

TP report: "FACTORIAL ANALYSIS OF CORRESPONDENCE"

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1 introduction

1.1 Definition of Factorial Analysis Of Correspondence :

is a multivariate technique that may be applied to any type of data . It detects associations and oppositions existing between subjects and objects.

1.2 The objective of Principal Component Analysis :

- The aim of correspondence analysis is to illustrate the relationships between two categorical variables.
- This method attempts to retain as far as possible the distances that exist between the categories of a variable with respect to its description by the respective other variable when generating a reduced solution.

1.3 presentation of our inputs

1.3.1 Presentation of Khi-2 table

Generally, the khi-2 table give precisely the probabilities $P(X_i | t)$ for different values of t and different degrees of freedom.

1.3.2 Presentation of observed data table

A raw data table that we seek to prove the similarity or difference between the variables it contains.

Code Matlab :

```
donnees_observees=[36 34 14 16]
```

1.4 The steps followed

1.4.1 calculate the table of theoretical values

in our case we only have one line , so we calculate it with the following steps

Code Matlab :

```

n=sum( donnees_observees )
val=n/w;
donnees_theoriques(1:4)=val

```

in the case that we have multi line we calculate the table with the following steps

Code Matlab :

```

somme1= sum( donnees_observees_2 ,1)
somme2= sum( donnees_observees_2 ,2)
somme3=sum(somme2,1)
for i=1:w
    for j=1:h
        donnees_theoriques(i,j)= (somme1(j)*somme2(i))/somme3;
    end
end

```

1.4.2 X-calculated

we calculate the value of X-calculated with the formula $\sqrt{\frac{(\Delta)^2}{T_e}}$
such as $\Delta = T_o - T_e$

Code Matlab :

```

x_calculer=0;
for i=1:h
    for j=1:w
        x_calculer=x_calculer+( ( donnees_observees(i,j) -
        donnees_theoriques(i,j) ).^2 /donnees_theoriques(i,j));
    end
end

```

1.4.3 degree of liberty

Code Matlab :

```

ddl=(w-1)*(h-1)

```

1.4.4 X-theoretical

In this example we have used significance level = 0.05
then we look for the value in the intersection of our significance level value with the value closest to our ddl value

Code Matlab :

```

for i=1:size(p,2)
    if p(i)==niveau_de_signification
        val2=i+1;
        break
    end
end

KHI_2(:,1)
for i=1:size(KHI_2(:,1),2)
    if KHI_2(i,1)>=ddl
        val3=i
        break
    end
end

x_theorique=KHI_2(val3, val2)

```

1.4.5 null hypothesis

deduce the rejection / non-rejection of the null hypothesis and deduce that the rows and columns are independent / dependent .

the contingency coefficient If the link exists, then we calculate the contingency coefficient and we deduce whether the link is strong or weak .

$$\text{contingency coefficient} = \sqrt{\frac{Xc^2}{n+Xc^2}}$$

- Si La valeur de ce coefficient est proche de 1, alors la liaison est forte
- S'il est proche de 0, la liaison est faible.

```

if (x_calculer > x_theorique )

    disp('null hypothesis rejected , So there is a link between
        the factors and the choice ')
    le_coefficient_de_contingence= ((x_calculer).^2/(n+
        (x_calculer).^2 ) ).^(1/2)

    if le_coefficient_de_contingence<0.5
        disp("The value is close to 0 , the bond is weak.")
    else
        disp("The value is close to 1, the bond is strong.")
    end

else
    disp('null hypothesis accepted , So there is no link between
        the factors and the choice ')
end

```

1.4.6 Diagram the response

Code Matlab :

```
x = 0:0.1:16;  
y = chi2pdf(x,3);  
x2= x_theorique  
  
figure;  
plot(x2,y,'g*')  
hold on  
plot(x,y,'b-o')  
xlabel('Observation', 'Color', 'b')  
ylabel('Probability Density', 'Color', 'b')  
hold on
```

In our example, we have the following diagram as result:

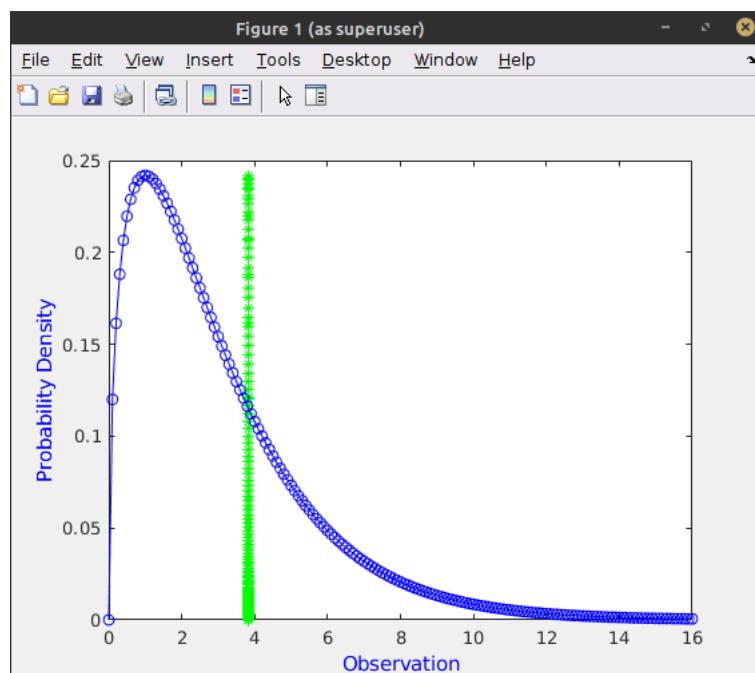


Figure 1: diagram

1.5 conclusion

Our result:

- $ddl = 0$
- donnees theoriques = 100 100 100 100
- $x \text{ calculer} = 40.9600$
- $x \text{ theorique} = 3.8415$
- null hypothesis rejected, So there is a link between the factors and the choice
- le coefficient de contingence = 0.9715
- The value is close to 1, the bond is strong.