CSE473 Homework #4 Due at 10:30 AM December 11th in Class on Paper Name:

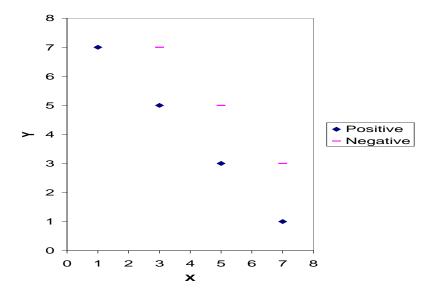
## Model ensembles

A significant disadvantage of model ensembles is that an ensemble is significantly more complex and harder to understand than a single model. Propose a computationally efficient method for reducing a set of bagged decision trees to a single tree that is approximately equivalent to it.

# Instance-based learning

## Voronoi Diagram

Draw the Voronoi diagram corresponding to the following training set:



The instance space is the square

$$0 \leq X \leq 8, 0 \leq Y \leq 8$$

Positive examples are located at

- (1,7)
- (3.5)
- (5,3)
- (7,1)

Negative examples are located at

- (3,7)
- (5,5)
- (7.3)

#### **Error Rate**

If the true frontier between positive and negative examples is the line

$$Y = 9 - X$$

with the positive class on the left, and the examples are uniformly distributed in the square above, what is the expected error rate of the nearest-neighbor classifier with Euclidean distance trained on the examples above?

# Genetic algorithms

Consider a genetic algorithm that uses fitness-proportionate selection and single-point crossover. Half the population is replaced by crossover at each step, and there is no mutation. Suppose the current population is composed of four hypotheses  $h_1$ ,  $h_2$ ,  $h_3$  and  $h_4$ , with the fitness of the *i*th hypothesis being i (e.g.,  $fitness(h_3) = 3$ ). If the first bit is 0 in the even hypotheses and 1 in the odd ones, what is the expected number of hypotheses with 1 in the first bit in the next generation?

### Neural networks

#### DNF

Write in pseudo-code a function that inputs a logical formula in DNF (disjunctive normal form) and outputs a neural network that implements it, with each neuron being represented as a list of inputs and their respective weights. The firing threshold for each neuron should be greater than zero (as opposed to greater than or equal to zero).

### **CNF**

How would you modify this function to input instead a logical formula in CNF (conjunctive normal form)?