) \Phi_4(\tilde{x}_4) \sum_{\tilde{x}_2} \Phi_{24}(\tilde{x}_{2,4}) \sum_{\tilde{x}_3} \Phi_{34}(\tilde{x}_{3,4}) \tag{2.22}$$

The first variable to marginalize can be \tilde{x}_2 or \tilde{x}_3 , since they are involved in the last terms of the sums products. The 'messages' $M_{2\to 4}$, $M_{3\to 4}$ are defined as follows:

$$M_{2\to 4}(\tilde{x}_4) = \sum_{\tilde{x}_2} \Phi_{24}(\tilde{x}_{2,4})$$

$$M_{3\to 4}(\tilde{x}_4) = \sum_{\tilde{x}_3} \Phi_{34}(\tilde{x}_{3,4})$$
(2.23)

²combinations having a null probability were omitted

2.2 Message Passing 9

Inserting $M_{2\rightarrow 4}$ and $M_{3\rightarrow 4}$ into equation (2.22) leads to:

$$\mathbb{P}(x_1) \propto \Phi_1(x_1) \sum_{\tilde{x}_5} \Phi_{15}(x_1, \tilde{x}_5) \sum_{\tilde{x}_4} \Phi_{14}(x_1, \tilde{x}_4) \Phi_4(\tilde{x}_4) M_{2 \to 4}(\tilde{x}_4) M_{3 \to 4}(\tilde{x}_4)$$
 (2.24)

At this point the messages $M_{4 \to 1}$ and $M_{5 \to 1}$ can be computed in the following way:

$$M_{4\to 1(x_1)} = \sum_{\tilde{x}_4} \Phi_{14}(x_1, \tilde{x}_4) \Phi_4(\tilde{x}_4) M_{2\to 4}(\tilde{x}_4) M_{3\to 4}(\tilde{x}_4)$$

$$M_{5\to 1}(x_1) = \sum_{\tilde{x}_7} \Phi_{15}(x_1, \tilde{x}_5)$$
(2.25)

After inserting $M_{4\rightarrow 1}$ and $M_{5\rightarrow 1}$ into equation (2.24) we obtain:

$$\mathbb{P}(x_1) \propto \Phi_1(x_1) M_{4\to 1}(x_1) M_{5\to 1}(x_1)
\mathbb{P}(x_1) = \frac{\Phi_1(x_1) M_{4\to 1}(x_1) M_{5\to 1}(x_1)}{\sum_{\tilde{x}_1} \Phi_1(\tilde{x}_1) M_{4\to 1}(\tilde{x}_1) M_{5\to 1}(\tilde{x}_1)}$$
(2.26)

which ends the computations. Messages are, in a certain sense, able to simplify the graph sending some information from an area of the graph to another one. Indeed, variables can be replace by messages, which can be treated as additional factors. Figure 2.3 resumes the computations exposed. Notice that the computation of $M_{4\to1}$ must be done after computing the messages $M_{2\to4}$ and $M_{3\to4}$, while $M_{5\to1}$ can be computed independently from all the others.

2.2.2 Message Passing

The aforementioned considerations can be extended to a general structured graph. Look at Figure 2.4: the computation of Message $M_{B \to A}$ can be performed only after having computed all the messages $M_{V_1,\dots,m \to B}$, i.e. the messages incoming from all the neighbours of B a part from A. Clearly $M_{B \to A}$ is computed as follows:

$$M_{B\to A}(a) = \sum_{\tilde{b}} \Phi_{AB}(a, \tilde{b}) M_{V1\to B}(\tilde{b}) \cdot \cdots \cdot M_{Vm\to B}(\tilde{b})$$

$$= \sum_{\tilde{b}} \Phi_{AB}(a, \tilde{b}) \prod_{i=1}^{m} M_{V_i\to B}(\tilde{b})$$
(2.27)

Essentially, it's like having simplified the graph: we can append to A the message $M_{B\to A}(a)$ as it's a Factor, deleting factor Ψ_{AB} and all the other portions of the graph, see Figure 2.4. In turn, $M_{B\to A}(a)$ will be adopted for computing the message outgoing from A.

The above elimination is not actually done: all messages incoming to all nodes of a graph are computed and stored for using them in subsequent queries. This is partially not true when considering the evidences. Indeed, when the values of the evidences are retrieved, variables in $\mathcal O$ are temporary deleted and replaced with messages, see Figure 2.5. Suppose variable C is connected to a variable C through a binary potential C0 and to variable C1 through C2. Suppose also that variable C3 is an evidence assuming a value equal to C3, then the messages sent to C4 and C5 can be computed independently as follows:

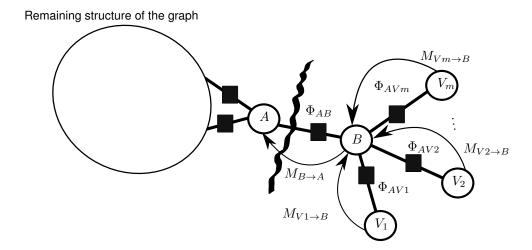
$$M_{C \to A}(a) = \Phi_{AC}(a, \hat{c})$$

 $M_{C \to B}(b) = \Phi_{BC}(b, \hat{c})$ (2.28)

Therefore all the variables that become evidences can be considered as leaves of the graph, sending messages to all the neighbouring nodes, possibly splitting an initial compact graph into many subgraphs, refer to Figure 2.5. Such computations are automatically handled by the library.

All the above considerations are valid when considering politree, i.e. graph without loops. Indeed, for these kind of graphs the message passing algorithm is able in a finite number of iterations to compute all the messages, see Figure 2.6. The same is not true when having loopy graphs (see Figure 2.7), since deadlocking situations arise: no further messages can be computed since for every nodes some incoming ones are missing. In such cases a variant of the message passing called loopy belief propagation can be adopted. Loopy belief propagation initializes all the messages to basic shapes having the values of the image all equal to 1 and then recomputes all the messages of all the variables till convergence.

You don't have to handle the latter aspect: the belief propagation mechanism is automatically handled by the library, according to the connectivity of the model for which a query is asked.



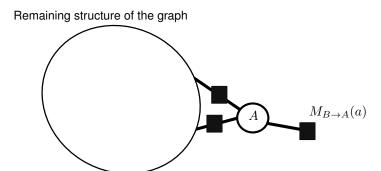


Figure 2.4 On the top the general mechanism involved in the message computation; on the bottom the simplification of the graph considering the computed message.

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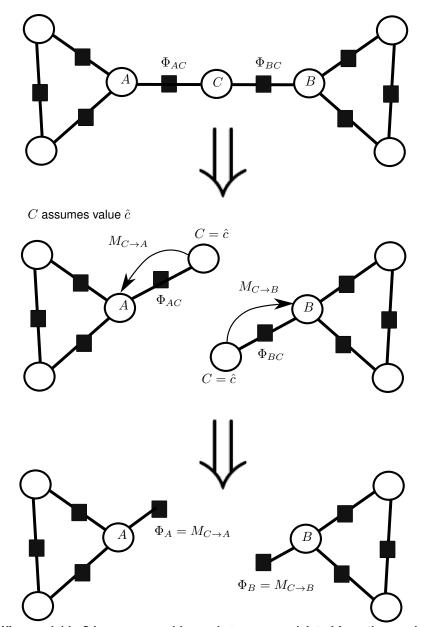


Figure 2.5 When variable C become an evidence, is temporary deleted from the graph, replaced by messages.

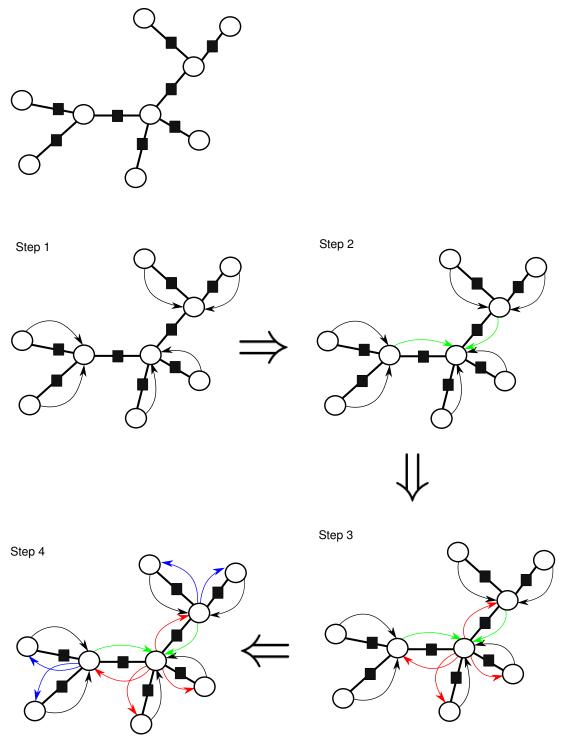


Figure 2.6 Steps involved for computing the messages of the politree represented at the top. The leaves are the first nodes for which the outgoing messages can be computed.

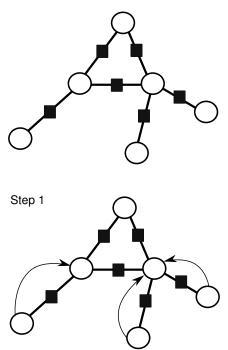


Figure 2.7 Steps involved for computing the messages on a loopy graph: after computing the messages outgoing from the leaves, a deadlock is reached since no further messages are computable.

2.3 Maximum a posteriori estimation

Suppose we are not interested in determining the marginal probability of a specific variable, but rather we want the combination in the hidden set \mathcal{H} that maximises the probability $\mathbb{P}(H_{1,\cdots,n}|O)$. Clearly, we could try to compute the entire distribution $\mathbb{P}(H_{1,\cdots,n}|O)$ and then take the value of H maximising that distribution. However, this is not computationally possible since even for low medium size graphs the size of $Dom(\cup_{\forall H_i \in \mathcal{H}} H_i)$ can be huge. Maximum a posteriori estimations solve this problem: the value maximising $\mathbb{P}(H_{1,\cdots,n}|O)$ is computed, without explicitly building the entire distribution $\mathbb{P}(H_{1,\cdots,n}|O)$. This is achieved by performing belief propagation with a slightly different version of the message passing algorithm presented in Section 2.2.2. Referring to Figure 2.4, the message to A is computed as follows when performing a maximum a posteriori estimation:

$$M_{B\to A}(a) = \max_{\tilde{b}} \{ \Phi_{AB}(a, \tilde{b}) \prod_{i=1}^{m} M_{V_i \to B}(\tilde{b}) \} \}$$
 (2.29)

Essentially, the summation in equation (2.27) is replaced with the max operator. After all messages are computed, the estimation $h_{MAP} = \{h_{1MAP}, h_{2MAP}, \cdots\}$ is obtained by considering for every variable in \mathcal{H} the value maximising:

$$h_{iMAP} = argmax\{\Phi_{Hi}(h_{iMAP}) \prod_{k=1}^{L} M_k(h_{iMAP})\}$$
 (2.30)

where $M_{1,\cdots,L}$ refer to all the messages incoming to H_i . To be precise, this procedure is not guaranteed to return the value actually maximising $\mathbb{P}(H_{1,\cdots,n}|O)$, but at least a strong local maximum is obtained. At this point it is worthy to clarify that the combination $h_{MAP}=\{h_{1MAP},h_{2MAP},\cdots\}$ could not be obtained by

simply assuming for every H_i the realization maximising the marginal distribution:

$$h_{MAP} \neq \{argmax(\mathbb{P}(h_1)), \cdots, argmax(\mathbb{P}(h_n))\}$$
 (2.31)

This is due to the fact that $\mathbb{P}(H_{1,\cdots,n}|O)$ is a joint probability distribution, while the marginals $\mathbb{P}(H_{i})$ are not. For better understanding this aspect consider the graph reported in Figure 2.8, with the potentials Φ_{XA} , Φ_{AB} and Φ_{YB} having the images defined in table 2.5. Suppose discovering that X=0 and Y=1. Then, performing the standard message passing algorithm explained in the previous Section we obtain the messages reported in Figure

	b_0	b_1		$ x_0 $	x_1		y_0	y_1
$\overline{a_0}$	2	0	a_0	1	0.1	b_0	1	0.1
$\overline{a_1}$	0	2	a_1	0.1	1	b_1	0.1	1

Table 2.5 Factors involved in the graph of Figure 2.8.

$\mid A$	$\mid B$	E(A, B, X = 0, Y = 1)
0	0	0.2
0	1	0
1	0	0
1	1	0.2

Table 2.6 Factors involved in the graph of Figure 2.8.

2.8. Clearly individual marginals for A and B would be equal to:

$$\mathbb{P}(A) = \begin{pmatrix} \mathbb{P}(A=0) \\ \mathbb{P}(A=1) \end{pmatrix} = \begin{pmatrix} 0.5 \\ 0.5 \end{pmatrix} \\
\mathbb{P}(B) = \begin{pmatrix} \mathbb{P}(B=0) \\ \mathbb{P}(B=1) \end{pmatrix} = \begin{pmatrix} 0.5 \\ 0.5 \end{pmatrix}$$
(2.32)

Therefore, all the combinations $\{A=0,B=0\}$, $\{A=0,B=1\}$, $\{A=1,B=0\}$, $\{A=1,B=1\}$ maximise $\mathbb{P}(A,B|O)$. However, it easy to prove that E(A,B,X,Y) assumes the values reported in table 2.6. Therefore, the combinations actually maximising the joint distribution $\mathbb{P}(A,B|O)$ are $\{A=0,B=0\}$ and $\{A=1,B=1\}$, leading to a different result.

2.4 Gibbs sampling

Gibbs sampling is a Monte Carlo method for obtaining samples from a joint distribution of variables $X_{1,\cdots,m}$, without explicitly compute that distribution. Indeed, Gibbs sampling is an iterative method which requires every time to determine the conditional distribution of a single variable X_i w.r.t to all the others in the group.

More formally the algorithm starts with an initial combination of values $\{x_{1,\cdots,m}^1\}$ for the variable $\cup_{i=\{1,\cdots,m\}}X_i$. At every iteration, all the values of that combination are recomputed. At the j^{th} iteration the value of x_k^{j+1} for the subsequent iteration is obtaining by sampling from the following marginal distribution:

$$x_k^{j+1} \sim \mathbb{P}(x_k | x_{\{1,\dots,m\}\setminus k}^j)$$
 (2.33)

After an initial transient, the samples cumulated during the iterations can be considered as drawn from the joint distribution involving group $X_{1.....m}$.

This algorithm can be easily applied to graphical model. Indeed the methodologies exposed in Section 2.2.2 can be applied for determining the conditional distribution of a single variable $H_i \in \mathcal{H}$ w.r.t all the others (as well the evidences in \mathcal{O}), assuming all variables in $\mathcal{H} \setminus H_i$ as additional observations and computing the marginal probability of H_i .

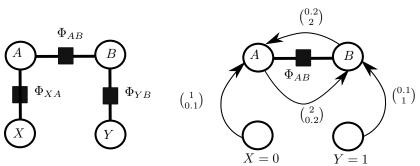


Figure 2.8 Example of graph adopted. When the evidences are retrieved, the messages computed by making use of the message passing algorithm are reported below.

2.5 Sub graphs 15

2.5 Sub graphs

As explained in Section 2.2.2, the marginal probability of a variable $H_i \in \mathcal{H}$ can be efficiently computed by considering the messages produced by the message passing algorithm. The same messages can be also used for performing graph reduction, with the aim to model the joint probability distribution of a subset of variables $\{H_1, H_2, H_3\} \subset \mathcal{H}$, i.e. $\mathbb{P}(H_{1,2,3}|O)$. The latter quantity is the marginal probability of the subset of variables of interest.

The aim of message passing is essentially to simplify the graph, condensing all the belief information into the messages. Such property is exploited for computing sub graphs. Without loss of generality assume from now on $\mathcal{O}=\emptyset$. Consider the graph in Figure 2.9 and suppose we are interested in modelling $\mathbb{P}(A,B,C)$, no matter the values of the other variables. After computing all the messages exploiting message passing, the sub graph reported in Figure 2.9 is the one modelling $\mathbb{P}(A,B,C)$. Actually, that sub graph is a graphical model itself, for which all the properties exposed so far hold. For example the energy function E is computable as follows:

$$E(A = a, B = b, C = c) = \Phi_{AB}(a, b)\Phi_{BC}(b, c)\Phi_{AC}(a, c)M_{X \to A}(a)M_{Y \to B}(b)$$
(2.34)

while the joint probability of A, B and C can be computed in this way:

$$\mathbb{P}(A=a,B=b,C=c) = \frac{E(a,b,c)}{\sum_{\forall \tilde{a},\tilde{b},\mathbf{c}} E(\tilde{a},\tilde{b},\tilde{c})}$$
(2.35)

Notice that in this case the graph is significantly smaller than the originating one, implying that the above computations can be performed in an acceptable time.

Also Gibbs sampling can be applied to a reduced graph, producing samples drawn from the marginal probability $\mathbb{P}(A, B, C)$.

The reduction described so far is always possible when considering a subset of variables forming a connected subportion of the original graph, i.e. after reduction there must be a unique sub structure. For instance, variables Xand Y of the graph in Figure 2.10 do not respect the latter specification, meaning that it is not possible to build a sub graph involving X and Y.

2.6 Learning

The aim of learning is to determine the optimal values for the w (equation (2.14)) of all the tunable potentials (see Section 2.1) Ψ . To this aim two cases must be distinguished:

- · Learning must be performed for a RandomField: see Section 2.6.1
- Learning must be performed for a ConditionalRandomField: see Section 2.6.2

No matter the case, the population of tunable weights, i.e. the weights of the tunable Exponential Factors of the model, will be indicated with W:

$$W = \{w_1, \cdots, w_D\} \tag{2.36}$$

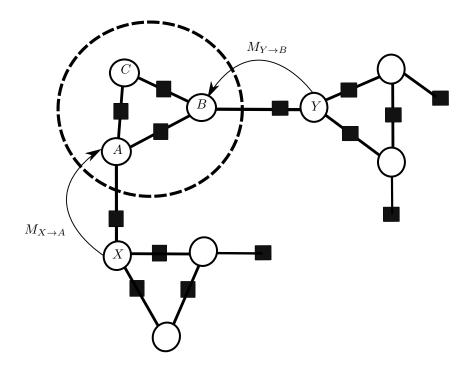
 w_i will refer to the i^{th} free parameter of the model. For the purpose of learning, we assume $\mathcal{O}=\emptyset$. Learning considers a training set $T=\{t_1,\cdots,t_N\}$ made of realizations of the joint distribution correlating all the variables in \mathcal{V} , no matter the fact that they are involved in tunable or non tunable potentials. As exposed in Section 2.1, if W is known, the probability of a combination t_i can be evaluated as follows:

$$\mathbb{P}(t_j) = \frac{E(t_j, W)}{\mathcal{Z}(W)} \tag{2.37}$$

At this point we can observe that the energy function is the product of two main factors: one depending from t_j and W and the other depending only upon t_j representing the contribution of all the non tunable potentials (Factors and Exponential Factors, see Section 2.1):

$$E(t_j, W) = exp(w_1\Phi_1(t_j)) \cdot \dots \cdot exp(w_D\Phi_D(t_j)) \cdot E_0(t_j)$$

$$= exp(\sum_{i=1}^D w_i\Phi_i(t_j)) \cdot E_0(t_j)$$
(2.38)



Sub graph involving A,B,C

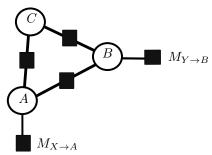


Figure 2.9 Example of graph reduction.

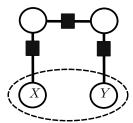


Figure 2.10 Example of a subset of variables for which the graph reduction is not possible.

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The likelihood function L can be defined as follows:

$$L = \prod_{t_j \in T} \mathbb{P}(t_j) \tag{2.39}$$

passing to the logarithmic likelihood and dividing by the training set size N we obtain:

$$J = \frac{\log(L)}{N} = \sum_{t_j \in T} \frac{\log(\mathbb{P}(t_j))}{N}$$

$$= \sum_{t_j \in T} \frac{\log(E(t_j, W)) - \log(\mathcal{Z}(W)}{N}$$

$$= \frac{1}{N} \sum_{t_j \in T} \log(E(t_j, W)) - \log(\mathcal{Z}(W))$$

$$= \frac{1}{N} \sum_{t_j \in T} \left(\sum_{i=1}^{D} w_i \Phi_i(t_j)\right) - \log(\mathcal{Z}(W)) + \cdots$$

$$+ \frac{1}{N} \sum_{t_j \in T} \log(E_0(t_j))$$
(2.40)

The aim of learning become essentially to find the value of W maximising J. This is typically done iteratively, by searching at every iteration the optimum along a direction similar to the one given by the gradient $\frac{\partial J}{\partial W}$. The way the gradient is exploited to update the searching direction characterize the kind of approach.

The basic gradient descend approach assumes the searching direction equal to the gradient, while Quasi Newton methods (https://www.jstor.org/stable/2006193) use an estimation of the hessian (computed using only the gradient variation) in order to correct the direction given by the gradient. Non linear conjugate approach (https://www.caam.rice.edu/~yzhang/caam554/pdf/cgsurvey.pdf) implements memory-based approaches that compute the new searching direction by considering both the actual value of the gradient as well as the old used direction.

The above methods are already implemented inside this library.

2.6.1 Learning of unconditioned model

The computations to perform for evaluating the gradient $\frac{\partial J}{\partial W}$ in case of unconditioned model will be exposed in this Section. Notice that in equation (2.40), term $\sum_{t_j \in T} log(E_0(t_j))$ is constant and consequently will be not considered for computing the gradient of J. Equation (2.40) can be rewritten as follows:

$$J = \alpha(T, W) - \beta(W)$$

$$\alpha = \frac{1}{N} \sum_{t_j \in T} \left(\sum_{i=1}^{D} w_i \Phi_i(t_j) \right)$$
(2.41)

 $\beta = log(\mathcal{Z}(W)) \tag{2.42}$

 α is influenced by T, while the same is not valid for β .

2.6.1.1 Gradient of α

By the analysis of the equation (2.41) it is clear that:

$$\frac{\partial \alpha}{\partial w_i} = \frac{1}{N} \sum_{t_j \in T} \Phi_i(t_j) \tag{2.43}$$

2.6.1.2 Gradient of β

The computation of $\frac{\partial \beta}{\partial w_i}$ requires to manipulate a little bit equation (2.42). Firstly the derivative of the logarithm must be computed:

$$\frac{\partial \beta}{\partial w_i} = \frac{1}{\mathcal{Z}} \frac{\partial \mathcal{Z}}{\partial w_i} \tag{2.44}$$

The normalizing coefficient \mathcal{Z} is made of the following terms (see also equation (2.7)):

$$\mathcal{Z}(W) = \sum_{\tilde{V} \in \bigcup_{i=1}^{p} V_i} \left(exp\left(\sum_{i=1}^{D} w_i \Phi_i(\tilde{V})\right) \cdot E_0(\tilde{V}) \right)$$
 (2.45)

Introducing equation (2.45) into (2.44) leads to:

$$\frac{\partial \beta}{\partial w_{i}} = \frac{1}{\mathcal{Z}} \frac{\partial}{\partial w_{i}} \left(\sum_{\tilde{V}} exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{V})\right) E_{0}(\tilde{V}) \right)
= \frac{1}{\mathcal{Z}} \sum_{\tilde{V}} \frac{\partial}{\partial w_{i}} \left(exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{V})\right) \right) E_{0}(\tilde{V})
= \frac{1}{\mathcal{Z}} \sum_{\tilde{V}} exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{V})\right) E_{0}(\tilde{V}) \Phi_{i}(\tilde{V})
= \sum_{\tilde{V}} \frac{exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{V})\right) E_{0}(\tilde{V})}{\mathcal{Z}} \Phi_{i}(\tilde{V})
= \sum_{\tilde{V}} \frac{E(\tilde{V})}{\mathcal{Z}} \Phi_{i}(\tilde{V})
= \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{i}(\tilde{V}) \tag{2.46}$$

Last term in the above equations can be further elaborated. Assume that the variables involved in potential Φ_j are $V_{1,2}$, then:

$$\frac{\partial \beta}{\partial w_{i}} = \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{i}(\tilde{V})$$

$$= \sum_{\tilde{V}_{1,2}} \Phi_{i}(\tilde{V}_{1,2}) \sum_{\tilde{V}_{3,4,\cdots}} \mathbb{P}(\tilde{V}_{1,2,3,4,\cdots})$$

$$= \sum_{\tilde{V}_{i,2}} \Phi_{i}(\tilde{V}_{1,2}) \mathbb{P}(\tilde{V}_{1,2})$$
(2.47)

where $\mathbb{P}(\tilde{V}_{1,2})$ is the marginal probability (see the initial part of Section 2.1) of the variables involved in the potential Φ_i , which can be easily computable by considering the sub graph containing only V_1 and V_2 as variables (see Section 2.5). Notice that in case Φ_i is a unary potential the same holds, considering the marginal distribution of the single variable involved by Φ_i :

$$\frac{\partial \beta}{\partial w_i} = \sum_{\forall \tilde{V}_1} \Phi_i(\tilde{V}_1) \mathbb{P}(\tilde{V}_1) \tag{2.48}$$

which can be easily obtained through the message passing algorithm (Section 2.2.2).

After all the manipulations performed, the gradient $\frac{\partial J}{\partial w_i}$ has the following compact expression:

$$\frac{\partial J}{\partial w_i} = \frac{1}{N} \sum_{j=1}^N \Phi_i(D_j^i) - \sum_{\tilde{D}^i} \mathbb{P}(\tilde{D}^i) \Phi_i(\tilde{D}^i)$$
 (2.49)

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2.6.2 Learning of conditioned model

For such models leaning is more demanding as will be exposed. Recalling the definition provided in the final part of Section 2.1, Conditional Random Fields are graphs for which the set of observations \mathcal{O} is fixed. The training set T is made of realizations of both \mathcal{H} and \mathcal{O} :

$$T = \{t_1, \dots, t_N\}$$

$$= \{\{h_1, o_1\}, \dots, \{h_N, o_N\}\}$$
(2.50)

We recall, equation (2.18), that the conditional probability of the hidden variables w.r.t. the observed ones is defined as follows:

$$\mathbb{P}(h_{j}, o_{j}) = \frac{E(h_{j}, o_{j}, W)}{\mathcal{Z}(o_{j}, W)}$$

$$E(h_{j}, o_{j}, W) = exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(h_{j}, o_{j})\right) E_{0}(h_{j}, o_{j})$$

$$\mathcal{Z}(o_{j}, W) = \sum_{\tilde{h}} E(\tilde{h}, o_{j}, W)$$
(2.51)

The aim of learning is to maximise a likelihood unction L defined in this case as follows:

$$L = \prod_{h_j \in T} \mathbb{P}(h_j | o_j) \tag{2.52}$$

Passing to the logarithms and dividing by the training set size we obtain the following objective function J:

$$J = \frac{\log(L)}{N}$$

$$= \frac{1}{N} \sum_{h_{j}, o_{j} \in T} log(E(h_{j}, o_{j}, W)) - \frac{1}{N} \sum_{h_{j}, o_{j} \in T} log(Z(o_{j}, W))$$

$$= \frac{1}{N} \sum_{h_{j}, o_{j} \in T} \left(\sum_{i=1}^{D} w_{i} \Phi_{i}(h_{j}, o_{j}) \right) - \frac{1}{N} \sum_{h_{j}, o_{j} \in T} log(Z(o_{j}, W))$$

$$+ \frac{1}{N} \sum_{h_{j}, o_{j} \in T} log(E_{0}(h_{j}, o_{j}))$$
(2.53)

Neglecting E_0 which not depends upon W, equation (2.53) can be rewritten as follows:

$$J = \alpha(T, W) - \beta(T, W)$$

$$\alpha(T, W) = \frac{1}{N} \sum_{h_j, o_j} \left(\sum_{i=1}^{D} w_i \Phi_i(h_j, o_j) \right)$$

$$\beta(T, W) = \frac{1}{N} \sum_{o_j} log(\mathcal{Z}(o_j, W))$$
(2.54)

At this point, an important remark must be done: differently from the β defined in equation (2.42), $\beta(T,W)$ of conditioned model is a function of the training set. The latter observation has an important consequence: when performing learning of unconditioned model, belief propagation (i.e. the computation of the messages through message passing with the aim of computing the marginal probabilities of the groups of variables involved in the factor of the model) must be performed once for every iteration of the gradient descend; on the opposite when considering conditioned model, belief propagation must be performed at every iteration for every element of the training set, see equation (2.58). This makes the learning of conditioned models much more computationally demanding. This price is paid in order to not model the correlation among the observations 3 , which can be interesting for many applications. The computation of $\frac{\partial \alpha}{\partial w_i}$ is analogous to the one of non conditioned model, equation (2.43).

³that can be highly correlated

2.6.2.1 Gradient of β

Following the same approach in Section 2.6.1.2, the gradient of β can be computed as follows:

$$\frac{\partial \beta}{\partial w_{i}} = \frac{1}{N} \sum_{j=1}^{N} \frac{\partial log(\mathcal{Z}(o_{j}, W))}{\partial w_{i}}$$

$$= \frac{1}{N} \sum_{j=1}^{N} \frac{1}{\mathcal{Z}(o_{j})} \frac{\partial \mathcal{Z}(o_{j}, W)}{\partial w_{i}}$$

$$= \frac{1}{N} \sum_{j=1}^{N} \frac{\partial}{\partial w_{i}} \left(\sum_{\tilde{h}} exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{h}, o_{j})\right) E_{0}(\tilde{h}, o_{j}) \right)$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}} \left(exp\left(\sum_{i=1}^{D} w_{i} \Phi_{j}(\tilde{h}, o_{j})\right) E_{0}(\tilde{h}, o_{j}) \Phi_{i}(\tilde{h}, o_{j}) \right)$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}} \frac{E(\tilde{h}, o_{j}, W)}{\mathcal{Z}(o_{1})} \Phi_{i}(\tilde{h}, o_{j})$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}} \mathbb{P}(\tilde{h}|o_{j}) \Phi_{i}(\tilde{h}, o_{j})$$
(2.55)

Suppose the variables involved in the factor Φ_j are $\tilde{h}_{1,2}$, then:

$$\frac{\partial \beta}{\partial w_{i}} = \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}} \mathbb{P}(\tilde{h}|o_{j}) \Phi_{i}(\tilde{h}, o_{j})$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}_{1,2}} \Phi_{i}(\tilde{h}_{1,2}) \sum_{\tilde{h}_{3,4,...}} \mathbb{P}(\tilde{h}_{1,2,3,4,...}|o_{j})$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}_{1,2}} \Phi_{i}(\tilde{h}_{1,2}) \mathbb{P}(\tilde{h}_{1,2}|o_{j})$$
(2.56)

where $\mathbb{P}(\tilde{h}_{1,2}|o_j)$ is the conditioned marginal probability of group $\tilde{h}_{1,2}$ w.r.t. the observations o_j .

Grouping all the simplifications we obtain:

$$\frac{\partial J}{\partial w_i} = \frac{1}{N} \sum_{j=1}^{N} \Phi_i(h_j, o_j) - \frac{1}{N} \sum_{j=1}^{N} \left(\sum_{\tilde{h}_{1,2}} \mathbb{P}(\tilde{h}_{1,2} | o_j) \Phi_i(\tilde{h}_{1,2}) \right)$$
(2.57)

Generalizing:

$$\frac{\partial J}{\partial w_i} = \frac{1}{N} \sum_{j=1}^N \Phi_i(D_j^i, o_j) - \frac{1}{N} \sum_{j=1}^N \left(\sum_{\tilde{D}^i} \mathbb{P}(\tilde{D}^i | o_j) \Phi_i(\tilde{D}^i, o_j) \right) \tag{2.58}$$

2.6 Learning 21

2.6.3 Learning of modular structure

Suppose to have a modular structure made of repeating units as for example the graph in Figure 2.11. Every single unit has the same population of potentials and we would like to enforce this fact when performing learning. In particular we'll have some sets of Exponential shape sharing the same weight w_1 (see Figure 2.11). Motivated by this example, we included in the library the possibility to specify that a potential must share its weight with another one. Then, learning is done consistently with the aforementioned specification.

2.6.3.1 Gradient of α

Considering the model in Figure 2.11, the α part of J (equation (2.41)) can be computed as follows:

$$\alpha = \frac{1}{N} \sum_{t_j} \left(w_1 \Phi_1(a_{1j}, b_{1j}) + w_1 \Phi_2(a_{2j}, b_{2j}) + w_1 \Phi_3(a_{3j}, b_{3j}) + \dots + \sum_{i=2}^{D} w_i \Phi_i(t_j) \right)$$

$$(2.59)$$

which leads to:

$$\frac{\partial \alpha}{\partial w_1} = \frac{1}{N} \sum_{t_j} \left(\Phi_1(a_{1j}, b_{1j}) + \Phi_2(a_{2j}, b_{2j}) + \Phi_3(a_{3j}, b_{3j}) \right) \tag{2.60}$$

2.6.3.2 Gradient of β

Regarding the β part of J we can write what follows:

$$\frac{\partial \beta}{\partial w_{1}} = \frac{1}{Z} \frac{\partial Z}{\partial w_{1}}
= \frac{1}{Z} \frac{\partial}{\partial w_{1}} \left(\sum_{\tilde{V}} \left(exp\left(w_{1}(\Psi_{1}(a_{1j}, b_{1j}) + \cdots + \Psi_{2}(a_{2j}, b_{2j}) + \Psi_{3}(a_{3j}, b_{3j})\right) + \sum_{i=2}^{D} w_{i} \Phi_{i}(\tilde{V}) \right) E_{0}(\tilde{V})) \right) \right)
= \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) (\Phi_{1}(\tilde{a}_{1}, \tilde{b}_{1}) + \Phi_{2}(\tilde{a}_{2}, \tilde{b}_{2}) + \Phi_{3}(\tilde{a}_{3}, \tilde{b}_{3}))
= \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{1}(\tilde{a}_{1}, \tilde{b}_{1}) + \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{2}(\tilde{a}_{2}, \tilde{b}_{2}) + \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{3}(\tilde{a}_{3}, \tilde{b}_{3})
= \sum_{\tilde{A}_{1}, \tilde{B}_{1}} \mathbb{P}(\tilde{A}_{1}, \tilde{B}_{1}) \Phi_{1}(\tilde{A}_{1}, \tilde{B}_{1}) + \sum_{\tilde{A}_{2}, \tilde{B}_{2}} \mathbb{P}(\tilde{A}_{2}, \tilde{B}_{2}) \Phi_{2}(\tilde{A}_{2}, \tilde{B}_{2}) + \cdots
\cdots + \sum_{\tilde{A}_{2}, \tilde{B}_{2}} \mathbb{P}(\tilde{A}_{3}, \tilde{B}_{3}) \Phi_{3}(\tilde{A}_{3}, \tilde{B}_{3}) \tag{2.61}$$

Notice that the gradient $\frac{\partial J}{\partial w_1}$ is the summation of three terms: the ones that would have been obtained considering separately the three potentials in which w_1 is involved (equation (2.49)):

$$\frac{\partial J}{\partial w_{1}} = \frac{1}{N} \sum_{j=1}^{N} \Phi_{1}(a_{i}^{1}, b_{i}^{1}) - \sum_{\tilde{a}^{1}, \tilde{b}^{1}} \mathbb{P}(\tilde{a}^{1}, \tilde{b}^{1}) \Phi_{1}(\tilde{a}^{1}, \tilde{b}^{1}) + \cdots
+ \frac{1}{N} \sum_{j=1}^{N} \Phi_{2}(a_{i}^{2}, b_{i}^{2}) - \sum_{\tilde{a}^{2}, \tilde{b}^{2}} \mathbb{P}(\tilde{a}^{2}, \tilde{b}^{2}) \Phi_{2}(\tilde{a}^{2}, \tilde{b}^{2}) + \cdots
+ \frac{1}{N} \sum_{j=1}^{N} \Phi_{3}(a_{i}^{3}, b_{i}^{3}) - \sum_{\tilde{a}^{3}, \tilde{b}^{3}} \mathbb{P}(\tilde{a}^{3}, \tilde{b}^{3}) \Phi_{3}(\tilde{a}^{3}, \tilde{b}^{3}) +$$
(2.62)

The above result has a general validity, also considering conditioned graphs.

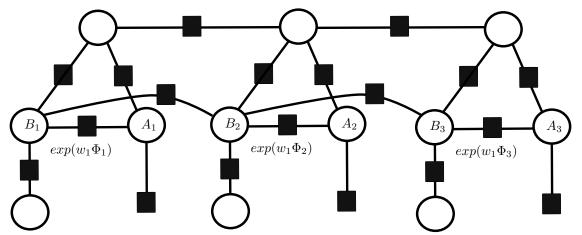


Figure 2.11 Example of modular structure: weight w_1 is simultaneously involved into potentials Φ_1,Φ_2 and Φ_3 .

Chapter 3

Import models from xml files

The aim of this Section is to expose how to build graphical models from XML files describing their structures. In particular, the syntax of such an XML will be clarified. Figure 3.1 visually explains the structure of a valid XML. Essentially two kind of tags must be incorporated:

- Variable: describes the information related to a variable present in the graph. There must a tag of this kind for every variable constituting the model. Fields description:
 - name: is a string indicating the name of this variable.
 - Size: is the size of the variable, i.e. the size of *Dom*, see Section 2.1.
 - flag[optional]: is a flag that can assume two possible values, 'O' or 'H' according to the fact that this variable is in set \mathcal{O} (Section 2.1) or not respectively. When non specifying this flag 'H' is assumed.
- Potential: describes the information related to a unary or a binary potential present in the graph (see Section 2.1). Fields description:
 - var: the name of the first variable involved.
 - var[optional]: the name of the second variable involved. Is omitted when considering unary potentials, while is mandatory when a binary potentials is described by this tag.
 - weight[optional]: when specifying an Exponential Factors (Section 2.1) it must be present for indicating the value of the weight w (equation (2.14)). When omitting, the potential is assumed to be a simple Factor.
 - tunability[optional]: it is a flag for specifying whether the weight of this Exponential Factor is tunable or not (see Section 2.1). Is ignored in case weight is omitted. It can assumes two possible values, 'Y' or 'N' according to the fact that the weight involved is tunable or not respectively. When weight is specified and tunability is omitted, a value equal to 'Y' is assumed.
- Share[optional]: you must specify this sub tag when the containing Exponential Factor shares its weight with another potential in the model. Sub fields var are exploited for specifying the variables involved by the potential whose weight is to share. If weight is omitted in the containing Potential tag, this sub tag is ignored, even though the value assigned to weight is ignored since it is shared with another potential. The potential sharing its weight must be clearly an Exponential shape, otherwise the sharing directive is ignored.

The following components are exclusive: only one of them can be specified in a Potential tag and at the same time at least one must be present.

Correlation: it can assume two possible values, 'T' or 'F'. When 'T' is passed, this potential is assumed to be a correlating potential (see sample 4.1.2.2), otherwise when passing 'F' a simple anti correlating factor is assumed. It is invalid in case this Potential is a unary one. In case weight was specified, an Exponential Factor is built, passing as input the correlating or anti-correlating Factor described by this tag.

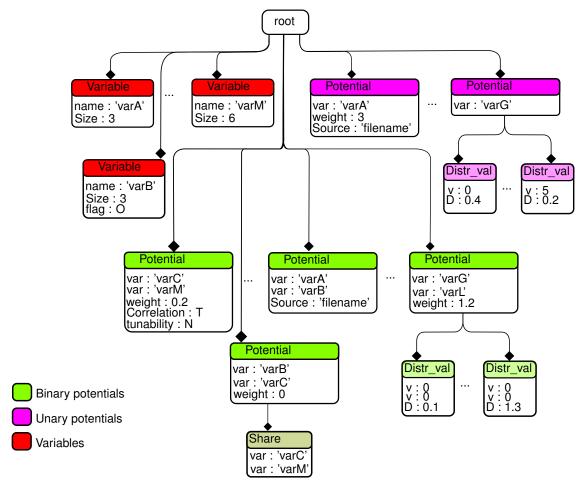


Figure 3.1 The structure of the XML describing a graphical model.

– Source: it is the location of a textual file describing the values of the distribution characterizing this potential. Rows of this file contain the values charactering the image of the potential. Combinations not specified are assumed to have an image value equal to 0. Clearly the number of values charactering the distribution must be consistent with the number of specified var fields. In case weight was specified, an Exponential Factor is built, starting from the Factor described by the values specified in the aforementioned file. For instance, the potential Φ_b of Section 2.1 would have been described by a file containing the following rows:

 $\begin{array}{ccccc} 0 & 0 & 1 \\ 0 & 1 & 4 \\ 1 & 1 & 1 \\ 2 & 2 & 5 \\ 2 & 4 & 1 \end{array}$

(3.1)

– Set of sub tags Distr_val: is a set of nested tags describing the distribution of the this potential. Similarly to Source, every element use fields v for describing the combination, while D is used for specifying the value assumed by the distribution. For example the potential Φ_b of Section 2.1 would have been described by the syntax reported in Figure 3.2. In case weight was specified, an Exponential Factor is built, starting from the Factor whose distribution is specified by the aforementioned sub tags.

Figure 3.2 Syntax to adopt for describing the potential Φ_b of Section 2.1, using a population of Distr_val sub tags.

Chapter 4

Samples

4.1 Sample 01: Potential handling

The aim of this series of examples is mainly to show how to handle the creation of variables and factors.

4.1.1 Variables creation

4.1.1.1 part 01

This example creates a tow initial variables A and B with a domain size equal to 2 and places them into a group storing them. Later, it adds variables C and D, with the same domain size. Finally, tries to add again C, showing the this further addition is correctly refused.

4.1.1.2 part 02

This example considers 3 variables A, B and C with a domain sizes equal to, respectively, 2,4 and 3, i.e:

$$Dom(A) = \{a_1 = 0, a_2 = 1\}$$

$$Dom(B) = \{b_1 = 0, b_2 = 1, b_3 = 2, b_4 = 3\}$$

$$Dom(C) = \{c_1 = 0, c_2 = 1, c_3 = 2\}$$

$$(4.1)$$

Then, evaluates the joint domain of: $A \cup B$, $A \cup C$ and $A \cup B \cup C$, which should results in the following combinations reported in, respectively, tables 4.1, 4.2 and 4.3.

4.1.2 Factors creation

4.1.2.1 part 01

Part 01 creates a shape factor Φ_{AB} , involving the pair of variables A and B. Both that variables have a domain size equal to 4, i.e. $Dom(A)=\{a_0=0,a_1=1,a_2=2,a_3=3\}$ and $Dom(B)=\{b_0=0,b_1=1,b_2=2,b_3=3\}$. The generic value in the image Φ_{AB} is equal to:

$$\Phi_{AB}(A = a, B = b) = a + 2 \cdot b \tag{4.2}$$

Table 4.4 reports the entire image of Φ_{AB} .

$\mid Dom(AB) = Dom(A \cup B)$
$\{a_1, b_1\}$
$\{a_1, b_2\}$
$\{a_1, b_3\}$
$\{a_1, b_4\}$
$\{a_2, b_1\}$
$\{a_2, b_2\}$
$\{a_2, b_3\}$
$\{a_2, b_4\}$

Table 4.1 Domain of AB.

$Dom(AC) = Dom(A \cup C)$
$\{a_1, c_1\}$
$\{a_1, c_2\}$
$\{a_1, c_3\}$
$\{a_2, c_1\}$
$\{a_2, c_2\}$
$\{a_2, c_3\}$

Table 4.2 Domain of AC.

$\begin{tabular}{ l } $Dom(ABC) = Dom(A \cup B \cup C) \end{tabular}$
$\{a_1, b_1, c_1\}$
$\{a_1, b_1, c_2\}$
$\{a_1, b_1, c_3\}$
$\{a_1, b_2, c_1\}$
$\{a_1, b_2, c_2\}$
$\{a_1, b_2, c_3\}$
$\{a_1, b_3, c_1\}$
$\{a_1, b_3, c_2\}$
$\{a_1, b_3, c_3\}$
$\{a_1, b_4, c_1\}$
$\{a_1, b_4, c_2\}$
$\{a_1, b_4, c_3\}$
$\{a_2, b_1, c_1\}$
$\{a_2, b_1, c_2\}$
$\{a_2, b_1, c_3\}$
$\{a_2, b_2, c_1\}$
$\{a_2, b_2, c_2\}$
$\{a_2, b_2, c_3\}$
$\{a_2, b_3, c_1\}$
$\{a_2, b_3, c_2\}$
$\{a_2, b_3, c_3\}$
$\{a_2, b_4, c_1\}$
$\{a_2, b_4, c_2\}$
$\{a_2, b_4, c_3\}$

Table 4.3 Domain of ABC.

	$b_0 = 0$	$b_1 = 1$	$b_2 = 2$	$b_3 = 3$
$a_0 = 0$	0	2	4	6
$a_1 = 1$	1	3	5	7
$a_2 = 2$	2	4	6	8
$a_3 = 3$	3	5	7	9

Table 4.4 The values in the image of Φ_{AB} .

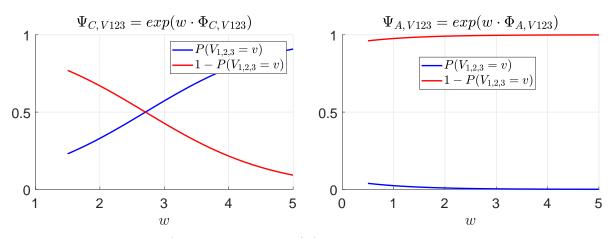


Figure 4.1 The probability $\mathbb{P}(V_1=v,V_2=v,V_3=v|w)$ and its complement, when considering a ternary correlating factor, on the left, and an anti-correlating one, on the right.

4.1.2.2 part 02

Part 02 considers a ternary correlating factor $\Phi_{C\ V123}$, involving variables V_1 , V_2 and V_3 , each having a domain size equal to 3. Ternary factors cannot be part of a graph, but it is anyway possible to build them as distribution object. The values in the image of Φ_{CV123} are all 0, except for those combination for which V_1, V_2 and V_3 assume the same value (0, 1 or 2) and in such cases, the image is equal to 1.

The same example builds at a second stage a ternary anti-correlating factor $\Phi_{A\ V123}$. The values in the image of $\Phi_{A\ V123}$ are all 1, except for those combination for which V_1,V_2 and V_3 assume the same value (0,1 or 2) and in such cases the image is equal to 1.

When considering a graph having only $\Psi_{C,V123} = exp(\Phi_{C,V123} \cdot w)$ as a factor, the ripartition function Z is equal to:

$$Z = (4^3 - 4) + 4 \cdot exp(w) \tag{4.3}$$

The probability to have as a realization a combination with the same values is equal to:

$$\mathbb{P}(V_1 = v, V_2 = v, V_3 = v) = \sum_{i=0}^{3} \mathbb{P}(V_1 = i, V_2 = i, V_3 = i)$$
(4.4)

$$= \sum_{i=0}^{3} \frac{\Psi_{C\ V123}(i,i,i)}{Z} \tag{4.5}$$

$$= 4 \cdot \frac{\Psi_{C\ V123}(0,0,0)}{Z} \tag{4.6}$$

$$= 4 \cdot \frac{\Psi_{C \ V123}(0, 0, 0)}{Z}$$

$$= \frac{4 \cdot exp(w)}{(4^{3} - 4) + 4 \cdot exp(w)}$$
(4.6)

The value assumed by $\mathbb{P}(V_1=v,V_2=v,V_3=v|w)$ is reported in Figure 4.1, together with the complementary probability $1 - \mathbb{P}(V_1 = v, V_2 = v, V_3 = v | w)$.

When considering a graph having only $\Psi_{A,\,V123}=exp(\Phi_{A\,\,V123}\cdot w)$ as factor, the ripartition function Z is equal

$$Z = (4^3 - 4) \cdot exp(w) + 4 \tag{4.8}$$

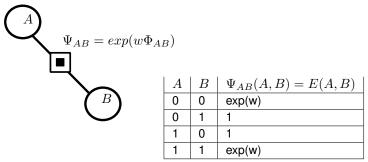


Figure 4.2 On the left the graph considered in this example, while on the right the image of factor Ψ_{AB} . Since that potential is the only one present in the graph, the values in the image of Ψ_{AB} are also the ones assume by the energy function E.

The probability to have as a realization a combination with the same values is equal to:

$$\mathbb{P}(V_1 = v, V_2 = v, V_3 = v) = \sum_{i=0}^{3} \mathbb{P}(V_1 = i, V_2 = i, V_3 = i)$$
(4.9)

$$= \sum_{i=0}^{3} \frac{\Psi_{A\ V123}(i,i,i)}{Z} \tag{4.10}$$

$$= 4 \cdot \frac{\Psi_{A\ V123}(0,0,0)}{Z} \tag{4.11}$$

$$= 4 \cdot \frac{\Psi_{A\ V123}(0,0,0)}{Z}$$

$$= \frac{4}{(4^{3}-4) \cdot exp(w) + 4}$$
(4.11)

The value assumed by $\mathbb{P}(V_1=v,V_2=v,V_3=v|w)$ is reported in Figure 4.1, together with its complement $1 - \mathbb{P}(V_1 = v, V_2 = v, V_3 = v | w)$. Indeed, when the variables are correlated, i.e. they share $\Psi_{C|V123}$, the probability $\mathbb{P}(V_1=v,V_2=v|w)$ is big. Moreover, the more w is high (i.e. the more the variables are correlated), the more the latter probability is big. On the opposite, when the variables are anti-correlated, the opposite situation arises.

4.2 Sample 02: Belief propagation, part A

The aim of this series of examples is to show how to perform probabilistic gueries on factor graphs.

4.2.1 part 01

This example creates a graph having a single binary exponential shape Ψ_{AB} , see Figure 4.2, with a A and Bhaving a Dom size equal to 2. $\Psi_{AB}=exp(w\Phi_{AB})$, where Φ_{AB} is a simple correlating factor. The image of Ψ_{AB} is reported in the right part of Figure 4.2.

Variable B is considered as an evidence, whose value is equal, for the first part of the example, to 0, while a value of 1 is assumed in the second part. The probability of A conditioned to B, is equal to (see equation (2.18)):

$$\mathbb{P}(A=a|B=0) = \frac{E(A=a,B=0)}{E(A=0,B=0) + E(A=1,B=0)} \Rightarrow \begin{bmatrix} \mathbb{P}(A=0|B=0) = \frac{exp(w)}{1 + exp(w)} \\ \mathbb{P}(A=1|B=0) = \frac{1}{1 + exp(w)} \end{bmatrix}$$
(4.13)

$$\mathbb{P}(A=a|B=1) = \frac{E(A=a,B=1)}{E(A=0,B=1) + E(A=1,B=1)} \Rightarrow \begin{bmatrix} \mathbb{P}(A=0|B=1) = \frac{1}{1 + exp(w)} \\ \mathbb{P}(A=1|B=1) = \frac{exp(w)}{1 + exp(w)} \end{bmatrix} \tag{4.14}$$

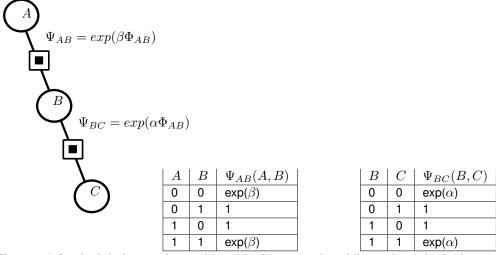
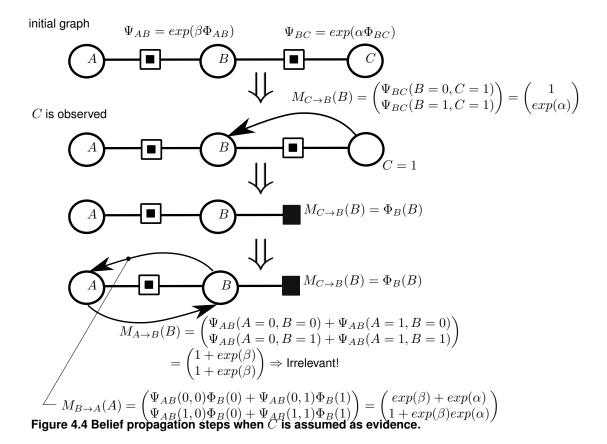


Figure 4.3 On the left the graph considered in this example, while on the right the images of factor Ψ_{AB} and Ψ_{BC} having, respectively, a weight equal to β and α .



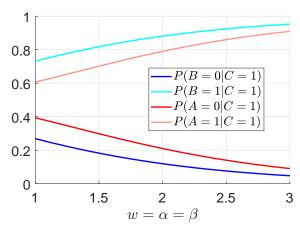


Figure 4.5 The marginals of variables B and A, when having a C=1 as evidence of the graph reported in Figure 4.4.

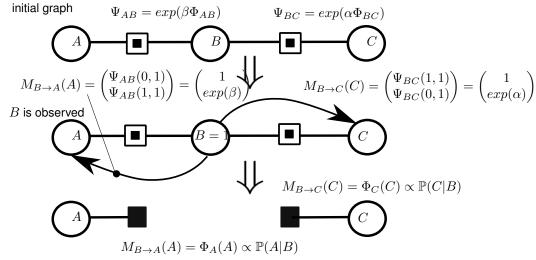
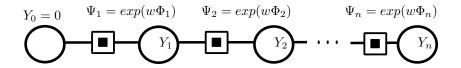


Figure 4.6 Belief propagation steps when \boldsymbol{B} is assumed as evidence.



$\Psi_i(Y_{i-1},Y_i)$	$Y_i = 0$	$Y_i = 1$		$Y_i = m$
$Y_{i-1} = 0$	exp(w)	1		1
$Y_{i-1} = 1$	1	exp(w)		1
:	:	:		
$Y_{i-1} = m$	1	1		exp(w)

Figure 4.7 On the top the chain considered in this example, while on the bottom the image of the generic factor $\Psi_i(Y_{i-1},Y_i)$.

4.2.2 part 02

A slightly more complex graph, made of two exponential correlating factors Ψ_{BC} and Ψ_{AB} , is built in this sample. The considered graph is reported in Figure 4.3. The two involved factors have two different weights, α and β : the resulting image sets are reported in the right part of Figure 4.3.

In the first part, C=1 is assumed as evidence and the marginal probabilities of A and B conditioned to C are computed. They are compared with the theoretical results, obtained by applying the message passing algorithm (Section 2.2.2), whose steps are here detailed 1 . The message passing steps are summarized in Figure 4.4. After having computed all the messages, it is clear that the marginal probabilities are equal to:

$$\mathbb{P}(A|C=1) = \frac{1}{Z} M_{B \to A}(A) = \frac{1}{Z} \begin{bmatrix} exp(\alpha) + exp(\beta) \\ 1 + exp(\alpha) \cdot exp(\beta) \end{bmatrix}$$
(4.15)

$$\mathbb{P}(B|C=1) = \frac{1}{Z}\Phi_B(B) \cdot M_{A \to B}(B) = \frac{1}{Z}\Phi_B(B) = \frac{1}{Z} \begin{bmatrix} 1\\ exp(\alpha) \end{bmatrix} \tag{4.16}$$

Figure 4.5 shows the values assumed by the marginals when varying the coefficients α and β . As can be seen, the more A,B and C are correlated (i.e. the more α and β are big) the more $\mathbb{P}(B=1|C=1)$ and $\mathbb{P}(A=1|C=1)$ are big. Notice also that when assuming $\alpha=\beta$, $\mathbb{P}(B=1|C=1)$ is always bigger than $\mathbb{P}(A=1|C=1)$. This is intuitively explained by the fact that C is directly connected to B, while A is indirectly connected to C, through B. In the second part, B=1 is assumed as evidence and the marginal probabilities of A and C conditioned to B are computed. The theoretical results can be computed again considering the message passing, whoe steps are reported in Figure 4.6. The marginal probabilities are in this case equal to:

$$\mathbb{P}(A|B=1) = \frac{1}{Z}\Phi_A(A) = \frac{1}{Z}\begin{bmatrix} 1\\ exp(\beta) \end{bmatrix}$$
 (4.17)

$$\mathbb{P}(C|B=1) = \frac{1}{Z}\Phi_C(C) = \frac{1}{Z}\begin{bmatrix} 1\\ exp(\alpha) \end{bmatrix} \tag{4.18}$$

4.2.3 part 03

In this sample, a linear chain of variables $Y_{0,1,2,\cdots,n}$ is considered. All variables in the chain have the same Dom size and all the factors $\Psi_{1,\cdots,n}$, Figure 4.7, are simple exponential correlating factors. The image of the generic factor Ψ_{i} is reported in the right part of Figure 4.7.

The evidence $Y_0=0$ is assumed and the marginals of the last variable in the chain Y_n , i.e. the one furthest to Y_0 , are computed. Figure 4.8 reports the probability $\mathbb{P}(Y_n=0|Y_0=0)$, when varying the chain size, as well the domain size of the variables. As can be seen, the more the chain is longer, the lower is the aforementioned probability, as Y_n is more and more indirectly correlated to Y_0 . Similar considerations hold for the domain size.

¹The same steps are internally execute by Node_factory.

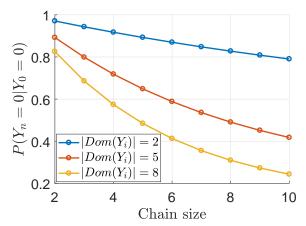


Figure 4.8 Marginal probability of Y_n when varying the chain size of the structure presented in Figure 4.7. w is assumed equal to 3.5.

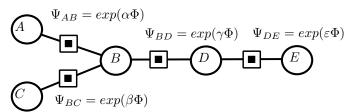


Figure 4.9 The factor graph considered by part 01.

4.3 Sample 03: Belief propagation, part B

The aim of this series of examples is to show how to perform probabilistic queries on articulated complex graphs.

4.3.1 part 01

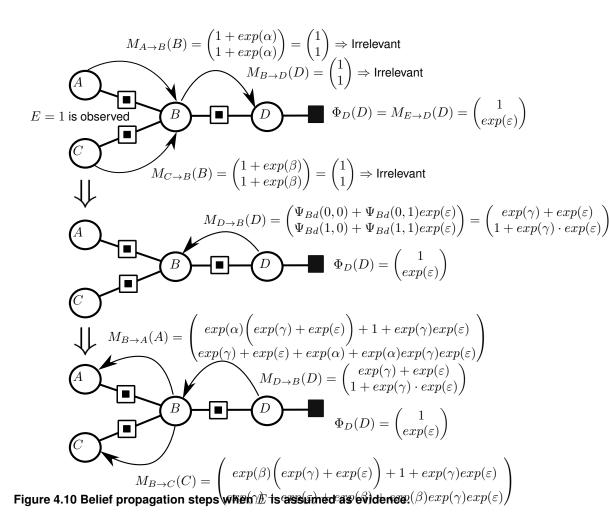
Part 01 considers a graph made of 5 variables with a Dom size equal to 2 and some simple exponential correlating factors, having different weights. The graph is reported in Figure 4.9, together with the weights of factor $\alpha, \beta, \gamma, \varepsilon$. At first stage, the evidence E=1 is assumed and the marginal probabilities of the other variables are computed with the message passing, whose steps are summarized in Figure 4.10. After the convergence of the message passing, the marginals of the variables are computed as similarly done for the previous examples. In a second phase, the evidence E=0 is assumed. The computation of the marginals is omitted since it is specular to the previous case.

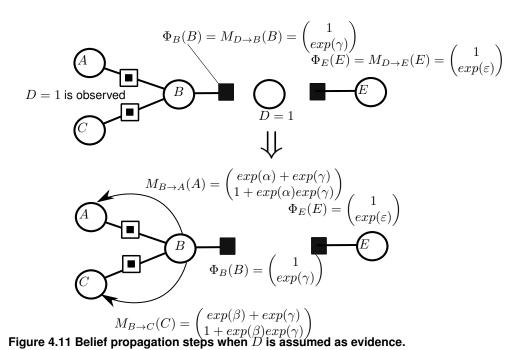
Finally, D=1 is assumed and a new belief propagation is done, whose computations are reported in Figure 4.11.

4.3.2 part 02

Part 02 considers the graph reported in Figure 4.12. All the variables in Figure 4.12 have a domain size equal to 2, and all the factors are simply correlating exponential shape, having a unitary weight. Variables v_1 , v_2 and v_3 are treated as evidences and the belief is propagated across the other ones, leading to the computation of the individual marginal probabilities. Since, the addressed structure is a politree (refer to Figure 2.6), the message passing algorithm converges within a finite number of steps.

In principle, the same approach followed in the previous examples can be followed to compute some theoretical results, with the aim of performing the comparisons. Anyway, for this kind of graph such an approach would be too complex. For this reason, results are compared with a Gibbs sampling approach: a series of samples $\mathcal{T}=\{T_1,\cdots,T_N\}$ are taken from the joint conditioned distribution $\mathbb{P}(T=v_{4,5,6,7,8,9,10,11,12,13}|v_{1,2,3})$. Then, to





Variables assumed as evidences

v_1 v_2 v_3 v_4 v_5 v_8 v_9 v_{10} v_{11} v_{12} v_{13}

Figure 4.12 The factor graph considered by part 02.

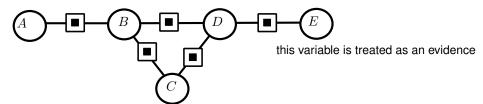


Figure 4.13 The factor graph considered by part 03.

evaluate the marginal probability $\mathbb{P}(v_i|v_{1,2,3})$ of a generic hidden variable v_i , the following empirical frequency is computed:

$$\mathbb{P}(v_i = v | v_{1,2,3}) = \frac{\sum_{T_j \in \mathcal{T}} L_{T_i}(T_j, v)}{N}$$
(4.19)

where $L_{Ti}(T_j, v)$ is an indicator function equal to 1 only for those samples for which v_i assumed a value equal to v.

4.3.3 part 03

Part 03 considers the graph reported in Figure 4.13. As for the example in the previous part, all variables are binary, and the potentials are simply exponential correlating with a unitary weight. However, this structure is loopy. E is treated as an evidence and the belief propagation is performed considering the loopy version of the message passing discussed in Section 2.2.2.

4.3.4 part 04

The last example in this series, considers a complex loopy graph, represented in Figure 4.14. As for other examples, all the variables are binary and the factors are exponential simply correlating with unitary weights. v_1 is assumed as evidence and the belief is propagated with the loopy version of message passing. Results are compared to the empirical frequencies obtained with a Gibbs sampler, as similarly done for the example of part 02.

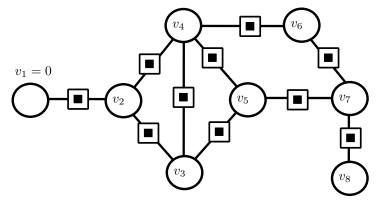


Figure 4.14 The factor graph considered by part 04.

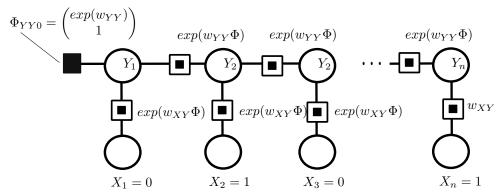


Figure 4.15 The chain structure considered by Sample 04.

4.4 Sample 04: Hidden Markov model like structure

The structure reported in Figure 4.15 is considered in this example. The reported chain is similar to those considered in Hidden Markov models, for which the chain of hidden variables $Y_{1,2,...}$ are connected to the chain of evidences $X_{1,2,...}$. The potential Φ_{YY0} , represents an a-priori knowledge about variable Y_1 . All the variables are binary and the potentials are simply correlating exponential potentials. In particular, the ones connecting the hidden variables have a weight equal to w_{YY} , while the ones connecting the evidences to the hidden set share a weight equal to w_{XY} . The evidences are set as indicated in Figure 4.15, i.e. 0 and 1 are alternated in the chain represented by $X_{1,2,...}$. The MAP estimation 2 of the hidden set (Section 2.3) is computed into two different situations:

- case a): $w_{XY} >> w_{YY}$
- case b): $w_{XY} << w_{YY}$

Here the point is that when considering case a), the information about the evidences and the correlations between $Y_{1,2,\cdots}$ and $X_{1,2,\cdots}$ is predominant. On the opposite, when dealing with case b), the correlations among the hidden variables as well as the prior knowledge about Y_0 is predominant. For this reason, for case a) the MAP estimation of the hidden variables is equal to $h^a_{MAP}=\{0,1,0,1,\cdots\}$, while for case b) the MAP estimation is equal to $h^b_{MAP}=\{0,0,0,0,\cdots\}$.

4.5 Sample 05: Matricial structure

The matrix-like structure reported in Figure 4.16 is considered in this example. The variables in the matrix have all the same domain size and the are correlated by the potentials populating the matrix, which are all simple exponential

²The Node_factory class is in charge of invoking the proper version of the message passing algorithm that leads to the MAP estimation computation.

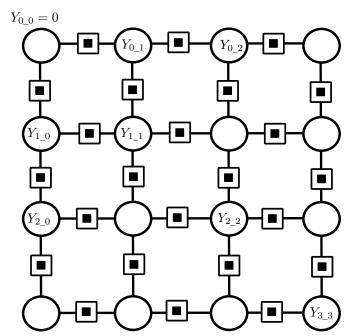


Figure 4.16 The matricial structure considered by Sample 05.

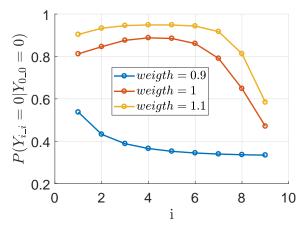


Figure 4.17 The marginals of variables Y_{i_i} , conditioned to $Y_{0_0}=0$ as evidence of the graph reported in Figure 4.16, when varying the weight of the correlating exponential factors involved in the structure.

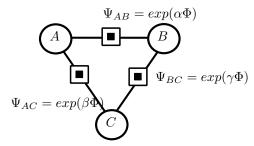


Figure 4.18 The graph considered by part 01.

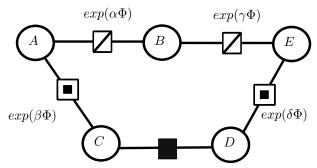


Figure 4.19 The graph considered by part 02.

correlating factors sharing the same weight. The example builds the matrix and then assumes $Y_{0_-0}=0$ as an evidence. Then, the marginals of the variables along the diagonal of the matrix, i.e. Y_{i_-i} , are evaluated. As can be seen, the marginal probability $\mathbb{P}(Y_{i_-i}=0|Y_{0_-0})$ decreases descending the diagonal. Figure 4.17 reports the results obtained when varying the weight of the correlating factors, on a matrix made of 10x10 variables having a Dom size equal to 3.

4.6 Sample 06: Learning, part A

The aim of this series of examples is to show how to perform the learning of factor graphs. In all the examples contained in this Section, learning is done with the following methodology. A Gibbs sampler is used to take samples from the joint distribution correlating all the variables in a model A. Model A is actually the model to learn. The training set obtained from model A, is used to train a model B. Model B has the same variables and factors of model A, but with different values for the free parameters $w_{1,2,\cdots}$ (Section 2.6). In this way, after having performed the learning, the value of the free parameters in model B will assume similar values to the ones in model A, showing the effectiveness of the functionalities contained in EFG. Clearly, this is not the approach followed in real applications, were the real coefficient of the model are unknown and only a training set of examples are available.

4.6.1 part 01

Part 01 considers the loopy graph reported in Figure 4.18. A,B and C are all binary variables, while Ψ_{AB},Ψ_{AC} and Ψ_{BC} are simple correlating exponential distributions having as weights, respectively, α,β and γ . Some samples are generated from the model with a Gibbs sampling, in order to use it later as a training set. All the weights in the model are set to 1, and tuned using a quasi newton trainer that consider the previously generated training set. The aim is to show that after training the values of the weights are similar to the initial ones.

4.6.2 part 02

Part 02 considers a structure made of both tunable and non-tunable factors. The considered structure is reported in Figure 4.19. Weights β and δ must be tuned through learning, as similarly described in Section 4.6.1, while α and γ are constant and known (refer also to the formalism described in Figure 2.2).

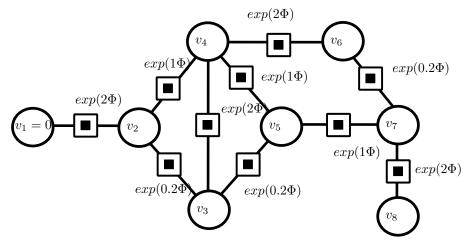


Figure 4.20 The graph considered by part 03.

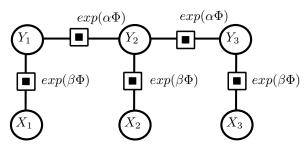


Figure 4.21 The graph considered by part 04.

4.6.3 part 03

Part 03 considers the loopy structure reported in Section 4.3.4. However, here instead of having constant exponential shapes, all the factors are made of tunable exponentials. The value assumed by the weight of model A (see the introduction of this Section) are showed in Figure 4.20. Weights are tuned through learning as similarly described in Section 4.6.1.

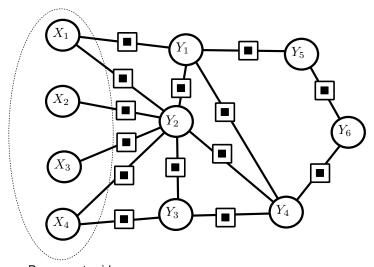
4.6.4 part 04

Part 04 considers the structure reported in Figure 4.21, for which all the potentials connecting pairs Y_{i-1}, Y_i share the same weight α , while the factors connecting pairs X_i, Y_i share the weight β . The approach described Weights are tuned through learning as similarly described in Section 4.6.1.

4.7 Sample 07: Learning, part B

The aim of this example is to show how the learning process can be done when dealing with Conditional random fields. In particular, the structure reported in Figure 4.22 is considered (values of the free parameters are not indicated, since the reader may refer to the sources provided).

The approach adopted is similar to the one followed in the previous series of example, considering a couple of model A and B (see the initial part of the previous Section). However, in this case we cannot simply draw samples from the joint distribution correlating the variables in the model, since such a distribution does not exists. Indeed, the conditional random field of Figure 4.22, models the conditional distribution of variables $Y_{1,2,...}$ w.r.t the evidences $X_{1,2,...}$ For this reason, all the possible combination of evidences are determined, considering all $x \in \{Dom(X_1) \cup Dom(X_2) \cup \cdots\}$. For each x, samples from the conditioned distribution $\mathbb{P}(Y_{1,2,...}|x)$ are taken with a Gibbs sampler. The entire population of samples determined is actually the training set adopted fro training the conditional random field in Figure 4.22.



Permanent evidences

Figure 4.22 The conditional random field considered in Sample 07.

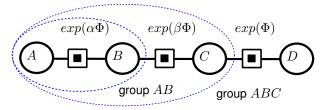


Figure 4.23 The chain considered in the example. All the underlying simple shapes are simple correlating.

4.8 Sample 08: Sub-graphing

4.8.1 part 01

The chain structure described in Figure 4.23 is addressed in this example. The sub-graphs containing variables A,B,C and A,B are built, in order to compute the joint marginal probability distributions of that two groups of variables.

The values are compared to the real ones, obtained by considering the joint distribution 3 of all the variables in the chain, which can be obtained by computing the energy function E, equation (2.6) (computations are here omitted for brevity). Knowing the joint distribution of a group of variables, the marginal distribution of a sub-group can be obtained by marginalization, equation (2.4):

$$\mathbb{P}(A=a,B=b,C=c) = \sum_{\tilde{d} \in Dom(D)} \mathbb{P}(A=a,B=b,C=c,D=\tilde{d})$$

$$\mathbb{P}(A=a,B=b) = \sum_{\tilde{c} \in Dom(C), \tilde{d} \in Dom(D)} \mathbb{P}(A=a,B=b,C=\tilde{c},D=\tilde{d})$$
(4.20)

Applying the above rules to the chain of Figure 4.23 leads to obtain the theoretical marginal distributions indicated in Figure 4.24.

4.8.2 part 02

The aim of this example is to show how sub-graphs (see Section 2.5) can be computed using SubGraph. The example starts building the structure described in Figure 4.25 (refer to the sources for the details regarding the

³Which is significantly time consuming to compute. For this reason, the SubGraph class is able to compute the marginals without explicitly compute the entire joint distribution of the variables in the model. Here we want just to compare the theoretical result with the one obtained by the SubGraph class.

A	B	$\mathbb{P}(A,B)$
0	0	$\frac{exp(\alpha)}{1+exp(\alpha)}$
0	1	$\frac{1}{1+exp(\alpha)}$
1	0	$\frac{\frac{1}{1+exp(\alpha)}}{exp(\alpha)}$
1	1	$\frac{exp(\alpha)}{1 + exp(\alpha)}$

A	$\mid B \mid$	C	$\mathbb{P}(A,B,C)$
0	0	0	$\frac{1}{Z_{ABC}} \cdot exp(\alpha)exp(\beta)$
0	1	0	$\frac{1}{Z_{ABC}}$
1	0	0	$\frac{1}{Z_{ABC}} \cdot exp(\beta)$
1	1	0	$\frac{1}{Z_{ABC}} \cdot exp(\alpha)$
0	0	1	$\frac{1}{Z_{ABC}} \cdot exp(\alpha)$
0	1	1	$\frac{1}{Z_{ABC}} \cdot exp(\beta)$
1	0	1	$\frac{1}{Z_{ABC}}$
1	1	1	$\frac{1}{Z_{ABC}} \cdot exp(\alpha)exp(\beta)$

Figure 4.24 Marginal probabilities of the sub-groups $\{A,B,C\}$ and $\{A,B\}$. The normalization coefficient Z_{ABC} is equal to $Z_{ABC}=2\bigg(1+exp(\alpha)+exp(\beta)+exp(\alpha)exp(\beta)\bigg)$.

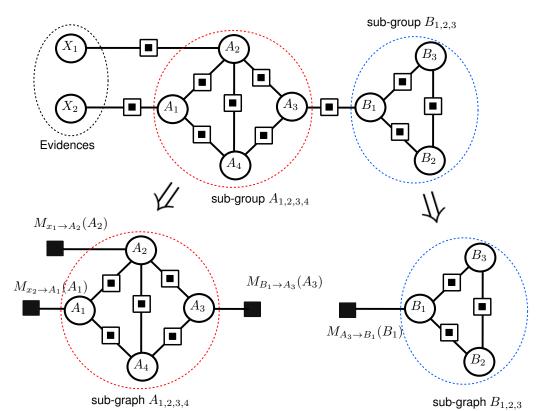


Figure 4.25 On the top, the graph considered by Sample 08, while on the bottom the sub-structures of the two groups $A_{1,2,3,4}$ ad $B_{1,2,3}$.

variables and factors involved in the structure) and assumes the following evidences: $X_1=0$ and $X_2=0$. Then, the two sub-graphs considering the sub-group of variables $A_{1,2,3,4}$ and $B_{1,2,3}$ are computed, refer to Figure 4.25. The marginal probabilities of some combinations for $A_{1,2,3,4}$ conditioned to the evidences $X_{1,2}$ are computed and compared with the empirical frequencies computed considering a samples set produced by a Gibb sampler on the entire graph: samples for $t=A_{1,2,3,4},B_{1,23}$ are drawn and the empirical frequencies of specific combinations of $A_{1,2,3,4}$ are computed as similarly done in 4.3.2. The same thing is done for the sub-graph $B_{1,2,3}$.

At a second stage, the evidences $X_{1,2}$ are changed and the sub-graphs, as well as the marginal probabilities, are consequently recomputed.

Chapter 5

Namespace Index

5.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

EFG														 										55
EFG::categor	ic													 					 					57
EFG::factor														 					 					58
EFG::io														 					 					59
EFG::io::json														 					 					60
EFG::io::xml														 					 					60
EFG::model														 					 					60
EFG::strct														 					 					61
FFG::train																								62

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Chapter 6

Hierarchical Index

6.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

EFG::factor::Factor::CloneTrasformedImagesTag
EFG::strct::PropagationResult::ClusterInfo
EFG::factor::Function::CombinationHasher
$EFG::Comparator < T > \dots \qquad \qquad$
EFG::strct::Node::Connection
EFG::strct::GibbsSampler::SamplerNode::DynamicDependency
EFG::io::json::Exporter
EFG::io::xml::Exporter
EFG::io::xml::ExportInfo
EFG::factor::Function
EFG::strct::StateAware::GraphState
EFG::categoric::Group
EFG::categoric::GroupRange
std::hash< EFG::categoric::Variable >
EFG::Hasher < T >
EFG::strct::HiddenCluster
EFG::factor::ImageFinder
EFG::factor::Immutable
EFG::factor::Factor
EFG::factor::UnaryFactor
EFG::factor::Evidence
EFG::factor::Indicator
EFG::factor::MergedUnaries
EFG::factor::MessageMAP
EFG::factor::MessageSUM
EFG::factor::FactorExponential
EFG::io::json::Importer
EFG::io::xml::Importer
EFG::factor::Function::Info
EFG::train::TrainSet::Iterator
EFG::strct::LoopyBeliefPropagationStrategy
EFG::strct::BaselineLoopyPropagator
EFG::detail::Merger < Separator >
· ·
EFG::factor::Mutable

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EFG::factor::Factor
EFG::detail::Node 10 EFG::strct::Node 10
EFG::detail::Node < Ts >
EFG::Visitor < Ts >
EFG::detail::NodeConst< T > 10 EFG::detail::NodeConst< Ts > 10
EFG::VisitorConst < Ts >
EFG::strct::StateAware::NodeLocation
EFG::strct::Pool
EFG::strct::PoolAware
EFG::strct::BeliefAware
EFG::strct::EvidenceRemover
EFG::model::ConditionalRandomField
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EFG::strct::EvidenceSetter
EFG::model::ConditionalRandomField
EFG::model::Graph
EFG::model::RandomField
EFG::strct::FactorsAware
EFG::model::ConditionalRandomField
EFG::strct::FactorsConstInserter
EFG::model::ConditionalRandomField
EFG::model::Graph
EFG::model::RandomField
EFG::train::FactorsTunableGetter
EFG::model::ConditionalRandomField
EFG::train::FactorsTunableInserter
EFG::model::ConditionalRandomField
EFG::strct::GibbsSampler
EFG::model::ConditionalRandomField
EFG::model::Graph
EFG::model::RandomField
EFG::strct::QueryManager
EFG::model::ConditionalRandomField
EFG::model::Graph
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EFG::strct::StateAware
EFG::strct::BeliefAware
EFG::strct::EvidenceRemover
EFG::strct::EvidenceSetter

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EFG::strct::QueryManager	11
EFG::strct::HiddenCluster::TopologyInfo	19
EFG::train::TrainInfo	19
EFG::train::TrainSet	19
EFG::train::Tuner	20
EFG::train::BaseTuner	ô5
EFG::train::BinaryTuner	ô7
EFG::train::UnaryTuner	
EFG::train::CompositeTuner	69
EFG::strct::UniformSampler	22
EFG::Cache < std::vector < EFG::strct::HiddenCluster::TopologyInfo > >	67
EFG::Cache < const EFG::factor::UnaryFactor >	67
EFG::Cache < T >	67
EFG::categoric::Variable	22

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Chapter 7

Class Index

7.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

EFG::strct::BaselineLoopyPropagator	65
EFG::train::BaseTuner	65
EFG::strct::BeliefAware	
The propagation relies on a concrete implementation of a BeliePropagationStrategy. In case no	
other is specified, a default one, BaselineBeliefPropagator, is instantiated and used internally.	
You can override this default propagator using setPropagationStrategy()	66
EFG::train::BinaryTuner	67
EFG::Cache < T >	67
EFG::factor::Factor::CloneTrasformedImagesTag	68
EFG::strct::PropagationResult::ClusterInfo	68
EFG::factor::Function::CombinationHasher	68
EFG::Comparator< T >	69
EFG::train::CompositeTuner	69
EFG::model::ConditionalRandomField	
Similar to RandomField, with the difference that the model structure is immutable after construc-	
tion. This applies also to the evidence set, which can't be changed over the time	70
EFG::strct::Node::Connection	72
EFG::strct::GibbsSampler::SamplerNode::DynamicDependency	73
EFG::Error	73
	73
EFG::strct::EvidenceRemover	74
EFG::strct::EvidenceSetter	75
EFG::io::json::Exporter	76
EFG::io::xml::Exporter	77
EFG::io::xml::ExportInfo	78
EFG::factor::Factor	79
EFG::factor::FactorExponential	
An exponential factor applies an exponential function to map the raw values inside the combina-	
tion map to the actual images. More precisely, given the weight w characterizing the factor the	
image value is obtained in this way: image = $exp(w * raw_value) \dots \dots \dots \dots \dots$	82
EFG::strct::FactorsAware	84
EFG::strct::FactorsConstGetter	84
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EFG::train::FactorsTunableGetter	86
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EFG::factor::Function	89
EFG::strct::GibbsSampler	
Refer also to https://en.wikipedia.org/wiki/Gibbs_sampling	91
EFG::model::Graph	
A simple graph object, that stores only const factors. Evidences may be changed over the time	92
EFG::strct::StateAware::GraphState	93
EFG::categoric::Group	
An ensemble of categoric variables. Each variable in the ensemble should have its own unique	
name	93
EFG::categoric::GroupRange	
This object allows to iterate all the elements in the joint domain of a group of variables, without	
precomputing all the elements in such domain. For example when having a domain made by	
variables = { A (size = 2), B (size = 3), C (size = 2) }, the elements in the joint domain that	
will be iterated are: $<0,0,0><0,0,1><0,1,0><0,1,1><0,2,0><0,2,1><1,0,0><1,0,1>$	
<1,1,0><1,1,1><1,2,0><1,2,1> After construction, the Range object starts to point to the	
first element in the joint domain <0,0,>. Then, when incrementing the object, the following	
element is pointed. When calling get() the current pointed element can be accessed	96
std::hash< EFG::categoric::Variable >	98
EFG::Hasher< T >	98
EFG::strct::HiddenCluster	
Clusters of hidden node. Each cluster is a group of connected hidden nodes. Nodes in different	
clusters are not currently connected, due to the model structure or the kind of evidences currently	00
applied	98
EFG::factor::ImageFinder	
An object used to search for the images associated to sub combinations that are part of a bigger one	00
EFG::factor::Immutable	99 100
EFG::io::json::Importer	100
EFG::io::xml::Importer	101
EFG::factor::Indicator	102
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EFG::train::TrainSet::Iterator	.00
Object able to iterate all the combinations that are part of a training set or a sub portion of it	103
EFG::strct::LoopyBeliefPropagationStrategy	105
EFG::factor::MergedUnaries	105
EFG::detail::Merger < Separator >	106
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EFG::factor::MessageSUM	107
EFG::factor::Mutable	107
EFG::detail::Node< T >	108
EFG::strct::Node	108
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Chapter 8

Namespace Documentation

8.1 EFG Namespace Reference

Namespaces

- · categoric
- factor
- io
- model
- strct
- train

Classes

- class Error
- class Cache
- struct Hasher
- struct Comparator
- struct Visitor
- struct VisitorConst

Typedefs

- template < typename K , typename V >
 using SmartMap = std::unordered_map < std::shared_ptr < K >, V, Hasher < K >, Comparator < K > >
 An unordered_map that stores as keys shared pointers that can't be null.
- template < typename T >
 using SmartSet = std::unordered_set < std::shared_ptr < T >, Hasher < T >, Comparator < T > >
 An unordered_set that stores shared pointers that can't be null.

Functions

- template<typename DownCastT, typename T, typename Predicate > void castConstAndUse (const T &subject, const Predicate &predicate)
- template<typename DownCastT, typename T, typename Predicate > void castAndUse (T &subject, const Predicate &predicate)
- template<typename K , typename V , typename Predicate > void for_each (SmartMap< K, V > &subject, const Predicate &pred)
- template<typename K , typename V , typename Predicate >
 void for_each (const SmartMap< K, V > &subject, const Predicate &pred)
- template<typename T, typename Predicate >
 void for_each (const SmartSet< T > &subject, const Predicate &pred)
- template<char Separator, typename... Args>
 void join (std::ostream &recipient, Args &&...args)
- template<char Separator, typename... Args> std::string join (Args &&...args)

8.1.1 Detailed Description

```
Author: Andrea Casalino Created: 01.01.2021 report any bug to andrecasa91@gmail.com.

Author: Andrea Casalino Created: 31.03.2022 report any bug to andrecasa91@gmail.com.
```

8.1.2 Typedef Documentation

8.1.2.1 SmartMap

```
template<typename K , typename V >
using EFG::SmartMap = typedef std::unordered_map<std::shared_ptr<K>, V, Hasher<K>, Comparator<K>
```

An unordered map that stores as keys shared pointers that can't be null.

Keys are hashed by hashing the elements wrapped inside the shared pointer.

Keys are compared by comparing the elements wrapped inside the shared pointer.

8.1.2.2 SmartSet

```
template<typename T >
using EFG::SmartSet = typedef std::unordered_set<std::shared_ptr<T>, Hasher<T>, Comparator<T>
>
```

An unordered_set that stores shared pointers that can't be null.

Elements are hashed by hashing the elements wrapped inside the shared pointer.

Elements are compared by comparing the elements wrapped inside the shared pointer.

8.2 EFG::categoric Namespace Reference

Classes

· class Group

An ensemble of categoric variables. Each variable in the ensemble should have its own unique name.

· class GroupRange

This object allows to iterate all the elements in the joint domain of a group of variables, without precomputing all the elements in such domain. For example when having a domain made by variables = $\{A \text{ (size = 2), } B \text{ (size = 3), } C \text{ (size = 2)} \}$, the elements in the joint domain that will be iterated are: <0.0,0.0 < 0.0,1.0 < 0.1,0.0 < 0.1,1.0 < 0.1,1.0 < 0.2,0.0 < 0.2,1.0 < 1.0,0.0 < 1.0,1.0 < 1.1,1.0 < 1.1,1.0 < 1.2,0.0 < 1.2,1.0 After construction, the Range object starts to point to the first element in the joint domain <math><0.0,.... Then, when incrementing the object, the following element is pointed. When calling get() the current pointed element can be accessed.

· class Variable

An object representing an immutable categoric variable.

Typedefs

- using VariablesSoup = std::vector< VariablePtr >
- using VariablesSet = SmartSet < Variable >
- using VariablePtr = std::shared ptr< Variable >

Functions

- VariablesSet to vars set (const VariablesSoup &soup)
- VariablesSet & operator== (VariablesSet &subject, const VariablesSet &to_remove)
 removes the second set from the first
- VariablesSet get_complementary (const VariablesSet &entire_set, const VariablesSet &subset)
- bool operator== (const GroupRange &a, const GroupRange &b)
- bool operator!= (const GroupRange &a, const GroupRange &b)
- template<typename Predicate >
 void for_each_combination (GroupRange &range, const Predicate &predicate)

Applies the passed predicate to all the elements that can be ranged using the passed range.

• VariablePtr make_variable (std::size_t size, const std::string &name)

8.2.1 Detailed Description

Author: Andrea Casalino Created: 01.01.2021

report any bug to andrecasa91@gmail.com.

8.2.2 Function Documentation

8.2.2.1 get_complementary()

Returns

the complementary group of the entire_set, i.e. returns entire_set \ subset

8.3 EFG::factor Namespace Reference

Classes

- · class UnaryFactor
- · class MergedUnaries
- class Evidence
- · class Indicator
- · class MessageSUM
- class MessageMAP
- · class Factor
- · class FactorExponential

An exponential factor applies an exponential function to map the raw values inside the combination map to the actual images. More precisely, given the weight w characterizing the factor the image value is obtained in this way: image = $\exp(w * raw_value)$

- class Function
- · class ImageFinder

An object used to search for the images associated to sub combinations that are part of a bigger one.

- · class Immutable
- · class Mutable

Typedefs

- using FunctionPtr = std::shared_ptr< Function >
- using ImmutablePtr = std::shared_ptr< Immutable >

Functions

• std::shared_ptr< const Function::Info > make_info (const categoric::Group &vars)

8.3.1 Detailed Description

```
Author: Andrea Casalino Created: 01.01.2021 report any bug to andrecasa91@gmail.com.

Author: Andrea Casalino Created: 31.03.2022 report any bug to andrecasa91@gmail.com.
```

8.4 EFG::io Namespace Reference

Namespaces

- json
- xml

Typedefs

- using **Getters** = std::tuple< const strct::StateAware *, const strct::FactorsConstGetter *, const train::FactorsTunableGetter *>
- using Inserters = std::pair< strct::FactorsConstInserter *, train::FactorsTunableInserter * >

Functions

template<typename ModelT >
 Getters castToGetters (ModelT &model)

• template<typename Model >

Inserters castToInserters (Model &model)

train::TrainSet import_train_set (const std::string &file_name)

Imports the training set from a file. The file should be a matrix of raw values. Each row represent a combination, i.e. a element of the training set to import.

8.4.1 Detailed Description

Author: Andrea Casalino Created: 01.01.2021

report any bug to andrecasa91@gmail.com.

8.4.2 Function Documentation

8.4.2.1 import train set()

Imports the training set from a file. The file should be a matrix of raw values. Each row represent a combination, i.e. a element of the training set to import.

Exceptions

	in	case the passed file is inexistent
ſ	in	case not all the combinations in file have the same size.

8.5 EFG::io::json Namespace Reference

Classes

- class Exporter
- · class Importer

8.5.1 Detailed Description

Author: Andrea Casalino Created: 01.01.2021

report any bug to andrecasa91@gmail.com.

8.6 EFG::io::xml Namespace Reference

Classes

- struct ExportInfo
- class Exporter
- · class Importer

8.6.1 Detailed Description

Author: Andrea Casalino Created: 01.01.2021

report any bug to andrecasa91@gmail.com.

8.7 EFG::model Namespace Reference

Classes

· class ConditionalRandomField

Similar to RandomField, with the difference that the model structure is immutable after construction. This applies also to the evidence set, which can't be changed over the time.

· class Graph

A simple graph object, that stores only const factors. Evidences may be changed over the time.

class RandomField

A complete undurected factor graph storing both constant and tunable factors. Evidences may be changed over the time.

8.7.1 Detailed Description

Author: Andrea Casalino Created: 01.01.2021

report any bug to andrecasa91@gmail.com.

8.8 EFG::strct Namespace Reference

Classes

- class BaselineLoopyPropagator
- · class EvidenceSetter
- · class EvidenceRemover
- · class FactorsConstGetter
- · class FactorsConstInserter
- class UniformSampler
- class GibbsSampler

Refer also to https://en.wikipedia.org/wiki/Gibbs_sampling.

- · class QueryManager
- struct Node
- struct HiddenCluster

Clusters of hidden node. Each cluster is a group of connected hidden nodes. Nodes in different clusters are not currently connected, due to the model structure or the kind of evidences currently applied.

- struct PropagationContext
- struct PropagationResult

a structure that can be exposed after having propagated the belief, providing info on the encountered structure.

- class LoopyBeliefPropagationStrategy
- · class BeliefAware

The propagation relies on a concrete implementation of a BeliePropagationStrategy. In case no other is specified, a default one, BaselineBeliefPropagator, is instantiated and used internally. You can override this default propagator using setPropagationStrategy(...).

- · class FactorsAware
- class Pool
- class PoolAware
- class StateAware

Typedefs

- using Nodes = SmartMap< categoric::Variable, std::unique_ptr< Node > >
- using HiddenClusters = std::list< HiddenCluster >
- using Evidences = SmartMap< categoric::Variable, std::size_t >
- using LoopyBeliefPropagationStrategyPtr = std::unique_ptr< LoopyBeliefPropagationStrategy >
- using **Task** = std::function< void(const std::size_t)>
- using Tasks = std::vector< Task >

Enumerations

enum class PropagationKind { SUM , MAP }

Functions

- template<typename MessageT >
 std::unique_ptr< MessageT > make_message (const factor::UnaryFactor &merged_unaries, const factor::Immutable &binary_factor)
- HiddenClusters compute_clusters (const std::unordered_set< Node * > &nodes)

8.8.1 Detailed Description

```
Author: Andrea Casalino Created: 01.01.2021 report any bug to andrecasa91@gmail.com.

Author: Andrea Casalino Created: 28.03.2022 report any bug to andrecasa91@gmail.com.
```

8.9 EFG::train Namespace Reference

Classes

- class FactorsTunableGetter
- · class FactorsTunableInserter
- struct TrainInfo
- class TrainSet
- class BaseTuner
- · class BinaryTuner
- · class CompositeTuner
- class Tuner
- class UnaryTuner

Typedefs

- using TunableClusters = std::vector< FactorExponentialPtr >
- using Combinations = std::vector< std::size_t >>
- using FactorExponentialPtr = std::shared_ptr< factor::FactorExponential >
- using TunerPtr = std::unique_ptr< Tuner >
- using **Tuners** = std::vector< TunerPtr >

Functions

- void set ones (FactorsTunableGetter &subject)
- void train_model (FactorsTunableGetter &subject, ::train::Trainer &trainer, const TrainSet &train_set, const TrainInfo &info=TrainInfo{})
- template<typename BasePred , typename CompositePred >
 void visitTuner (const Tuner *tuner, BasePred &&base, CompositePred &&composite)
- template<typename BasePred , typename CompositePred >
 void visitTuner (Tuner *tuner, BasePred &&base, CompositePred &&composite)

8.9.1 Detailed Description

```
Author: Andrea Casalino Created: 01.01.2021 report any bug to andrecasa91@gmail.com.
```

8.9.2 Function Documentation

8.9.2.1 set_ones()

Parameters

sets equal to 1 the weight of all the tunable clusters	
--	--

8.9.2.2 train_model()

Parameters

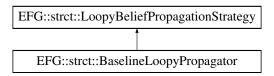
the	model to tune
the	training approach to adopt
the	train set to use

Chapter 9

Class Documentation

9.1 EFG::strct::BaselineLoopyPropagator Class Reference

Inheritance diagram for EFG::strct::BaselineLoopyPropagator:



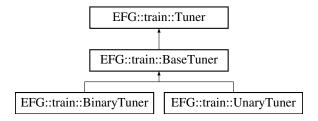
Public Member Functions

 bool propagateBelief (HiddenCluster &subject, PropagationKind kind, const PropagationContext &context, Pool &pool) final

The documentation for this class was generated from the following file:

9.2 EFG::train::BaseTuner Class Reference

Inheritance diagram for EFG::train::BaseTuner:



Public Member Functions

- FactorExponentialPtr getFactorPtr () const
- · const factor::FactorExponential & getFactor () const
- float getGradientAlpha (const TrainSet::Iterator &iter) final
- · void setWeight (float w) final
- · float getWeight () const final

Protected Member Functions

- BaseTuner (const FactorExponentialPtr &factor, const categoric::VariablesSoup &variables_in_model)
- float dotProduct (const std::vector< float > &prob) const

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/trainable/tuners/BaseTuner.h

9.3 EFG::strct::BeliefAware Class Reference

The propagation relies on a concrete implementation of a BeliePropagationStrategy. In case no other is specified, a default one, BaselineBeliefPropagator, is instantiated and used internally. You can override this default propagator using setPropagationStrategy(...).

#include <BeliefAware.h>

Inheritance diagram for EFG::strct::BeliefAware:



Public Member Functions

- const PropagationContext & getPropagationContext () const
- void setPropagationContext (const PropagationContext &ctxt)
- · bool hasPropagationResult () const
- const PropagationResult & getLastPropagationResult () const
- void **setLoopyPropagationStrategy** (LoopyBeliefPropagationStrategyPtr strategy)

Protected Member Functions

- void resetBelief ()
- bool wouldNeedPropagation (PropagationKind kind) const
- · void propagateBelief (PropagationKind kind)

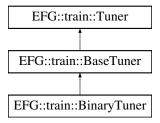
9.3.1 Detailed Description

The propagation relies on a concrete implementation of a BeliePropagationStrategy. In case no other is specified, a default one, BaselineBeliefPropagator, is instantiated and used internally. You can override this default propagator using setPropagationStrategy(...).

The documentation for this class was generated from the following file:

9.4 EFG::train::BinaryTuner Class Reference

Inheritance diagram for EFG::train::BinaryTuner:



Public Member Functions

- **BinaryTuner** (strct::Node &nodeA, strct::Node &nodeB, const std::shared_ptr< factor::FactorExponential > &factor, const categoric::VariablesSoup &variables in model)
- float getGradientBeta () final

Protected Attributes

- strct::Node & nodeA
- strct::Node & nodeB

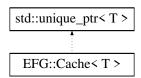
Additional Inherited Members

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/trainable/tuners/Binary
 — Tuner.h

9.5 EFG::Cache < T > Class Template Reference

Inheritance diagram for EFG::Cache< T >:



Public Member Functions

- T & reset (std::unique_ptr< T > new_value=nullptr)
- bool empty () const
- T * get ()
- const T * get () const

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/misc/Cache.h

9.6 EFG::factor::Factor::CloneTrasformedImagesTag Struct Reference

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Factor.h

9.7 EFG::strct::PropagationResult::ClusterInfo Struct Reference

Public Attributes

- bool tree_or_loopy_graph
- std::size t size

number of nodes that constitutes the sub-graph cluster.

The documentation for this struct was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/Types.h

9.8 EFG::factor::Function::CombinationHasher Struct Reference

Public Member Functions

std::size_t operator() (const std::vector< std::size_t > &comb) const

Public Attributes

std::shared ptr< const Info > info

The documentation for this struct was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Function.h

9.9 EFG::Comparator< T > Struct Template Reference

Public Member Functions

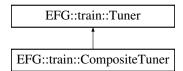
bool operator() (const std::shared_ptr< T > &a, const std::shared_ptr< T > &b) const

The documentation for this struct was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/misc/SmartPointerUtils.h

9.10 EFG::train::CompositeTuner Class Reference

Inheritance diagram for EFG::train::CompositeTuner:



Public Member Functions

- Tuners & getElements ()
- · const Tuners & getElements () const
- CompositeTuner (TunerPtr elementA, TunerPtr elementB)
- float getGradientAlpha (const TrainSet::Iterator &iter) final
- · float getGradientBeta () final
- · void setWeight (float w) final
- float getWeight () const final
- · void addElement (TunerPtr element)

The documentation for this class was generated from the following file:

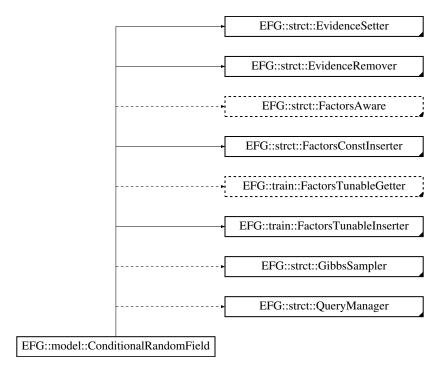
/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/trainable/tuners/Composite
 — Tuner.h

9.11 EFG::model::ConditionalRandomField Class Reference

Similar to RandomField, with the difference that the model structure is immutable after construction. This applies also to the evidence set, which can't be changed over the time.

#include <ConditionalRandomField.h>

Inheritance diagram for EFG::model::ConditionalRandomField:



Public Member Functions

- ConditionalRandomField (const ConditionalRandomField &o)
- ConditionalRandomField & operator= (const ConditionalRandomField &)=delete
- ConditionalRandomField (const RandomField &source, bool copy)

All the factors of the passed source are inserted/copied. The evidence set is deduced by the passed source.

void setEvidences (const std::vector< std::size t > &values)

Sets the new set of evidences.

• std::vector< std::vector< std::size_t >> makeTrainSet (const GibbsSampler::SamplesGenerationContext &context, float range_percentage=1.f, std::size_t threads=1)

Builds a training set for the conditioned model. Instead of using Gibbs sampler for a single combination of evidence, it tries to span all the possible combination of evidences and generate some samples conditioned to each of this evidences value. Then, gather results to build the training set. Actually, not ALL possible evidence are spwan if that would be too much computationally demanding. In such cases, simply pass a number lower than 1 as range_\cup percentage.

Protected Member Functions

• std::vector< float > getWeightsGradient (const train::TrainSet::Iterator &train set combinations) final

Additional Inherited Members

9.11.1 Detailed Description

Similar to RandomField, with the difference that the model structure is immutable after construction. This applies also to the evidence set, which can't be changed over the time.

9.11.2 Constructor & Destructor Documentation

9.11.2.1 ConditionalRandomField()

All the factors of the passed source are inserted/copied. The evidence set is deduced by the passed source.

Parameters

the	model to emulate for building the structure of this one.
then	passing true the factors are deep copied, while in the contrary case the smart pointers storing the
	factors of the source are copied and inserted.

Exceptions

in case the passed source has no evidences

9.11.3 Member Function Documentation

9.11.3.1 makeTrainSet()

Builds a training set for the conditioned model. Instead of using Gibbs sampler for a single combination of evidence, it tries to span all the possible combination of evidences and generate some samples conditioned to each of this evidences value. Then, gather results to build the training set. Actually, not ALL possible evidence are spwan if that would be too much computationally demanding. In such cases, simply pass a number lower than 1 as range_\circ percentage.

Parameters

information	used for samples generation
parameter	handling how many evidence values are accounted for the samples generation
the	number of threads to use for speeding up the process

9.11.3.2 setEvidences()

Sets the new set of evidences.

Parameters

the	new set of evidence values. The variables order is the same of the set obtained using	
	getObservedVariables().	

Exceptions

the	number of passed values does not match the number of evidences.
in	case some evidence values are inconsistent

The documentation for this class was generated from the following file:

 $• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/model/ConditionalRandom {\leftarrow} Field.h$

9.12 EFG::strct::Node::Connection Struct Reference

Public Attributes

- · factor::ImmutablePtr factor
- std::unique_ptr< const factor::UnaryFactor > message

The documentation for this struct was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/Types.h

9.13 EFG::strct::GibbsSampler::SamplerNode::DynamicDependency Struct Reference

Public Attributes

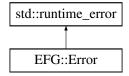
- categoric::VariablePtr sender
- const std::size_t * sender_value_in_combination
- · factor::ImmutablePtr factor

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/GibbsSampler.h

9.14 EFG::Error Class Reference

Inheritance diagram for EFG::Error:



Public Member Functions

• Error (const std::string &what)

Static Public Member Functions

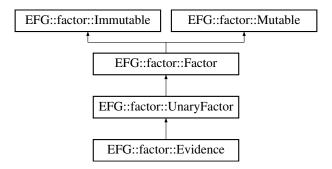
template<typename... Args>
 static Error make (Args &&...args)

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/Error.h

9.15 EFG::factor::Evidence Class Reference

Inheritance diagram for EFG::factor::Evidence:



Public Member Functions

Evidence (const Immutable &binary_factor, const categoric::VariablePtr &evidence_var, std::size_t evidence)

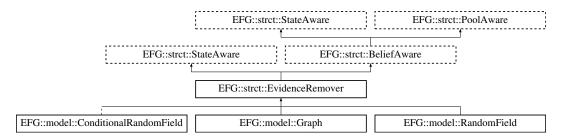
Additional Inherited Members

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/SpecialFactors.h

9.16 EFG::strct::EvidenceRemover Class Reference

Inheritance diagram for EFG::strct::EvidenceRemover:



Public Member Functions

- void removeEvidence (const categoric::VariablePtr &variable)
 update the evidence set by removing the specified variable.
- void removeEvidence (const std::string &variable)
 - similar to removeEvidence(const categoric::VariablePtr &), but passing the variable name, which is internally searched
- void removeEvidences (const categoric::VariablesSet &variables)
 - update the evidence set by removing all the specified variables.
- void removeEvidences (const std::unordered_set< std::string > &variables)
 similar to removeEvidences(const categoric::VariablesSet &), but passing the variable names, which are internally searched.
- · void removeAllEvidences ()

removes all the evidences currently set for this model.

Additional Inherited Members

9.16.1 Member Function Documentation

9.16.1.1 removeEvidence()

update the evidence set by removing the specified variable.

Parameters

the	involved variable
-----	-------------------

Exceptions

in case the passed variable is not part of the model.	
in	case the passed variable is not part of the current evidence set.

9.16.1.2 removeEvidences()

update the evidence set by removing all the specified variables.

Parameters

the involved variab	les
---------------------	-----

Exceptions

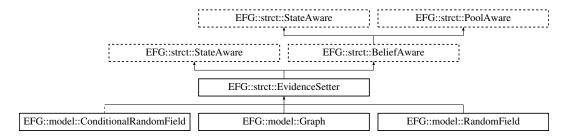
in	case one of the passed variable is not part of the model.
in	case one of the passed variable is not part of the current evidence set.

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/EvidenceManager. ←

9.17 EFG::strct::EvidenceSetter Class Reference

Inheritance diagram for EFG::strct::EvidenceSetter:



Public Member Functions

• void setEvidence (const categoric::VariablePtr &variable, std::size_t value)

update the evidence set with the specified new evidence. In case the involved variable was already part of the evidence set, the evidence value is simply updated. On the contrary case, the involved variable is moved into the evidence set, with the specified value.

• void setEvidence (const std::string &variable, std::size_t value)

Similar to setEvidence(const categoric::VariablePtr &, const std::size_t) , but passing the variable name, which is interally searched.

Additional Inherited Members

9.17.1 Member Function Documentation

9.17.1.1 setEvidence()

update the evidence set with the specified new evidence. In case the involved variable was already part of the evidence set, the evidence value is simply updated. On the contrary case, the involved variable is moved into the evidence set, with the specified value.

Parameters

the	involved variable
the	evidence value

Exceptions

in case the passed variable is not part of the model.

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/EvidenceManager. ←
 h

9.18 EFG::io::json::Exporter Class Reference

Static Public Member Functions

```
    template < typename Model >
        static nlohmann::json exportToJson (const Model &model)
        exports the model (variables and factors) into a json.
```

```
    template<typename Model >
        static void exportToFile (const Model &model, const std::filesystem::path &file_path)
        exports the model (variables and factors) into an json file
```

9.18.1 Member Function Documentation

9.18.1.1 exportToFile()

exports the model (variables and factors) into an json file

Parameters

the	model to export
the	file to generate storing the exported json

9.18.1.2 exportToJson()

exports the model (variables and factors) into a json.

Parameters

```
the model to export
```

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/io/json/Exporter.h

9.19 EFG::io::xml::Exporter Class Reference

Static Public Member Functions

- template < typename Model >
 static std::string exportToString (const Model & model, const std::string & model_name)
 exports the model (variables and factors) into a string, describing an xml.
- template < typename Model >
 static void exportToFile (const Model &model, const ExportInfo &info)
 exports the model (variables and factors) into an xml file

9.19.1 Member Function Documentation

9.19.1.1 exportToFile()

exports the model (variables and factors) into an xml file

Parameters

the	model to export
info	describing the xml to generate.

9.19.1.2 exportToString()

exports the model (variables and factors) into a string, describing an xml.

Parameters

the	model to export
the	model name to report in the xml

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/io/xml/Exporter.h

9.20 EFG::io::xml::ExportInfo Struct Reference

Public Attributes

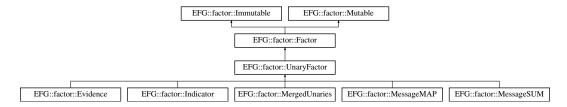
- · std::string file_path
- std::string model_name = "Model"

The documentation for this struct was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/io/xml/Exporter.h

9.21 EFG::factor::Factor Class Reference

Inheritance diagram for EFG::factor::Factor:



Classes

- struct CloneTrasformedImagesTag
- struct SimplyAntiCorrelatedTag
- struct SimplyCorrelatedTag

Public Member Functions

- Factor (const Factor &o)
- Factor (const categoric::Group &vars)

The variables set representing this factor is assumed equal to the passed one. No combinations is instanciated, implicitly assuming all the images equal to 0.

Factor (const Immutable &to_clone, CloneTrasformedImagesTag)

The variables set representing this factor is copied from the passed one. All the combinations instanciated in the passed factor, are copied in the combinations map of the factor to build, assigning the images values obtained by evaluating the passed factor.

Factor (const categoric::Group &vars, SimplyCorrelatedTag)

A simply correlating factor is built. All the variables in the passed group should have the same size. The images pertaining to the combinations having all values equal, are assumed equal to 1, all the others to 0. For instance assume to pass a variable set equal to: $\{<A: size 3>, <B: size 3>, <C: size 3>\}$. Then, the following combinations map is built: <0,0,0> -> 1<0,0,1> -> 0<0,0,2> -> 0.

· Factor (const categoric::Group &vars, SimplyAntiCorrelatedTag)

Similar to Factor(const categoric::Group &, const UseSimpleCorrelation &), but considering a simple anti-correlation. Therefore, to all combinations having all equal values, an image equal to 0 is assigned. All the other ones, are assigned a value equal to 1. For instance assume to pass a variable set equal to: $\{<A: size 2>, <B: size 2>\}$. Then, the following combinations map is built: <0,0,0> -> 0<0,0,1> -> 1<0,0,2> -> 1.

- Factor (const std::vector < const Immutable * > &factors)
- Factor cloneWithPermutedGroup (const categoric::Group &new_order) const

Generates a Factor similar to this one, permuting the group of variables.

Static Public Member Functions

template<typename... Immutables>
static Factor merge (const Immutable &first, const Immutable &second, const Immutables &...others)

Builds the factor by merging all the passed factors. The variables set representing this factor is obtained as the union of the all the variables sets of the passed distribution.

Protected Member Functions

Factor (FunctionPtr data)

9.21.1 Constructor & Destructor Documentation

9.21.1.1 Factor() [1/2]

A simply correlating factor is built. All the variables in the passed group should have the same size. The images pertaining to the combinations having all values equal, are assumed equal to 1, all the others to 0. For instance assume to pass a variable set equal to: $\{<A: size 3>, <B: size 3>, <C: size 3>\}$. Then, the following combinations map is built: <0,0,0>->1<0,0,1>->0<0,0,2>->0.

```
<0,1,0> -> 0 <0,1,1> -> 0 <0,1,2> -> 0
<0,2,0> -> 0 <0,2,1> -> 0 <0,2,2> -> 0
<1,0,0> -> 0 <1,0,1> -> 0 <1,0,2> -> 0
<1,1,0> -> 0 <1,1,1> -> 1 <1,1,2> -> 0
<1,2,0> -> 0 <1,2,1> -> 0 <1,2,2> -> 0
<2,0,0> -> 0 <2,0,1> -> 0 <2,0,2> -> 0
<2,1,0> -> 0 <2,1,1> -> 0 <2,1,2> -> 0
<2,2,0> -> 0 <2,1,1> -> 0 <2,1,2> -> 0
```

9.21.1.2 Factor() [2/2]

Similar to Factor(const categoric::Group &, const UseSimpleCorrelation &), but considering a simple anti-correlation. Therefore, to all combinations having all equal values, an image equal to 0 is assigned. All the other ones, are assigned a value equal to 1. For instance assume to pass a variable set equal to: $\{<A: size 2>\}$. Then, the following combinations map is built: <0,0,0>->0<0,0,1>->1<0,0,2>->1.

$$<0,1,0> -> 1 < 0,1,1> -> 1 < 0,1,2> -> 1$$
 $<0,2,0> -> 1 < 0,2,1> -> 1 < 0,2,2> -> 1$
 $<1,0,0> -> 1 < 1,0,1> -> 1 < 1,0,2> -> 1$
 $<1,1,0> -> 1 < 1,1,1> -> 0 < 1,1,2> -> 1$
 $<1,2,0> -> 1 < 1,2,1> -> 1 < 1,2,2> -> 1$
 $<2,0,0> -> 1 < 2,0,1> -> 1 < 2,0,2> -> 1$
 $<2,1,0> -> 1 < 2,1,1> -> 1 < 2,0,2> -> 1$
 $<2,1,0> -> 1 < 2,1,1> -> 1 < 2,2,2> -> 1$
 $<2,2,0> -> 1 < 2,2,1> -> 1 < 2,2,2> -> 0$

9.21.2 Member Function Documentation

9.21.2.1 cloneWithPermutedGroup()

Generates a Factor similar to this one, permuting the group of variables.

Parameters

the new variables group order to assume

Returns

the permuted variables factor

Exceptions

```
in case new_order.getVariablesSet() != this->getVariables().getVariablesSet()
```

The documentation for this class was generated from the following file:

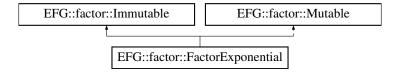
· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Factor.h

9.22 EFG::factor::FactorExponential Class Reference

An exponential factor applies an exponential function to map the raw values inside the combination map to the actual images. More precisely, given the weight w characterizing the factor the image value is obtained in this way: $image = exp(w * raw_value)$

```
#include <FactorExponential.h>
```

Inheritance diagram for EFG::factor::FactorExponential:



Public Member Functions

FactorExponential (const Factor &factor, float weigth)

The same variables describing the passed factor are assumed for the object to build. The map of combinations is built by iterating all the possible ones of the group of variables describing the passed factor. The raw values are computed by evaluating the passed factor over each possible combination.

· FactorExponential (const Factor &factor)

Same as FactorExponential(const Factor &, float), assuming weigth = 1.

- FactorExponential (const FactorExponential &o)
- void setWeight (float w)

sets the weight used by the exponential evaluator.

- float getWeight () const
- void replaceVariables (const categoric::VariablesSoup &new_variables)

Replaces the variables this distribution should refer to.

Protected Member Functions

• FactorExponential (FunctionPtr data)

9.22.1 Detailed Description

An exponential factor applies an exponential function to map the raw values inside the combination map to the actual images. More precisely, given the weight w characterizing the factor the image value is obtained in this way: $image = exp(w * raw_value)$

All the combinations are instanciated in the combinations map when building this object.

9.22.2 Constructor & Destructor Documentation

9.22.2.1 FactorExponential()

The same variables describing the passed factor are assumed for the object to build. The map of combinations is built by iterating all the possible ones of the group of variables describing the passed factor. The raw values are computed by evaluating the passed factor over each possible combination.

Parameters

ſ	the	baseline factor
	the	weight that will be considered by the exponential evaluator

9.22.3 Member Function Documentation

9.22.3.1 getWeight()

```
\verb|float EFG::factor::FactorExponential::getWeight () const|\\
```

Returns

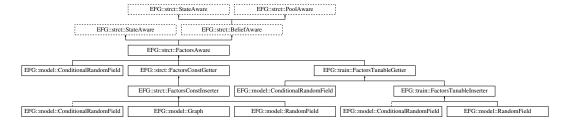
the weight used by the exponential evaluator.

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/FactorExponential.h

9.23 EFG::strct::FactorsAware Class Reference

Inheritance diagram for EFG::strct::FactorsAware:



Public Member Functions

• const auto & getAllFactors () const

Protected Member Functions

void addDistribution (const EFG::factor::ImmutablePtr &distribution)

9.23.1 Member Function Documentation

9.23.1.1 getAllFactors()

```
const auto& EFG::strct::FactorsAware::getAllFactors ( ) const [inline]
```

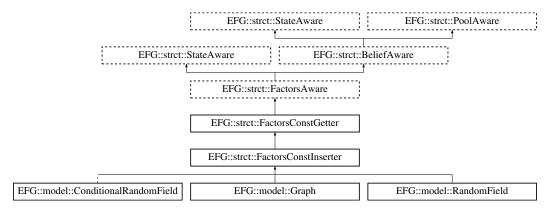
Returns

all the factors in the model, tunable and constant.

The documentation for this class was generated from the following file:

9.24 EFG::strct::FactorsConstGetter Class Reference

Inheritance diagram for EFG::strct::FactorsConstGetter:



Public Member Functions

• const auto & getConstFactors () const

Protected Attributes

 $\bullet \quad \text{std::unordered_set} < \text{factor::} \\ \text{ImmutablePtr} > \\ \textbf{const_factors}$

Additional Inherited Members

9.24.1 Member Function Documentation

9.24.1.1 getConstFactors()

```
const auto& EFG::strct::FactorsConstGetter::getConstFactors ( ) const [inline]
```

Returns

the collection of const factors that are part of the model. Tunable factors are not accounted in this collection.

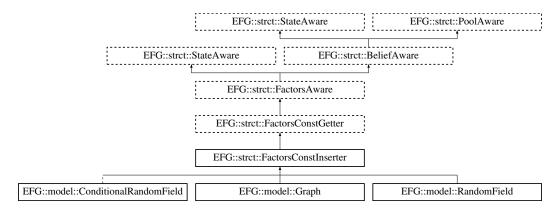
The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/FactorsConst

 Manager.h

9.25 EFG::strct::FactorsConstInserter Class Reference

Inheritance diagram for EFG::strct::FactorsConstInserter:



Public Member Functions

- void addConstFactor (const factor::ImmutablePtr &factor)
 add a shallow copy of the passed const factor to this model
- void copyConstFactor (const factor::Immutable &factor)
 add a deep copy of the passed const factor to this model
- template < typename DistributionIt > void absorbConstFactors (const DistributionIt & begin, const DistributionIt & end, bool copy)

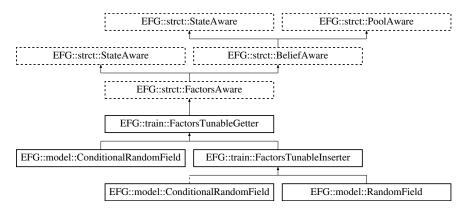
adds a collection of const factors of this model. Passing copy = true, deep copies are created and inserted in this model. Passing copy = false, shallow copies are created and inserted in this model.

Additional Inherited Members

The documentation for this class was generated from the following file:

9.26 EFG::train::FactorsTunableGetter Class Reference

Inheritance diagram for EFG::train::FactorsTunableGetter:



Public Member Functions

- const std::unordered_set< FactorExponentialPtr > & getTunableFactors () const
 Get the collections of tunable exponential factors.
- std::vector< std::variant< FactorExponentialPtr, TunableClusters >> getTunableClusters () const
 Get the clusters of tunable exponential factors. Elements in the same cluster, shares the weight.
- std::vector< float > getWeights () const
- void setWeights (const std::vector< float > &weights)
- std::vector< float > getWeightsGradient (const TrainSet::Iterator &train_set_combinations, std::size_← t threads=1)

Protected Member Functions

virtual std::vector< float > getWeightsGradient_ (const TrainSet::Iterator &train_set_combinations)=0

Protected Attributes

- std::unordered_set< FactorExponentialPtr > tunable_factors
- · Tuners tuners

9.26.1 Member Function Documentation

9.26.1.1 getWeights()

```
\mathtt{std}::\mathtt{vector} < \mathtt{float} > \mathtt{EFG}::\mathtt{train}::\mathtt{FactorsTunableGetter}::\mathtt{getWeights} ( ) const
```

Returns

the weights of all the tunable factors that are part of the model. The same order assumed by getTunableClusters() is assumed.

9.26.1.2 getWeightsGradient()

Returns

the gradients of the weights of all the tunable factors that are part of the model, w.r.t a certain training set. The same order assumed by getTunableClusters() is assumed.

Parameters

the	training set to use
the	number of threads to use for the gradient computation

9.26.1.3 setWeights()

Returns

sets the weights to use for of all the tunable factors that are part of the model. The same order assumed by getTunableClusters() should be assumed.

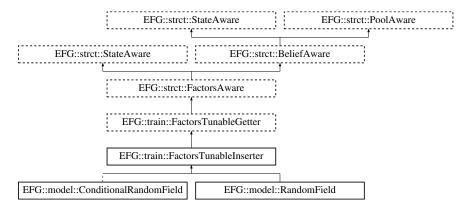
Exceptions

in case the number of specified weights is inconsistent

The documentation for this class was generated from the following file:

9.27 EFG::train::FactorsTunableInserter Class Reference

Inheritance diagram for EFG::train::FactorsTunableInserter:



Public Member Functions

- void addTunableFactor (const FactorExponentialPtr &factor, const std::optional < categoric::VariablesSet > &group sharing weight=std::nullopt)
 - add a shallow copy of the passed tunable expoenential factor to this model.
- void copyTunableFactor (const factor::FactorExponential &factor, const std::optional < categoric::VariablesSet
 &group sharing weight=std::nullopt)
 - add a deep copy of the passed tunable expoenential factor to this model.
- $\bullet \quad {\sf template}{<} {\sf typename FactorExponentialIt} >$
 - void absorbTunableFactors (const FactorExponentialIt &begin, const FactorExponentialIt &end, bool copy)
 - adds a collection of tunable expoenential factors of this model. Passing copy = true, deep copies are created and inserted in this model. Passing copy = false, shallow copies are created and inserted in this model.
- void absorbTunableClusters (const FactorsTunableGetter &source, bool copy)
 - adds a collection of tunable expoenential factors of this model, preserving the fact that elements in the same cluster should share the weight. Passing copy = true, deep copies are created and inserted in this model. Passing copy = false, shallow copies are created and inserted in this model.

Protected Member Functions

• Tuners::iterator findTuner (const categoric::VariablesSet &tuned_vars_group)

Additional Inherited Members

9.27.1 Member Function Documentation

9.27.1.1 addTunableFactor()

add a shallow copy of the passed tunable expoenential factor to this model.

Parameters

the	factor to insert
an	optional group of variables specifying the tunable factor that should share the weight with the one to
	insert. When passing a nullopt the factor will be inserted without sharing its weight.

9.27.1.2 copyTunableFactor()

add a deep copy of the passed tunable expoenential factor to this model.

Parameters

the	factor to insert
an	optional group of variables specifying the tunable factor that should share the weight with the one to
	insert. When passing a nullopt the factor will be inserted without sharing its weight.

The documentation for this class was generated from the following file:

9.28 EFG::factor::Function Class Reference

Classes

- struct CombinationHasher
- struct Info

Public Member Functions

- Function (const categoric::Group &variables)
- void clonelmages (const Function &o)
- void set (const std::vector< std::size t > &combination, float image)
- float **findTransformed** (const std::vector< std::size_t > &combination) const
- float findImage (const std::vector< std::size_t > &combination) const
- · void clear ()
- template<bool UseTransformed, typename Pred > void forEachCombination (Pred &&pred) const
- template<bool UseTransformed, typename Pred > void forEachNonNullCombination (Pred &&pred) const
- · const Info & getInfo () const
- · const auto & vars () const
- auto & vars ()

Protected Types

- using **SparseContainer** = std::unordered_map< std::vector< std::size_t >, float, CombinationHasher >
- using DenseContainer = std::vector< float >

Protected Member Functions

- virtual float transform (float input) const
 applies a specific function to obtain the image from the passed rwa value
- SparseContainer makeSparseContainer ()

Protected Attributes

- categoric::Group variables_
- std::shared ptr< const Info > info
- std::variant < SparseContainer, DenseContainer > data_

9.28.1 Member Function Documentation

9.28.1.1 transform()

applies a specific function to obtain the image from the passed rwa value

Parameters

the raw value to convert

Returns

the converted image

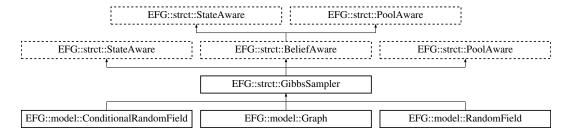
The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Function.h

9.29 EFG::strct::GibbsSampler Class Reference

```
Refer also to https://en.wikipedia.org/wiki/Gibbs_sampling.
#include <GibbsSampler.h>
```

Inheritance diagram for EFG::strct::GibbsSampler:



Classes

- struct SamplerNode
- · struct SamplesGenerationContext

Public Member Functions

Use Gibbs sampling approach to draw empirical samples. Values inside the returned combiantion are ordered with the same order used for the variables returned by getAllVariables().

Additional Inherited Members

9.29.1 Detailed Description

Refer also to https://en.wikipedia.org/wiki/Gibbs_sampling.

9.29.2 Member Function Documentation

9.29.2.1 makeSamples()

Use Gibbs sampling approach to draw empirical samples. Values inside the returned combiantion are ordered with the same order used for the variables returned by getAllVariables().

In case some evidences are set, their values will appear as is in the sampled combinations.

Parameters

number	parameters for the samples generation
number	of threads to use for the samples generation

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/GibbsSampler.h

9.30 EFG::model::Graph Class Reference

A simple graph object, that stores only const factors. Evidences may be changed over the time.

```
#include <Graph.h>
```

Inheritance diagram for EFG::model::Graph:



Public Member Functions

- Graph (const Graph &o)
- Graph & operator= (const Graph &)=delete
- void absorb (const strct::FactorsAware &to_absorb, bool copy)

Gather all the factors (tunable and constant) of another model and insert/copy them into this object.

Additional Inherited Members

9.30.1 Detailed Description

A simple graph object, that stores only const factors. Evidences may be changed over the time.

9.30.2 Member Function Documentation

9.30.2.1 absorb()

Gather all the factors (tunable and constant) of another model and insert/copy them into this object.

Parameters

the	model whose factors should be inserted/copied
wher	passing true the factors are deep copied, while in the contrary case shallow copies of the smart
	pointers are inserted into this model.

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/model/Graph.h

9.31 EFG::strct::StateAware::GraphState Struct Reference

Public Attributes

- categoric::VariablesSoup variables
- · Nodes nodes
- · HiddenClusters clusters
- · Evidences evidences

The documentation for this struct was generated from the following file:

9.32 EFG::categoric::Group Class Reference

An ensemble of categoric variables. Each variable in the ensemble should have its own unique name.

```
#include <Group.h>
```

Public Member Functions

- Group (const VariablesSoup &group)
- Group (const VariablePtr &var)
- template<typename... Vars>

Group (const VariablePtr &varA, const VariablePtr &varB, const Vars &...vars)

• void replace Variables (const Variables Soup &new_variables)

replaces the group of variables.

- bool **operator==** (const Group &o) const
- void add (const VariablePtr &var)
- std::size_t size () const
- const VariablesSoup & getVariables () const
- const VariablesSet & getVariablesSet () const

Protected Attributes

- VariablesSoup group
- VariablesSet group_sorted

9.32.1 Detailed Description

An ensemble of categoric variables. Each variable in the ensemble should have its own unique name.

9.32.2 Constructor & Destructor Documentation

9.32.2.1 Group() [1/3]

Parameters

the initial variables of the grou	р
-----------------------------------	---

Exceptions

when	passing an empty collection
when	passing a collection containing multiple times a certain variable

9.32.2.2 Group() [2/3]

Parameters

the initial variable to put in the group

9.32.2.3 Group() [3/3]

```
template<typename... Vars>
EFG::categoric::Group::Group (
```

```
const VariablePtr & varA,
const VariablePtr & varB,
const Vars &... vars ) [inline]
```

Parameters

the	first initial variable to put in the group
the	second initial variable to put in the group
all	the other initial variables

Exceptions

when	passing a collection containing multiple times a certain
------	--

9.32.3 Member Function Documentation

9.32.3.1 add()

Parameters

Exceptions

in case a variable with the same name is already part of the group

9.32.3.2 getVariables()

```
const VariablesSoup& EFG::categoric::Group::getVariables ( ) const [inline]
```

Returns

the ensamble of variables as an unsorted collection

9.32.3.3 getVariablesSet()

```
const VariablesSet& EFG::categoric::Group::getVariablesSet ( ) const [inline]
```

Returns

the ensamble of variables as a sorted collection

9.32.3.4 replaceVariables()

replaces the group of variables.

Exceptions

In case of size mismatch with the previous variables set: the sizes of the 2 groups should be the same and the elements in the same positions must have the same domain size

9.32.3.5 size()

```
std::size_t EFG::categoric::Group::size ( ) const
```

Returns

the size of the joint domain of the group. For example the group <A,B,C> with sizes <2,4,3> will have a joint domain of size 2x4x3 = 24

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/categoric/Group.h

9.33 EFG::categoric::GroupRange Class Reference

This object allows to iterate all the elements in the joint domain of a group of variables, without precomputing all the elements in such domain. For example when having a domain made by variables = { A (size = 2), B (size = 3), C (size = 2) }, the elements in the joint domain that will be iterated are: <0.0,0.0><0.0,1.0><0.1,0.0><0.1,1.0><0.1,1.0><0.1,1.0><0.1,1.0><1.1,1.0><1.2,0.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1

```
#include <GroupRange.h>
```

Public Types

- using iterator_category = std::input_iterator_tag
- using value_type = std::vector< std::size_t >
- using **pointer** = const std::vector< std::size t > *
- using reference = const std::vector< std::size_t > &

Public Member Functions

- GroupRange (const std::vector< std::size_t > &sizes)
- GroupRange (const Group &variables)
- GroupRange (const GroupRange &o)
- pointer **operator-**> () const
- reference operator* () const
- GroupRange & operator++ ()

Make the object to point to the next element in the joint domain.

• bool isEqual (const GroupRange &o) const

Static Public Member Functions

• static GroupRange end ()

9.33.1 Detailed Description

This object allows to iterate all the elements in the joint domain of a group of variables, without precomputing all the elements in such domain. For example when having a domain made by variables = { A (size = 2), B (size = 3), C (size = 2) }, the elements in the joint domain that will be iterated are: <0.0,0.0><0.0,1.0><0.1,0.0><0.1,1.0><0.1,1.0><0.1,1.0><1.1,1.0><1.1,1.0><1.2,0.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1.2,1.0><1

This object should be recognized by the compiler as an stl iterator.

9.33.2 Constructor & Destructor Documentation

9.33.2.1 GroupRange()

Parameters

the group of variables whose joint domain must be iterated

9.33.3 Member Function Documentation

9.33.3.1 operator++()

```
GroupRange& EFG::categoric::GroupRange::operator++ ( )
```

Make the object to point to the next element in the joint domain.

Exceptions

if the current pointed element is the last one.

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/categoric/GroupRange.h

9.34 std::hash< EFG::categoric::Variable > Struct Reference

Public Member Functions

• std::size_t operator() (const EFG::categoric::Variable &subject) const

The documentation for this struct was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/categoric/Variable.h

9.35 EFG::Hasher< T > Struct Template Reference

Public Member Functions

std::size_t operator() (const std::shared_ptr< T > &subject) const

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/misc/SmartPointerUtils.h

9.36 EFG::strct::HiddenCluster Struct Reference

Clusters of hidden node. Each cluster is a group of connected hidden nodes. Nodes in different clusters are not currently connected, due to the model structure or the kind of evidences currently applied.

```
#include <Types.h>
```

Classes

struct TopologyInfo

Public Member Functions

void updateConnectivity ()

Public Attributes

- std::unordered set< Node * > nodes
- Cache < std::vector < TopologyInfo > > connectivity

9.36.1 Detailed Description

Clusters of hidden node. Each cluster is a group of connected hidden nodes. Nodes in different clusters are not currently connected, due to the model structure or the kind of evidences currently applied.

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/Types.h

9.37 EFG::factor::ImageFinder Class Reference

An object used to search for the images associated to sub combinations that are part of a bigger one.

```
#include <ImageFinder.h>
```

Public Member Functions

- float findTransformed (const std::vector< std::size_t > &comb) const

 Searches for matches. For example assume having built this object with a bigger_group equal to <A,B,C,D> while the variables describing the distribution this finder refers to is equal to <B,D>. When passing a comb equal to <0,1,2,0>, this object searches for the immage associated to the sub combination <B,D> = <1,0>.
- float findImage (const std::vector< std::size_t > &comb) const

Friends

· class Immutable

9.37.1 Detailed Description

An object used to search for the images associated to sub combinations that are part of a bigger one.

9.37.2 Member Function Documentation

9.37.2.1 findTransformed()

Searches for matches. For example assume having built this object with a bigger_group equal to <A,B,C,D> while the variables describing the distribution this finder refers to is equal to <B,D>. When passing a comb equal to <0,1,2,0>, this object searches for the immage associated to the sub combination <B,D> = <1,0>.

Parameters

the combination of values referring to the bigger_group, which contains the sub combination to search.

Returns

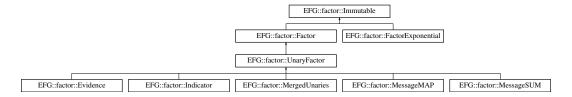
image associated to the passed combination

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/ImageFinder.h

9.38 EFG::factor::Immutable Class Reference

Inheritance diagram for EFG::factor::Immutable:



Public Member Functions

- Immutable (const Immutable &o)=delete
- Immutable & operator= (const Immutable &)=delete
- Immutable (Immutable &&o)=delete
- Immutable & operator= (Immutable &&)=delete
- · const auto & function () const
- ImageFinder makeFinder (const categoric::VariablesSoup &bigger_group) const
- std::vector< float > getProbabilities () const

Protected Member Functions

• Immutable (FunctionPtr data)

9.38.1 Member Function Documentation

9.38.1.1 getProbabilities()

```
std::vector<float> EFG::factor::Immutable::getProbabilities ( ) const
```

Returns

the probabilities associated to each combination in the domain, when assuming only the existance of this distribution. Such probabilities are actually the normalized images. The order of returned values, refer to the combinations that can be iterated by categoric::GroupRange on the variables representing this distribution.

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Immutable.h

9.39 EFG::io::json::Importer Class Reference

Static Public Member Functions

template<typename Model >
 static void importFromFile (Model &model, const std::filesystem::path &file_path)
 imports the structure (variables and factors) described in an xml file and add it to the passed model

 template < typename Model > static void importFromJson (Model & model, const nlohmann::json & source)

parse the model (variables and factors) described by the passed json and tries to add its factors to the passed model.

9.39.1 Member Function Documentation

9.39.1.1 importFromFile()

imports the structure (variables and factors) described in an xml file and add it to the passed model

Parameters

the	model receiving the parsed data
the	path storing the xml to import

9.39.1.2 importFromJson()

parse the model (variables and factors) described by the passed json and tries to add its factors to the passed model.

Parameters

recipient	of the model parsed from file
json	describing the model to parse and add to the passed one

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/io/json/Importer.h

9.40 EFG::io::xml::Importer Class Reference

Static Public Member Functions

template<typename Model >
 static void importFromFile (Model &model, const std::filesystem::path &file_path)
 parse the model (variables and factors) described by the specified file and tries to add its factors to the passed model.

9.40.1 Member Function Documentation

9.40.1.1 importFromFile()

parse the model (variables and factors) described by the specified file and tries to add its factors to the passed model.

Parameters

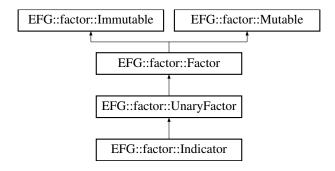
recipier		of the model parsed from file
	location	of the model to parse and add to the passed one

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/io/xml/Importer.h

9.41 EFG::factor::Indicator Class Reference

Inheritance diagram for EFG::factor::Indicator:



Public Member Functions

Indicator (const categoric::VariablePtr &var, std::size_t value)

Additional Inherited Members

The documentation for this class was generated from the following file:

 $\bullet \ / home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/SpecialFactors.h$

9.42 EFG::factor::Function::Info Struct Reference

Public Attributes

- std::vector< std::size t > sizes
- std::size_t totCombinations
- std::size_t critical_size

The documentation for this struct was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Function.h

9.43 EFG::train::TrainSet::Iterator Class Reference

an object able to iterate all the combinations that are part of a training set or a sub portion of it.

#include <TrainSet.h>

Public Member Functions

Iterator (const TrainSet &subject, float percentage)
 involved train set

template<typename Predicate >
 void forEachSample (const Predicate &pred) const

• std::size_t size () const

9.43.1 Detailed Description

an object able to iterate all the combinations that are part of a training set or a sub portion of it.

9.43.2 Constructor & Destructor Documentation

9.43.2.1 Iterator()

involved train set

Parameters

the

percentage of combinations to extract from the passed subject. Passing a value equal to 1, means to use all the combinations of the passed subject.

9.43.3 Member Function Documentation

9.43.3.1 size()

```
std::size_t EFG::train::TrainSet::Iterator::size ( ) const
```

Returns

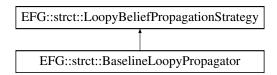
number of combinations considered by this train set iterator.

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/trainable/TrainSet.h

9.44 EFG::strct::LoopyBeliefPropagationStrategy Class Reference

Inheritance diagram for EFG::strct::LoopyBeliefPropagationStrategy:



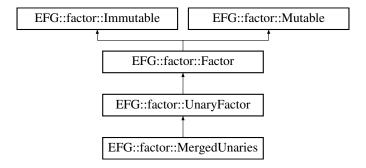
Public Member Functions

 virtual bool propagateBelief (HiddenCluster &subject, PropagationKind kind, const PropagationContext &context, Pool &pool)=0

The documentation for this class was generated from the following file:

9.45 EFG::factor::MergedUnaries Class Reference

Inheritance diagram for EFG::factor::MergedUnaries:



Public Member Functions

- MergedUnaries (const categoric::VariablePtr &var)
- MergedUnaries (const std::vector< const Immutable * > &factors)
- void merge (const Immutable &to_merge)
- void normalize ()

Additional Inherited Members

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/SpecialFactors.h

9.46 EFG::detail::Merger < Separator > Struct Template Reference

Public Member Functions

- template<typename Last > void join_ (Last &&last)
- template<typename First, typename... Args> void join_ (First &&first, Args &&...args)

Public Attributes

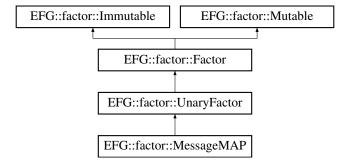
std::ostream & recipient

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/misc/Strings.h

9.47 EFG::factor::MessageMAP Class Reference

Inheritance diagram for EFG::factor::MessageMAP:



Public Member Functions

• MessageMAP (const UnaryFactor &merged_unaries, const Immutable &binary_factor)

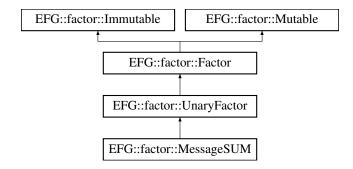
Additional Inherited Members

The documentation for this class was generated from the following file:

 $\bullet \ / home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/SpecialFactors.h$

9.48 EFG::factor::MessageSUM Class Reference

Inheritance diagram for EFG::factor::MessageSUM:



Public Member Functions

MessageSUM (const UnaryFactor &merged_unaries, const Immutable &binary_factor)

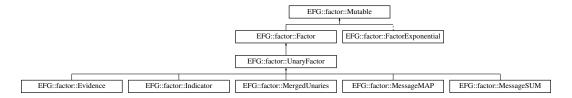
Additional Inherited Members

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/SpecialFactors.h

9.49 EFG::factor::Mutable Class Reference

Inheritance diagram for EFG::factor::Mutable:



Public Member Functions

- Mutable (const Mutable &o)=delete
- Mutable & operator= (const Mutable &)=delete
- Mutable (Mutable &&o)=delete
- Mutable & operator= (Mutable &&)=delete
- void set (const std::vector< std::size_t > &comb, float value)

sets the raw value of the image related to the passed combination. In case the combination is currently not part of the distribution, it is added to the combinations map, with the passed raw image value.

· void clear ()

Removes all the combinations from the combinations map.

void replaceVariables (const categoric::VariablesSoup &new_variables)

Replaces the variables this distribution should refer to.

Protected Member Functions

- Mutable (FunctionPtr data)
- auto & functionMutable ()

9.49.1 Member Function Documentation

9.49.1.1 set()

sets the raw value of the image related to the passed combination. In case the combination is currently not part of the distribution, it is added to the combinations map, with the passed raw image value.

Parameters

the	combination whose raw image must be set
the	raw image value to assume

Exceptions

a negative number for value	passing
-----------------------------	---------

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Mutable.h

9.50 EFG::detail::Node < T > Struct Template Reference

Public Attributes

Predicate < T > pred_

The documentation for this struct was generated from the following file:

 $\bullet \ \ / home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/misc/Visitor.h$

9.51 EFG::strct::Node Struct Reference

Classes

struct Connection

Public Member Functions

• void updateMergedUnaries ()

Static Public Member Functions

- static std::pair < Connection *, Connection * > activate (Node &a, Node &b, factor::ImmutablePtr factor)
- static std::pair< Connection *, Connection * > disable (Node &a, Node &b, factor::ImmutablePtr factor=nullptr)

Public Attributes

- · categoric::VariablePtr variable
- std::unordered_map< Node *, Connection > active_connections
- std::unordered_map< Node *, Connection > disabled_connections
- std::vector< factor::ImmutablePtr > unary_factors
- Cache < const factor::UnaryFactor > merged_unaries

The documentation for this struct was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/Types.h

9.52 EFG::detail::NodeConst< T > Struct Template Reference

Public Attributes

PredicateConst< T > pred_

The documentation for this struct was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/misc/Visitor.h

9.53 EFG::strct::StateAware::NodeLocation Struct Reference

Public Attributes

- Node * node
- std::variant< HiddenClusters::iterator, Evidences::iterator > location

The documentation for this struct was generated from the following file:

9.54 EFG::strct::Pool Class Reference

Public Member Functions

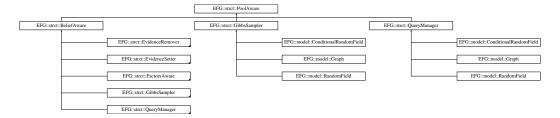
- Pool (std::size_t size)
- void parallelFor (const Tasks &tasks)
- std::size_t size () const

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/bases/PoolAware.h

9.55 EFG::strct::PoolAware Class Reference

Inheritance diagram for EFG::strct::PoolAware:



Classes

· class ScopedPoolActivator

Protected Member Functions

- · void resetPool ()
- Pool & getPool ()
- void **setPoolSize** (std::size_t new_size)

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/bases/PoolAware.h

9.56 EFG::strct::PropagationContext Struct Reference

Public Attributes

std::size_t max_iterations_loopy_propagation
 maximum number of iterations to use when trying to calibrate a loopy graph

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/Types.h

9.57 EFG::strct::PropagationResult Struct Reference

a structure that can be exposed after having propagated the belief, providing info on the encountered structure.

```
#include <Types.h>
```

Classes

struct ClusterInfo

Public Attributes

- PropagationKind propagation_kind_done
- bool was completed
- std::vector < ClusterInfo > structures

9.57.1 Detailed Description

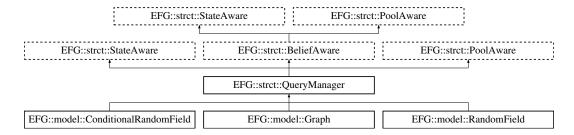
a structure that can be exposed after having propagated the belief, providing info on the encountered structure.

The documentation for this struct was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/Types.h

9.58 EFG::strct::QueryManager Class Reference

Inheritance diagram for EFG::strct::QueryManager:



Public Member Functions

- std::vector< float > getMarginalDistribution (const categoric::VariablePtr &var, std::size_t threads=1)
- std::vector < float > getMarginalDistribution (const std::string &var, std::size_t threads=1)
 same as getMarginalDistribution(const categoric::VariablePtr &, std::size_t), but passing the name of the variable, which is internally searched.
- factor::Factor getJointMarginalDistribution (const categoric::Group &subgroup, std::size t threads=1)
- factor::Factor getJointMarginalDistribution (const std::vector< std::string > &subgroup, std::size_t threads=1) same as getJointMarginalDistribution(const categoric::VariablesSet &, std::size_t), but passing the names of the variables, which are internally searched.
- std::size t getMAP (const categoric::VariablePtr &var, std::size t threads=1)
- std::size_t getMAP (const std::string &var, std::size_t threads=1)

 same as getMAP(const categoric::VariablePtr &, std::size_t), but passing the name of the variable, which is internally searched.
- std::vector< size_t > getHiddenSetMAP (std::size_t threads=1)

Additional Inherited Members

9.58.1 Member Function Documentation

9.58.1.1 getHiddenSetMAP()

Returns

the Maximum a Posteriori estimation of the hidden variables, conditioned to the last set of evidences. Values are ordered with the same order used by the set of variables returned in getHiddenVariables()

Parameters

the number of threads to use for propagating the belief before returning the result.

9.58.1.2 getJointMarginalDistribution() [1/2]

Returns

a factor representing the joint distribution of the subgraph described by the passed set of variables.

Parameters

the	involved variables
the	number of threads to use for propagating the belief before returning the result.

Exceptions

when	some of the passed variable names are not found
------	---

9.58.1.3 getJointMarginalDistribution() [2/2]

```
factor::Factor EFG::strct::QueryManager::getJointMarginalDistribution (
```

```
const std::vector< std::string > & subgroup,
std::size_t threads = 1 )
```

same as getJointMarginalDistribution(const categoric::VariablesSet &, std::size_t), but passing the names of the variables, which are internally searched.

Exceptions

```
in case the passed set of variables is not representative of a valid group
```

9.58.1.4 getMAP()

Returns

the Maximum a Posteriori estimation of a specific variable in the model, conditioned to the last set of evidences.

Parameters

the	involved variable]
the	number of threads to use for propagating the belief before returning the result.]

Exceptions

when	the passed variable name is not found
------	---------------------------------------

9.58.1.5 getMarginalDistribution()

Returns

the marginal probabilty of the passed variable, i.e. P(var|observations), conditioned to the last set of evidences.

Parameters

the	involved variable
the	number of threads to use for propagating the belief before returning the result.

Exceptions

when the passed variable name is not found

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/QueryManager.h

9.59 EFG::model::RandomField Class Reference

A complete undurected factor graph storing both constant and tunable factors. Evidences may be changed over the time.

#include <RandomField.h>

Inheritance diagram for EFG::model::RandomField:



Public Member Functions

- · RandomField (const RandomField &o)
- RandomField & operator= (const RandomField &)=delete
- void absorb (const strct::FactorsAware &to absorb, bool copy)

Gather all the factors (tunable and constant) of another model and insert/copy them into this object. Tunable factors (Exponential non constant) are recognized and inserted/copied using the train::FactorsTunableAdder interface. All the others inserted/copied using the strct::FactorsAdder interface.

Protected Member Functions

• std::vector< float > getWeightsGradient_ (const train::TrainSet::Iterator &train_set_combinations) final

Additional Inherited Members

9.59.1 Detailed Description

A complete undurected factor graph storing both constant and tunable factors. Evidences may be changed over the time.

9.59.2 Member Function Documentation

9.59.2.1 absorb()

Gather all the factors (tunable and constant) of another model and insert/copy them into this object. Tunable factors (Exponential non constant) are recognized and inserted/copied using the train::FactorsTunableAdder interface. All the others inserted/copied using the strct::FactorsAdder interface.

Parameters

the	model whose factors should be inserted/copied
when	passing true the factors are deep copied, while in the contrary case shallow copies of the smart
	pointers storing the factors are inserted into this model.

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/model/RandomField.h

9.60 EFG::strct::GibbsSampler::SamplerNode Struct Reference

Classes

struct DynamicDependency

Public Member Functions

bool noChangingDeps (const std::unordered set< const std::size t * > &will change) const

Public Attributes

- std::size t * value in combination
- const factor::UnaryFactor * static_dependencies
- std::vector< DynamicDependency > dynamic_dependencies

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/GibbsSampler.h

9.61 EFG::strct::GibbsSampler::SamplesGenerationContext Struct Reference

Public Attributes

- std::size_t samples_number
- std::optional < std::size_t > delta_iterations

number of iterations used to evolve the model between the drawing of one sample and another

 $\bullet \quad \mathsf{std} :: \mathsf{optional} < \mathsf{std} :: \mathsf{size_t} > \mathsf{seed}$

sets the seed of the random engine. Passing a nullopt will make the sampler to generate a random seed by using the current time.

std::optional < std::size_t > transient

number of samples to discard before actually starting the sampling procedure.

9.61.1 Member Data Documentation

9.61.1.1 transient

std::optional<std::size_t> EFG::strct::GibbsSampler::SamplesGenerationContext::transient

number of samples to discard before actually starting the sampling procedure.

When nothing is specified, 10 times delta_iterations is assumed.

The documentation for this struct was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/GibbsSampler.h

9.62 EFG::strct::PoolAware::ScopedPoolActivator Class Reference

Public Member Functions

• ScopedPoolActivator (PoolAware &subject, std::size_t new_size)

The documentation for this class was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/bases/PoolAware.h

9.63 EFG::factor::Factor::SimplyAntiCorrelatedTag Struct Reference

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Factor.h

9.64 EFG::factor::Factor::SimplyCorrelatedTag Struct Reference

The documentation for this struct was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/factor/Factor.h

9.65 EFG::strct::StateAware Class Reference

Inheritance diagram for EFG::strct::StateAware:



Classes

- · struct GraphState
- struct NodeLocation

Public Member Functions

- const auto & getAllVariables () const
- categoric::VariablesSet getHiddenVariables () const
- categoric::VariablesSet getObservedVariables () const
- · const auto & getEvidences () const
- categoric::VariablePtr findVariable (const std::string &name) const
- StateAware (const StateAware &)=delete
- StateAware & operator= (const StateAware &)=delete
- StateAware (StateAware &&)=delete
- StateAware & operator= (StateAware &&)=delete

Protected Member Functions

- const GraphState & state () const
- GraphState & stateMutable ()
- std::optional < NodeLocation > locate (const categoric::VariablePtr &var) const
- std::optional < NodeLocation > locate (const std::string &var_name) const

9.65.1 Member Function Documentation

9.65.1.1 findVariable()

Returns

the variable in the model with the passed name

Exceptions

in case no variable with the specified name exists in this model

table the variable that the opening hame oxide in the model

9.65.1.2 getAllVariables()

```
const auto& EFG::strct::StateAware::getAllVariables ( ) const [inline]
```

Returns

all the variables that are part of the model.

9.65.1.3 getEvidences()

```
const auto& EFG::strct::StateAware::getEvidences ( ) const [inline]
```

Returns

all the variables defining the evidence set, together with the associated values

9.65.1.4 getHiddenVariables()

```
\verb|categoric::VariablesSet| EFG::strct::StateAware::getHiddenVariables () const|
```

Returns

all the variables defining the hidden set of variables

9.65.1.5 getObservedVariables()

```
categoric::VariablesSet EFG::strct::StateAware::getObservedVariables ( ) const
```

Returns

all the variables defining the evidence set

The documentation for this class was generated from the following file:

9.66 EFG::strct::HiddenCluster::TopologyInfo Struct Reference

Public Member Functions

- · bool canUpdateMessage () const
- std::optional< float > updateMessage (PropagationKind kind)

Public Attributes

- Node * sender
- Node::Connection * connection
- std::vector< const Node::Connection * > dependencies

The documentation for this struct was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/Types.h

9.67 EFG::train::TrainInfo Struct Reference

Public Attributes

• std::size t threads = 1

Number of threads to use for the training procedure.

float stochastic_percentage = 1.f

1 means actually to use all the train set, adopting a classical gradient based approach. A lower value implies to a stochastic gradient based approach.

The documentation for this struct was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/trainable/ModelTrainer.h

9.68 EFG::train::TrainSet Class Reference

Classes

· class Iterator

an object able to iterate all the combinations that are part of a training set or a sub portion of it.

Public Member Functions

- TrainSet (const std::vector< std::vector< std::size_t >> &combinations)
- const auto & getCombinations () const
- Iterator makelterator () const
- · Iterator makeSubSetIterator (float percentage) const

9.68.1 Constructor & Destructor Documentation

9.68.1.1 TrainSet()

Parameters

the	set of combinations that will be part of the train set.	Ì
-----	---	---

Exceptions

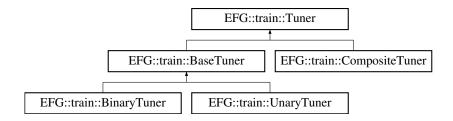
if	the combinations don't have all the same size
if	the combinations container is empty

The documentation for this class was generated from the following file:

 $\bullet \ / home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/trainable/TrainSet.h$

9.69 EFG::train::Tuner Class Reference

Inheritance diagram for EFG::train::Tuner:



Public Member Functions

- virtual float getGradientAlpha (const TrainSet::Iterator &iter)=0
- virtual float getGradientBeta ()=0
- virtual void setWeight (float w)=0
- virtual float getWeight () const =0

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/trainable/tuners/Tuner.h

9.70 EFG::factor::UnaryFactor Class Reference

Inheritance diagram for EFG::factor::UnaryFactor:



Public Member Functions

- const categoric::VariablePtr & getVariable () const
- float diff (const UnaryFactor &o) const

Protected Member Functions

• UnaryFactor (FunctionPtr data)

Protected Attributes

• categoric::VariablePtr variable

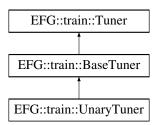
Additional Inherited Members

The documentation for this class was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/SpecialFactors.h

9.71 EFG::train::UnaryTuner Class Reference

Inheritance diagram for EFG::train::UnaryTuner:



Public Member Functions

- UnaryTuner (strct::Node &node, const std::shared_ptr< factor::FactorExponential > &factor, const categoric::VariablesSoup &variables_in_model)
- float getGradientBeta () final

Protected Attributes

strct::Node & node

Additional Inherited Members

The documentation for this class was generated from the following file:

/home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/trainable/tuners/Unary
 — Tuner.h

9.72 EFG::strct::UniformSampler Class Reference

Public Member Functions

- std::size t sampleFromDiscrete (const std::vector< float > &distribution) const
- void resetSeed (std::size_t newSeed)

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/structure/GibbsSampler.h

9.73 EFG::categoric::Variable Class Reference

An object representing an immutable categoric variable.

```
#include <Variable.h>
```

Public Member Functions

- Variable (std::size_t size, const std::string &name)
- std::size_t size () const
- const std::string & name () const
- bool operator== (const Variable &o) const

Protected Attributes

- · const size_t size_
- const std::string name_

9.73.1 Detailed Description

An object representing an immutable categoric variable.

9.73.2 Constructor & Destructor Documentation

9.73.2.1 Variable()

Parameters

domain	size of this variable	
name	used to label this varaible.	

Exceptions

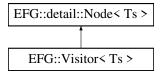
passing	0 as size
passing	an empty string as name

The documentation for this class was generated from the following file:

· /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/categoric/Variable.h

9.74 EFG::Visitor < Ts > Struct Template Reference

Inheritance diagram for EFG::Visitor< Ts >:



Public Member Functions

- Visitor (detail::Predicate < Ts > &&...predicates)
- template < typename T >
 void operator() (T & subject) const
- void visit (std::variant< Ts... > &subject) const
- template<typename T > void set (detail::Predicate< T > &&last)

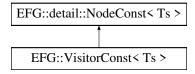
Additional Inherited Members

The documentation for this struct was generated from the following file:

• /home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/misc/Visitor.h

9.75 EFG::VisitorConst< Ts > Struct Template Reference

Inheritance diagram for EFG::VisitorConst< Ts >:



Public Member Functions

- VisitorConst (detail::PredicateConst< Ts > &&...predicates)
- template<typename T > void operator() (const T &subject) const
- void visit (const std::variant< Ts... > &subject) const
- $\label{eq:typename} \begin{array}{ll} \bullet & \text{template} < \text{typename T , typename... Tothers} \\ & \text{void } \textbf{set} \; (\text{detail::PredicateConst} < \; T > \&\& \text{first, detail::PredicateConst} < \; \text{Tothers} > \&\& ... \text{preds}) \end{array}$
- template<typename T > void set (detail::PredicateConst< T > &&last)

Additional Inherited Members

The documentation for this struct was generated from the following file:

 $\bullet \ / home/andrea/Scrivania/GitProj/EFG-refactoring/src/header/EasyFactorGraph/misc/Visitor.h$

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