

## Instructions:

- Write your name and EID on **every page**.
  - Put your answers on the last sheet of paper.
  - No other outside resources, such as books, notes, the internet, or other people, are allowed.
  - There are 110 possible points. The max possible score is 105. It will be graded out of 100.
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1. (7 points) If  $f(x) = x^2 + 2x + e^{2x}$ , find  $f'(0)$

- (A) 1      (B) 2      (C) 3      (D) 4      (E) 5      (F) 6

2. (7 points) Find the x-intercept of the line tangent to  $f(x) = 2\sin(2x) + 3\cos(x)$  at the point  $(0, f(0))$ .

- (A) 0      (B)  $-\frac{1}{4}$       (C)  $-\frac{1}{3}$       (D)  $-\frac{1}{2}$       (E)  $-\frac{2}{3}$       (F)  $-\frac{3}{4}$

3. (7 points) Let  $f(x) = \frac{\sinh(4x)}{\cosh(3x) + 2}$ . Find  $f'(0)$

- (A) 0      (B)  $\frac{1}{4}$       (C)  $\frac{1}{2}$       (D)  $\frac{2}{3}$       (E) 1      (F)  $\frac{4}{3}$

4. (7 points) If  $f(x) = x^2 \sin(x) + 2x \cos(x)$ , then  $f'(x) =$

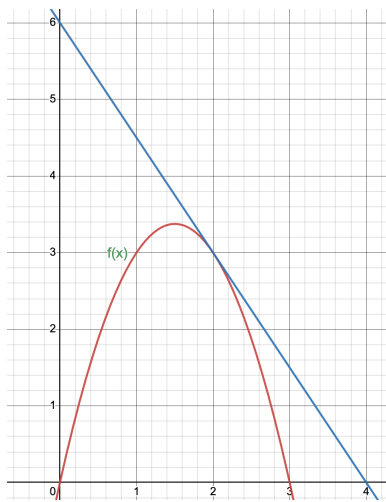
- (A)  $(x^2 - 2) \cos(x)$     (B)  $(x^2 + 2) \cos(x)$     (C)  $(x^2 - 2) \sin(x)$     (D)  $(x^2 + 2) \sin(x)$     (E) None of These

5. (7 points) Let  $h(x) = f(f(x)) \cdot g(x)$ . Use the table of values below to find  $h'(1)$ .

$x$	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
1	4	2	-1	4
2	3	3	3	5
3	2	4	-2	-1
4	-1	2	3	4

- (A) 0      (B) -6      (C) -8      (D) 4      (E) 1      (F) None of These

6. (7 points) The graph  $f(x)$  and the tangent line at  $x = 2$  are shown below. Let  $g(x) = \ln(f(x))$ . Find  $g'(2)$



- (A)  $\frac{1}{3}$       (B)  $\frac{2}{3}$       (C)  $-\frac{2}{3}$       (D)  $-\frac{1}{2}$       (E)  $\frac{2}{9}$       (F)  $-\frac{1}{9}$

7. (7 points) The function  $f(x) = 3x + 2\sin(3x) + 2e^{3x}$  is 1-1, Find  $(f^{-1})'(2)$ .

- (A)  $\frac{1}{15}$       (B)  $\frac{1}{13}$       (C)  $\frac{1}{12}$       (D)  $\frac{1}{9}$       (E)  $\frac{1}{6}$       (F)  $\frac{1}{5}$

8. (7 points) A ferris wheel with radius 10m is tangent to the ground. The wheel makes one full rotation every two minutes. How fast, in m/min, is a person moving vertically when they are 19m above the ground?

- (A)  $\sqrt{19}\pi$       (B)  $4\pi$       (C)  $8\pi$       (D)  $\sqrt{15}\pi$       (E)  $\sqrt{11}\pi$       (F)  $2\pi$

9. (7 points) Use linearization to estimate the value of  $\sqrt{0.9}$ .

- (A)  $\frac{9}{10}$       (B)  $\frac{11}{12}$       (C)  $\frac{15}{16}$       (D)  $\frac{19}{20}$       (E)  $\frac{37}{40}$       (F)  $\frac{80}{83}$

10. (7 points) The critical numbers(s) of  $f(x) = x^{1/3}(4 - x)^{2/3}$  are  $x = 0, 4$ , and:

- (A)  $\frac{4}{5}$       (B) 1      (C)  $\frac{3}{2}$       (D)  $\frac{7}{4}$       (E)  $\frac{4}{3}$       (F) 2

11. (7 points) Find the absolute minimum value of  $f(x) = \cos^2(x) - \cos(x)$  on the interval  $[0, \pi/2]$

- (A) 0      (B)  $-\frac{1}{12}$       (C)  $-\frac{1}{8}$       (D)  $-\frac{1}{6}$       (E)  $-\frac{1}{4}$       (F)  $-\frac{1}{3}$

12. (4 points): True or False: If  $f(x) = |x^2 - 5|$ , then  $f'(2) = -4$ .
13. (4 points): True or False: The function  $f(x) = x^2 - 2x + 1$  on  $[0, 2]$  satisfies the Mean Value Theorem.
14. (4 points): True or False: The function  $f(x) = 1 - x^{2/3}$  on  $[-1, 1]$  satisfies Rolle's Theorem.
15. (9 points) Free Response: Find all the critical numbers of  $f(x) = \frac{x^2 + 6}{2x + 1}$ . Put a box around your final answer.

16. (12 points) Free Response: There is one line tangent to  $2xy + y^2 = 7$  that passes through the point  $(7, 0)$ . Find the **slope** of this tangent line. Put a box around your final answer.

Multiple Choice (7 points each):

1)

2)

3)

4)

5)

6)

7)

8)

9)

10)

11)

True or False (4 points each):

12)

13)

14)