

Résumé

Le système "Per unit"

• Tension entre Phase $U = \sqrt{3} V$ • La puissance $S = 3 V \cdot I = \sqrt{3} U I = P + jQ$

$$V = Z I$$

$$S_{PU} = \frac{S_{actuel}}{S_{base}} ; U_{PU} = \frac{U}{U_B} ; I_{PU} = \frac{I}{I_B} ; Z_{PU} = \frac{Z}{Z_B}$$

$$U_B = \sqrt{3} V_B ; S_B = \sqrt{3} U_B I_B ; V_B = Z_B \cdot I_B$$

$$Z_{PU} = V_{PU} ; S_{PU} = U_{PU} \cdot I_{PU}$$

Admittance et impédance de Base

$$S = 3 V I \Rightarrow S = 3 V \cdot \frac{V}{Z} \Rightarrow S = \frac{3V^2}{Z}$$

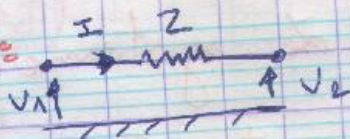
$$S = 3 \times \left(\left(\frac{U}{\sqrt{3}} \right)^2 \cdot \frac{1}{Z} \right) \Rightarrow S = \frac{U^2}{Z}$$

$$S_{B_z} = \frac{U_B^2}{Z_B} \Rightarrow Z_B = \frac{U_B^2}{S_B} \text{ et } Z_{PU} = \frac{U_{PU}^2}{S_{PU}}$$

$$Z = \frac{1}{Y} \Rightarrow Y_B = \frac{S_B}{U_B^2} \text{ et } Y_{PU} = \frac{S_{PU}}{U_{PU}^2}$$

$$S_{By} = Y_B \cdot U_B^2$$

chute de tension:



Par Kirchhoff)

$$V_1 = V_2 + Z I$$

$$V_{Pu1} = V_{Pu2} + Z_{Pu} \cdot I_{Pu}$$

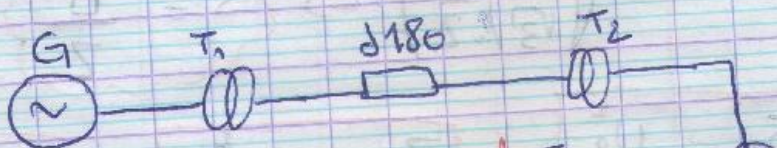
Changement de Base:

$$Z = Z_{Pu1} \cdot Z_{B1} = Z_{Pu2} \cdot Z_{B2}$$

$$Z_{Pu2} = Z_{Pu1} \cdot \frac{Z_{B1}}{Z_{B2}} = Z_{Pu1} \cdot \frac{U_{B1}^2 \cdot S_{B2}}{S_{B1} \cdot U_{B2}^2}$$

$$\text{et } Y_{Pu2} = Y_{Pu1} \cdot \frac{U_{B2}^2 \cdot S_{B2}}{S_{B1} \cdot U_{B1}^2}$$

Exmp:



G ↓

$$S = 204 \text{ VA}$$

$$U = 13,8 \text{ KV}$$

$$Z_{Pu1} = j0,2 \text{ Pu}$$

$$M \Rightarrow S = 30 \text{ KV}$$

$$U = 18 \text{ KV}$$

$$Z_{Pu1} = j0,2 \text{ Pu}$$

T1 ↓

$$S = 25 \text{ MVA}$$

$$U = 13,8 - 220 \text{ KV}$$

$$Z_{Pu1} = j0,1 \text{ Pu}$$

T2 ↓

$$S = 30 \text{ MVA}$$

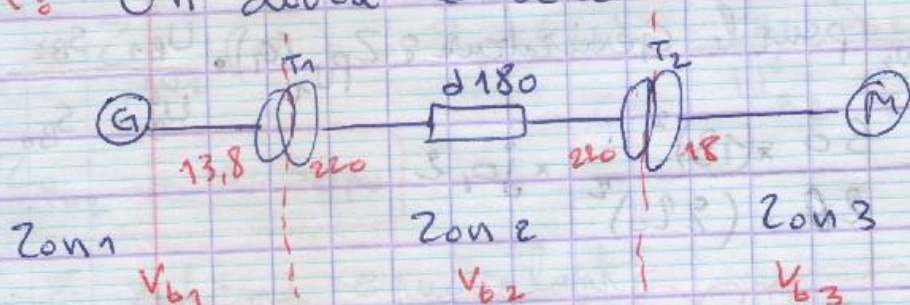
$$U = 220 - 18 \text{ KV}$$

$$Z_{Pu1} = j0,1 \text{ Pu}$$

avec $S_{b_2}(H) = S_{b_2}(T) = S_{b_2}(T_2) = 50 \text{ kVA}$

et $V_{B_1} = 13,8 \text{ KV}$ pour le generateur

R: On divise le schema en 3 Zone



1. calcul V_{b_2} , V_{b_3}

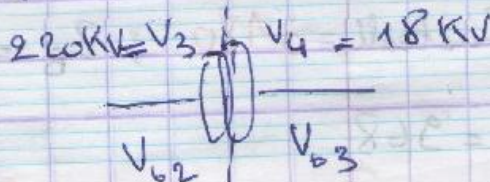
$$V_{b_2} = V_{b_1} \cdot \frac{V_2}{V_1}$$

$$V_{b_2} = 13,8 \cdot \frac{220}{13,8}$$

$$V_{b_2} = 220 \text{ KV}$$

$$V_{b_3} = V_{b_2} \cdot \frac{V_3}{V_4} = 220 \cdot \frac{18}{220}$$

$$V_{b_3} = 18 \text{ KV}$$



2. calculer Z_{PU2} de chaque

$$Z_{PU2} = Z_{PU1} \cdot \frac{U_{B1}^2 S_{B2}}{U_{B2}^2 S_{B1}}$$

Alors Z_{PU2} pour le Générateur : $Z_{PU1}(G) \cdot \frac{U_{B1}^2 S_{B2}}{U_{B2}^2 S_{B1}}$

$$\bullet Z_{PU2}(G) = \frac{50 \times (13.8)^2}{20 \times (13.8)^2} \times j0.2$$

$$Z_{PU2}(G) = j0.5 \text{ pu}$$

$$\bullet Z_{PU2}(T_1) = \frac{U_{B1}^2 S_{B2}}{U_{B2}^2 S_{B1}} Z_{PU1} = \frac{(13.8)^2 \times 50}{(13.8)^2 \times 25} \times j0.1$$

$$Z_{PU2}(T_1) = j0.2 \text{ pu}$$

$$\bullet Z_{PU2}(\text{La ligne } (\delta 180)) : Z_{PU2} = \frac{Z_{\text{actual}}}{Z_{\text{base}}}$$

$$Z_{\text{actual}} = \delta 180 ; Z_B = \frac{U_{B2}^2}{S_{B2}} = \frac{220 \text{ kV}}{50 \text{ kVA}}$$

$$Z_B = 968$$

$$Z_{PU2}(L) = \delta \frac{180}{968}$$

$$\Rightarrow Z_{PU2}(L) = 0.186 \text{ pu} \quad 6$$

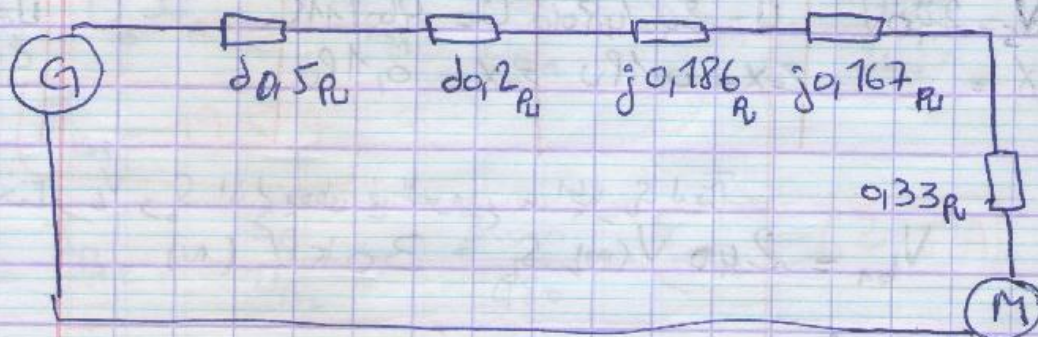
$$\bullet Z_{Pu_2}(T_2) = Z_{Pu_1} \cdot \frac{U_{B_1}^2 \cdot S_{B_2}}{S_{B_1} \cdot U_{B_2}^2} = 0,1 \frac{50 \times 220^2}{30 \times 220^2}$$

$$Z_{Pu_2}(T_2) = j0,167$$

$$\bullet Z_{Pu_2}(M) = Z_{Pu_1}(M) \cdot \frac{U_{B_1}^2 \cdot S_{B_2}}{U_{B_2}^2 \cdot S_{B_1}}$$

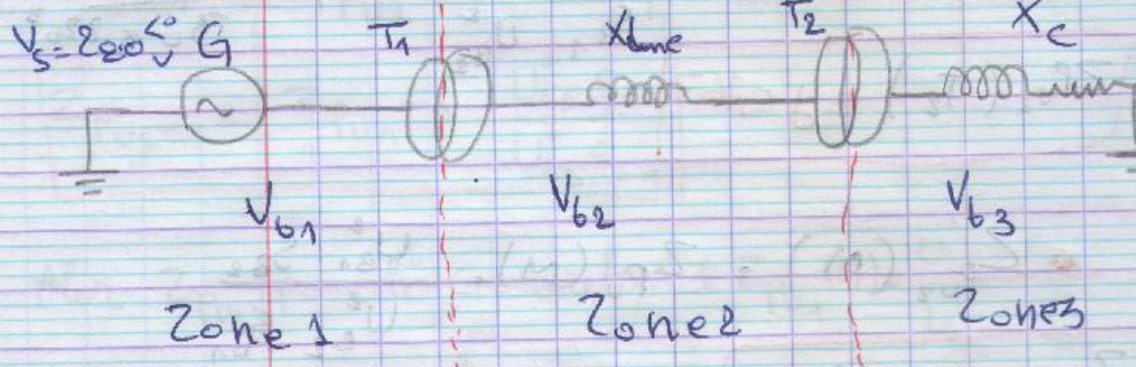
$$Z_{Pu_2} = 0,33 \text{ pu}$$

Le schema equivalent



$N \rightarrow \text{New}, O \rightarrow \text{old}$

EXO :



G	T ₁	T ₂	line	ch
$S = 30 \text{ kVA}$	$S = 30 \text{ kVA}$	$S = 20 \text{ kVA}$	$X_{\text{line}} = 2 \Omega$	$Z = X_c = 9.1 \mu$
$V_s = 220 \text{ V}$	$U = 240/480 \text{ V}$	$U = 460/115 \text{ V}$		$U = 115 \text{ V}$
$X =$	$Z = X = 0.1 \mu$	$Z = X = 0.1 \mu$		$S =$

نختار V_b و S_b ان لم يعطى في المرفوع من اجل S_b لدينا

$$V_{b1} = 240 \text{ V (N)}, S_b = 30 \text{ kV (N)}$$

• calculate V_{b2}, V_{b3}

$$V_{b2} = V_{b1} \cdot \frac{V_2}{V_1} \Rightarrow V_{b2} = V_{b1} \cdot \frac{480}{240}$$

$$V_{b2} = 480 \text{ V (N)}$$

$$V_{b3} = V_{b2} \cdot \frac{V_4}{V_3} = 480 \times \frac{115}{460}$$

$$V_{b3} = 120 \text{ V (N)}$$

- calcul des impédances de Base:

$$Z_{B1} = \frac{U_{B1}^2}{S_{B1}} \Rightarrow Z_{B1} = \frac{(240)^2}{30000} \Rightarrow Z_{B1} = 1,92 \Omega$$

$$Z_{B2} = \frac{U_{B2}^2}{S_B} = Z_{B2} = \frac{480^2}{30000} \Rightarrow Z_{B2} = 7,68 \Omega$$

$$Z_{B3} = \frac{120^2}{30000} = Z_{B3} = 0,48 \Omega$$

- calcul des courants de Base:

$$S_B = U_B I_B \Rightarrow I_{B1} = \frac{S_{B1}}{U_{B1}} \Rightarrow I_{B1} = \frac{30000}{240}$$

$$I_{B1} = 125 A$$

$$I_{B2} = \frac{S_B}{U_{B2}} = \frac{30000}{480} \Rightarrow I_{B2} = 62,5 A$$

$$I_{B3} = 250 A$$

- changement de Base: $N \rightarrow N_{\text{new}}$, $O \rightarrow \text{old}$

$$Z_{P0}(N)_{T2} = Z_{P0}(O)_{T2} \times \left[\frac{U_b(O)}{U_b(N)} \right]^2 \frac{S_b(N)}{S_b(O)}$$

$$Z_{P0}(N)_{T2} = 0,1 \times \left[\frac{460}{480} \right]^2 \times \frac{30000}{20000} = (1,5)$$

$$Z_{P0}(N)_{T2} = 0,137 p.u. \quad (9)$$

Zapartie 2 cure de transf(2)

$$\bullet \text{ or } \rightarrow Z_{pu}(T_2) = Z_{pu}(T_1) T_2 \times \left[\frac{115}{120} \right]^2 \times \frac{30K}{20K}$$

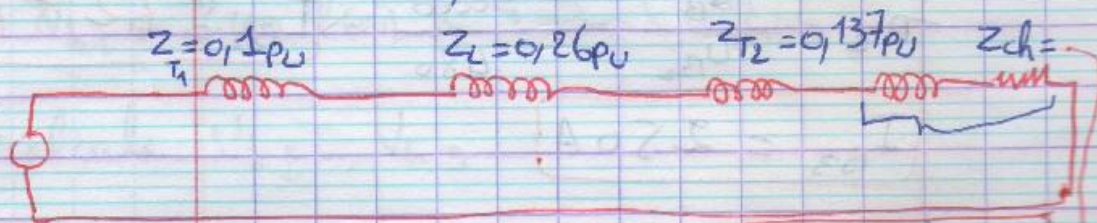
$$Z_{pu}(N) T_2 = 0,137_{pu}$$

$$\bullet Z_{pu}(\text{line}) = \frac{Z(\text{old})}{Z_{b2}} = \frac{2}{7,68} \Rightarrow Z_{pu}(\text{line}) = 0,26$$

$$\bullet Z_{pu}(\text{charge}) = \frac{Z(\text{old})}{Z_{b3}} = 1,87 + j0,47$$

$$\bullet V_{s pu} = \frac{V_s}{V_{b1}} = \frac{220}{240} \Rightarrow V_{s pu} = 0,916_{pu}$$

• Le schema equivalent:



$$Z_{ch} = 1,87 + j0,47$$

$$\bullet I_{ch} = \frac{V_{s pu}}{Z_{eq}}$$

$$Z_{eq} = j(0,1 + 0,26 + 0,137 + 1,87 + j0,47)$$

$$I_{ch} = \frac{0,916}{(-0,417 + 2,368)}$$

$$I_{ch} = \frac{9916 L^0}{2,4 (99,989)}$$

$$I_{ch} = 0,38 < 99,98$$

A, B → 8
2 Fnc AB

↓
2 Fnc BB