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# **Chapter 1**

# Foundamental concepts about graphical models

METTERE subito in evidenza caratteristiche strane che questa libreria ha rispetto alle altre.

This Section will provide a background about the basic concepts in probabilistic graphical models. Moreover, a precise notation will be introduced and used for the rest of this guide.

#### 1.1 Preliminaries

This library is intended for managing network of <u>categorical variables</u>. Formally, the generic categorical variable V has a discrete domain Dom:

$$Dom(V) = \{v_0, \cdots, v_n\} \tag{1.1}$$

Essentially, Dom(V) contains all the possible realizations of V. The above notation will be adopted for the rest of the guide: capital letters will refer to variable names, while non capital refer to their realizations. Group of categorical variables can be considered categorical variables too, having a domain that is the Cartesian product of the domains of the variables constituting the group. Suppose X is obtained as the union of variables  $V_{1,2,3,4}$ , i.e.  $X = \bigcup_{i=1}^4 V_i$ , then:

$$Dom(X) = Dom(V_1) \times Dom(V_2) \times Dom(V_3) \times Dom(V_4)$$
(1.2)

The generic realization x of X is a set of realizations of the variables  $V_{1,2,3,4}$ , i.e.  $x=\{v_1,v_2,v_3,v_4\}$ . Suppose  $V_{1,2,3}$  have the domains reported in the tables 1.1. The union  $X=\bigcup_{i=1}^3 V_i$  is a categoric variable whose domain is made by the combinations reported in table 1.2.

The entire population of variables contained in a model is a set denoted as  $\mathcal{V}=\{V_1,\cdots,V_m\}$ . As will be exposed in the following, the probability of  $\bigcup_{V_i\in\mathcal{V}}V_i^{-1}$  is computed as the product of a certain number of components called factors.

<sup>&</sup>lt;sup>1</sup>Which is the joint probability distribution of all the variables in a model

D (II)	$\mid Dom(V_2) \mid$	D (II)
$Dom(V_1)$	$v_{20}$	$Dom(V_3)$
$v_{10}$		$v_{30}$
$v_{11}$	$v_{21}$	$v_{31}$
	$\mid v_{22} \mid$	

Table 1.1 Example of domains for the group of variables  ${\cal V}_{1,2,3}.$ 

$Dom(X) = Dom(V_1 \cup V_2 \cup V_3)$
$x_0 = \{v_{10}, v_{20}, v_{30}\}$
$x_1 = \{v_{10}, v_{20}, v_{31}\}$
$x_2 = \{v_{11}, v_{20}, v_{30}\}$
$x_3 = \{v_{11}, v_{20}, v_{31}\}$
$x_4 = \{v_{10}, v_{21}, v_{30}\}$
$x_5 = \{v_{10}, v_{21}, v_{31}\}$
$x_6 = \{v_{11}, v_{21}, v_{30}\}$
$x_7 = \{v_{11}, v_{21}, v_{31}\}$
$x_8 = \{v_{10}, v_{22}, v_{30}\}$
$x_9 = \{v_{10}, v_{22}, v_{31}\}$
$x_{10} = \{v_{11}, v_{22}, v_{30}\}$
$x_{11} = \{v_{11}, v_{22}, v_{31}\}$

Table 1.2 Example of domains for the group of variables  $V_{1,2,3}$ .

Knowing the joint probability of  $V_{1,\cdots,m}$ , the probability distribution of a subset  $S\subset\{V_1,\cdots,V_m\}$  can be in general (not only for graphical models) obtained through <u>marginalization</u>. Assume C is the complement of S:  $C\cup S=\bigcup_{i=1}^m V_i$  and  $C\cap S=\emptyset$ , then:

$$\mathbb{P}(S=s) = \sum_{\forall \hat{c} \in Dom(C)} \mathbb{P}(S=s, C=\hat{c})$$
(1.3)

In the above computation, variables in C were marginalized. Indeed they were in a certain sense eliminated, since the probability of the sub set S was of interest, no matter the realizations of all the variables in C.

A <u>factor</u>, sometimes also called a <u>potential</u>, is a positive real function describing the correlation existing among a subset of variables  $D^i \subset \mathcal{V}$ . Suppose factor  $\Phi_i$  involves  $\{X,Y,Z\}$ , i.e.  $D^i = \{X,Y,Z\}$ . Then,  $\Phi_i(X,Y,Z)$  is a function defined over  $Dom(D^i)$ . More formally:

$$\Phi_i(D^i) = \Phi_i(X, Y, Z) : \mathsf{Domain}(X) \times \mathsf{Domain}(Y) \times \mathsf{Domain}(Z) \longrightarrow \mathbb{R}^+ \tag{1.4}$$

The aim of  $\Phi_i$  is to assume 'high' values for those combinations  $d^i=\{x,y,z\}$  that are probable and low values (at least a null) for those being improbable. The entire population of factors  $\{\Phi_1,\cdots\Phi_p\}$  is considered for computing  $\mathbb{P}(V_{1,\cdots,m})$ , i.e. the joint probability distribution of all the variables in the model. The energy function E of a graph is defined as the product of the factors:

$$E(V_{1,\dots,m}) = \Phi_1(D^1) \cdot \dots \cdot \Phi_p(D^p) = \prod_{i=1}^p \Phi_i(D^i)$$
 (1.5)

E is addressed for computing the joint probability distribution of the variables in  $\mathcal{V}$ :

$$\mathbb{P}(V_{1,\cdots,m}) = \frac{E(V_{1,\cdots,m})}{\mathcal{Z}} \tag{1.6}$$

where  ${\cal Z}$  is a normalization coefficient defined as follows:

$$\mathcal{Z} = \sum_{\forall \tilde{V}_1, \dots, m \in Dom(\bigcup_{i=1,\dots,m} V_i))} E(\tilde{V}_{1,\dots,m})$$
(1.7)

Although the general theory behind graphical models supports the existance of generic multivaried factors, this library will address only two possible types:

- Binary potentials: they involve a pair of variables.
- Unary potentials: they involve a single variable.

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	$b_0$	$b_1$	$b_2$	$b_3$	$b_4$
$a_0$	1	4	0	0	0
$a_1$	0	1	0	0	0
$a_2$	0	0	5	0	1

Table 1.3 The values in the image of  $\Phi_b(A,B)$ .

$$\begin{array}{c|c|c|c|c}
a_0 & a_1 & a_2 \\
\hline
0 & 2 & 0.5 \\
\end{array}$$

Table 1.4 The values in the image of  $\Phi_u(A)$ .

We can store the values in the image of a Binary potential in a two dimensional table. For instance, suppose  $\Phi_b$  involves variables A and B, whose domains contains 3 and 5 possible values respectively:

$$\begin{aligned} \mathsf{DOM}(A) &= \{a_1, a_2, a_3\} \\ \mathsf{DOM}(B) &= \{b_1, b_2, b_3, b_4, b_5\} \end{aligned} \tag{1.8}$$

The values assumed by  $\Phi_b(A,B)$  are described by table 1.3. Essentially,  $\Phi_b(A,B)$  tells us that the combinations  $\{a_0,b_1\}$ ,  $\{a_2,b_2\}$  are highly probable; while  $\{a_0,b_0\}$ ,  $\{a_1,b_1\}$  and  $\{a_2,b_4\}$  are moderately probable. Let be  $\Phi_u(A)$  a Unary potential involving variable A. The values characterizing  $\Phi_u$  can be stored in a simple vector, see table 1.4. If  $\Phi_b(A,B)$  would be the only potential in the model, the joint probability density of A and B will assume the following values  $^2$ :

$$\mathbb{P}(a_0, b_1) = \frac{\Phi_b(a_0, b_1)}{\mathcal{Z}} = \frac{4}{\mathcal{Z}} = 0.3333$$

$$\mathbb{P}(a_2, b_2) = \frac{\Phi_b(a_2, b_2)}{\mathcal{Z}} = \frac{5}{\mathcal{Z}} = 0.4167$$

$$\mathbb{P}(a_0, b_0) = \frac{\Phi_b(a_0, b_0)}{\mathcal{Z}} = \mathbb{P}(a_1, b_1) = \mathbb{P}(a_2, b_4) = \frac{1}{\mathcal{Z}} = 0.0833$$
(1.9)

since  $\mathcal{Z}$  is equal to:

$$\mathcal{Z} = \sum_{\forall i = \{0,1,2\}, \forall j = \{0,1,2,3,4\}} \Phi_b(A = a_i, B = b_j) = 12$$
(1.10)

Both Unary and Binary potentials, can be of two possible classes:

- Simple shape. The potential is simply described by a set of values characterizing the image of the factor.  $\overline{\Phi_b(A,B)}$  and  $\overline{\Phi_u(A)}$  of the previous example are both Simple shapes. Class Potential\_Shape 5.40 handles this kind of factors.
- Exponential shape. They are indicated with  $\Psi_i$  and their image set is defined as follows:

$$\Psi_i(X) = exp(w \cdot \Phi_i(X)) \tag{1.11}$$

where  $\Phi_i$  is a Simple shape. Class Potential\_Exp\_Shape 5.39 handles this kind of factors. The weight w, can be tunable or not. In the first case, w is a free parameter whose value is decided after training the model (see Section 1.6), otherwise is a constant . Exponential shapes with fixed weight will be denoted with  $\overline{\Psi}_i$ .

Figure 1.1 resumes all the possible categories of factors that can be present in the models handled by this library.

Figure 1.2 reports an example of undirected graph. Set  $\mathcal{V}$  is made of 4 variables: A,B,C,D. There are 5 Binary potentials and 2 Unary ones. The graphical notation adopted for Fig. 1.2 will be adopted for the rest of this

<sup>&</sup>lt;sup>2</sup>combinations having a null probability were omitted

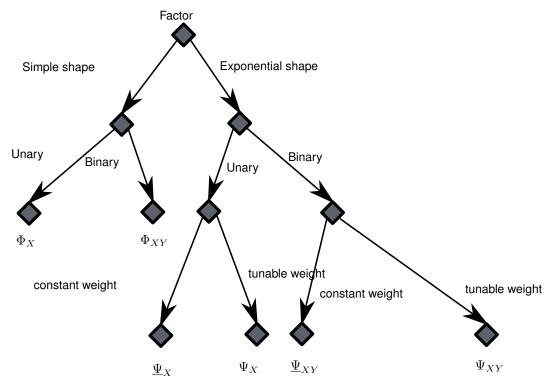


Figure 1.1 All the possible categories of factors, with the corresponding notation.

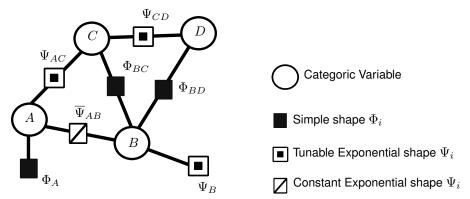


Figure 1.2 Example of graph: the legend of the right applies.

guide. Weights  $\alpha, \beta, \gamma$  and  $\delta$  are assumed for respectively  $\Psi_{AC}, \Psi_{AB}, \Psi_{CD}, \Psi_{B}$ . For the sake of clarity, the joint probability of the variables in Fig. 1.2 is computable as follows:

$$\mathbb{P}(A,B,C,D) = \frac{E(A,B,C,D)}{\mathcal{Z}(\alpha,\beta,\gamma,\delta)} = \frac{E(A,B,CD)}{\sum_{\tilde{A},\tilde{B},\tilde{C},\tilde{D}} E(\tilde{A},\tilde{B},\tilde{C},\tilde{D})}$$

$$E(A,B,C,D) = \Phi_{A}(A) \cdot exp(\alpha \Phi_{AC}(A,C)) \cdot exp(\beta \Phi_{AB}(A,B)) \cdots$$

$$\cdots \Phi_{BC}(B,C) \cdot exp(\gamma \Phi_{CD}(C,D)) \cdot \Phi_{BD}(B,D) \cdot exp(\delta \Phi_{B}(B))$$
(1.12)

Graphical models are mainly used for performing belief propagation. Subset  $\mathcal{O}=\{O_1,\cdots,O_f\}\subset\mathcal{V}$  is adopted for denoting the set of evidences: those variables in the net whose value become known.  $\mathcal{O}$  can be dynamical or not. The hidden variables are contained in the complementary set  $\mathcal{H}=\{H_1,\cdots,H_t\}$ . Clearly  $\mathcal{O}\cup\mathcal{H}=\mathcal{V}$  and  $\mathcal{O}\cap\mathcal{H}=\emptyset$ .  $\mathcal{H}$  will be used for referring to the union of all the variables in the hidden set:

$$H = \bigcup_{i=1}^{t} H_i \tag{1.13}$$

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while O is used for indicating the evidences:

$$O = \bigcup_{i=1}^{f} O_i \tag{1.14}$$

Knowing the joint probability distribution of variables in  $\mathcal{V}$  (equation (1.6)) the conditional distribution of H w.r.t. O can be determined as follows:

$$\mathbb{P}(H = h | O = o) = \frac{\mathbb{P}(H = h, O = o)}{\sum_{\forall \hat{h} \in Dom(H)} \mathbb{P}(H = \hat{h}, O = o)}$$

$$= \frac{E(h, o)}{\sum_{\forall \hat{h} \in Dom(H)} E(\hat{h}, o)} = \frac{E(h, o)}{\mathcal{Z}(o)}$$
(1.15)

The above computations are not actually done, since the number of combinations in the domain of  $\mathcal H$  is huge also when considering a low-medium size graph. On the opposite, the marginal probability  $\mathbb P(H_i=h_i|O=0)$  of a single variable in  $H_i\in\mathcal H$  is computationally tractable. Formally  $\mathbb P(H_i=h_i|O=0)$  is defined as follows:

$$\mathbb{P}(H_i = h_i | O = o) = \sum_{\forall \tilde{h} \in \{\mathcal{H} \setminus H_i\}} \mathbb{P}(H_i = h_i, \tilde{h} | O = o)$$

$$\tag{1.16}$$

The above marginal distribution is essentially the conditional distribution of  $H_i$  w.r.t. O, no matter the other variables in  $\mathcal{H}$ .

A generic Random Field is a graphical model for which set  $\mathcal{O}$  (and consequently  $\mathcal{H}$ ) is dynamical: the set of observations as well the values assumed by the evidences may change during time. Random field are handled by class Random\_Field 5.41. Conditional Random Field are Random Field for which set  $\mathcal{O}$  must be decided once and cannot change after. Only the values of the evidences during time may change. Class Conditional\_Random\_Field 5.13 is in charge of handling Conditional Random Field. Both Random Fields and Conditional Random Fields can be learnt knowing a training set, see Section 1.6. On the opposite, class Graph 5.20 handles constant graphs: they are conceptually similar to Random Fields but learning is not possible. Indeed, all the Exponential Shape involved must be constant.

The rest of this Chapter is structured as follows. Section 1.2 will introduce the message passing algorithm, which is the pillar for performing belief propagation. Section 1.3 will expose the concept of maximum a posteriori estimation, useful when querying a graph, while Section 1.4 will address Gibbs sampling for producing a training set of a known model. Section 1.5 will present the concept of subgraph which is a useful way for computing the marginal probabilities of a sub group of variables in  $\mathcal{H}$ . Finally, 1.6 will discuss how the learning of a graphical model is done, with the aim of computing the weights of the Exponential shapes that are tunable.

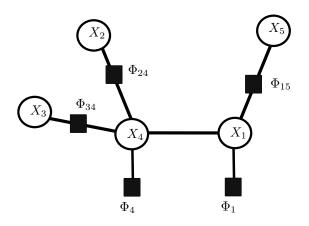
### 1.2 Message Passing

Message passing is a powerful but conceptually simple algorithm adopted for propagating the belief across a net. Such a propagation is the starting point for performing many important operations, like computing the marginal distributions of single variables or obtaining sub graphs. Before detailing the steps involved in the message passing algorithm, let's start from an example of belief propagation. Without loss of generality we assume all the factors as Simple shapes.

#### 1.2.1 Belief propagation

Consider the graph reported in Figure 1.3. Supposing for the sake of simplicity that no evidences are available (i.e.  $\mathcal{O} = \emptyset$ ). We are interested in computing  $\mathbb{P}(X_1)$ , i.e. the marginal probability of  $X_1$ . Recalling the definition introduced in the previous Section, the marginal probability is obtained by the following computation:

$$\mathbb{P}(x_1) = \sum_{\forall \tilde{x}_{2,3,4,5} \in \cup_{i=2}^5 X_i} \mathbb{P}(x_1, \tilde{x}_{2,3,4,5})$$
(1.17)



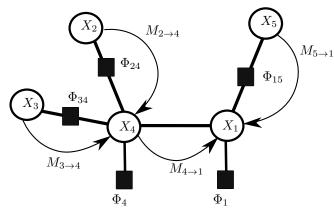


Figure 1.3 Example of graph adopted for explaining the message passing algorithm. Below are reported the messages to compute for obtaining the marginal probability of variable  $x_1$ 

Simplifying the notation and getting rid of the normalization coefficient  $\mathcal Z$  we can state the following:

$$\mathbb{P}(x_1) \propto \sum_{\tilde{x}_{2,3,4,5}} E(x_1, \tilde{x}_{2,3,4,5}) \tag{1.18}$$

Adopting the algebraic properties of the sums-products we can distribute the computations as follows:

$$\mathbb{P}(x_1) \propto \Phi_1(x_1) \sum_{\tilde{x}_5} \Phi_{15}(x_1, \tilde{x}_5) \sum_{\tilde{x}_4} \Phi_{14}(x_1, \tilde{x}_4) \Phi_4(\tilde{x}_4) \sum_{\tilde{x}_2} \Phi_{24}(\tilde{x}_{2,4}) \sum_{\tilde{x}_3} \Phi_{34}(\tilde{x}_{3,4}) \tag{1.19}$$

The first variable to marginalize can be  $\tilde{x}_2$  or  $\tilde{x}_3$ , since they are involved in the last terms of the sums products. The 'messages'  $M_{2\to 4}$ ,  $M_{3\to 4}$  are defined as follows:

$$M_{2\to 4}(\tilde{x}_4) = \sum_{\tilde{x}_2} \Phi_{24}(\tilde{x}_{2,4})$$

$$M_{3\to 4}(\tilde{x}_4) = \sum_{\tilde{x}_3} \Phi_{34}(\tilde{x}_{3,4})$$
(1.20)

Inserting  $M_{2 \to 4}$  and  $M_{3 \to 4}$  into equation (1.19) leads to:

$$\mathbb{P}(x_1) \propto \Phi_1(x_1) \sum_{\tilde{x}_5} \Phi_{15}(x_1, \tilde{x}_5) \sum_{\tilde{x}_4} \Phi_{14}(x_1, \tilde{x}_4) \Phi_4(\tilde{x}_4) M_{2 \to 4}(\tilde{x}_4) M_{3 \to 4}(\tilde{x}_4)$$
(1.21)

At this point the messages  $M_{4 \to 1}$  and  $M_{5 \to 1}$  can be computed in the following way:

$$M_{4\to 1(x_1)} = \sum_{\tilde{x}_4} \Phi_{14}(x_1, \tilde{x}_4) \Phi_4(\tilde{x}_4) M_{2\to 4}(\tilde{x}_4) M_{3\to 4}(\tilde{x}_4)$$

$$M_{5\to 1}(x_1) = \sum_{\tilde{x}_5} \Phi_{15}(x_1, \tilde{x}_5)$$
(1.22)

1.2 Message Passing 7



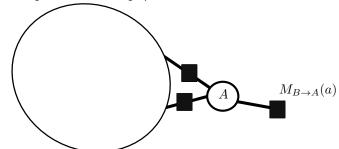


Figure 1.4 On the top the general mechanism involved in the message computation; on the bottom the simplification of the graph considering the computed message.

After inserting  $M_{4\rightarrow 1}$  and  $M_{5\rightarrow 1}$  into equation (1.21) we obtain:

$$\mathbb{P}(x_1) \propto \Phi_1(x_1) M_{4\to 1}(x_1) M_{5\to 1}(x_1) 
\mathbb{P}(x_1) = \frac{\Phi_1(x_1) M_{4\to 1}(x_1) M_{5\to 1}(x_1)}{\sum_{\tilde{x}_1} \Phi_1(\tilde{x}_1) M_{4\to 1}(\tilde{x}_1) M_{5\to 1}(\tilde{x}_1)}$$
(1.23)

which ends the computations. Messages are, in a certain sense, able to simplify the graph sending some information from an area of the graph to another one. Indeed, variables can be replace by messages, which can be treated as additional factors. Figure 1.3 resumes the computations exposed. Notice that the computation of  $M_{4\to1}$  must be done after computing the messages  $M_{2\to4}$  and  $M_{3\to4}$ , while  $M_{5\to1}$  can be computed independently from all the others.

#### 1.2.2 Message Passing

The aforementioned considerations can be extended to a general structured graph. Look at Figure 1.4: the computation of Message  $M_{B \to A}$  can be performed only after having computed all the messages  $M_{V_1, \dots, m \to B}$ , i.e. the messages incoming from all the neighbours of B a part from A. Clearly  $M_{B \to A}$  is computed as follows:

$$M_{B\to A}(a) = \sum_{\tilde{b}} \Phi_{AB}(a,\tilde{b}) M_{V1\to B}(\tilde{b}) \cdots M_{Vm\to B}(\tilde{b})$$

$$= \sum_{\tilde{b}} \Phi_{AB}(a,\tilde{b}) \prod_{i=1}^{m} M_{V_i\to B}(\tilde{b})$$
(1.24)

Essentially, it's like having simplified the graph: we can append to A the message  $M_{B\to A}(a)$  as it's a Simple shape, deleting factor  $\Psi_{AB}$  and all the other portions of the graph, see Figure 1.4. In turn,  $M_{B\to A}(a)$  will be adopted for

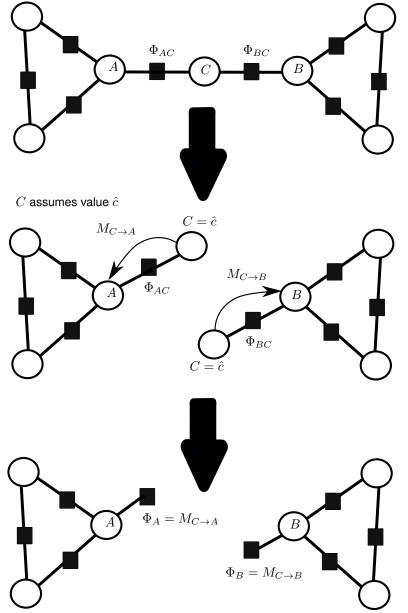


Figure 1.5 When variable C become an evidence, is temporary deleted from the graph, replaced by messages.

computing the message outgoing from A.

The above elimination is not actually done: all messages incoming to all nodes of a graph are computed by a derivation of 5.23 and are stored to be used for subsequent queries. This is partially not true when considering the evidences. Indeed, when the values of the evidences are retrieved, variables in  $\mathcal O$  are temporary deleted and replaced with messages, see Figure 1.5. Suppose variable C is connected to a variable A through a binary potential  $\Phi_{AC}(A,C)$  and to variable B through  $\Phi_{B,C}$ . Suppose also that variable C is an evidence assuming a value equal to  $\hat{c}$ , then the messages sent to A and B can be computed independently as follows:

$$M_{C \to A}(a) = \Phi_{AC}(a, \hat{c})$$

$$M_{C \to B}(b) = \Phi_{BC}(b, \hat{c})$$
(1.25)

Therefore all the variables that become evidences can be considered as leaves of the graph, sending messages to all the neighbouring nodes, possibly splitting an initial compact graph into many subgraphs, refer to Figure 1.5. Such computations are automatically handled by the library.

All the above considerations are valid when considering politree, i.e. graph without loops. Indeed, for these kind of graphs the message passing algorithm is able in a finite number of iterations to compute all the messages, see

Figure 1.6. The same is not true when having loopy graphs (see Figure 1.7), since deadlocking situations arise: no further messages can be computed since for every nodes some incoming ones are missing. In such cases a variant of the message passing called loopy belief propagation can be adopted. Loopy belief propagation initializes all the messages to basic shapes having the values of the image all equal to 1 and then recomputes all the messages of all the variables till convergence.

You don't have to handle the latter aspect: when a belief propagation is performed, the library automatically chooses to deploy 5.34 or 5.32, according to the structure of the graph for which the propagation is asked.

### 1.3 Maximum a posteriori estimation

Suppose we are not interested in determining the marginal probability of a specific variable, but rather we want the combination in the hidden set  $\mathcal{H}$  that maximises the probability  $\mathbb{P}(H_{1,\cdots,n}|O)$ . Clearly, we could try to compute the entire distribution  $\mathbb{P}(H_{1,\cdots,n}|O)$  and then take the value of H maximising that distribution. However, this is not computationally possible since even for low medium size graphs the size of  $Dom(\cup_{\forall H_i \in \mathcal{H}} H_i)$  can be huge. Maximum a posteriori estimations solve this problem: the value maximising  $\mathbb{P}(H_{1,\cdots,n}|O)$  is computed, without explicitly building the entire distribution  $\mathbb{P}(H_{1,\cdots,n}|O)$ . This is achieved by performing belief propagation with a slightly different version of the message passing algorithm presented in Section 1.2. Referring to Figure 1.4, the message to A is computed as follows when performing a maximum a posteriori estimation:

$$M_{B\to A}(a) = \max_{\tilde{b}} \{ \Phi_{AB}(a, \tilde{b}) \prod_{i=1}^{m} M_{V_i \to B}(\tilde{b}) \} \}$$
 (1.26)

Essentially, the summation in equation (1.24) is replaced with the max operator. After all messages are computed, the estimation  $h_{MAP} = \{h_{1MAP}, h_{2MAP}, \cdots\}$  is obtained by considering for every variable in  $\mathcal{H}$  the value maximising:

$$h_{iMAP} = argmax\{\Phi_{Hi}(h_{iMAP}) \prod_{k=1}^{L} M_k(h_{iMAP})\}$$
 (1.27)

where  $M_{1,\dots,L}$  refer to all the messages incoming to  $H_{i}$ . To be precise, this procedure is not guaranteed to return the value actually maximising  $\mathbb{P}(H_{1,\dots,n}|O)$ , but at least a strong local maximum is obtained.

At this point it is worthy to clarify that the combination  $h_{MAP} = \{h_{1MAP}, h_{2MAP}, \cdots\}$  could not be obtained by simply assuming for every  $H_i$  the realization maximising the marginal distribution:

$$h_{MAP} \neq \{argmax(\mathbb{P}(h_1)), \cdots, argmax(\mathbb{P}(h_n))\}$$
 (1.28)

This is due to the fact that  $\mathbb{P}(H_{1,\cdots,n}|O)$  is a joint probability distribution, while the marginals  $\mathbb{P}(H_{i})$  are not. For better understanding this aspect consider the graph reported in Figure 1.8, with the potentials  $\Phi_{XA}$ ,  $\Phi_{AB}$  and  $\Phi_{YB}$  having the images defined in table 1.5. Suppose discovering that X=0 and Y=1. Then, performing the standard message passing algorithm explained in the previous Section we obtain the messages reported in Figure 1.8. Clearly individual marginals for A and B would be equal to:

$$\mathbb{P}(A) = \begin{pmatrix} \mathbb{P}(A=0) \\ \mathbb{P}(A=1) \end{pmatrix} = \begin{pmatrix} 0.5 \\ 0.5 \end{pmatrix} \\
\mathbb{P}(B) = \begin{pmatrix} \mathbb{P}(B=0) \\ \mathbb{P}(B=1) \end{pmatrix} = \begin{pmatrix} 0.5 \\ 0.5 \end{pmatrix}$$
(1.29)

Therefore, all the combinations  $\{A=0,B=0\}$ ,  $\{A=0,B=1\}$ ,  $\{A=1,B=0\}$ ,  $\{A=1,B=1\}$  maximise  $\mathbb{P}(A,B|O)$ . However, it easy to prove that E(A,B,X,Y) assumes the values reported in table 1.6. Therefore, the combinations actually maximising the joint distribution  $\mathbb{P}(A,B|O)$  are  $\{A=0,B=0\}$  and  $\{A=1,B=1\}$ , leading to a different result.

Maximum a posteriori estimation can be performing invoking MAP\_on\_Hidden\_set 5.37.2.6 on a particular derivation of class 5.37. Maximum a posteriori estimation for sub graphs (see Section 1.5) is also supported by method MAP 5.3.2.3.

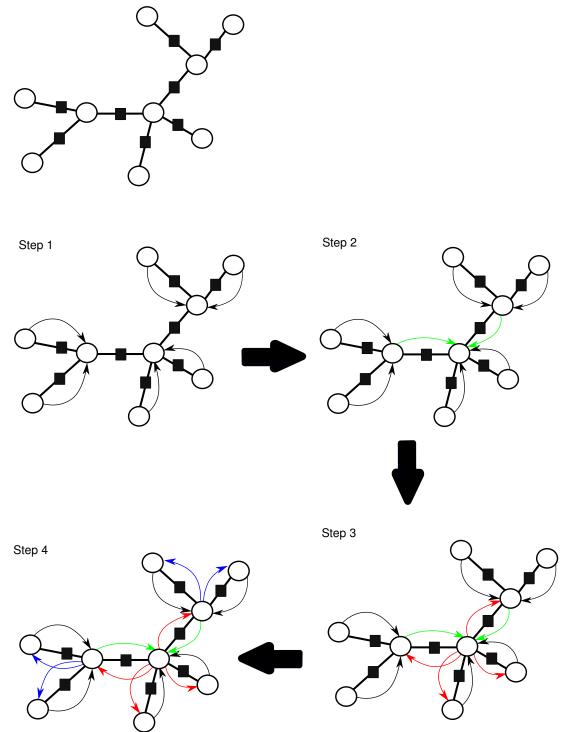


Figure 1.6 Steps involved for computing the messages of the politree represented at the top. The leaves are the first nodes for which the outgoing messages can be computed.

	$b_0$	$b_1$		$ x_0 $	$x_1$		$y_0$	$y_1$
$\overline{a_0}$	2	0	$a_0$	1	0.1	$b_0$	1	0.1
$\overline{a_1}$	0	2	$\overline{a_1}$	0.1	1	$\overline{b_1}$	0.1	1

Table 1.5 Factors involved in the graph of Figure 1.8.

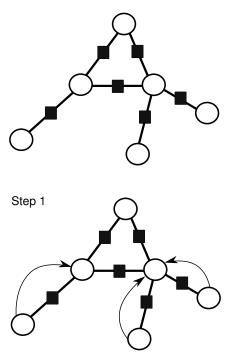


Figure 1.7 Steps involved for computing the messages on a loopy graph: after computing the messages outgoing from the leaves, a deadlock is reached since no further messages are computable.

A	$\mid B \mid$	E(A, B, X = 0, Y = 1)
0	0	0.2
0	1	0
1	0	0
1	1	0.2

Table 1.6 Factors involved in the graph of Figure 1.8.

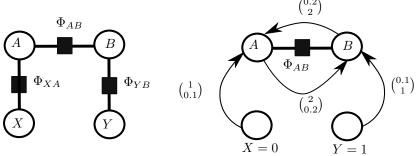


Figure 1.8 Example of graph adopted. When the evidences are retrieved, the messages computed by making use of the message passing algorithm are reported below.

## 1.4 Gibbs sampling

Gibbs sampling is a Monte Carlo method for obtaining samples from a joint distribution of variables  $X_{1,\cdots,m}$ , without explicitly compute that distribution. Indeed, Gibbs sampling is an iterative method which requires every time to determine the conditional distribution of a single variable  $X_i$  w.r.t to all the others in the group.

More formally the algorithm starts with an initial combination of values  $\{x_{1,\dots,m}^1\}$  for the variable  $\cup_{i=\{1,\dots,m\}}X_i$ . At every iteration, all the values of that combination are recomputed. At the  $j^{th}$  iteration the value of  $x_k^{j+1}$  for the subsequent iteration is obtaining by sampling from the following marginal distribution:

$$x_k^{j+1} \sim \mathbb{P}(x_k | x_{\{1,\dots,m\}\setminus k}^j) \tag{1.30}$$

After an initial transient, the samples cumulated during the iterations can be considered as drawn from the joint distribution involving group  $X_{1,\dots,m}$ .

This algorithm can be easily applied to graphical model. Indeed the methodologies exposed in Section 1.2 can be applied for determining the conditional distribution of a single variable  $H_i \in \mathcal{H}$  w.r.t all the others (as well the evidences in  $\mathcal{O}$ ), assuming all variables in  $\mathcal{H} \setminus H_i$  as additional observations and computing the marginal probability of  $H_i$ . Gibbs\_Sampling\_on\_Hidden\_set 5.37.2.5 is in charge of performing Gibbs sampling on a generic graph, while method Gibbs\_Sampling 5.3.2.2 performs the same for sub graphs (see 1.5).

### 1.5 Sub graphs

As explained in Section 1.2, the marginal probability of a variable  $H_i \in \mathcal{H}$  can be efficiently computed by considering the messages produced by the message passing algorithm. The same messages can be also used for performing graph reduction, with the aim to model the joint probability distribution of a subset of variables  $\{H_1, H_2, H_3\} \subset \mathcal{H}$ , i.e.  $\mathbb{P}(H_{1,2,3}|O)$ . The latter quantity is the marginal probability of the subset of variables of interest.

The aim of message passing is essentially to simplify the graph, condensing all the belief information into the messages. Such property is exploited for computing sub graphs. Without loss of generality assume from now on  $\mathcal{O}=\emptyset$ . Consider the graph in Figure 1.9 and suppose we are interested in modelling  $\mathbb{P}(A,B,C)$ , no matter the values of the other variables. After computing all the messages exploiting message passing, the sub graph reported in Figure 1.9 is the one modelling  $\mathbb{P}(A,B,C)$ . Actually, that sub graph is a graphical model itself, for which all the properties exposed so far hold. For example the energy function E is computable as follows:

$$E(A = a, B = b, C = c) = \Phi_{AB}(a, b)\Phi_{BC}(b, c)\Phi_{AC}(a, c)M_{X \to A}(a)M_{Y \to B}(b)$$
(1.31)

while the joint probability of A,B and C can be computed in this way:

$$\mathbb{P}(A=a,B=b,C=c) = \frac{E(a,b,c)}{\sum_{\forall \tilde{a},\tilde{b},\mathbf{c}} E(\tilde{a},\tilde{b},\tilde{c})}$$
(1.32)

Notice that in this case the graph is significantly smaller than the originating one, implying that the above computations can be performed in an acceptable time.

Also Gibbs sampling can be applied to a reduced graph, producing samples drawn from the marginal probability  $\mathbb{P}(A,B,C)$ .

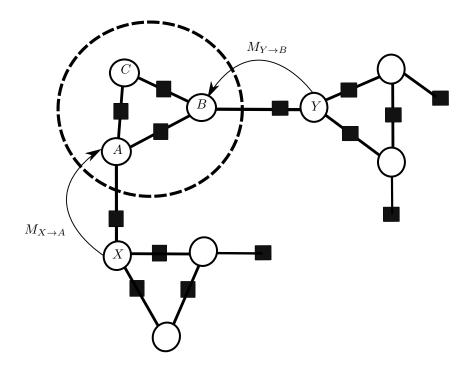
The reduction described so far is always possible when considering a subset of variables forming a connected subportion of the original graph, i.e. after reduction there must be a unique sub structure. For instance, variables X and Y of the graph in Figure 1.10 do not respect the latter specification, meaning that it is not possible to build a sub graph involving X and Y.

The class in charge of handling graph reduction is 5.3.

#### 1.6 Learning

The aim of learning is to determine the optimal values for the w (equation (1.11) ) of all the tunable potentials (see Section 1.1)  $\Psi$ . To this aim two cases must be distinguished:

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Sub graph involving A,B,C

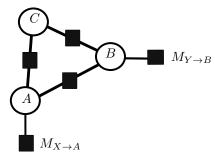


Figure 1.9 Example of graph reduction.

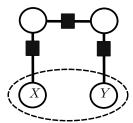


Figure 1.10 Example of a subset of variables for which the graph reduction is not possible.

- Learning must be performed for a Graph 5.20 or a Random\_Field 5.41: see Section 1.6.1
- Learning must be performed for a Conditional Random Field 5.13: see Section 1.6.2

No matter the case, the population of tunable weights will be indicated with W:

$$W = \{w_1, \cdots, w_D\} \tag{1.33}$$

 $w_i$  will refer to the  $i^{th}$  free parameter of the model. Learning can be performed using class METTERE.

### 1.6.1 Learning of unconditioned model

For the purpose of learning, we assume  $\mathcal{O}=\emptyset$ . Learning considers a training set  $T=\{t_1,\cdots,t_N\}$  made of realizations of the joint distribution correlating all the variables in  $\mathcal{V}$ , no matter the fact that they are involved in tunable or non tunable potentials. As exposed in Section 1.1, if W is known, the probability of a combination  $t_j$  can be evaluated as follows:

$$\mathbb{P}(t_j) = \frac{E(t_j, W)}{\mathcal{Z}(W)} \tag{1.34}$$

At this point we can observe that the energy function is the product of two main factors: one depending from  $t_j$  and W and the other depending only upon  $t_j$  representing the contribution of all the non tunable potentials (Simple shapes and fixed Exponential shapes, see Section 1.1):

$$E(t_j, W) = exp(w_1\Phi_1(t_j)) \cdot \dots \cdot exp(w_D\Phi_D(t_j)) \cdot E_0(t_j)$$

$$= exp(\sum_{i=1}^D w_i\Phi_i(t_j)) \cdot E_0(t_j)$$
(1.35)

The likelihood function L can be defined as follows:

$$L = \prod_{t_j \in T} \mathbb{P}(t_j) \tag{1.36}$$

passing to the logarithmic likelihood and dividing by the training set size N we obtain:

$$J = \frac{\log(L)}{N} = \sum_{t_j \in T} \frac{\log(\mathbb{P}(t_j))}{N}$$

$$= \sum_{t_j \in T} \frac{\log(E(t_j, W)) - \log(\mathcal{Z}(W)}{N}$$

$$= \frac{1}{N} \sum_{t_j \in T} \log(E(t_j, W)) - \log(\mathcal{Z}(W))$$

$$= \frac{1}{N} \sum_{t_j \in T} \left( \sum_{i=1}^{D} w_i \Phi_i(t_j) \right) - \log(\mathcal{Z}(W)) + \cdots$$

$$+ \frac{1}{N} \sum_{t_j \in T} \log(E_0(t_j))$$
(1.37)

The aim of learning is to find the value of W maximising J. This is done iteratively, exploiting a gradient descend approach (see METTERE possibili strategie). The computations to perform for evaluating the gradient  $\frac{\partial J}{\partial W}$  will be exposed in the following part of this Section. Notice that in equation (1.37), term  $\sum_{t_j \in T} log(E_0(t_j))$  is constant and consequently will be not considered for computing the gradient of J. Equation (1.37) can be rewritten as follows:

$$J = \alpha(T, W) - \beta(W)$$

$$\alpha = \frac{1}{N} \sum_{t_j \in T} \left( \sum_{i=1}^{D} w_i \Phi_i(t_j) \right)$$
(1.38)

$$\beta = log(\mathcal{Z}(W)) \tag{1.39}$$

 $\alpha$  is influenced by T, while the same is not valid for  $\beta$ .

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#### 1.6.1.1 Gradient of $\alpha$

By the analysis of the equation (1.38) it is clear that:

$$\frac{\partial \alpha}{\partial w_i} = \frac{1}{N} \sum_{t_i \in T} w_i \Phi_i(t_j) \tag{1.40}$$

#### **1.6.1.2** Gradient of $\beta$

The computation of  $\frac{\partial \beta}{\partial w_i}$  requires to manipulate a little bit equation (1.39). Firstly the derivative of the logarithm must be computed:

$$\frac{\partial \beta}{\partial w_i} = \frac{1}{\mathcal{Z}} \frac{\partial \mathcal{Z}}{\partial w_i} \tag{1.41}$$

The normalizing coefficient Z is made of the following terms (see also equation (1.6)):

$$\mathcal{Z}(W) = \sum_{\tilde{V} \in \bigcup_{i=1}^{p} V_i} \left( exp\left(\sum_{i=1}^{D} w_i \Phi_i(\tilde{V})\right) \cdot E_0(\tilde{V}) \right)$$
 (1.42)

Introducing equation (1.42) into (1.41) leads to:

$$\frac{\partial \beta}{\partial w_{i}} = \frac{1}{\mathcal{Z}} \frac{\partial}{\partial w_{i}} \left( \sum_{\tilde{V}} exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{V})\right) E_{0}(\tilde{V}) \right) 
= \frac{1}{\mathcal{Z}} \sum_{\tilde{V}} \frac{\partial}{\partial w_{i}} \left( exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{V})\right) \right) E_{0}(\tilde{V}) 
= \frac{1}{\mathcal{Z}} \sum_{\tilde{V}} exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{V})\right) E_{0}(\tilde{V}) \Phi_{i}(\tilde{V}) 
= \sum_{\tilde{V}} \frac{exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{V})\right) E_{0}(\tilde{V})}{\mathcal{Z}} \Phi_{i}(\tilde{V}) 
= \sum_{\tilde{V}} \frac{E(\tilde{V})}{\mathcal{Z}} \Phi_{i}(\tilde{V}) 
= \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{i}(\tilde{V}) \tag{1.43}$$

Last term in the above equations can be further elaborated. Assume that the variables involved in potential  $\Phi_j$  are  $V_{1,2}$ , then:

$$\frac{\partial \beta}{\partial w_{i}} = \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{i}(\tilde{V})$$

$$= \sum_{\tilde{V}_{1,2}} \Phi_{i}(\tilde{V}_{1,2}) \sum_{\tilde{V}_{3,4,\cdots}} \mathbb{P}(\tilde{V}_{1,2,3,4,\cdots})$$

$$= \sum_{\tilde{V}_{1,2}} \Phi_{i}(\tilde{V}_{1,2}) \mathbb{P}(\tilde{V}_{1,2})$$
(1.44)

where  $\mathbb{P}(\tilde{V}_{1,2})$  is the marginal probability (see the initial part of Section 1.1) of the variables involved in the potential  $\Phi_i$ , which can be easily computable by considering the sub graph containing only  $V_1$  and  $V_2$  as variables (see Section 1.5). Notice that in case  $\Phi_i$  is a unary potential the same holds, considering the marginal distribution of the single variable involved by  $\Phi_i$ :

$$\frac{\partial \beta}{\partial w_i} = \sum_{\forall \tilde{V}_1} \Phi_i(\tilde{V}_1) \mathbb{P}(\tilde{V}_1) \tag{1.45}$$

which can be easily obtained through the message passing algorithm (Section 1.2).

After all the manipulations performed, the gradient  $\frac{\partial J}{\partial w_i}$  has the following compact expression:

$$\frac{\partial J}{\partial w_i} = \frac{1}{N} \sum_{j=1}^N \Phi_i(D_j^i) - \sum_{\tilde{D}^i} \mathbb{P}(\tilde{D}^i) \Phi_i(\tilde{D}^i)$$
(1.46)

#### 1.6.2 Learning of conditioned model

For such models leaning is more demanding as will be exposed. Recalling the definition provided in the final part of Section 1.1, Conditional Random Fields are graphs for which the set of observations  $\mathcal{O}$  is fixed. The training set T is made of realizations of both  $\mathcal{H}$  and  $\mathcal{O}$ :

$$T = \{t_1, \dots, t_N\}$$

$$= \{\{h_1, o_1\}, \dots, \{h_N, o_N\}\}$$
(1.47)

We recall, equation (1.15), that the conditional probability of the hidden variables w.r.t. the observed ones is defined as follows:

$$\mathbb{P}(h_j, o_j) = \frac{E(h_j, o_j, W)}{\mathcal{Z}(o_j, W)}$$

$$E(h_j, o_j, W) = exp\left(\sum_{i=1}^{D} w_i \Phi_i(h_j, o_j)\right) E_0(h_j, o_j)$$

$$\mathcal{Z}(o_j, W) = \sum_{\tilde{h}} E(\tilde{h}, o_j, W)$$
(1.48)

The aim of learning is to maximise a likelihood unction  ${\cal L}$  defined in this case as follows:

$$L = \prod_{h_j \in T} \mathbb{P}(h_j | o_j) \tag{1.49}$$

Passing to the logarithms and dividing by the training set size we obtain the following objective function J:

$$J = \frac{\log(L)}{N}$$

$$= \frac{1}{N} \sum_{h_{j}, o_{j} \in T} log(E(h_{j}, o_{j}, W)) - \frac{1}{N} \sum_{h_{j}, o_{j} \in T} log(Z(o_{j}, W))$$

$$= \frac{1}{N} \sum_{h_{j}, o_{j} \in T} \left( \sum_{i=1}^{D} w_{i} \Phi_{i}(h_{j}, o_{j}) \right) - \frac{1}{N} \sum_{h_{j}, o_{j} \in T} log(Z(o_{j}, W))$$

$$+ \frac{1}{N} \sum_{h_{j}, o_{j} \in T} log(E_{0}(h_{j}, o_{j}))$$
(1.50)

Neglecting  $E_0$  which not depends upon W, equation (1.50) can be rewritten as follows:

$$J = \alpha(T, W) - \beta(T, W)$$

$$\alpha(T, W) = \frac{1}{N} \sum_{h_j, o_j} \left( \sum_{i=1}^{D} w_i \Phi_i(h_j, o_j) \right)$$

$$\beta(T, W) = \frac{1}{N} \sum_{o_i} log(\mathcal{Z}(o_j, W))$$
(1.51)

At this point, an important remark must be done: differently from the  $\beta$  defined in equation (1.39),  $\beta(T,W)$  of conditioned model is a function of the training set. The latter observation has an important consequence: when

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performing learning of unconditioned model, belief propagation (i.e. the computation of the messages through message passing with the aim of computing the marginal probabilities of the groups of variables involved in the factor of the model) must be performed once for every iteration of the gradient descend; on the opposite when considering conditioned model, belief propagation must be performed at every iteration for every element of the training set, see equation (1.55). This makes the learning of conditioned models much more computationally demanding. This price is paid in order to not model the correlation among the observations  $^3$ , which can be interesting for many applications. The computation of  $\frac{\partial \alpha}{\partial w_i}$  is analogous to the one of non conditioned model, equation (1.40).

#### **1.6.2.1** Gradient of $\beta$

Following the same approach in Section 1.6.1.2, the gradient of  $\beta$  can be computed as follows:

$$\frac{\partial \beta}{\partial w_{i}} = \frac{1}{N} \sum_{j=1}^{N} \frac{\partial log(\mathcal{Z}(o_{j}, W))}{\partial w_{i}}$$

$$= \frac{1}{N} \sum_{j=1}^{N} \frac{1}{\mathcal{Z}(o_{j})} \frac{\partial \mathcal{Z}(o_{j}, W)}{\partial w_{i}}$$

$$= \frac{1}{N} \sum_{j=1}^{N} \frac{\partial}{\partial w_{i}} \left( \sum_{\tilde{h}} exp\left(\sum_{i=1}^{D} w_{i} \Phi_{i}(\tilde{h}, o_{j})\right) E_{0}(\tilde{h}, o_{j}) \right)$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}} \left( exp\left(\sum_{i=1}^{D} w_{i} \Phi_{j}(\tilde{h}, o_{j})\right) E_{0}(\tilde{h}, o_{j}) \Phi_{i}(\tilde{h}, o_{j}) \right)$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}} \frac{E(\tilde{h}, o_{j}, W)}{\mathcal{Z}(o_{1})} \Phi_{i}(\tilde{h}, o_{j})$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}} \mathbb{P}(\tilde{h}|o_{j}) \Phi_{i}(\tilde{h}, o_{j})$$
(1.52)

Suppose the variables involved in the factor  $\Phi_j$  are  $\tilde{h}_{1,2}$ , then:

$$\frac{\partial \beta}{\partial w_{i}} = \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}} \mathbb{P}(\tilde{h}|o_{j}) \Phi_{i}(\tilde{h}, o_{j})$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}_{1,2}} \Phi_{i}(\tilde{h}_{1,2}) \sum_{\tilde{h}_{3,4,...}} \mathbb{P}(\tilde{h}_{1,2,3,4,...}|o_{j})$$

$$= \frac{1}{N} \sum_{j=1}^{N} \sum_{\tilde{h}_{1,2}} \Phi_{i}(\tilde{h}_{1,2}) \mathbb{P}(\tilde{h}_{1,2}|o_{j})$$
(1.53)

where  $\mathbb{P}(\tilde{h}_{1,2}|o_j)$  is the conditioned marginal probability of group  $\tilde{h}_{1,2}$  w.r.t. the observations  $o_j$ .

Grouping all the simplifications we obtain:

$$\frac{\partial J}{\partial w_i} = \frac{1}{N} \sum_{j=1}^{N} \Phi_i(h_j, o_j) - \frac{1}{N} \sum_{j=1}^{N} \left( \sum_{\tilde{h}_{1,2}} \mathbb{P}(\tilde{h}_{1,2} | o_j) \Phi_i(\tilde{h}_{1,2}) \right)$$
(1.54)

Generalizing:

$$\frac{\partial J}{\partial w_i} = \frac{1}{N} \sum_{j=1}^N \Phi_i(D^i_j, o_j) - \frac{1}{N} \sum_{j=1}^N \left( \sum_{\tilde{D}^i} \mathbb{P}(\tilde{D}^i | o_j) \Phi_i(\tilde{D}^i, o_j) \right) \tag{1.55}$$

<sup>&</sup>lt;sup>3</sup>that can be highly correlated

#### 1.6.3 Learning of modular structure

Suppose to have a modular structure made of repeating units as for example the graph in Figure 1.11. Every single unit has the same population of potentials and we would like to enforce this fact when performing learning. In particular we'll have some sets of Exponential shape sharing the same weight  $w_1$  (see Figure 1.11). Motivated by this example, we included in the library the possibility to specify that a potential must share its weight with another one. Then, learning is done consistently with the aforementioned specification.

#### 1.6.3.1 Gradient of $\alpha$

Considering the model in Figure 1.11, the  $\alpha$  part of J (equation (1.38)) can be computed as follows:

$$\alpha = \frac{1}{N} \sum_{t_j} \left( w_1 \Phi_1(a_{1j}, b_{1j}) + w_1 \Phi_2(a_{2j}, b_{2j}) + w_1 \Phi_3(a_{3j}, b_{3j}) + \dots + \sum_{i=2}^{D} w_i \Phi_i(t_j) \right)$$

$$(1.56)$$

which leads to:

$$\frac{\partial \alpha}{\partial w_1} = \frac{1}{N} \sum_{t_j} \left( \Phi_1(a_{1j}, b_{1j}) + \Phi_2(a_{2j}, b_{2j}) + \Phi_3(a_{3j}, b_{3j}) \right)$$
(1.57)

#### **1.6.3.2** Gradient of $\beta$

Regarding the  $\beta$  part of J we can write what follows:

$$\frac{\partial \beta}{\partial w_{1}} = \frac{1}{Z} \frac{\partial Z}{\partial w_{1}} 
= \frac{1}{Z} \frac{\partial}{\partial w_{1}} \left( \sum_{\tilde{V}} \left( exp\left(w_{1}(\Psi_{1}(a_{1j}, b_{1j}) + \cdots + \Psi_{2}(a_{2j}, b_{2j}) + \Psi_{3}(a_{3j}, b_{3j})\right) + \sum_{i=2}^{D} w_{i} \Phi_{i}(\tilde{V}) \right) E_{0}(\tilde{V}) \right) \right) 
= \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \left( \Phi_{1}(\tilde{a}_{1}, \tilde{b}_{1}) + \Phi_{2}(\tilde{a}_{2}, \tilde{b}_{2}) + \Phi_{3}(\tilde{a}_{3}, \tilde{b}_{3}) \right) 
= \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{1}(\tilde{a}_{1}, \tilde{b}_{1}) + \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{2}(\tilde{a}_{2}, \tilde{b}_{2}) + \sum_{\tilde{V}} \mathbb{P}(\tilde{V}) \Phi_{3}(\tilde{a}_{3}, \tilde{b}_{3}) 
= \sum_{\tilde{A}_{1}, \tilde{B}_{1}} \mathbb{P}(\tilde{A}_{1}, \tilde{B}_{1}) \Phi_{1}(\tilde{A}_{1}, \tilde{B}_{1}) + \sum_{\tilde{A}_{2}, \tilde{B}_{2}} \mathbb{P}(\tilde{A}_{2}, \tilde{B}_{2}) \Phi_{2}(\tilde{A}_{2}, \tilde{B}_{2}) + \cdots 
\cdots + \sum_{\tilde{A}_{3}, \tilde{B}_{3}} \mathbb{P}(\tilde{A}_{3}, \tilde{B}_{3}) \Phi_{3}(\tilde{A}_{3}, \tilde{B}_{3})$$
(1.58)

Notice that the gradient  $\frac{\partial J}{\partial w_1}$  is the summation of three terms: the ones that would have been obtained considering separately the three potentials in which  $w_1$  is involved (equation (1.46)):

$$\frac{\partial J}{\partial w_{1}} = \frac{1}{N} \sum_{j=1}^{N} \Phi_{1}(a_{i}^{1}, b_{i}^{1}) - \sum_{\tilde{a}^{1}, \tilde{b}^{1}} \mathbb{P}(\tilde{a}^{1}, \tilde{b}^{1}) \Phi_{1}(\tilde{a}^{1}, \tilde{b}^{1}) + \cdots 
+ \frac{1}{N} \sum_{j=1}^{N} \Phi_{2}(a_{i}^{2}, b_{i}^{2}) - \sum_{\tilde{a}^{2}, \tilde{b}^{2}} \mathbb{P}(\tilde{a}^{2}, \tilde{b}^{2}) \Phi_{2}(\tilde{a}^{2}, \tilde{b}^{2}) + \cdots 
+ \frac{1}{N} \sum_{j=1}^{N} \Phi_{3}(a_{i}^{3}, b_{i}^{3}) - \sum_{\tilde{a}^{3}, \tilde{b}^{3}} \mathbb{P}(\tilde{a}^{3}, \tilde{b}^{3}) \Phi_{3}(\tilde{a}^{3}, \tilde{b}^{3}) +$$
(1.59)

The above result has a general validity, also considering conditioned graphs.

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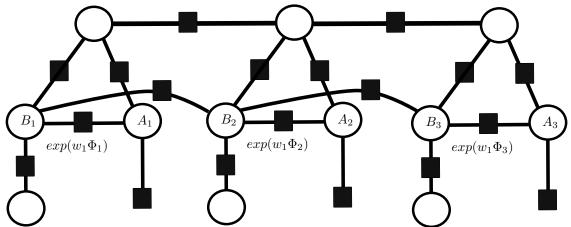


Figure 1.11 Example of modular structure: weight  $w_1$  is simultaneously involved into potentials  $\Phi_1,\Phi_2$  and  $\Phi_3$ .

Foundamental concepts about graphical models

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## **Chapter 2**

## XML notation

The aim of this Section is to expose how to build graphical models from XML files describing their structures. In particular, the syntax of such an XML will be clarified. XMI files can be passed as input for the constructor of Graph 5.20.2.2, Random\_Field 5.41.2.2 and Conditional\_Random\_Field 5.13.2.1. Figure 2.1 visually explains the structure of a valid XML.

Essentially two kind of tags must be incorporated:

- Variable: describes the information related to a variable present in the graph. There must a tag of this kind for every variable constituting the model. Fields description:
  - name: is a string indicating the name of this variable.
  - Size: is the size of the variable, i.e. the size of *Dom*, see Section 1.1.
  - flag[optional]: is a flag that can assume two possible values, 'O' or 'H' according to the fact that this variable is in set  $\mathcal{O}$  (Section 1.1) or not respectively. When non specifying this flag 'H' is assumed.
- Potential: describes the information related to a unary or a binary potential present in the graph (see Section 1.1). Fields description:
  - var: the name of the first variable involved.
  - var[optional]: the name of the second variable involved. Is omitted when considering unary potentials,
     while is mandatory when a binary potentials is described by this tag.
  - weight[optional]: when specifying an Exponential shape (Section 1.1) it must be present for indicating the value of the weight w (equation (1.11)). When omitting, the potential is assumed as a Simple shape one.
  - tunability[optional]: it is a flag for specifying whether the weight of this Exponential shape is tunable or not (see Section 1.1). Is ignored in case weight is omitted. It can assumes two possible values, 'Y' or 'N' according to the fact that the weight involved is tunable or not respectively. When weight is specified and tunability is omitted, a value equal to 'Y' is assumed.
- Share[optional]: you must specify this sub tag when the containing Exponential shape shares its weight with another potential in the model. Sub fields var are exploited for specifying the variables involved by the potential whose weight is to share. If weight is omitted in the containing Potential tag, this sub tag is ignored, even though the value assigned to weight is ignored since it is shared with another potential. The potential sharing its weight must be clearly an Exponential shape, otherwise the sharing directive is ignored.

The following components are exclusive: only one of them can be specified in a Potential tag and at the same time at least one must be present.

- Correlation: it can assume two possible values, 'T' or 'F'. When 'T' is passed, this potential is assumed to be a simple shape correlating shape (see 5.40.2.3), otherwise when passing 'F' a simple anti correlating shape is assumed (see 5.40.2.3). It is invalid in case this Potential is a unary one. In case weight was specified, an Exponential shape is built, wrapping a simple correlating or anti-correlating shape.

22 XML notation

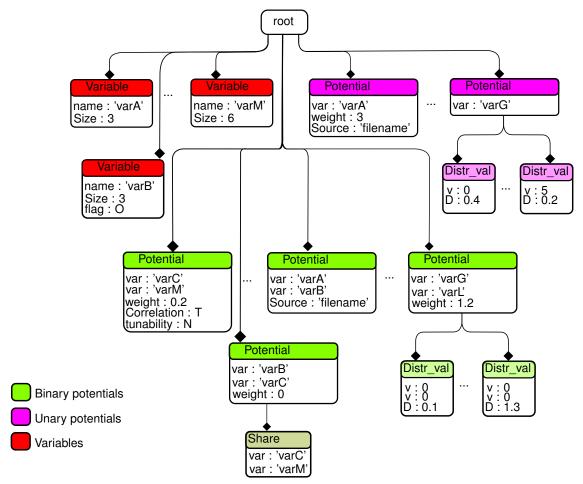


Figure 2.1 The structure of the XML describing a graphical model.

– Source: it is the location of a textual file describing the values of the distribution characterizing this potential. Rows of this file contain the values charactering the image of the potential. Combinations not specified are assumed to have an image value equal to 0. Clearly the number of values charactering the distribution must be consistent with the number of specified var fields. In case weight was specified, an Exponential shape is built, wrapping the Simple shape whose values are specified in the aforementioned file. For instance, the potential  $\Phi_b$  of Section 1.1 would have been described by a file containing the following rows:

2 2 5

2 4 1

– Set of sub tags Distr\_val: is a set of nested tags describing the distribution of the this potential. Similarly to Source, every element use fields v for describing the combination, while D is used for specifying the value assumed by the distribution. For example the potential  $\Phi_b$  of Section 1.1 would have been described by the syntax reported in Figure 2.2. In case weight was specified, an Exponential shape is built, wrapping the Simple shape whose distribution is specified by the aforementioned sub tags.

Figure 2.2 Syntax to adopt for describing the potential  $\Phi_b$  of Section 1.1, using a population of Distr\_val sub tags.

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# **Chapter 3**

# **Hierarchical Index**

# 3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

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Segugio::Node::Node_factory::_Baseline_4_Insertion <t></t>	29
Segugio::Node::Node_factory::_SubGraph	30
Segugio::Categoric_var	36
Segugio::Categoric_domain	35
Segugio::I_Potential::Getter_4_Decorator	42
Segugio::I_Potential_Decorator < I_Potential >	52
Segugio::Potential	64
Segugio::Message_Unary	56
Segugio::I_Potential_Decorator< Potential_Exp_Shape >	52
Segugio::atomic_Learning_handler	
Segugio::Binary_handler	
Segugio::Binary_handler_with_Observation	
Segugio::Unary_handler	
Segugio::I_Potential_Decorator< Potential_Shape >	
Segugio::Potential_Exp_Shape	
Segugio::I_Potential_Decorator< Wrapped_Type >	
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Segugio::atomic_Learning_handler	
5 5 5=	46
Segugio::Trainer_Decorator	
Segugio::Entire_Set	
Segugio::Stoch_Set_variation	
9-9	47
Segugio::Loopy_belief_propagation	
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Segugio::Distribution_exp_value	
Segugio::Distribution_value	
Segugio::Training_set::I_Extractor < Array >	
Segugio::Training_set::Basic_Extractor< Array >	33
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Segugio::atomic_Learning_handler	32
Segugio::composite_Learning_handler	37
Segugio::I_Potential	49
Segugio::I_Potential_Decorator< I_Potential >	52
Segugio::I_Potential_Decorator< Potential_Exp_Shape >	52
Segugio::I_Potential_Decorator < Potential_Shape >	52
Segugio::I_Potential_Decorator< Wrapped_Type >	52
Segugio::Potential_Shape	69
Segugio::I_Trainer	53
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Segugio::Fixed_step	41
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Segugio::Graph_Learnable::Weights_Manager	80

# Chapter 4

# **Class Index**

## 4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

Segugio::Node::Node_factory::_Baseline_4_Insertion< T >	29
Segugio::Node::Node_factory::_Pot_wrapper_4_Insertion	29
Segugio::Node::Node_factory::_SubGraph	30
Segugio::Advancer_Concrete	32
Segugio::atomic_Learning_handler	32
Segugio::Training_set::Basic_Extractor < Array >	
Basic extractor, see Training_set(const std::list <std::string>&amp; variable_names, std::list<array></array></std::string>	
	33
Segugio::BFGS	34
Segugio::Binary_handler	34
Segugio::Binary_handler_with_Observation	35
Segugio::Categoric_domain	35
Segugio::Categoric_var	
Describes a categoric variable	36
	37
Segugio::Conditional_Random_Field	
This class describes Conditional Random fields	38
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Segugio::Distribution_value	40
Segugio::Entire_Set	41
Segugio::Fixed_step	41
Segugio::I_Potential::Getter_4_Decorator	42
Segugio::Potential_Exp_Shape::Getter_weight_and_shape	42
Segugio::Graph	
Interface for managing generic graphs	42
Segugio::Graph Learnable	
Interface for managing learnable graphs, i.e. graphs for which it is possible perform learning 4	45
	46
Segugio::I belief propagation strategy	47
Segugio::I_Potential::I_Distribution_value	
Abstract interface for describing a value in the domain of a potential	48
Segugio::Training_set::I_Extractor< Array >	
This class is adopted for parsing a set of samples to import as a novel training set. You have to	
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Segugio::I_Potential	
Abstract interface for potentials handled by graphs	49
Segugio::I_Potential_Decorator< Wrapped_Type >	
Abstract decorator of a Potential, wrapping an Abstract potential	52
Segugio::I_Trainer	
This class is used by a Graph_Learnable, to perform training with an instance of a Training_set	53
Segugio::info_neighbourhood::info_neigh	55
Segugio::info_neighbourhood	55
Segugio::Loopy_belief_propagation	55
Segugio::Message_Unary	
This class is adopted by belief propagation algorithms. It is the message incoming to a node of the graph. Every node of a graph refers to a single Categorical variable. Internally it keeps track of the difference in time of the messages produced, in order to arrest loopy belief propagation.	56
Segugio::Messagge_Passing	58
Segugio::Node::Neighbour_connection	59
Segugio::Node	59
Segugio::Node::Node_factory	
Interface for describing a net: set of nodes representing random variables	60
Segugio::Potential	
This class is mainly adopted for computing operations on potentials	64
Segugio::Potential_Exp_Shape	
Represents an exponential potential, wrapping a normal shape one: every value of the domain	
are assumed as exp(mWeight * val_in_shape_wrapped)	66
Segugio::Potential_Shape	
It's the only possible concrete potential. It contains the domain and the image of the potential .	69
Segugio::Random_Field	
This class describes a generic Random Field, not having a particular set of variables observed	73
Segugio::Stoch_Set_variation	76
Segugio::Training_set::subset	
This class is describes a portion of a training set, obtained by sampling values in the original set.	
Mainly used by stochastic gradient computation strategies	76
Segugio::Trainer_Decorator	77
Segugio::Training_set	70
This class is used for describing a training set for a graph	78
Segugio::Unary_handler	80
Segugio: Graph Learnable: Weights Manager	80

# **Chapter 5**

# **Class Documentation**

5.1 Segugio::Node::Node\_factory::\_Baseline\_4\_Insertion< T > Struct Template Reference

Inheritance diagram for Segugio::Node::Node\_factory::\_Baseline\_4\_Insertion< T >:

### **Public Member Functions**

- \_Baseline\_4\_Insertion (T \*wrp)
- virtual const std::list< Categoric\_var \* > \* Get\_involved\_var\_safe ()
- virtual Potential \* Get\_Potential\_to\_Insert (const std::list< Categoric\_var \* > &var\_involved, const bool &get\_cloned)

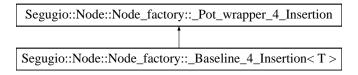
### **Protected Attributes**

T \* wrapped

The documentation for this struct was generated from the following file:

- C:/Users/andre/Desktop/CRF/CRF/Header/Node.h
- 5.2 Segugio::Node::Node\_factory::\_Pot\_wrapper\_4\_Insertion Struct Reference

Inheritance diagram for Segugio::Node::Node\_factory::\_Pot\_wrapper\_4\_Insertion:



### **Public Member Functions**

- virtual const std::list< Categoric var \* > \* Get\_involved\_var\_safe ()=0
- virtual Potential \* Get\_Potential\_to\_Insert (const std::list< Categoric\_var \* > &var\_involved, const bool &get cloned)=0

The documentation for this struct was generated from the following file:

· C:/Users/andre/Desktop/CRF/CRF/Header/Node.h

# 5.3 Segugio::Node::Node\_factory::\_SubGraph Class Reference

#### **Public Member Functions**

- \_SubGraph (Node\_factory \*Original\_graph, const std::list< Categoric\_var \* > &sub\_set\_to\_consider)

  Builds a reduction of the actual net, considering the actual observation values.
- void Get\_marginal\_prob\_combinations (std::list< float > \*result, const std::list< std::list< size\_t >> &combinations, const std::list< Categoric\_var \* > &var\_order\_in\_combination)

Returns the marginal probabilty of a some particular combinations of values assumed by the variables in this subgraph.

void Get\_marginal\_prob\_combinations (std::list< float > \*result, const std::list< size\_t \* > &combinations, const std::list< Categoric\_var \* > &var\_order\_in\_combination)

nst std::list< Categoric\_var \* > &var\_order\_in\_combination)

Similar to Get\_marginal\_prob\_combinations(std::list<float>\* result, const std::list< std::list< size\_t>>& combinations, const std::list<

void MAP (std::list< size t > \*result)

passing the combinations as pointer arrays.

Returns the Maximum a Posteriori estimation of the hidden set in the sugraph. .

void Gibbs\_Sampling (std::list< std::list< size\_t >> \*result, const unsigned int &N\_samples, const unsigned int &initial\_sample\_to\_skip)

Returns a set of samples for the variables involved in this subgraph. .

void Get All variables (std::list< Categoric var \* > \*result)

Returns the cluster of varaibles involved in this sub graph.

### 5.3.1 Constructor & Destructor Documentation

### 5.3.1.1 \_SubGraph()

Builds a reduction of the actual net, considering the actual observation values.

The subgraph is not automatically updated w.r.t. modifications of the originating net: in such cases just create a novel subgraph with the same sub\_set of variables involved

### 5.3.2 Member Function Documentation

### 5.3.2.1 Get\_marginal\_prob\_combinations()

Returns the marginal probabilty of a some particular combinations of values assumed by the variables in this subgraph.

The marginal probabilities computed are conditioned to the observations set when extracting this subgraph.

#### **Parameters**

out	result	the computed marginal probabilities	
in	combinations	combinations of values for which the marginals are computed: must have same size of var_order_in_combination.	
in	var_order_in_combination	order of variables considered when assembling the combinations.	

### 5.3.2.2 Gibbs\_Sampling()

Returns a set of samples for the variables involved in this subgraph. .

Sampling is done considering the marginal probability distribution of this cluster of variables, conditioned to the observations set at the time this subgraph was created. Samples are obtained through Gibbs sampling. Calculations are done considering the last last observations set (see Node factory::Set Observation Set var)

#### **Parameters**

in	N_samples	number of desired samples
in	initial_sample_to_skip	number of samples to skip for performing Gibbs sampling
out	result	returned samples: every element of the list is a combination of values for the hidden set, with the same order returned when calling _SubGraph::Get_All_variables

### 5.3.2.3 MAP()

Returns the Maximum a Posteriori estimation of the hidden set in the sugraph. .

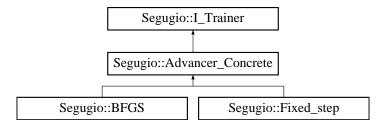
Values are ordered as returned by \_SubGraph::Get\_All\_variables. This MAP is conditioned to the observations set at the time this subgraph was created.

The documentation for this class was generated from the following files:

- · C:/Users/andre/Desktop/CRF/CRF/Header/Node.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Subgraph.cpp

# 5.4 Segugio::Advancer\_Concrete Class Reference

Inheritance diagram for Segugio::Advancer Concrete:



### **Public Member Functions**

- · virtual void Reset ()
- void **Train** (Graph\_Learnable \*model\_to\_train, Training\_set \*Train\_set, const unsigned int &Max\_Iterations, std::list< float > \*descend story)
- virtual float \_advance (Graph\_Learnable \*model\_to\_advance, const std::list< size\_t \* > &comb\_in\_train
   \_set, const std::list< Categoric\_var \* > &comb\_var)=0

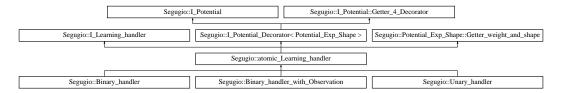
### **Additional Inherited Members**

The documentation for this class was generated from the following file:

C:/Users/andre/Desktop/CRF/CRF/Source/Trainer.cpp

# 5.5 Segugio::atomic\_Learning\_handler Class Reference

Inheritance diagram for Segugio::atomic\_Learning\_handler:



### **Public Member Functions**

- virtual void Get\_weight (float \*w)
- virtual void Set\_weight (const float &w\_new)
- virtual void Get\_grad\_alfa\_part (float \*alfa, const std::list< size\_t \* > &comb\_in\_train\_set, const std::list<</li>
   Categoric\_var \* > &comb\_var)
- bool is\_here\_Pot\_to\_share (const std::list< Categoric\_var \* > &vars\_of\_pot\_whose\_weight\_is\_to\_share)

#### **Protected Member Functions**

- atomic\_Learning\_handler (Potential\_Exp\_Shape \*pot\_to\_handle)
- atomic\_Learning\_handler (atomic\_Learning\_handler \*other)

#### **Protected Attributes**

- float \* pWeight
- std::list< I\_Distribution\_value \* > Extended\_shape\_domain

### **Additional Inherited Members**

The documentation for this class was generated from the following files:

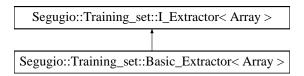
- C:/Users/andre/Desktop/CRF/CRF/Header/Graphical model.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Graphical\_model.cpp

# 5.6 Segugio::Training\_set::Basic\_Extractor < Array > Class Template Reference

Basic extractor, see Training\_set(const std::list<std::string>& variable\_names, std::list<Array>\* extractor)

```
#include <Training_set.h>
```

Inheritance diagram for Segugio::Training\_set::Basic\_Extractor< Array >:



### **Additional Inherited Members**

### 5.6.1 Detailed Description

```
template<typename Array> class Segugio::Training_set::Basic_Extractor< Array >
```

Basic extractor, see Training\_set(const std::list<std::string>& variable\_names, std::list<Array> samples, I\_← Extractor<Array>\* extractor)

The documentation for this class was generated from the following file:

C:/Users/andre/Desktop/CRF/CRF/Header/Training\_set.h

# 5.7 Segugio::BFGS Class Reference

Inheritance diagram for Segugio::BFGS:



#### **Public Member Functions**

· void Reset ()

### **Additional Inherited Members**

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Trainer.cpp

# 5.8 Segugio::Binary\_handler Class Reference

Inheritance diagram for Segugio::Binary\_handler:



### **Public Member Functions**

• Binary\_handler (Node \*N1, Node \*N2, Potential\_Exp\_Shape \*pot\_to\_handle)

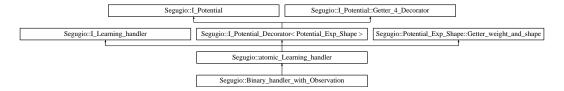
### **Additional Inherited Members**

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Graphical\_model.cpp

# 5.9 Segugio::Binary\_handler\_with\_Observation Class Reference

Inheritance diagram for Segugio::Binary\_handler\_with\_Observation:



### **Public Member Functions**

Binary\_handler\_with\_Observation (Node \*Hidden\_var, size\_t \*observed\_val, atomic\_Learning\_handler \*handle\_to\_substitute)

### **Additional Inherited Members**

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Graphical\_model.cpp

# 5.10 Segugio::Categoric\_domain Class Reference

Inheritance diagram for Segugio::Categoric\_domain:



### **Public Member Functions**

const float & operator[] (const size\_t &pos)

#### **Additional Inherited Members**

The documentation for this class was generated from the following files:

- · C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.11 Segugio::Categoric\_var Class Reference

Describes a categoric variable.

```
#include <Potential.h>
```

Inheritance diagram for Segugio::Categoric\_var:

```
Segugio::Categoric_var

Segugio::Categoric_domain
```

### **Public Member Functions**

- Categoric\_var (const size\_t &size, const std::string &name)
   domain is assumed to be {0,1,2,3,...,size}
- Categoric\_var (const Categoric\_var &to\_copy)
- const size\_t & size () const
- const std::string & Get\_name ()

### **Protected Attributes**

- size\_t Size
- std::string Name

# 5.11.1 Detailed Description

Describes a categoric variable.

, having a finite set as domain, assumed by default as  $\{0,1,2,3,...,\text{size}\}$ 

### 5.11.2 Constructor & Destructor Documentation

### 5.11.2.1 Categoric\_var()

domain is assumed to be {0,1,2,3,...,size}

#### **Parameters**

in size domain size of this variable		domain size of this variable
in	name	name to attach to this variable. It cannot be an empty string ""

#### 5.11.3 Member Data Documentation

#### 5.11.3.1 Name

```
std::string Segugio::Categoric_var::Name [protected]
```

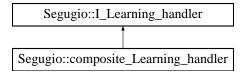
#### domain size

The documentation for this class was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.12 Segugio::composite\_Learning\_handler Class Reference

Inheritance diagram for Segugio::composite\_Learning\_handler:



### **Public Member Functions**

- composite Learning handler (atomic Learning handler \*initial A, atomic Learning handler \*initial B)
- virtual void Get\_weight (float \*w)
- virtual void Set\_weight (const float &w\_new)
- virtual void Get\_grad\_alfa\_part (float \*alfa, const std::list< size\_t \* > &comb\_in\_train\_set, const std::list<</li>
   Categoric\_var \* > &comb\_var)
- virtual void Get\_grad\_beta\_part (float \*beta)
- void Append (atomic Learning handler \*to add)
- bool is\_here\_Pot\_to\_share (const std::list< Categoric\_var \* > &vars\_of\_pot\_whose\_weight\_is\_to\_share)
- std::list< atomic\_Learning\_handler \* > \* Get\_components ()

The documentation for this class was generated from the following files:

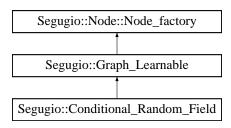
- · C:/Users/andre/Desktop/CRF/CRF/Header/Graphical model.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Graphical\_model.cpp

# 5.13 Segugio::Conditional\_Random\_Field Class Reference

This class describes Conditional Random fields.

```
#include <Graphical_model.h>
```

Inheritance diagram for Segugio::Conditional\_Random\_Field:



#### **Public Member Functions**

- Conditional\_Random\_Field (const std::string &config\_xml\_file, const std::string &prefix\_config\_xml\_file="")

  The model is built considering the information contained in an xml configuration file.
- Conditional\_Random\_Field (const std::list< Potential\_Exp\_Shape \* > &potentials, const std::list<</li>
   Categoric\_var \* > &observed\_var, const bool &use\_cloning\_Insert=true, const std::list< bool > &tunable← \_\_mask={}, const std::list< Potential\_Shape \* > &shapes={})

This constructor initializes the graph with the specified potentials passed as input, setting the variables passed as the one observed.

void Set\_Observation\_Set\_val (const std::list< size\_t > &new\_observed\_vals)
 see Node::Node\_factory::Set\_Observation\_Set\_val(const std::list< size\_t>& new\_observed\_vals)

### **Additional Inherited Members**

### 5.13.1 Detailed Description

This class describes Conditional Random fields.

Set\_Observation\_Set\_var is depracated: the observed set of variables cannot be changed after construction.

### 5.13.2 Constructor & Destructor Documentation

#### 5.13.2.1 Conditional\_Random\_Field() [1/2]

The model is built considering the information contained in an xml configuration file. .

See Section 2 of the documentation for the syntax to adopt.

#### **Parameters**

in	configuration	file
in	prefix	to use. The file prefix_config_xml_file/config_xml_file is searched.

### 5.13.2.2 Conditional\_Random\_Field() [2/2]

This constructor initializes the graph with the specified potentials passed as input, setting the variables passed as the one observed.

#### **Parameters**

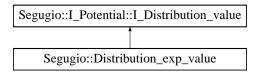
in	potentials	the initial set of exponential potentials to insert (can be empty)
in	observed_var	the set of variables to assume as observations
in	use_cloning_Insert	when is true, every time an Insert of a novel potential is called (this includes the passed potentials), a copy of that potential is actually inserted. Otherwise, the passed potential is inserted as is: this can be dangerous, cause that potential cna be externally modified, but the construction of a novel graph is faster.
in	tunable_mask	when passed as non default value, it is must have the same size of potentials.  Every value in this list is true if the corresponfing potential in the potentials list is tunable, i.e. has a weight whose value can vary with learning
in	shapes	A list of additional non learnable potentials to insert in the model

The documentation for this class was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Graphical\_model.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Graphical\_model.cpp

# 5.14 Segugio::Distribution\_exp\_value Struct Reference

Inheritance diagram for Segugio::Distribution\_exp\_value:



### **Public Member Functions**

- Distribution\_exp\_value (Distribution\_value \*to\_wrap, float \*weight)
- void Set\_val (const float &v)
- void Get\_val (float \*result)
- size\_t \* Get\_indeces ()

### **Protected Attributes**

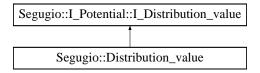
- float \* w
- Distribution\_value \* wrapped

The documentation for this struct was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.15 Segugio::Distribution\_value Struct Reference

Inheritance diagram for Segugio::Distribution\_value:



### **Public Member Functions**

- Distribution\_value (size\_t \*ind, const float &v=0.f)
- void Set\_val (const float &v)
- void Get\_val (float \*result)
- size t \* Get\_indeces ()

### **Protected Attributes**

- size\_t \* indices
- · float val

### **Friends**

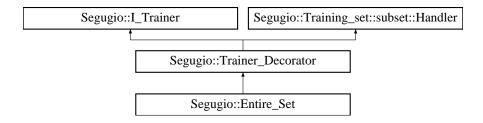
• struct Distribution\_exp\_value

The documentation for this struct was generated from the following file:

C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.16 Segugio::Entire\_Set Class Reference

Inheritance diagram for Segugio::Entire\_Set:



### **Public Member Functions**

- Entire\_Set (Advancer\_Concrete \*to\_wrap)
- void Train (Graph\_Learnable \*model\_to\_train, Training\_set \*Train\_set, const unsigned int &Max\_Iterations, std::list< float > \*descend\_story)

### **Additional Inherited Members**

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Trainer.cpp

# 5.17 Segugio::Fixed\_step Class Reference

Inheritance diagram for Segugio::Fixed\_step:



### **Public Member Functions**

• Fixed\_step (const float &step)

### **Additional Inherited Members**

The documentation for this class was generated from the following file:

C:/Users/andre/Desktop/CRF/CRF/Source/Trainer.cpp

# 5.18 Segugio::I\_Potential::Getter\_4\_Decorator Struct Reference

Inheritance diagram for Segugio::I\_Potential::Getter\_4\_Decorator:

			Segugio::I_Potential	::Getter_4_Decorator			
Segugio::I_Potential_Decorator< I_Potential >		Segugio::I_Potential_Decorat	tor< Potential_Exp_Shape >	Segugio::I_Potential_Dec	orator< Potential_Shape >	Segugio::I_Potential_Dec	orator< Wrapped_Type >
Segugio::Potential		Segugio::atomic_I	Learning_handler	Segugio::Poten	tial_Exp_Shape		
					1		
Segugio::Message_Unary	Segugio::Binary_handler	Segugio::Binary_hand	ler_with_Observation	Segugio::Ur	nary_handler		

#### Static Protected Member Functions

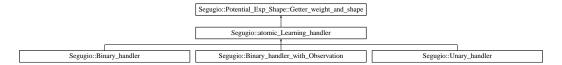
- static const std::list< Categoric\_var \* > \* Get\_involved\_var (I\_Potential \*pot)
- static std::list< I\_Distribution\_value \* > \* Get\_distr (I\_Potential \*pot)

The documentation for this struct was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h

# 5.19 Segugio::Potential\_Exp\_Shape::Getter\_weight\_and\_shape Struct Reference

Inheritance diagram for Segugio::Potential\_Exp\_Shape::Getter\_weight\_and\_shape:



### **Static Protected Member Functions**

- static float \* Get weight (Potential Exp Shape \*pot)
- static Potential\_Shape \* Get\_shape (Potential\_Exp\_Shape \*pot)

The documentation for this struct was generated from the following file:

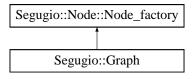
• C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h

# 5.20 Segugio::Graph Class Reference

Interface for managing generic graphs.

#include <Graphical\_model.h>

Inheritance diagram for Segugio::Graph:



#### **Public Member Functions**

- Graph (const bool &use\_cloning\_Insert=true)
  - empty constructor
- Graph (const std::string &config\_xml\_file, const std::string &prefix\_config\_xml\_file="")

The model is built considering the information contained in an xml configuration file. .

Graph (const std::list< Potential\_Shape \* > &potentials, const std::list< Potential\_Exp\_Shape \* > &potentials exp, const bool &use cloning Insert=true)

This constructor initializes the graph with the specified potentials passed as input.

void Insert (Potential\_Shape \*pot)

The model is built considering the information contained in an xml configuration file.

void Insert (Potential\_Exp\_Shape \*pot)

The model is built considering the information contained in an xml configuration file.

void Set\_Observation\_Set\_var (const std::list< Categoric\_var \* > &new\_observed\_vars)

see Node::Node factory::Set Observation Set var(const std::list<Categoric var\*>& new observed vars)

void Set\_Observation\_Set\_val (const std::list< size\_t > &new\_observed\_vals)

see Node::Node\_factory::Set\_Observation\_Set\_val(const std::list<size\_t>& new\_observed\_vals)

#### **Additional Inherited Members**

### 5.20.1 Detailed Description

Interface for managing generic graphs.

Both Exponential and normal shapes can be included into the model. Learning is not possible: all belief propagation operations are performed assuming the mdoel as is. Every Potential\_Shape or Potential\_Exp\_Shape is copied and that copy is inserted into the model.

### 5.20.2 Constructor & Destructor Documentation

### empty constructor

#### **Parameters**

in	use_cloning_Insert	when is true, every time an Insert of a novel potential is called, a copy of that
		potential is actually inserted. Otherwise, the passed potential is inserted as is:
		this can be dangerous, cause that potential cna be externally modified, but the
		construction of a novel graph is faster.

### **5.20.2.2 Graph()** [2/3]

The model is built considering the information contained in an xml configuration file. .

See Section 2 of the documentation for the syntax to adopt.

#### **Parameters**

in	configuration	file
in	prefix	to use. The file prefix_config_xml_file/config_xml_file is searched.

### **5.20.2.3 Graph()** [3/3]

This constructor initializes the graph with the specified potentials passed as input.

### **Parameters**

in	potentials	the initial set of potentials to insert (can be empty)
in	potentials_exp	the initial set of exponential potentials to insert (can be empty)
in	use_cloning_Insert	when is true, every time an Insert of a novel potential is called (this includes the passed potentials), a copy of that potential is actually inserted. Otherwise, the passed potential is inserted as is: this can be dangerous, cause that potential cna be externally modified, but the construction of a novel graph is faster.

### 5.20.3 Member Function Documentation

The model is built considering the information contained in an xml configuration file.

#### **Parameters**

in	the	potential to insert. It can be a unary or a binary potential. In case it is binary, at least one of the
		variable involved must be already inserted to the model before (with a previous Insert having as
		input a potential which involves that variable).

The model is built considering the information contained in an xml configuration file.

#### **Parameters**

in	the	potential to insert. It can be a unary or a binary potential. In case it is binary, at least one of the
		variable involved must be already inserted to the model before (with a previous Insert having as
		input a potential which involves that variable).

The documentation for this class was generated from the following files:

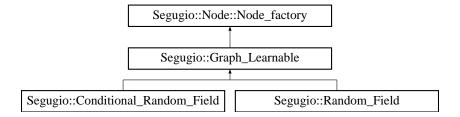
- C:/Users/andre/Desktop/CRF/CRF/Header/Graphical\_model.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Graphical\_model.cpp

# 5.21 Segugio::Graph\_Learnable Class Reference

Interface for managing learnable graphs, i.e. graphs for which it is possible perform learning.

```
#include <Graphical_model.h>
```

Inheritance diagram for Segugio::Graph\_Learnable:



### **Classes**

struct Weights\_Manager

#### **Public Member Functions**

size\_t Get\_model\_size ()

Returns the model size, i.e. the number of tunable parameters of the model, i.e. the number of weights that can vary with learning.

void Get\_Likelihood\_estimation (float \*result, const std::list< size\_t \* > &comb\_train\_set, const std::list<</li>
 Categoric\_var \* > &comb\_var\_order)

### **Protected Member Functions**

- virtual \_Pot\_wrapper\_4\_Insertion \* Get\_Inserter (Potential\_Exp\_Shape \*pot, const bool &weight\_tunability)
- Graph\_Learnable (const bool &use\_cloning\_Insert)
- **Graph\_Learnable** (const std::list< Potential\_Exp\_Shape \* > &potentials\_exp, const bool &use\_cloning\_← Insert, const std::list< bool > &tunable mask, const std::list< Potential Shape \* > &shapes)
- void Get complete atomic handler list (std::list< atomic Learning handler \* > \*atomic list)
- void Remove (atomic Learning handler \*to remove)
- void Share\_weight (I\_Learning\_handler \*pot\_involved, const std::list< Categoric\_var \* > &vars\_of\_pot\_
   whose\_weight\_is\_to\_share)
- · void Import XML sharing weight info (XML reader &reader)

#### **Protected Attributes**

std::list< | Learning handler \* > Model\_handlers

### 5.21.1 Detailed Description

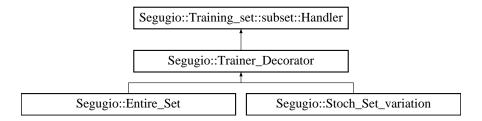
Interface for managing learnable graphs, i.e. graphs for which it is possible perform learning.

The documentation for this class was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Graphical\_model.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Graphical\_model.cpp

# 5.22 Segugio::Training\_set::subset::Handler Struct Reference

Inheritance diagram for Segugio::Training\_set::subset::Handler:



### **Static Protected Member Functions**

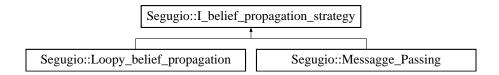
- static std::list< size t \* > \* Get\_list (subset \*sub\_set)
- static std::list< std::string > \* Get\_names (subset \*sub\_set)
- static std::list< std::string > \* Get\_names (Training\_set \*set)

The documentation for this struct was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Header/Training set.h

# 5.23 Segugio::I\_belief\_propagation\_strategy Class Reference

Inheritance diagram for Segugio::I\_belief\_propagation\_strategy:



### **Static Public Member Functions**

 static bool Propagate (std::list< Node \* > &cluster, const bool &sum\_or\_MAP=true, const unsigned int &Iterations=1000)

### **Protected Member Functions**

- void Instantiate\_message (Node::Neighbour\_connection \*outgoing\_mex\_to\_compute, const bool &sum
   —or\_MAP)
- void **Update\_message** (float \*variation\_to\_previous, Node::Neighbour\_connection \*outgoing\_mex\_to\_

   compute, const bool &sum\_or\_MAP)
- void **Gather\_incoming\_messages** (std::list< Potential \* > \*result, Node::Neighbour\_connection \*outgoing\_mex\_to\_compute)
- std::list< Node::Neighbour connection \* > \* Get Neighbourhood (Node::Neighbour connection \*conn)
- Message Unary \*\* Get Mex to This (Node::Neighbour connection \*conn)
- Message\_Unary \*\* Get\_Mex\_to\_Neigh (Node::Neighbour\_connection \*conn)

The documentation for this class was generated from the following files:

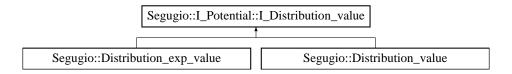
- C:/Users/andre/Desktop/CRF/CRF/Header/Node.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Belief\_propagation.cpp

# 5.24 Segugio::I\_Potential::I\_Distribution\_value Struct Reference

Abstract interface for describing a value in the domain of a potential.

```
#include <Potential.h>
```

Inheritance diagram for Segugio::I\_Potential::I\_Distribution\_value:



### **Public Member Functions**

- virtual void Set\_val (const float &v)=0
- virtual void Get\_val (float \*result)=0
- virtual size\_t \* Get\_indeces ()=0

### 5.24.1 Detailed Description

Abstract interface for describing a value in the domain of a potential.

The documentation for this struct was generated from the following file:

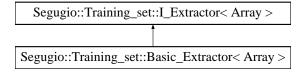
· C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h

# 5.25 Segugio::Training\_set::I\_Extractor < Array > Class Template Reference

This class is adopted for parsing a set of samples to import as a novel training set. You have to derive yout custom extractor, implementing the two vritual method.

```
#include <Training_set.h>
```

Inheritance diagram for Segugio::Training\_set::I\_Extractor< Array >:



### **Public Member Functions**

- virtual const size\_t & get\_val\_in\_pos (const Array &container, const size\_t &pos)=0
- virtual size\_t get\_size (const Array &container)=0

### 5.25.1 Detailed Description

template<typename Array>
class Segugio::Training\_set::I\_Extractor< Array>

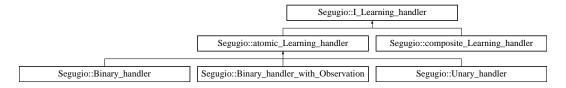
This class is adopted for parsing a set of samples to import as a novel training set. You have to derive yout custom extractor, implementing the two vritual method.

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Header/Training\_set.h

# 5.26 Segugio::I\_Learning\_handler Class Reference

Inheritance diagram for Segugio::I\_Learning\_handler:



### **Public Member Functions**

- virtual void Get\_weight (float \*w)=0
- virtual void Set\_weight (const float &w\_new)=0
- virtual void Get\_grad\_alfa\_part (float \*alfa, const std::list< size\_t \* > &comb\_in\_train\_set, const std::list<</li>
   Categoric\_var \* > &comb\_var)=0
- virtual void Get grad beta part (float \*beta)=0

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Header/Graphical\_model.h

# 5.27 Segugio::I\_Potential Class Reference

Abstract interface for potentials handled by graphs.

#include <Potential.h>

Inheritance diagram for Segugio::I\_Potential:



#### **Classes**

- · struct Getter 4 Decorator
- · struct I Distribution value

Abstract interface for describing a value in the domain of a potential.

#### **Public Member Functions**

- I\_Potential (const | Potential &to copy)
- void Print\_distribution (std::ostream &f, const bool &print\_entire\_domain=false)

when print\_entire\_domain is true, the entire domain is printed, even though the potential has a sparse distribution

- const std::list< Categoric\_var \* > \* Get\_involved\_var\_safe () const
  - return list of references to the variables representing the domain of this Potential
- void Find\_Comb\_in\_distribution (std::list< float > \*result, const std::list< size\_t \* > &comb\_to\_search, const std::list< Categoric\_var \* > &comb\_to\_search\_var\_order)
- float max in distribution ()

Returns the maximum value in the distribution describing this potential.

### **Static Public Member Functions**

static void Get\_entire\_domain (std::list< std::list< size\_t >> \*domain, const std::list< Categoric\_var \* >
 &Vars\_in\_domain)

get entire domain of a group of variables: list of possible combinations

static void Get\_entire\_domain (std::list< size\_t \* > \*domain, const std::list< Categoric\_var \* > &Vars\_in←
 \_domain)

Same as Get\_entire\_domain(std::list<std::list<size\_t>>\* domain, const std::list<Categoric\_var\*>& Vars\_in\_domain), but adopting array internally allocated with malloc instead of list: remembre to delete combinations.

### **Protected Member Functions**

- virtual const std::list< Categoric var \* > \* Get\_involved\_var () const =0
- virtual std::list< I\_Distribution\_value \* > \* Get\_distr ()=0

### **Static Protected Member Functions**

- static void Find\_Comb\_in\_distribution (std::list< I\_Distribution\_value \* > \*result, const std::list< size\_t \* > &comb\_to\_search, const std::list< Categoric\_var \* > &comb\_to\_search\_var\_order, I\_Potential \*pot)
- static void Find\_Comb\_in\_distribution (std::list< I\_Distribution\_value \* > \*result, size\_t \*partial\_comb
   —
   — to\_search, const std::list< Categoric\_var \* > &partial\_comb\_to\_search\_var\_order, I\_Potential \*pot)

### 5.27.1 Detailed Description

Abstract interface for potentials handled by graphs.

### 5.27.2 Member Function Documentation

### 5.27.2.1 Find\_Comb\_in\_distribution()

#### **Parameters**

out	result	the list of values matching the combinations to find sent as input
in	comb_to_search	domain list of combinations (i.e. values of the domain) whose values
		are to find
in	comb_to_search_var_order	order of variables used for assembling the combinations to find

### **5.27.2.2 Get\_entire\_domain()** [1/2]

get entire domain of a group of variables: list of possible combinations

#### **Parameters**

	out	domain	the entire set of possible combinations
Ī	in	Vars_in_domain	variables involved whose domain has to be compute

### **5.27.2.3** Get\_entire\_domain() [2/2]

Same as Get\_entire\_domain(std::list<std::list<size\_t>>\* domain, const std::list<Categoric\_var\*>& Vars\_in\_domain), but adopting array internally allocated with malloc instead of list: remembre to delete combinations.

### **Parameters**

out	domain	the entire set of possible combinations
in	Vars_in_domain	variables involved whose domain has to be compute

### 5.27.2.4 Print\_distribution()

when print\_entire\_domain is true, the entire domain is printed, even though the potential has a sparse distribution

#### **Parameters**

in	f	out stream to target
in	print_entire_domain	

The documentation for this class was generated from the following files:

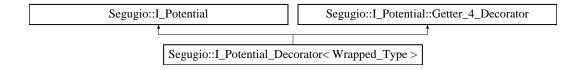
- · C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.28 Segugio::I\_Potential\_Decorator < Wrapped\_Type > Class Template Reference

Abstract decorator of a Potential, wrapping an Abstract potential.

```
#include <Potential.h>
```

Inheritance diagram for Segugio::I\_Potential\_Decorator< Wrapped\_Type >:



### **Protected Member Functions**

- I\_Potential\_Decorator (Wrapped\_Type \*to\_wrap)
- virtual const std::list< Categoric var \* > \* Get involved var () const
- virtual std::list< I\_Distribution\_value \* > \* Get\_distr ()

### **Protected Attributes**

- bool Destroy\_wrapped
- Wrapped\_Type \* pwrapped

### **Additional Inherited Members**

### 5.28.1 Detailed Description

```
template<typename Wrapped_Type>
class Segugio::I_Potential_Decorator< Wrapped_Type>
```

Abstract decorator of a Potential, wrapping an Abstract potential.

### 5.28.2 Member Data Documentation

#### 5.28.2.1 pwrapped

```
template<typename Wrapped_Type>
Wrapped_Type* Segugio::I_Potential_Decorator< Wrapped_Type >::pwrapped [protected]
```

when false, the wrapped abstract potential is wrapped also in another decorator, whihc is in charge of deleting the wrapped potential

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h

# 5.29 Segugio::I\_Trainer Class Reference

This class is used by a Graph\_Learnable, to perform training with an instance of a Training\_set.

```
#include <Trainer.h>
```

Inheritance diagram for Segugio:: I Trainer:



### **Public Member Functions**

• virtual void **Train** (Graph\_Learnable \*model\_to\_train, Training\_set \*Train\_set, const unsigned int &Max\_← lterations=100, std::list< float > \*descend\_story=NULL)=0

### **Static Public Member Functions**

- static I\_Trainer \* Get\_fixed\_step (const float &step\_size=0.1f, const float &stoch\_grad\_percentage=1.f)

  Creates a fixed step gradient descend solver.
- static I\_Trainer \* Get\_BFGS (const float &stoch\_grad\_percentage=1.f)

Creates a BFGS gradient descend solver ( https://en.wikipedia.org/wiki/Broyden%E2%80%93 $\leftarrow$  Fletcher%E2%80%93Goldfarb%E2%80%93Shanno\_algorithm)

### **Protected Member Functions**

- virtual void Clean\_Up ()
- void Get\_w\_grad (Graph\_Learnable \*model, std::list< float > \*grad\_w, const std::list< size\_t \* > &comb
   —
   in\_train\_set, const std::list< Categoric\_var \* > &comb\_var)
- void Set\_w (const std::list< float > &w, Graph\_Learnable \*model)

### **Static Protected Member Functions**

static void Clean\_Up (I\_Trainer \*to\_Clean)

### 5.29.1 Detailed Description

This class is used by a Graph\_Learnable, to perform training with an instance of a Training\_set.

Instantiate a particular class of trainer to use by calling Get\_fixed\_step or Get\_BFGS. That methods allocate in the heap a trainer to use later, for multiple training sessions. Remember to delete the instantiated trainer.

### 5.29.2 Member Function Documentation

### 5.29.2.1 Get\_BFGS()

Creates a BFGS gradient descend solver (https://en.wikipedia.org/wiki/Broyden%← E2%80%93Fletcher%E2%80%93Goldfarb%E2%80%93Shanno\_algorithm)

### **Parameters**

in	stoch_grad_percentage	percentage of the training set to use every time for evaluating the gradient

# 5.29.2.2 Get\_fixed\_step()

Creates a fixed step gradient descend solver.

### **Parameters**

in	step_size	learinig degree
in	stoch_grad_percentage	percentage of the training set to use every time for evaluating the gradient

The documentation for this class was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Trainer.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Trainer.cpp

# 5.30 Segugio::info\_neighbourhood::info\_neigh Struct Reference

### **Public Attributes**

- Potential \* shared\_potential
- Categoric\_var \* Var
- size\_t Var\_pos

The documentation for this struct was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Node.cpp

# 5.31 Segugio::info\_neighbourhood Struct Reference

#### Classes

• struct info\_neigh

### **Public Attributes**

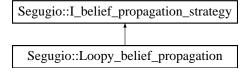
- size\_t Involved\_var\_pos
- list< info neigh > Info
- list < Potential \* > Unary\_potentials

The documentation for this struct was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Node.cpp

# 5.32 Segugio::Loopy\_belief\_propagation Class Reference

Inheritance diagram for Segugio::Loopy\_belief\_propagation:



### **Public Member Functions**

- Loopy\_belief\_propagation (const int &max\_iter)
- bool \_propagate (std::list< Node \* > &cluster, const bool &sum\_or\_MAP)

#### **Protected Attributes**

· unsigned int Iter

### **Additional Inherited Members**

The documentation for this class was generated from the following files:

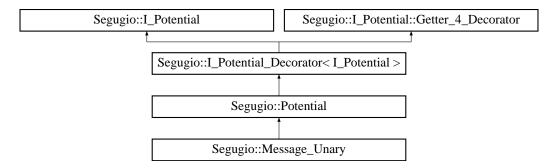
- C:/Users/andre/Desktop/CRF/CRF/Header/Belief propagation.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Belief\_propagation.cpp

# 5.33 Segugio::Message\_Unary Class Reference

This class is adopted by belief propagation algorithms. It is the message incoming to a node of the graph. Every node of a graph refers to a single Categorical variable. Internally it keeps track of the difference in time of the messages produced, in order to arrest loopy belief propagation.

```
#include <Potential.h>
```

Inheritance diagram for Segugio::Message Unary:



### **Public Member Functions**

Message Unary (Categoric var \*var involved)

Creates a Message with all 1 as values for the image.

 Message\_Unary (Potential \*binary\_to\_merge, const std::list< Potential \* > &potential\_to\_merge, const bool &Sum or MAP=true)

Firstly, all potential\_to\_merge are merged together using Potential::Potential(potential\_to\_merge, false) obtaining a merged potential. Secondly, the product of binary\_to\_merge and the merged potential is obtained. Finally the message is obtained by marginalizing from the second product, the variable of potential\_to\_merge, adopting a sum or a MAP. Exploited by message passing algorithms.

• Message\_Unary (Potential \*binary\_to\_merge, Categoric\_var \*var\_to\_marginalize, const bool &Sum\_or\_← MAP=true)

Same as  $Message\_Unary::Message\_Unary(Potential* binary\_to\_merge, const std::list<Potential*>& potential\_\leftarrow to\_merge, const bool& Sum\_or\_MAP = true), but in the case potential\_to\_merge is empty.$ 

void Update (float \*diff\_to\_previous, Potential \*binary\_to\_merge, const std::list< Potential \* > &potential ←
 \_to\_merge, const bool &Sum\_or\_MAP=true)

Adopted by loopy belief propagation.

• void Update (float \*diff\_to\_previous, Potential \*binary\_to\_merge, Categoric\_var \*var\_to\_marginalize, const bool &Sum\_or\_MAP=true)

Adopted by loopy belief propagation.

### **Additional Inherited Members**

### 5.33.1 Detailed Description

This class is adopted by belief propagation algorithms. It is the message incoming to a node of the graph. Every node of a graph refers to a single Categorical variable. Internally it keeps track of the difference in time of the messages produced, in order to arrest loopy belief propagation.

### 5.33.2 Constructor & Destructor Documentation

Creates a Message with all 1 as values for the image.

#### **Parameters**

in	var_involved	the only variable in the domain	
----	--------------	---------------------------------	--

### **5.33.2.2** Message\_Unary() [2/2]

Firstly, all potential\_to\_merge are merged together using Potential::Potential(potential\_to\_merge, false) obtaining a merged potential. Secondly, the product of binary\_to\_merge and the merged potential is obtained. Finally the message is obtained by marginalizing from the second product, the variable of potential\_to\_merge, adopting a sum or a MAP. Exploited by message passing algorithms.

### **Parameters**

in	binary_to_merge	binaty potential to consider
in	potential_to_merge	list of potentials to merge. The must be unary potentials

### 5.33.3 Member Function Documentation

### 5.33.3.1 Update() [1/2]

Adopted by loopy belief propagation.

#### **Parameters**

out	diff_to_previous	The difference with respect to the previous message camptation
-----	------------------	----------------------------------------------------------------

### **5.33.3.2 Update()** [2/2]

Adopted by loopy belief propagation.

#### **Parameters**

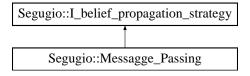
	out	diff_to_previous	The difference with respect to the previous message camptation	]
--	-----	------------------	----------------------------------------------------------------	---

The documentation for this class was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.34 Segugio::Messagge\_Passing Class Reference

Inheritance diagram for Segugio::Messagge\_Passing:



### **Public Member Functions**

bool \_propagate (std::list< Node \* > &cluster, const bool &sum\_or\_MAP)

### **Additional Inherited Members**

The documentation for this class was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Belief\_propagation.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Belief\_propagation.cpp

# 5.35 Segugio::Node::Neighbour\_connection Struct Reference

#### **Friends**

- · class Node
- · class I\_belief\_propagation\_strategy

The documentation for this struct was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Node.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Node.cpp

# 5.36 Segugio::Node Class Reference

#### Classes

- struct Neighbour\_connection
- class Node\_factory

Interface for describing a net: set of nodes representing random variables.

### **Public Member Functions**

- Categoric\_var \* Get\_var ()
- void Gather\_all\_Unaries (std::list< Potential \* > \*result)
- void Append\_temporary\_permanent\_Unaries (std::list< Potential \* > \*result)
- void Append permanent Unaries (std::list< Potential \* > \*result)
- $\bullet \ \ \ \ \text{const std::list} < \ \ \text{Neighbour\_connection} * > * \ \ \textbf{Get\_Active\_connections} \ ()$
- void Compute\_neighbour\_set (std::list< Node \* > \*Neigh\_set)
- void Compute neighbour set (std::list< Node \* > \*Neigh set, std::list< Potential \* > \*binary involved)
- void Compute\_neighbourhood\_messages (std::list< Potential \* > \*messages, Node \*node\_involved\_← in connection)

The documentation for this class was generated from the following files:

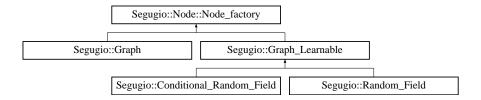
- · C:/Users/andre/Desktop/CRF/CRF/Header/Node.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Node.cpp

# 5.37 Segugio::Node::Node\_factory Class Reference

Interface for describing a net: set of nodes representing random variables.

#include <Node.h>

Inheritance diagram for Segugio::Node::Node\_factory:



#### **Classes**

- struct \_Baseline\_4\_Insertion
- struct \_Pot\_wrapper\_4\_Insertion
- · class \_SubGraph

### **Public Member Functions**

Categoric\_var \* Find\_Variable (const std::string &var\_name)

Returns a pointer to the variable in this graph with that name.

• Categoric\_var \* Find\_Variable (Categoric\_var \*var\_with\_same\_name)

Returns a pointer to the variable in this graph with the same name of the variable passed as input.

void Get\_Actual\_Hidden\_Set (std::list< Categoric\_var \* > \*result)

Returns the current set of hidden variables.

void Get\_Actual\_Observation\_Set (std::list< Categoric\_var \* > \*result)

Returns the current set of observed variables.

void Get\_All\_variables\_in\_model (std::list< Categoric\_var \* > \*result)

Returns the set of all variable contained in the net.

void Get\_marginal\_distribution (std::list< float > \*result, Categoric\_var \*var)

Returns the marginal probabilty of the variable passed P(var|model, observations),.

void MAP\_on\_Hidden\_set (std::list< size\_t > \*result)

Returns the Maximum a Posteriori estimation of the hidden set. .

void Gibbs\_Sampling\_on\_Hidden\_set (std::list< std::list< size\_t >> \*result, const unsigned int &N\_← samples, const unsigned int &initial\_sample\_to\_skip)

Returns a set of samples of the conditional distribution P(hidden variables | model, observed variables). .

unsigned int Get\_Iteration\_4\_belief\_propagation ()

Returns the current value adopted when performing a loopy belief propagation.

void Set\_Iteration\_4\_belief\_propagation (const unsigned int &iter\_to\_use)

Returns the value to adopt when performing a loopy belief propagation.

void Eval\_Log\_Energy\_function (float \*result, size\_t \*combination, const std::list< Categoric\_var \* > &var←
 \_order\_in\_combination)

Returns the logartihmic value of the energy function.

void Eval\_Log\_Energy\_function (float \*result, const std::list< size\_t > &combination, const std::list<</li>
 Categoric\_var \* > &var\_order\_in\_combination)

Same as Eval\_Log\_Energy\_function(float\* result, size\_t\* combination, const std::list<Categoric\_var\*>& var\_order\_in\_combination), passing a list instead of an array size\_t\*, a list<size\_t> for describing the combination for which you want to evaluate the energy.

void Eval\_Log\_Energy\_function (std::list< float > \*result, const std::list< size\_t \* > &combinations, const std::list< Categoric\_var \* > &var\_order\_in\_combination)

Same as Eval\_Log\_Energy\_function(float\* result, size\_t\* combination, const std::list<Categoric\_var\*>& var\_order\_in\_combination), passing a list of combinations: don't iterate yourself many times using Eval\_Log\_Energy\_function(float\* result, size\_t\* combination, const but call this function.

void Eval\_Log\_Energy\_function\_normalized (float \*result, size\_t \*combination, const std::list
 Categoric var \* > &var order in combination)

Similar as Eval\_Log\_Energy\_function(float\* result, size\_t\* combination, const std::list< Categoric\_var\*>& var\_order\_in\_combination), but computing the Energy function normalized:  $E_norm = E(Y_1, 2, ...., n) / max possible \{ E \}$ .  $E_norm$  is in [0,1]. The logarithmic value of  $E_norm$  is actually returned.

void Eval\_Log\_Energy\_function\_normalized (float \*result, const std::list< size\_t > &combination, const std::list< Categoric\_var \* > &var\_order\_in\_combination)

Similar as Eval\_Log\_Energy\_function(float\* result, const std::list< size\_t>& combination, const std::list< Categoric\_var\*>& var\_order\_in\_combination.

void Eval\_Log\_Energy\_function\_normalized (std::list< float > \*result, const std::list< size\_t \* > &combinations, const std::list< Categoric\_var \* > &var\_order\_in\_combination)

is, const std::list< Categoric\_var \* > &var\_order\_in\_combination)

Similar as Eval\_Log\_Energy\_function(std::list<float>\* result, const std::list<size\_t\*>& combinations, const std::list<Categoric\_var\*>

Output

Description:

void Get\_Observation\_Set\_val (std::list< size\_t > \*result)

but computing the Energy function normalized.

but computing the Energy function normalized.

Returns the attual values set observations. This function can be invokated after a call to void Set\_Observation\_Set\_val(const std::list< size

void Get structure (std::list< const Potential \* > \*structure)

Returns the list of potentials constituting the net. Usefull for structural learning.

• size t Get structure size ()

Returns the number of potentials constituting the graph, no matter of their type (simple shape, exponential shape fixed or exponential shape tunable)

### **Protected Member Functions**

- Node\_factory (const bool &use\_cloning\_Insert)
- void Import\_from\_XML (XML\_reader \*xml\_data, const std::string &prefix\_config\_xml\_file)
- void Insert (\_Pot\_wrapper\_4\_Insertion \*element\_to\_add)
- void Insert (std::list< \_Pot\_wrapper\_4\_Insertion \* > &elements\_to\_add)
- virtual \_Pot\_wrapper\_4\_Insertion \* Get\_Inserter (Potential\_Exp\_Shape \*pot, const bool &weight\_tunability)
- void Insert (Potential\_Shape \*pot)
- void Insert (Potential Exp Shape \*pot, const bool &weight tunability)
- Node \* Find\_Node (const std::string &var\_name)
- void Set\_Observation\_Set\_var (const std::list< Categoric\_var \* > &new\_observed\_vars)

Set the values for the observations. Must call after calling Node\_factory::Set\_Observation\_Set\_val.

void Set Observation Set val (const std::list< size t > &new observed vals)

Set the observation set: which variables are treated like evidence when performing belief propagation.

- void Belief\_Propagation (const bool &sum\_or\_MAP)
- size\_t \* Get\_observed\_val\_in\_case\_is\_in\_observed\_set (Categoric\_var \*var)

### 5.37.1 Detailed Description

Interface for describing a net: set of nodes representing random variables.

### 5.37.2 Member Function Documentation

### 5.37.2.1 Eval\_Log\_Energy\_function()

Returns the logartihmic value of the energy function.

Energy function  $E=Pot_1(Y_1,2,...,n)*Pot_2(Y_1,2,...,n)*...*Pot_m(Y_1,2,...,n)$ . The combinations passed as input must contains values for all the variables present in this graph.

### **Parameters**

out	result	
in	combination	set of values in the combination for which the energy function has to be
		eveluated
in	var_order_in_combination	order of variables considered when assembling combination. They must
		be references to the variables actually wrapped by this graph.

### **5.37.2.2** Find\_Variable() [1/2]

Returns a pointer to the variable in this graph with that name.

Returns NULL when the variable is not present in the graph.

### **Parameters**

```
in var_name name to search
```

### **5.37.2.3** Find\_Variable() [2/2]

Returns a pointer to the variable in this graph with the same name of the variable passed as input.

Returns NULL when the variable is not present in the graph

#### **Parameters**

in	var_with_same_name	variable having the same of name of the variable to search
----	--------------------	------------------------------------------------------------

### 5.37.2.4 Get\_marginal\_distribution()

Returns the marginal probabilty of the variable passed P(var|model, observations),.

on the basis of the last observations set (see Node\_factory::Set\_Observation\_Set\_var)

### 5.37.2.5 Gibbs\_Sampling\_on\_Hidden\_set()

```
void Segugio::Node::Node_factory::Gibbs_Sampling_on_Hidden_set (
    std::list< std::list< size_t >> * result,
    const unsigned int & N_samples,
    const unsigned int & initial_sample_to_skip )
```

Returns a set of samples of the conditional distribution P(hidden variables | model, observed variables). .

Samples are obtained through Gibbs sampling. Calculations are done considering the last last observations set (see Node\_factory::Set\_Observation\_Set\_var)

#### **Parameters**

in	N_samples	number of desired samples
in	initial_sample_to_skip	number of samples to skip for performing Gibbs sampling
ou	t result	returned samples: every element of the list is a combination of values for the hidden set, with the same order returned when calling Node_factory::Get_Actual_Hidden_Set

### 5.37.2.6 MAP\_on\_Hidden\_set()

Returns the Maximum a Posteriori estimation of the hidden set. .

Values are ordered as returned by Node\_factory::Get\_Actual\_Hidden\_Set. Calculations are done considering the last last observations set (see Node\_factory::Set\_Observation\_Set\_var)

The documentation for this class was generated from the following files:

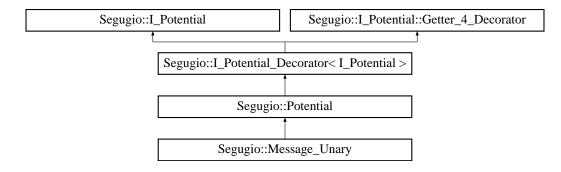
- C:/Users/andre/Desktop/CRF/CRF/Header/Node.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Node.cpp

# 5.38 Segugio::Potential Class Reference

This class is mainly adopted for computing operations on potentials.

```
#include <Potential.h>
```

Inheritance diagram for Segugio::Potential:



### **Public Member Functions**

- Potential (Potential Shape \*pot)
- Potential (Potential Exp Shape \*pot)
- Potential (const std::list< Potential \* > &potential\_to\_merge, const bool &use\_sparse\_format=true)

The potential to create is obtained by merging a set of potentials referring to the same variables (i.e. values in the image are obtained as a product of the ones in the potential\_to\_merge set)

Potential (const std::list< size\_t > &val\_observed, const std::list< Categoric\_var \* > &var\_observed,
 Potential \*pot to reduce)

The potential to create is obtained by marginalizing the observed variable passed as input.

void Get\_marginals (std::list< float > \*prob\_distr)

Obtain the marginal probabilities of the variables in the domain of this potential, when considering this potential only.

### **Additional Inherited Members**

### 5.38.1 Detailed Description

This class is mainly adopted for computing operations on potentials.

### 5.38.2 Constructor & Destructor Documentation

## **Parameters**

in	pot	potential shape to wrap
----	-----	-------------------------

## **5.38.2.2 Potential()** [2/4]

#### **Parameters**

	in	pot	exponential potential shape to wrap
--	----	-----	-------------------------------------

# **5.38.2.3 Potential()** [3/4]

The potential to create is obtained by merging a set of potentials referring to the same variables (i.e. values in the image are obtained as a product of the ones in the potential\_to\_merge set)

## Parameters

in	potential_to_merge	list of potential to merge, i.e. compute their product
in	use_sparse_format	when false, the entire domain is allocated even if some values are equal to 0

## **5.38.2.4** Potential() [4/4]

The potential to create is obtained by marginalizing the observed variable passed as input.

## **Parameters**

	in	pot_to_reduce	the potential from which the variables observed are marginalized
	in	var_observed	variables observed in pot_to_reduce
Ī	in	val_observed	values observed (same oreder of var_observed)

## 5.38.3 Member Function Documentation

## 5.38.3.1 Get\_marginals()

Obtain the marginal probabilities of the variables in the domain of this potential, when considering this potential only.

#### **Parameters**

```
in prob_distr marginals
```

The documentation for this class was generated from the following files:

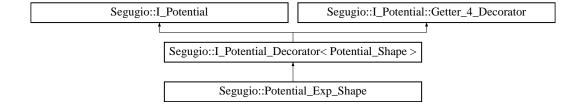
- C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.39 Segugio::Potential\_Exp\_Shape Class Reference

Represents an exponential potential, wrapping a normal shape one: every value of the domain are assumed as exp(mWeight \* val\_in\_shape\_wrapped)

```
#include <Potential.h>
```

Inheritance diagram for Segugio::Potential\_Exp\_Shape:



## Classes

• struct Getter\_weight\_and\_shape

## **Public Member Functions**

• Potential\_Exp\_Shape (Potential\_Shape \*shape, const float &w=1.f)

When building a new exponential shape potential, all the values of the domain are computed according to the new shape passed as input.

Potential\_Exp\_Shape (const std::list< Categoric\_var \* > &var\_involved, const std::string &file\_to\_read, const float &w=1.f)

When building a new exponential shape potential, all the values of the domain are computed according to the potential shape to wrap, which is instantiated in the constructor by considering the textual file provided, see also Potential\_\circ Shape(const std::list<Categoric\_var\*>& var\_involved, const std::string& file\_to\_read)

- Potential\_Exp\_Shape (const Potential\_Exp\_Shape \*to\_copy, const std::list< Categoric\_var \* > &var\_← involved)
- void Substitute\_variables (const std::list< Categoric\_var \* > &new\_var)

Use this method for replacing the set of variables this potential must refer. Variables in new\_var must be equal in number to the original set of variables and must have the same sizes.

#### **Protected Member Functions**

- virtual std::list< I\_Distribution\_value \* > \* Get\_distr ()
- void Wrap (Potential Shape \*shape)

## **Protected Attributes**

- · float mWeight
- std::list< I\_Distribution\_value \* > Distribution

## **Additional Inherited Members**

## 5.39.1 Detailed Description

Represents an exponential potential, wrapping a normal shape one: every value of the domain are assumed as exp(mWeight \* val in shape wrapped)

## 5.39.2 Constructor & Destructor Documentation

```
5.39.2.1 Potential_Exp_Shape() [1/3]
```

When building a new exponential shape potential, all the values of the domain are computed according to the new shape passed as input.

#### **Parameters**

i	n	shape	shape distribution to wrap
i	n	W	weight of the exponential

## **5.39.2.2 Potential\_Exp\_Shape()** [2/3]

When building a new exponential shape potential, all the values of the domain are computed according to the potential shape to wrap, which is instantiated in the constructor by considering the textual file provided, see also Potential\_Shape(const std::list<Categoric\_var\*>& var\_involved, const std::string& file\_to\_read)

#### **Parameters**

ſ	in	var_involved	variables involved in the domain of this variables
	in	file_to_read	textual file to read containing the values for the image
Ī	in	W	weight of the exponential

## **5.39.2.3 Potential\_Exp\_Shape()** [3/3]

Use this constructor for cloning an exponential shape, but considering a different set of variables. Variables in var—involved must be equal in number to those in the potential to clone and must have the same sizes of the variables involved in the potential to clone.

## **Parameters**

in	to_copy	shape to clone
in	var_involved	new set of variables to consider when cloning

#### 5.39.3 Member Function Documentation

## 5.39.3.1 Substitute\_variables()

Use this method for replacing the set of variables this potential must refer. Variables in new\_var must be equal in number to the original set of variables and must have the same sizes.

#### **Parameters**

in	new_var	variables to consider for the substitution
----	---------	--------------------------------------------

## 5.39.4 Member Data Documentation

## 5.39.4.1 Distribution

```
std::list<I_Distribution_value*> Segugio::Potential_Exp_Shape::Distribution [protected]
```

Weight assumed for modulating the exponential (see description of the class)

The documentation for this class was generated from the following files:

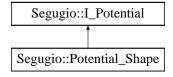
- C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.40 Segugio::Potential\_Shape Class Reference

It's the only possible concrete potential. It contains the domain and the image of the potential.

```
#include <Potential.h>
```

Inheritance diagram for Segugio::Potential Shape:



#### **Public Member Functions**

Potential\_Shape (const std::list< Categoric\_var \* > &var\_involved)

When building a new shape potential, all values of the image are assumed as all zeros.

- Potential\_Shape (const std::list< Categoric\_var \* > &var\_involved, const std::string &file\_to\_read)
- Potential\_Shape (const std::list< Categoric\_var \* > &var\_involved, const bool &correlated\_or\_not)

Returns simple correlating or anti\_correlating shapes. .

- Potential Shape (const Potential Shape \*to copy, const std::list< Categoric var \* > &var involved)
- Potential Shape (const Potential Shape &to copy)
- void Import (const std::string &file\_to\_read)

For populating the image of the domain with the values reported in the textual file.

void Add\_value (const std::list< size\_t > &new\_indeces, const float &new\_val)

Add a new value in the image set.

· void Set\_ones ()

All values in the image of the domain are set to 1.

void Set\_random (const float zeroing\_threashold=1.f)

All values in the image of the domain are randomly set.

void Normalize\_distribution ()

All values in the image of the domain are multipled by a scaling factor, in order to to have maximal value equal to 1. Exploited for computing messages.

void Substitute\_variables (const std::list< Categoric\_var \* > &new\_var)

Use this method for replacing the set of variables this potential must refer. Variables in new\_var must be equal in number to the original set of variables and must have the same sizes.

## **Protected Member Functions**

- void Check\_add\_value (const std::list< size\_t > &indices)
- virtual const std::list<  $Categoric\_var * > * Get\_involved\_var$  () const
- virtual std::list< I\_Distribution\_value \* > \* Get\_distr ()

# **Additional Inherited Members**

## 5.40.1 Detailed Description

It's the only possible concrete potential. It contains the domain and the image of the potential.

## 5.40.2 Constructor & Destructor Documentation

When building a new shape potential, all values of the image are assumed as all zeros.

#### **Parameters**

in	var_involved	variables involved in the domain of this variables
----	--------------	----------------------------------------------------

#### **5.40.2.2** Potential\_Shape() [2/4]

#### **Parameters**

	in	var_involved	variables involved in the domain of this variables
ſ	in	file_to_read	textual file to read containing the values for the image

## **5.40.2.3 Potential\_Shape()** [3/4]

Returns simple correlating or anti\_correlating shapes. .

A simple correlating shape is a distribution having a value of 1 for every combinations  $\{0,0,...,0\}$ ;  $\{1,1,...,1\}$  etc. and 0 for all other combinations. A simple anti\_correlating shape is a distribution having a value of 0 for every combinations  $\{0,0,...,0\}$ ;  $\{1,1,...,1\}$  etc. and 1 for all other combinations.

## **Parameters**

in	var_involved	variables involved in the domain of this variables: they must have all the same size
in	correlated_or_not	when true produce a simple correlating shape, when false produce a
		anti_correlating function

## **5.40.2.4** Potential\_Shape() [4/4]

Use this constructor for cloning a shape, but considering a different set of variables. Variables in var\_involved must be equal in number to those in the potential to clone and must have the same sizes of the variables involved in the potential to clone.

#### **Parameters**

in	to_copy	shape to clone
in	var_involved	new set of variables to consider when cloning

## 5.40.3 Member Function Documentation

## 5.40.3.1 Add\_value()

Add a new value in the image set.

## **Parameters**

in	new_indices	combination related to the new value to add for the image
in	new_val	new val to insert

## 5.40.3.2 Import()

For populating the image of the domain with the values reported in the textual file.

## **Parameters**

г			
	in	file_to_read	textual file to read containing the values for the image

## 5.40.3.3 Substitute\_variables()

Use this method for replacing the set of variables this potential must refer. Variables in new\_var must be equal in number to the original set of variables and must have the same sizes.

#### **Parameters**

in new_var variables to consider for the substitution
-------------------------------------------------------

The documentation for this class was generated from the following files:

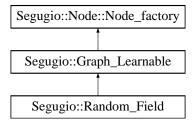
- C:/Users/andre/Desktop/CRF/CRF/Header/Potential.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Potential.cpp

# 5.41 Segugio::Random\_Field Class Reference

This class describes a generic Random Field, not having a particular set of variables observed.

```
#include <Graphical_model.h>
```

Inheritance diagram for Segugio::Random\_Field:



## **Public Member Functions**

- Random\_Field (const bool &use\_cloning\_Insert=true)
   empty constructor
- Random\_Field (const std::string &config\_xml\_file, const std::string &prefix\_config\_xml\_file="")

The model is built considering the information contained in an xml configuration file. .

Random\_Field (const std::list< Potential\_Exp\_Shape \* > &potentials\_exp, const bool &use\_cloning\_←
 Insert=true, const std::list< bool > &tunable\_mask={}, const std::list< Potential\_Shape \* > &shapes={})

This constructor initializes the graph with the specified potentials passed as input.

void Insert (Potential\_Shape \*pot)

Similar to Graph::Insert(Potential\_Shape\* pot)

• void Insert (Potential\_Exp\_Shape \*pot, const bool &is\_weight\_tunable=true)

Similar to Graph::Insert(Potential\_Exp\_Shape\* pot).

void Insert (Potential\_Exp\_Shape \*pot, const std::list< Categoric\_var \* > &vars\_of\_pot\_whose\_weight\_is
 \_to\_share)

Insert a tunable exponential shape, whose weight is shared with another already inserted tunable shape.

void Set\_Observation\_Set\_var (const std::list< Categoric\_var \* > &new\_observed\_vars)

 $\textbf{\textit{see}} \ \textit{Node} :: \textit{Node\_factory} :: \textit{Set\_Observation\_Set\_var}(\textit{const std} :: \textit{list} < \textit{Categoric\_var*} > \& \ \textit{new\_observed\_vars})$ 

void Set\_Observation\_Set\_val (const std::list< size\_t > &new\_observed\_vals)

 $see \ \textit{Node} :: \textit{Node\_factory} :: \textit{Set\_Observation\_Set\_val} (\textit{const std} :: \textit{list} < \textit{size\_t} > \& \ \textit{new\_observed\_vals})$ 

## **Additional Inherited Members**

## 5.41.1 Detailed Description

This class describes a generic Random Field, not having a particular set of variables observed.

## 5.41.2 Constructor & Destructor Documentation

## empty constructor

#### **Parameters**

in	use_cloning_Insert	when is true, every time an Insert of a novel potential is called, a copy of that
		potential is actually inserted. Otherwise, the passed potential is inserted as is:
		this can be dangerous, cause that potential cna be externally modified, but the
		construction of a novel graph is faster.

## **5.41.2.2** Random\_Field() [2/3]

The model is built considering the information contained in an xml configuration file. .

See Section 2 of the documentation for the syntax to adopt.

#### **Parameters**

	in	configuration	file
Ī	in	prefix	to use. The file prefix_config_xml_file/config_xml_file is searched.

```
5.41.2.3 Random_Field() [3/3]
```

```
const bool & use_cloning_Insert = true,
const std::list< bool > & tunable_mask = {},
const std::list< Potential_Shape * > & shapes = {} )
```

This constructor initializes the graph with the specified potentials passed as input.

## **Parameters**

in	potentials_exp	the initial set of exponential potentials to insert (can be empty)
in	use_cloning_Insert	when is true, every time an Insert of a novel potential is called (this includes the passed potentials), a copy of that potential is actually inserted. Otherwise, the passed potential is inserted as is: this can be dangerous, cause that potential cna be externally modified, but the construction of a novel graph is faster.
in	tunable_mask	when passed as non default value, it is must have the same size of potentials.  Every value in this list is true if the corresponfing potential in the potentials list is tunable, i.e. has a weight whose value can vary with learning
in	shapes	A list of additional non learnable potentials to insert in the model

## 5.41.3 Member Function Documentation

Similar to Graph::Insert(Potential\_Exp\_Shape\* pot).

## **Parameters**

in	is_weight_tunable	When true, you are specifying that this potential has a weight learnable, otherwise	
		the value of the weight is assumed constant.	

```
5.41.3.2 Insert() [2/2]
```

Insert a tunable exponential shape, whose weight is shared with another already inserted tunable shape.

This allows having many exponential tunable potetials which share the value of the weight: this is automatically account for when performing learning.

#### **Parameters**

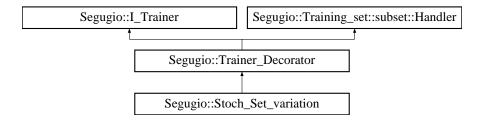
in	vars_of_pot_whose_weight_is_to_share	the list of varaibles involved in a potential already inserted
		whose weight is to share with the potential passed. They
		must be references to the variables actually wrapped into
		the model.

The documentation for this class was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Graphical\_model.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Graphical model.cpp

# 5.42 Segugio::Stoch\_Set\_variation Class Reference

Inheritance diagram for Segugio::Stoch\_Set\_variation:



## **Public Member Functions**

- Stoch\_Set\_variation (Advancer\_Concrete \*to\_wrap, const float &percentage\_to\_use)
- void Train (Graph\_Learnable \*model\_to\_train, Training\_set \*Train\_set, const unsigned int &Max\_Iterations, std::list< float > \*descend\_story)

## **Additional Inherited Members**

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Trainer.cpp

# 5.43 Segugio::Training\_set::subset Struct Reference

This class is describes a portion of a training set, obtained by sampling values in the original set. Mainly used by stochastic gradient computation strategies.

```
#include <Training_set.h>
```

## Classes

struct Handler

## **Public Member Functions**

• subset (Training\_set \*set, const float &size\_percentage=1.f)

## 5.43.1 Detailed Description

This class is describes a portion of a training set, obtained by sampling values in the original set. Mainly used by stochastic gradient computation strategies.

## 5.43.2 Constructor & Destructor Documentation

## 5.43.2.1 subset()

#### **Parameters**

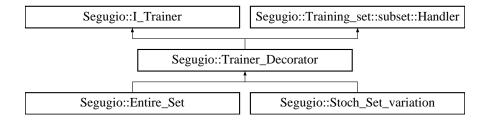
in	set	the training set from which this subset must be extracted
in	size_percentage	percentage to use for the extraction

The documentation for this struct was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Training\_set.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Training\_set.cpp

# 5.44 Segugio::Trainer\_Decorator Class Reference

Inheritance diagram for Segugio::Trainer\_Decorator:



## **Public Member Functions**

- Trainer\_Decorator (Advancer\_Concrete \*to\_wrap)
- void Clean\_Up ()

#### **Protected Member Functions**

void <u>\_\_check\_tunable\_are\_present</u> (Graph\_Learnable \*model\_to\_train)

## **Protected Attributes**

Advancer\_Concrete \* Wrapped

## **Additional Inherited Members**

The documentation for this class was generated from the following file:

• C:/Users/andre/Desktop/CRF/CRF/Source/Trainer.cpp

# 5.45 Segugio::Training\_set Class Reference

This class is used for describing a training set for a graph.

```
#include <Training_set.h>
```

#### **Classes**

class Basic\_Extractor

Basic extractor, see Training\_set(const std::list<std::string>& variable\_names, std::list<Array> samples,  $I\_\leftarrow$  Extractor<Array>\* extractor)

class I\_Extractor

This class is adopted for parsing a set of samples to import as a novel training set. You have to derive yout custom extractor, implementing the two vritual method.

struct subset

This class is describes a portion of a training set, obtained by sampling values in the original set. Mainly used by stochastic gradient computation strategies.

## **Public Member Functions**

- Training\_set (const std::string &file\_to\_import)
- template<typename Array >

Training\_set (const std::list< std::string > &variable\_names, std::list< Array > &samples, I\_Extractor< Array > \*extractor)

Similar to Training\_set(const std::string& file\_to\_import),.

template<typename Array >

Training\_set (const std::list< Categoric\_var \* > &variable\_in\_the\_net, std::list< Array > &samples, I\_Extractor< Array > \*extractor)

Same as Training\_set(const std::list<std::string>& variable\_names, std::list<Array> samples, I\_Extractor<Array>\* extractor) passing the variables involved instead of the names.

void Print (const std::string &file\_name)

This training set is reprinted in the location specified.

## 5.45.1 Detailed Description

This class is used for describing a training set for a graph.

A set is described in a textual file, where the first row must contain the list of names of the variables (all the variables) constituting a graph. All other rows are a single sample of the set, reporting the values assumed by the variables, with the order described by the first row

## 5.45.2 Constructor & Destructor Documentation

#### **Parameters**

in	file_to_import	file containing the set to import
----	----------------	-----------------------------------

## **5.45.2.2 Training\_set()** [2/2]

Similar to Training\_set(const std::string& file\_to\_import),.

with the difference that the training set is not red from a textual file but it is imported from a list of container (generic can be list, vector or other) describing the samples of the set. You have to derived your own extractor for managing your particular container. Basic\_Extractor is a baseline extractor that can be used for all those type having the method size() and the operator[].

#### **Parameters**

in	variable_names the ordered list of variables to assume for the samples	
in	samples the list of generic Array representing the samples of the training	
in	extractor	the particular extractor to use, see I_Extractor

## 5.45.3 Member Function Documentation

## 5.45.3.1 Print()

This training set is reprinted in the location specified.

#### **Parameters**

```
in file_name is the path of the file where the set must be printed
```

The documentation for this class was generated from the following files:

- · C:/Users/andre/Desktop/CRF/CRF/Header/Training set.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Training set.cpp

# 5.46 Segugio::Unary\_handler Class Reference

Inheritance diagram for Segugio::Unary\_handler:



## **Public Member Functions**

Unary\_handler (Node \*N, Potential\_Exp\_Shape \*pot\_to\_handle)

## **Additional Inherited Members**

The documentation for this class was generated from the following file:

C:/Users/andre/Desktop/CRF/CRF/Source/Graphical\_model.cpp

# 5.47 Segugio::Graph\_Learnable::Weights\_Manager Struct Reference

## **Static Public Member Functions**

static void Get\_tunable\_w (std::list< float > \*w, Graph\_Learnable \*model)
 Returns the values of the tunable weights, those that can vary when learning the model.

#### **Friends**

· class I\_Trainer

The documentation for this struct was generated from the following files:

- C:/Users/andre/Desktop/CRF/CRF/Header/Graphical\_model.h
- C:/Users/andre/Desktop/CRF/CRF/Source/Graphical model.cpp

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