

# Integer Multiplication

Given TWO LARGE positive integers of  $N$  digits/each. Each integer is stored in 1D array.  
Implement an **efficient algorithm** based on **Karatsuba's** method to multiply them?

## NOTES:

- $N$  is power of 2 (i.e. 2, 4, 8, 16, 32...  $2^i$ )
- Result MUST be stored in  $2 \times N$  digits (left padded by 0's if necessary)
- Least significant** digit is stored at **index 0** while most significant is stored at index  $N-1$

Index	$N - 1$	...	1	0
Digit	Most signif. digit	...	2 <sup>nd</sup> digit	Least signif. digit

## Complexity

The complexity of your algorithm should be **less than  $O(N^2)$**

## Evaluation

Sample Cases (Correctness)	<b>UNSEEN</b> Large Cases (Efficiency)	Total
2 Marks	6 Marks	8 MARKS

## Bonus & Competition#2

	Criteria	BONUS
Vs. Naïve (on Large Cases)	<b>Just Faster</b>	+1 Mark
	<b>1x Faster</b>	+3 Marks
	<b>[N]x Faster</b>	+[N]x2 Marks
<b>TOP5</b>	Correct & Speed	2~4 Marks

**Function:** **Implement it!**

```
static public byte[] IntegerMultiply(byte[] X, byte[] Y, int N)
```

`IntegerMultiplication.cs` includes this method.

## Examples

EX#1								EX#2																																							
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## C# Help

### Getting the size of 1D array

```
int size = array1D.GetLength(0);
```

### Getting the size of 2D array

```
int size1 = array2D.GetLength(0);
```

```
int size2 = array2D.GetLength(1);
```

### Creating 1D array

```
int [] array1D = new int [size]
```

### Creating 2D array

```
int [,] array2D = new int [size1, size2]
```

### Sorting single array

Sort the given array "items" in ascending order

```
Array.Sort(items);
```

### Sorting parallel arrays

Sort the first array "master" and re-order the 2<sup>nd</sup> array "slave" according to this sorting

```
Array.Sort(master, slave);
```