

This print-out should have 46 questions. Multiple-choice questions may continue on the next column or page – find all choices before answering.

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**001 10.0 points**

Determine

$$\lim_{x \rightarrow 0} \left( \frac{1}{x^2 + x} - \frac{1}{x} \right).$$

1. limit =  $-\frac{1}{2}$
2. limit = 1
3. limit =  $\frac{1}{3}$
4. limit =  $\frac{1}{2}$
5. limit =  $-\frac{1}{3}$
6. limit = -1

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**002 10.0 points**

When  $f$  is the function defined by

$$f(x) = \begin{cases} 3x - 4, & x \leq 4, \\ 2x - 1, & x > 4, \end{cases}$$

determine if

$$\lim_{x \rightarrow 4^+} f(x)$$

exists, and if it does, find its value.

1. limit = 9
2. limit = 5
3. limit does not exist
4. limit = 6
5. limit = 8
6. limit = 7

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**003 10.0 points**

Consider the function

$$f(x) = \begin{cases} 3 - x, & x < -1 \\ x, & -1 \leq x < 3 \\ (x - 1)^2, & x \geq 3. \end{cases}$$

Find all the values of  $a$  for which the limit

$$\lim_{x \rightarrow a} f(x)$$

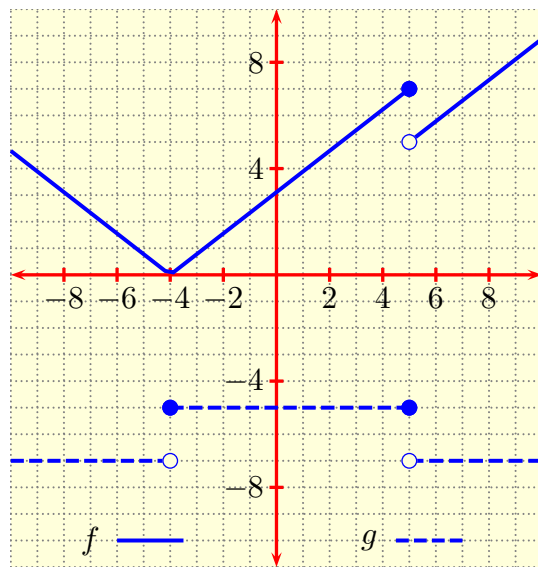
exists, expressing your answer in interval notation.

1.  $(-\infty, -1) \cup (-1, 3) \cup (3, \infty)$
2.  $(-\infty, -1) \cup (-1, \infty)$
3.  $(-\infty, 3) \cup (3, \infty)$
4.  $(-\infty, -1] \cup [3, \infty)$
5.  $(-\infty, \infty)$

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**004 10.0 points**

Functions  $f$  and  $g$  are defined on  $(-10, 10)$  by their respective graphs in



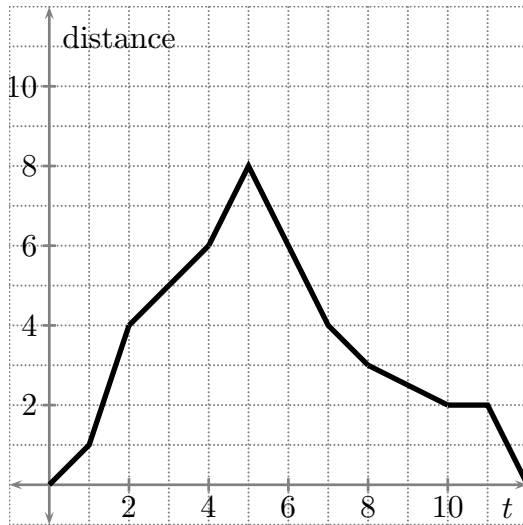
Find all values of  $x$  where the product,  $fg$ , of  $f$  and  $g$  is continuous, expressing your answer in interval notation.

1.  $(-10, 5) \cup (5, 10)$
2.  $(-10, -4] \cup [5, 10)$
3.  $(-10, -4) \cup (-4, 5) \cup (5, 10)$
4.  $(-10, 10)$
5.  $(-10, -4) \cup (-4, 10)$

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**005 (part 1 of 3) 10.0 points**

A Calculus student leaves the RLM building and walks in a straight line to the PCL Library. His distance (in multiples of 40 yards) from RLM after  $t$  minutes is given by the graph



i) What is his speed after 3 minutes, and in what direction is he heading at that time?

1. away from RLM at 30 yds/min
2. away from RLM at 40 yds/min
3. away from RLM at 20 yds/min
4. towards RLM at 20 yds/min
5. towards RLM at 40 yds/min

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**006 (part 2 of 3) 10.0 points**

ii) What is his speed after 9 minutes, and in what direction is he heading at that time?

1. towards RLM at 40 yds/min
2. away from RLM at 5 yds/min.
3. away from RLM at 10 yds/min.
4. away from RLM at 20 yds/min.
5. towards RLM at 20 yds/min.

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**007 (part 3 of 3) 10.0 points**

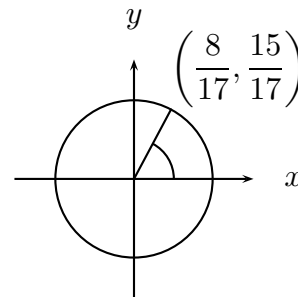
iii) How far is he from RLM when he turns back?

1. distance = 320 yards
2. distance = 160 yards
3. distance = 200 yards
4. distance = 240 yards
5. distance = 280 yards

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**008 (part 1 of 6) 10.0 points**

Consider the angle  $t$  defined by the point  $\left(\frac{8}{17}, \frac{15}{17}\right)$



on the unit circle.

Find  $\sin(t)$ .

1.  $\frac{8}{15}$
2. None of these

3.  $\frac{17}{15}$

4.  $\frac{17}{8}$

5.  $\frac{8}{17}$

6.  $\frac{15}{8}$

7.  $\frac{15}{17}$

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**009 (part 2 of 6) 10.0 points**

Find  $\cos(t)$ .

1.  $\frac{17}{8}$

2.  $\frac{15}{17}$

3.  $\frac{8}{15}$

4. None of these

5.  $\frac{8}{17}$

6.  $\frac{17}{15}$

7.  $\frac{15}{8}$

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**010 (part 3 of 6) 10.0 points**

Find  $\tan(t)$ .

1.  $\frac{8}{17}$

2. None of these

3.  $\frac{8}{15}$

4.  $\frac{17}{15}$

5.  $\frac{15}{17}$

6.  $\frac{17}{8}$

7.  $\frac{15}{8}$

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**011 (part 4 of 6) 10.0 points**

Find  $\csc(t)$ .

1.  $\frac{17}{15}$

2.  $\frac{8}{15}$

3.  $\frac{8}{17}$

4. None of these

5.  $\frac{17}{8}$

6.  $\frac{15}{8}$

7.  $\frac{15}{17}$

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**012 (part 5 of 6) 10.0 points**

Find  $\sec(t)$ .

1.  $\frac{15}{8}$

2. None of these

3.  $\frac{15}{17}$

4.  $\frac{8}{15}$

5.  $\frac{17}{15}$

6.  $\frac{17}{8}$

7.  $\frac{8}{17}$

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**013 (part 6 of 6) 10.0 points**

Find  $\cot(t)$ .

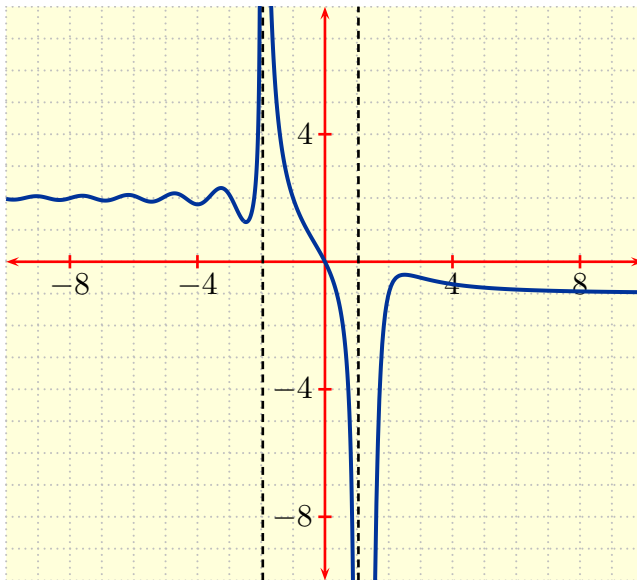
1.  $\frac{17}{15}$

2.  $\frac{8}{15}$
3.  $\frac{8}{17}$
4.  $\frac{15}{17}$
5. None of these
6.  $\frac{15}{8}$
7.  $\frac{17}{8}$

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**014 (part 1 of 3) 10.0 points**

A certain function  $f$  is given by the graph



(i) What is the value of

$$\lim_{x \rightarrow -\infty} f(x)$$

1. limit = -1
2. limit = -2
3. limit does not exist
4. limit = 1
5. limit = 2

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**015 (part 2 of 3) 10.0 points**

(ii) What is the value of

$$\lim_{x \rightarrow \infty} f(x)$$

1. limit does not exist
2. limit = 1
3. limit = -1
4. limit = -2
5. limit = 2

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**016 (part 3 of 3) 10.0 points**

(iii) What is the value of

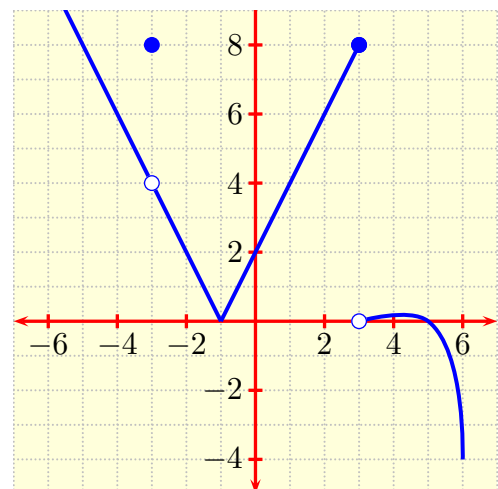
$$\lim_{x \rightarrow -2} f(x)$$

1. limit = -2
2. limit = -1
3. limit = 2
4. limit =  $\infty$
5. limit = 1

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**017 10.0 points**

Below is the graph of a function  $f$ .



Use the graph to determine all the values of  $x$  on  $(-6, 6)$  at which  $f$  fails to be continuous.

1.  $x = -3, 3$
2. none of the other answers
3. no values of  $x$
4.  $x = 3$
5.  $x = -3$

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**018 (part 1 of 3) 10.0 points**

Determine the value of

$$\lim_{x \rightarrow 5^+} \frac{x-6}{x-5}.$$

1. limit =  $\infty$
2. limit =  $-\infty$
3. none of the other answers
4. limit =  $-\frac{6}{5}$
5. limit =  $\frac{6}{5}$

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**019 (part 2 of 3) 10.0 points**

Determine the value of

$$\lim_{x \rightarrow 5^-} \frac{x-6}{x-5}.$$

1. limit =  $-\frac{6}{5}$
2. none of the other answers
3. limit =  $\frac{6}{5}$
4. limit =  $-\infty$
5. limit =  $\infty$

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**020 (part 3 of 3) 10.0 points**

Determine the value of

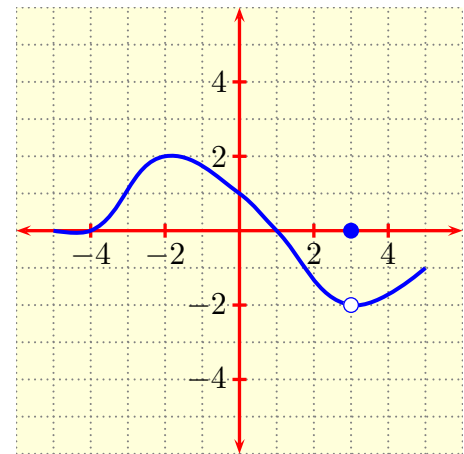
$$\lim_{x \rightarrow 5} \frac{x-6}{x-5}.$$

1. limit =  $-\infty$
2. limit =  $\frac{6}{5}$
3. limit =  $\infty$
4. limit =  $-\frac{6}{5}$
5. none of the other answers

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**021 10.0 points**

Below is the graph of a function  $f$ .



Use the graph to determine  $\lim_{x \rightarrow 3} f(x)$ .

1. limit = 0
2. does not exist
3. limit = 1
4. limit = -2
5. limit = -1

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**022 10.0 points**

Find the value of

$$\lim_{x \rightarrow \infty} \frac{2+3x+2x^4}{3-5x^3}.$$

1. none of the other answers
2. limit =  $-\infty$

3. limit =  $\infty$

4. limit =  $\frac{2}{3}$

5. limit =  $-\frac{2}{5}$

6. limit = 0

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**023 (part 1 of 3) 10.0 points**

If  $t = \frac{\pi}{4}$ , evaluate (if possible)

a)  $\sin t$

1.  $\frac{1}{2}$

2.  $-\frac{\sqrt{3}}{2}$

3. 1

4. None of these

5.  $\frac{\sqrt{3}}{2}$

6.  $\frac{1}{\sqrt{2}}$

7. 0

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**024 (part 2 of 3) 10.0 points**

b)  $\cos t$

1. 0

2. -1

3.  $\frac{1}{2}$

4. None of these

5.  $\frac{\sqrt{3}}{2}$

6.  $-\frac{\sqrt{3}}{2}$

7.  $\frac{1}{\sqrt{2}}$

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**025 (part 3 of 3) 10.0 points**

c)  $\tan t$

1. -1

2.  $-\frac{\sqrt{3}}{2}$

3. None of these

4.  $\frac{1}{2}$

5. 0

6. 1

7.  $\frac{\sqrt{3}}{2}$

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**026 10.0 points**

Determine where

$$f(x) = \begin{cases} 20 - x, & x \leq -5, \\ x^2, & -5 < x < 2, \\ 2 + x, & x \geq 2. \end{cases}$$

is continuous, expressing your answer in interval notation.

1.  $(-\infty, -5) \cup (2, \infty)$

2.  $(-\infty, \infty)$

3.  $(-\infty, -5) \cup (-5, 2) \cup (2, \infty)$

4.  $(-\infty, 2) \cup (2, \infty)$

5.  $(-\infty, -5) \cup (-5, \infty)$

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**027 10.0 points**

Find the largest value of  $c$  so that the function  $g$  defined by

$$g(x) = \begin{cases} x^2 + x - c^2, & x > -1, \\ cx - 12, & x \leq -1, \end{cases}$$

is continuous for all  $x$ .

1.  $c = 7$

2.  $c = -3$

3.  $c = 3$

4. none of these

5.  $c = -7$

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**028 10.0 points**

Find the solution of the exponential equation

$$3^{2x} = 9^{\frac{5}{2}x-3}.$$

1. none of these

2.  $x = 3$

3.  $x = -2$

4.  $x = 2$

5.  $x = -3$

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**029 10.0 points**

Let  $F$  be the function defined by

$$F(x) = \frac{x^2 - 4}{|x - 2|}.$$

Determine if

$$\lim_{x \rightarrow 2^-} F(x)$$

exists, and if it does, find its value.

1. limit = 2

2. limit = -2

3. limit = 4

4. limit does not exist

5. limit = -4

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**030 10.0 points**

Find all values of  $x$  at which the function  $f$  defined by

$$f(x) = \frac{x - 6}{x^2 - 4x - 12}$$

is continuous, expressing your answer in interval notation.

1.  $(-\infty, -2) \cup (-2, \infty)$

2.  $(-\infty, -2) \cup (-2, 6) \cup (6, \infty)$

3.  $(-\infty, 6) \cup (6, \infty)$

4.  $(-\infty, -2) \cup (-2, -6) \cup (-6, \infty)$

5.  $(-\infty, -6) \cup (-6, 2) \cup (2, \infty)$

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**031 10.0 points**

Find the value of

$$\lim_{x \rightarrow 3} \frac{2x - 6}{\sqrt{x} - \sqrt{3}}$$

if the limit exists.

1. limit =  $3\sqrt{3}$

2. limit =  $2\sqrt{3}$

3. limit = 12

4. limit =  $6\sqrt{3}$

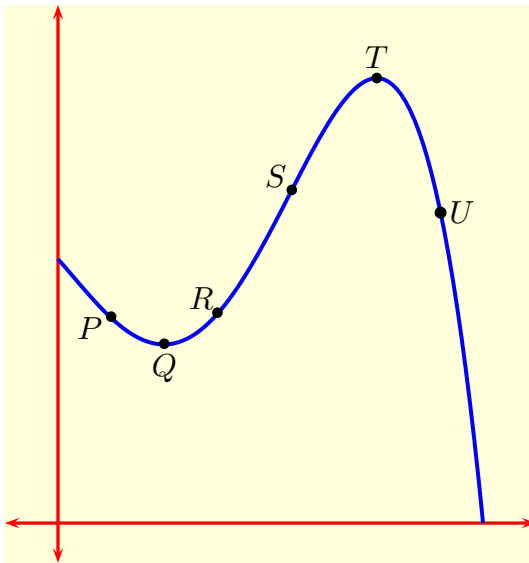
5. limit =  $4\sqrt{3}$

6. limit does not exist

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**032 (part 1 of 5) 10.0 points**

At which point on the graph



is the slope greatest (*i.e.*, most positive)?

1.  $S$
2.  $P$
3.  $R$
4.  $U$
5.  $T$
6.  $Q$

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**033 (part 2 of 5) 10.0 points**

At which point is the slope smallest (*i.e.*, most negative)?

1.  $U$
2.  $S$
3.  $P$
4.  $R$
5.  $T$
6.  $Q$

---

**034 (part 3 of 5) 10.0 points**

At which point does the slope change from

positive to negative?

1.  $P$
2.  $T$
3.  $U$
4.  $Q$
5.  $R$
6.  $S$

---

**035 (part 4 of 5) 10.0 points**

At which point does the slope change from negative to positive?

1.  $P$
2.  $R$
3.  $U$
4.  $Q$
5.  $T$
6.  $S$

---

**036 (part 5 of 5) 10.0 points**

At which point is the tangent line parallel to the secant line  $\overline{PT}$ ?

1.  $S$
2.  $P$
3.  $R$
4.  $U$
5.  $Q$
6.  $T$

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**037 10.0 points**



Determine

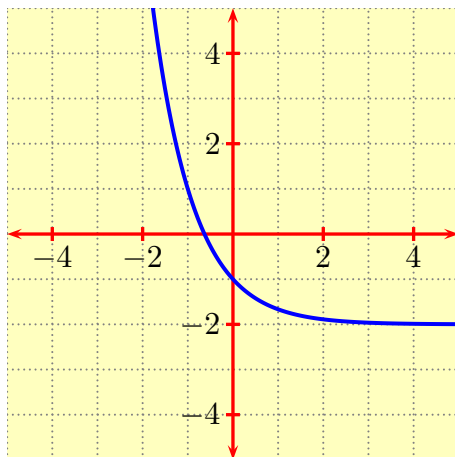
$$\lim_{x \rightarrow 3} \left\{ \frac{1}{x-3} - \frac{3}{x^2-3x} \right\}.$$

1. limit does not exist
2. limit =  $-3$
3. limit =  $\frac{1}{2}$
4. limit =  $-\frac{1}{2}$
5. limit =  $3$
6. limit =  $\frac{1}{3}$
7. limit =  $-\frac{1}{3}$

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**038 10.0 points**

Which function has



as its graph?

1.  $f(x) = 2 - 2^{-x-1}$
2.  $f(x) = 2^{x-1} - 3$
3.  $f(x) = 2 - 3^{-x}$
4.  $f(x) = 2^{-x-1} - 2$
5.  $f(x) = 3^{-x} - 2$
6.  $f(x) = 3^x - 3$

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**039 10.0 points**

If the function  $f$  is continuous everywhere and

$$f(x) = \frac{x^2 - 16}{x + 4}$$

when  $x \neq -4$ , find the value of  $f(-4)$ .

1.  $f(-4) = -4$
2.  $f(-4) = 8$
3.  $f(-4) = 16$
4.  $f(-4) = -16$
5.  $f(-4) = -8$
6.  $f(-4) = 4$

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**040 (part 1 of 2) 10.0 points**

Write the polynomial

$$1 - 2x + 8x^2 - 4x^3$$

in standard form.

a) What is its degree?

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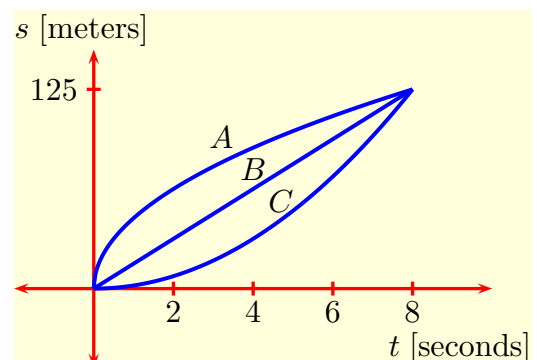
**041 (part 2 of 2) 10.0 points**

b) What is the leading coefficient?

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**042 10.0 points**

Shown are the graphs of distance versus time for three runners A, B, and C who run a 125 -m race and finish in tie. Which of the following statements about the runners is **false**?



1. Runner C gradually speeds up throughout the race.

2. At  $t = 7$ , runner B has a lower velocity than runner A.

3. At  $t = 1$ , runner A has a higher velocity than B.

4. Runner B runs as a constant speed throughout the race.

5. Runner A gradually slows down throughout the race.

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**043 10.0 points**

Find the value of

$$\lim_{x \rightarrow 2} \frac{2}{x-2} \left( 1 + \frac{6}{x-8} \right)$$

if the limit exists.

1. limit =  $-\frac{1}{3}$

2. limit =  $\frac{1}{2}$

3. limit =  $-\frac{1}{2}$

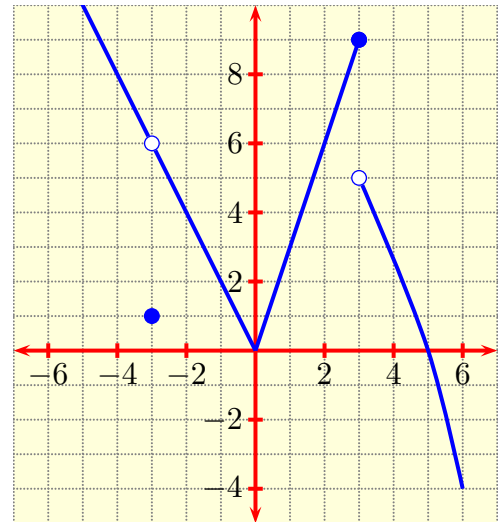
4. limit does not exist

5. limit =  $\frac{1}{3}$

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**044 10.0 points**

Below is the graph of a function  $f$ .



Use the graph to determine  $\lim_{x \rightarrow -3} f(x)$ .

1.  $\lim_{x \rightarrow -3} f(x) = 1$

2.  $\lim_{x \rightarrow -3} f(x) = 9$

3.  $\lim_{x \rightarrow -3} f(x) = 12$

4.  $\lim_{x \rightarrow -3} f(x)$  does not exist

5.  $\lim_{x \rightarrow -3} f(x) = 6$

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**045 10.0 points**

Find the value of  $b$ ,  $b \geq 0$ , for which

$$\lim_{x \rightarrow 0} \left\{ \frac{\sqrt{6x+b}-1}{x} \right\}$$

exists.

1.  $b = 3$

2.  $b = 4$

3.  $b = 2$

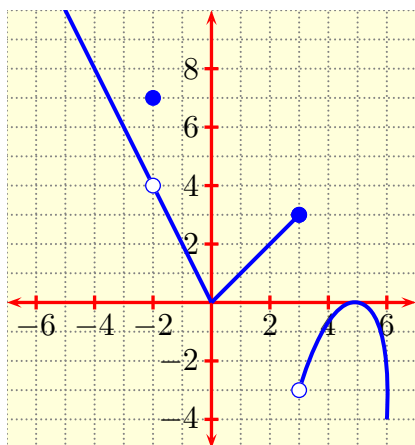
4.  $b = 1$

5.  $b = 0$

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**046 10.0 points**

Below is the graph of a function  $f$ .



Use the graph to determine

$$\lim_{x \rightarrow 3} f(x).$$

1. limit does not exist
2. limit = 7
3. limit = 4
4. limit = 3
5. limit = 12