

C:\Windows\system32\cmd.exe

Enter function $f(x)$: $x^{**8} + 2*x - 5$

Enter initial guess $x0$: 0

n	x
1	0.000000
2	2.500000
3	2.187628
4	1.914785
5	1.677615
6	1.474767
7	1.310028
8	1.195525
9	1.143253
10	1.134116
11	1.133875

The approximate root is $x = 1.13387$.

Press any key to continue . . .

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# -*- coding: utf-8 -*-

import math

def f(expr, x):
    return eval(expr, {"x": x, "math": math, **math.__dict__})

# Numerical derivative f'(x)

def df(expr, x, h=1e-6):
    return (f(expr, x + h) - f(expr, x - h)) / (2 * h)

# Newton-Raphson Method

def newton(expr, x0, tol=1e-5, max_iter=20):
    x = x0

    print("\n\n\tx")
    print("-----")

    for n in range(1, max_iter + 1):
        print(f"{n}\t{x:.6f}")

        fx = f(expr, x)
        dfx = df(expr, x)

        if abs(dfx) < 1e-12:
            print("\nDerivative too small. Stopping.")
            break

        x_new = x - fx / dfx

        if abs(x_new - x) < tol:
            x = x_new
            break

        x = x_new

    print(f"\nThe approximate root is x = {x:.5f}.")

# MAIN

expr = input("Enter function f(x): ")
x0 = float(input("Enter initial guess x0: "))

newton(expr, x0)

```