

Homework 4

Question 2

Part 1:

My **HashTable** class is implemented by using the following private variables.

private:

int table;*

LocationStatus status;*

int hashTableSize;

CollisionStrategy strategy;

int curSize;

Where I defined enum `LocationStatus { OCCUPIED, EMPTY, DELETED }` for knowing the status of a location in the hashTable. The variables `table` and `status` are used as the arrays for hashTable storage. Note that they could also have been packed into a struct but the current implementation keeps them separate.

While probing, the *stopping conditions* are designed such that a search can be stopped and returned unsuccessful if the search reaches an `EMPTY` location. In order to avoid *infinite loops*, the total number of probes is limited to `hashTableSize`, since the indices repeat after that. This can be proved mathematically for all strategies as follows.

Proof:

Initial starting index is,

$$\text{index} = \text{key} \% \text{tableSize}$$

for ith probing iteration,

For linear probing:

$$\text{newIndex} = (\text{index} + i) \% \text{tableSize}$$

after tableSize probes ($i = \text{tableSize} + k$),

$$\text{newIndex} = (\text{index} + \text{tableSize} + k) \% \text{tableSize} = (\text{index} + k) \% \text{tableSize}$$

which shows that index repeats after tableSize probes.

For quadratic Probing:

$$\text{newIndex} = (\text{index} + i^2) \% \text{tableSize}$$

after tableSize probes ($i = \text{tableSize} + k$),

$$\text{newIndex} = (\text{index} + \text{tableSize}^2 + k^2 + (2k) * \text{tableSize}) \% \text{tableSize} = (\text{index} + k^2) \% \text{tableSize}$$

which shows that index repeats after tableSize probes.

For double hashing:

$$\text{newIndex} = (\text{index} + (i * \text{hash2}(\text{item}))) \% \text{tableSize}$$

after tableSize probes ($i = \text{tableSize} + k$),

$$\text{newIndex} = (\text{index} + ((\text{tableSize} + k) * \text{hash2}(\text{item}))) \% \text{tableSize}$$

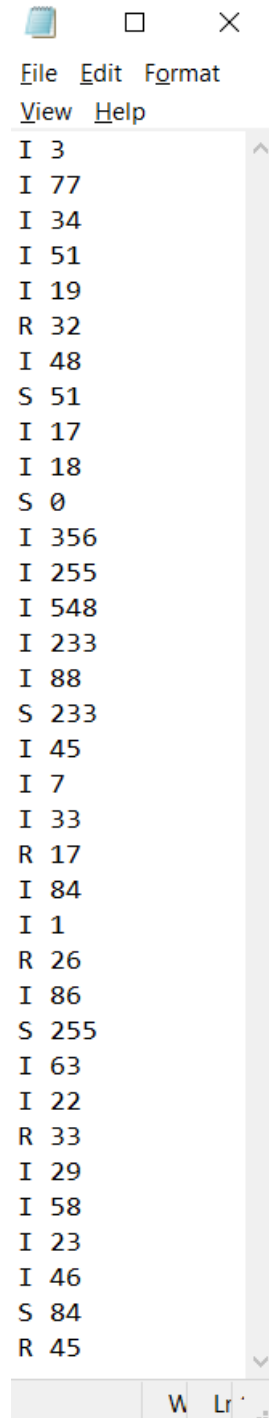
$$\text{newIndex} = (\text{index} + ((\text{tableSize} * \text{hash2}(\text{item})) + (k * \text{hash2}(\text{item})))) \% \text{tableSize}$$

$$\text{newIndex} = (\text{index} + (k * \text{hash2}(\text{item}))) \% \text{tableSize}$$

which shows that index repeats after tableSize probes.

Part 2:

The table size used was 29. The data used for the driver function and the corresponding outputs are as follows:



Using Linear probing:

3 inserted	0: 29
77 inserted	1: 233
34 inserted	2: 88
51 inserted	3: 3
19 inserted	4: 58
32 not removed	5: 34
48 inserted	6: 1
51 found after 1 probes	7: 7
17 inserted	8: 356
18 inserted	9: 63
0 not found after 1 probes	10:
356 inserted	11:
255 inserted	12:
548 inserted	13:
233 inserted	14:
88 inserted	15:
233 found after 1 probes	16:
45 inserted	17: 46
7 inserted	18: 18
33 inserted	19: 77
17 removed	20: 19
84 inserted	21: 48
1 inserted	22: 51
26 not removed	23: 255
86 inserted	24: 22
255 found after 1 probes	25: 23
63 inserted	26: 548
22 inserted	27: 84
33 removed	28: 86
29 inserted	
58 inserted	
23 inserted	
46 inserted	
84 found after 2 probes	
45 removed	

Using Quadratic probing:

3 inserted	0: 29
77 inserted	1: 233
34 inserted	2: 88
51 inserted	3: 3
19 inserted	4: 58
32 not removed	5: 34
48 inserted	6: 63
51 found after 1 probes	7: 7
17 inserted	8: 356
18 inserted	9: 22
0 not found after 1 probes	10: 1
356 inserted	11:
255 inserted	12:
548 inserted	13:
233 inserted	14: 23
88 inserted	15:
233 found after 1 probes	16:
45 inserted	17: 46
7 inserted	18: 18
33 inserted	19: 77
17 removed	20: 19
84 inserted	21:
1 inserted	22: 51
26 not removed	23: 48
86 inserted	24: 255
255 found after 2 probes	25:
63 inserted	26: 548
22 inserted	27: 84
33 removed	28: 86
29 inserted	
58 inserted	
23 inserted	
46 inserted	
84 found after 2 probes	
45 removed	

Using Double Hashing:

3 inserted	0: 29
77 inserted	1: 233
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19 inserted	4:
32 not removed	5: 34
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51 found after 1 probes	7: 7
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255 found after 2 probes	25:
63 inserted	26: 548
22 inserted	27: 58
33 removed	28: 86
29 inserted	
58 inserted	
23 inserted	
46 inserted	
84 found after 3 probes	
45 removed	

Part 3:

We obtain the following results after using different collision resolution schemes like linear and quadratic probing and double hashing.

Using Linear probing:

```
Load factor: 0.758621
Average empirical Successful probes: 1.51724
Average empirical UnSuccessful probes: 10.5172
Average theoretical Successful probes: 2.57143
Average theoretical UnSuccessful probes: 9.08163
```

Where the theoretical values are obtained using,

$$\frac{1}{2} \left[1 + \frac{1}{1-\alpha} \right] \quad \text{for a successful search} , \quad \frac{1}{2} \left[1 + \frac{1}{(1-\alpha)^2} \right] \quad \text{for an unsuccessful search}$$

Using Quadratic probing:

```
Load factor: 0.758621
Average empirical Successful probes: 1.55172
Average empirical UnSuccessful probes: 4.65517
Average theoretical Successful probes: 1.87364
Average theoretical UnSuccessful probes: 4.14286
```

Using Double Hashing:

```
Load factor: 0.758621
Average empirical Successful probes: 1.7931
Average empirical UnSuccessful probes: -1
Average theoretical Successful probes: 1.87364
Average theoretical UnSuccessful probes: 4.14286
```

Where the theoretical values are obtained using,

$$\frac{-\log_e(1-\alpha)}{\alpha} \quad \text{for a successful search} , \quad \frac{1}{1-\alpha} \quad \text{for an unsuccessful search}$$

It can be observed that the theoretical and empirical values are very close to each other. Moreover, we also observe that linear probing performs the worst mainly due to the clustering problem. Quadratic probing and double hashing perform fairly better.

Conclusion:

This homework was a good exercise to understand and implement hashTables and the understanding different collision resolution strategies and their comparison and analysis.