

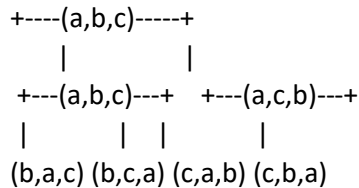
- 1) How many ways can 12 students in a class take 3 different tests if 4 students are to take each test?

$$C(12,4) = 12! / (4! * 8!) = 495$$

$$C(8,4) = 70$$

$$495 \times 70 \times 1 = 34,650$$

- 2) Construct the tree diagram for the number of permutations of {a, b, c}.



- 3) Consider two items be selected randomly from a box that has containing 12 items. From these 12 items, 4 items are defective. If A is the event represents that both the tow items are defective” while B represents that “both the two items are non-defective”

- i) Find $P(A)$ and $P(B)$

$$2 \text{ items from } 12 \ C(12,2) = 66$$

$$2 \text{ defective items out of } 4 \ C(4,2) = 6, \ P(A) = 6/66 = 1/11$$

$$2 \text{ non-defective items out of } 8, \ C(8,2) = 28, \ P(B) = 28/66 = 14/33$$

- ii) Find $P(\text{at least one item is defective})$?

$$\text{non-defective } 66 - 28 = 38$$

$$P(\text{at least one item is defective}) = 38/66 = 19/33$$

- 4) A box contains three 15 items of which five are defective. If three items are chosen at random from this box, find the probability that:

$$3 \text{ items from } 15 \ C(15,3) = 455$$

- (i) none of the three selected items is defective,

$$3 \text{ non-defective items out of } 10, \ C(10,3) = 120$$

$$P(\text{none defective}) = 120/455 = 24/91$$

- (ii) exactly one item of the three items is defective,

$$C(5,1) = 5 \text{ ways and the non-defective items in } C(10,2) = 45 \text{ ways}$$

$$P(\text{exactly one defective}) = (5 \times 45) / 455 = 1/3$$

- (iii) at least one item of the three items is defective

$$P(\text{at least one defective}) = 1 - P(\text{none defective}) = 1 - 24/91 = 67/91$$

- 5) A class contains 10 boys and 20 girls of which half the boys and half the girls have from Mansoura. Find the probability that a person chosen randomly is a boy or from Mansoura university

$$\text{Boy } 10 \rightarrow P(A \cup B) = 15/30 = \frac{1}{2}$$

$$\text{Man } 5 \rightarrow B$$

- 6) Let A and B be events with $P(A) = 3/8$, $P(B) = 1/2$ and $P(A \cap B) = 1/2$. Find

(i) $P(A^c)$,

$$P(A^c) = 1 - P(A) = 1 - 3/8 = 5/8$$

(ii) $P(B^c)$

$$P(B^c) = 1 - P(B) = 1 - 1/2 = 1/2$$

(iii) $P(A^c \cap B^c)$, 2 | 2

$$P(A^c \cap B^c) = P((A \cup B)^c) = 1 - P(A \cup B)$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B) = 3/8 + 1/2 - 1/2 = 7/8$$

$$P(A^c \cap B^c) = 1 - P(A \cup B) = 1 - 7/8 = 1/8$$

(iv) $P(A^c \cup B^c)$,

$$P(A^c \cup B^c) = P((A \cap B)^c) = 1 - P(A \cap B)$$

$$P(A^c \cup B^c) = 1 - 1/2 = \frac{1}{2}$$

(v) $P(A \cap B^c)$

$$P(A \cap B^c) = P(A) - P(A \cap B)$$

$$P(A) = 3/8 \text{ and } P(A \cap B) = \frac{1}{2}$$

$$P(A \cap B^c) = 3/8 - 1/2 = -1/8$$

(vi) $P(B \cap A^c)$

$$P(B \cap A^c) = P(B) - P(A \cap B)$$

$$P(B) = 1/2 \text{ and } P(A \cap B) = 1/2,$$

$$P(B \cap A^c) = 1/2 - 1/2 = 0$$

- 7) When you are rolling a pair of (fair) dice three times. What is the probability that, least one of the three tries, you roll a 7

$$P(A) = 36$$

- 8) If $\sum P(x) = k^2 - 8$, find the value of k?

$$\sum p(x) = n^2 - 8$$

$$n^2 - 8 = 1, \quad n^2 = 9, \quad n = 3, \quad n = -3$$

$$n = 3$$

9) If A and B are mutually exclusive events, $P(A) = 0.35$ and $P(B) = 0.45$, find $P(A' \cap B')$

$$P(A' \cap B') = 1 - P(A \cup B) = 1 - 0.8 = 0.2$$

$$P(A \cup B) = P(A) + P(B) = 0.35 + 0.45 = 0.8$$