Quiz 2 427J

1. Use the method of separable equations to solve

$$\frac{dy}{dt} = \frac{e^y}{t^2 + 1}$$

NOTE: Leave your solution implicit.

2. Compute

$$\frac{2-3i}{1+i}$$

1).
$$\frac{dy}{dt} = \frac{e^{y}}{t^{2}+1} \cdot \frac{1}{e^{y}}$$

$$\int \frac{1}{e^{y}} dy = \int \frac{1}{t^{2}+1} dt + C$$

$$\int e^{-y} = tan^{-1}(t) + C$$

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Let $z = \alpha + i\beta$ where $\alpha, \beta \in \mathbb{R}$ and $2 - 3i$

$$Re(z) = \alpha, \qquad 1 = 2 - 3i$$

$$Im(z) = \beta \qquad -i - 2i = 3i^{2}$$

$$\frac{2 - 3i}{1 + i} \cdot \frac{(1 - i)}{(1 - i)} = \frac{2 - 5i + 3i^{2}}{1 - i^{2}}$$

$$= \frac{2 - 5i - 1}{2}$$

$$= \frac{-5i - 1}{2}$$