

Case Study: Intersection of Sets

In algebra, the intersection of two sets is defined as a new set that contains all the values common to both sets. For instance, consider the following two sets, A and B :

$A = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

$B = \{2, 4, 8, 12, 14, 20, 25, 28, 30, 32\}$

The only values common to both sets are 2, 4, and 8. The intersection of A and B , which is denoted as $A \cap B$, is

$A \cap B = \{2, 4, 8\}$

This case study illustrates how array contents can be processed to perform an operation such as finding the intersection of two sets. The program will ask the user to enter two sets of values, each stored in an array. Then it will scan the two arrays looking for values common to both. The common values will be stored in a third array, whose contents are displayed on the screen.

Variables

Table 1 lists the variables needed.

Table 1

Variable	Description
set1	An array of 10 integers to hold the first set
set2	An array of 10 integers to hold the second set
intersection	An array of 10 integers to hold the intersection of set1 and set2
numIntValues	An integer holding the number of intersecting values

Functions

Table 2 lists the functions used by the program.

Table 2

Function	Description
getArray	set1 and set2 are passed into the function. It prompts the user to enter 10 values for each array.
findIntersection	set1, set2, and intersection are passed into the function. It scans the arrays for values that appear in both. The intersecting values are stored in intersection. This function returns the number of intersecting values found.
displayIntValue	The intersection array and the numIntValues variable are passed into this function. If numIntValues contains a number greater than zero, the function displays that many elements in the intersection array. If there are no intersecting values, the function displays a message indicating so.

The findIntersection Function

The findIntersection function uses two array parameters, first and second. The arrays set1 and set2 are passed into these parameters. The function uses nested loops to find the values that appear in both arrays. Here is the pseudocode.

```

For each element in the first array
  For each element in the second array
    Compare the selected elements in both arrays.
    If they contain the same value
      Store the value in the intersect array.
      Increment the count of intersecting values.
    End If.
  End For.
End For.
Return the count of intersecting values.

```

In the actual code, the outer loop cycles a counter variable (index1) through the values 0 through 9. This variable is used as the subscript for set1. The inner loop also cycles a counter variable (index2) through the values 0 through 9. This variable is used as a subscript for set2. For each iteration of the outer loop, the inner loop goes through all its iterations. An if statement in the inner loop compares first[index1] to second[index2]. Because the inner loop iterates 10 times for each iteration of the outer loop, the function will compare each individual element of the first array to every element of the second array. Here is the C++ code for the function.

```

int findIntersection(int first[], int second[], int intersect[], int size)
{
    int intCount = 0,           // Number of intersecting values
        index3 = 0;           // Subscript variable for intersect array
    for (int index1 = 0; index1 < size; index1++)
    {
        for(int index2 = 0; index2 < size; index2++)
        {
            if (first[index1] == second[index2])
            {
                intersect[index3] = first[index1];
                index3++;
                intCount++;
            }
        }
    }
    return intCount;           // Return the number of intersecting values.
}

```

Program 7-28 shows the entire program's source code.

Program 7-28

```

1 // This program allows the user to enter two sets of numbers.
2 // It finds the intersection of the two sets (which is the
3 // set of numbers contained in both sets). The intersecting
4 // values are displayed.
5 #include <iostream>
6 using namespace std;
7
8 // Function Prototypes
9 void getArrays(int [], int [], int);
10 int findIntersection(int [], int [], int [], int);
11 void displayIntValues(int [], int);
12
13 int main()
14 {
15     const int NUM_VALUES = 10;    // Number of values in each array
16     int set1[NUM_VALUES],         // First set
        set2[NUM_VALUES],         // Second set
        intersection[NUM_VALUES], // Set containing intersection values
        numIntValues;              // number of values in intersection
17
18     // Get values for the sets.
19     getArrays(set1, set2, NUM_VALUES);
20
21     // Find the intersection of the two sets
22     numIntValues = findIntersection(set1, set2,
23                                     intersection, NUM_VALUES);
24
25
26
27

```

(program continues)

Program 7-28*(continued)*

```

28     // Display the intersecting values
29     displayIntValues(intersection, numIntValues);
30     return 0;
31 }
32
33 //*****
34 // Definition of function getArrays *
35 // This function accepts two int arrays as arguments. *
36 // It prompts the user to enter 10 values for each array *
37 //*****
38
39 void getArrays(int first[], int second[], int size)
40 {
41     // Get values for first array.
42     cout << "Enter 10 values for the first set:\n";
43     for (int index = 0; index < size; index++)
44         cin >> first[index];
45
46     // Get values for second array.
47     cout << "Enter 10 values for the second set:\n";
48     for (index = 0; index < size; index++)
49         cin >> second[index];
50 }
51
52
53 //*****
54 // Definition of function findIntersection *
55 // This function accepts three arrays as arguments. *
56 // The first two arrays (first and second) are scanned, *
57 // and all values appearing in both are stored in the *
58 // third array (intersect). The number of values that appear *
59 // in both arrays is returned. *
60 //*****
61
62 int findIntersection(int first[], int second[], int intersect[], int size)
63 {
64     int intCount = 0, // Number of intersecting values
65     index3 = 0; // Subscript variable for intersect array
66
67     for (int index1 = 0; index1 < size; index1++)
68     {
69         for(int index2 = 0; index2 < size; index2++)
70         {

```

(program continues)

Program 7-28*(continued)*

```

71         if (first[index1] == second[index2])
72         {
73             intersect[index3] = first[index1];
74             index3++;
75             intCount++;
76         }
77     }
78 }
79 return intCount; // Return the number of intersecting values.
80 }
81
82 //*****
83 // Definition of function displayIntValues *
84 // This function accepts two arguments: an array of ints *
85 // and an int. The second argument is the number of *
86 // valid elements contained in the array. *
87 // These values are displayed, if there are any. *
88 //*****
89
90 void displayIntValues(int intersect[], int num)
91 {
92     if (!num)
93         cout << "There are no intersecting values.\n";
94     else
95     {
96         cout << "Here is a list of the intersecting values:\n";
97         for (int index = 0; index < num; index++)
98             cout << intersect[index] << " ";
99         cout << endl;
100     }
101 }

```

Program Output with Example Input Shown in Bold

Enter 10 values for the first set:

1 2 3 4 5 6 7 8 9 10

Enter 10 values for the second set:

2 4 8 12 14 20 25 28 30 32

Here is a list of the intersecting values:

2 4 8