A Monad

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Abstract

We present a new programming model for deterministic parallel computation in a pure functional language. The model is monadic and has explicit granularity, but allows dynamic construction of dataflow networks that are scheduled at runtime, while remaining deterministic and pure. The implementation is based on monadic concurrency, which has until now only been used to simulate concurrency in functional languages, rather than to provide parallelism. We present the API with its semantics, and argue that parallel exe-

cution is deterministic. Furthermore, we present a complete workstealing scheduler implemented as a Haskell library, and we show that it performs at least as well as the existing parallel programming models in Haskell.

Categories and Subject Descriptors D.1.3 [Software]: Programming Techniques—Concurrent Programming (Parallel programming)

General Terms Languages, Performance

1. Introduction

The prospect of being able to express parallel algorithms in a pure functional language and thus obtain a guarantee of determinism is tantalising. Haskell, being a language in which effects are explicitly controlled by the type system, should be an ideal environment for deterministic parallel programming.

For many years we have advocated the use of the par and pseq¹ operations as the basis for general-purpose deterministic parallelism in Haskell, and there is an elaborate parallel programming framework, Evaluation Strategies, built in terms of them [14, 20]. However, a combination of practical experience and investigation has lead us to conclude that this approach is not without drawbacks. In a nutshell, the problem is this: achieving parallelism with par requires that the programmer understand *operational* properties of the language that are at best implementation-defined (and at worst undefined). This makes par difficult to use, and pitfalls abound — new users have a high failure rate unless they restrict themselves to the pre-defined abstractions provided by the Strategies library. Section 2 elaborates.

In this paper we propose a new programming model for deterministic parallel programming in Haskell. It is based on a monad,

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for Deterministic Parallelism

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has explicit granularity, and uses I-structures [1] for communication. The monadic interface, with its explicit fork and communication, resembles a non-deterministic concurrency API; however by carefully restricting the operations available to the programmer we are able to retain determinism and hence present a pure interface, while allowing a parallel implementation. We give a formal

¹ formerly seq

operational semantics for the new interface.

Our programming model is closely related to a number of others; a detailed comparison can be found in Section 8. Probably the closest relative is pH [16], a variant of Haskell that also has I-structures; the principal difference with our model is that the monad allows us to retain referential transparency, which was lost in pH with the introduction of I-structures. The target domain of our programming model is large-grained irregular parallelism, rather than fine-grained regular data parallelism (for the latter Data Parallel Haskell [6] is more appropriate).

Our implementation is based on *monadic concurrency* [18], a technique that has previously been used to good effect to simulate concurrency in a sequential functional language [7], and to unify threads with event-driven programming for scalable I/O [13]. In this paper, we put it to a new use: implementing deterministic parallelism.

We make the following contributions:

- We propose a new programming model for deterministic parallel programming, based on a monad, and using I-structures to exchange information between parallel tasks (Section 3).
- We give a semantics (Section 5) for the language and a (sketch) proof of determinism (Section 5.2).
- Our programming model is implemented entirely in a Haskell library, using techniques developed for implementing concurrency as a monad. This paper contains the complete implementation of the core library (Section 6), including a work-stealing scheduler. Being a Haskell library, the implementation can be readily modified, for example to implement alternative schedul-

ing policies. This is not a possibility with existing parallel programming models for Haskell.

 We present results demonstrating good performance on a range of parallel benchmarks, comparing Par with Strategies (Section 7).

2. The challenge

To recap, the basic operations provided for parallel Haskell programming are par and pseq:

```
par :: a -> b -> b
pseq :: a -> b -> b
```

Informally, par annotates an expression (its first argument) as being potentially profitable to evaluate in parallel, and evaluates to the value of its second argument. The pseq operator expresses sequen-

tial evaluation ordering: its first argument is evaluated, followed by its second.

The par operator is an attractive language design because it capitalises on the overlap between lazy evaluation and *futures*. To implement lazy evaluation we must have a representation for expressions which are not yet evaluated but whose value may later be demanded; and similarly a future is a computation whose value is being evaluated in parallel and which we may wait for. Hence, par was conceived as a mechanism for annotating a lazy computation as being potentially profitable to evaluate in parallel, in effect turning a lazy computation into a future.

Evaluation Strategies [14, 20] further capitalise on lazy-evaluationfor-parallelism by building composable abstractions that express parallel evaluation over lazy data structures.

However, difficulties arise when we want to be able to program parallel algorithms with these mechanisms. To use par effectively, the programmer must

- (a) pass an unevaluated computation to par,
- (b) ensure that its value will not be required by the enclosing computation for a while, and
- (c) ensure that the result is shared by the rest of the program.

If either (a) or (b) are violated, then little or no parallelism is achieved. If (c) is violated then the garbage collector may (or may not) garbage-collect the parallelism before it can be used. We often observe both expert and non-expert users alike falling foul of one or more of these requirements.

These preconditions on par are *operational* properties, and so to use par the programmer must have an operational understanding

of the execution — and that is where the problem lies. Even experts find it difficult to reason about the evaluation behaviour, and in general the operational semantics of Haskell is undefined.

For example, one easy mistake is to omit pseq, leading to a program with undefined parallelism. For example, in

it is unspecified whether the arguments of (+) are evaluated left-to-right or right-to-left. The first choice will allow y to be evaluated in parallel, while the second will not. Compiling the program with different options may yield different amounts of parallelism.

A closely-related pitfall is to reason incorrectly about strictness. Parallelism can be lost either by the program being unexpectedly strict, or by being unexpectedly lazy. As an example of the former, consider

Here the programmer presumably intended to evaluate x in parallel with the call to f. However, if f is strict, the compiler may decide to use call-by-value for f, which will lose all parallelism. As an example of the latter, consider this attempt to evaluate all the elements of a list in parallel:

```
parList :: [a] -> [a]
parList [] = []
parList (x:xs) = x 'par' (x : parList xs)
```

The problem is that this is probably too lazy: the head is evaluated in parallel, but the tail of the list is lazy, and so further parallelism is not created until the tail of the list is demanded.

There is an operational semantics for par in Baker-Finch et al. [2], and indeed it can be used to reason about some aspects of parallel execution. However, the host language for that semantics

is Core, not Haskell, and there is no direct operational relationship between the two. A typical compiler will perform a great deal of optimisation and transformation between Haskell and Core (for example, strictness analysis). Hence this semantics has limited usefulness for reasoning about programs written in Haskell with par.

In Marlow et al. [14] we attempted to improve matters with the introduction of the Eval monad; a monad for "evaluation order". The purpose of the Eval monad is to allow the programmer to express an ordering between instances of par and pseq, something which is difficult when using them in their raw infix form. In this it is somewhat successful: Eval would guide the programmer away from the parList mistake above, although it would not help with the other two examples. In general, Eval does not go far enough — it partially helps with requirements (a) and (b), and does not help with (c) at all.

In practice programmers can often avoid the pitfalls by using the higher-level abstractions provided by Evaluation Strategies. However, similar problems emerge at this higher level too: Strategies consume lazy data structures, so the programmer must still understand where the laziness is (and not accidentally introduce strictness). Common patterns such as parMap work, but achieving parallelism with larger or more complex examples can be something of an art.

In the next section we describe our new programming model that avoids, or mitigates, the problems described above. We will return to evaluate the extent to which our new model is successful in Section 8.1.

3. The Par Monad

Our goal with this work is to find a parallel programming model that is expressive enough to subsume Strategies, robust enough to reliably express parallelism, and accessible enough that non-expert programmers can achieve parallelism with little effort.

Our parallel programming interface² is structured around a monad, Par:

newtype Par a instance Functor Par instance Applicative Par instance Monad Par

Computations in the Par monad can be extracted using runPar:

```
runPar :: Par a -> a
```

Note that the type of runPar indicates that the result has no side effects and does no I/O; hence, we are guaranteed that runPar produces a deterministic result for any given computation in the Par monad.

The purpose of Par is to introduce parallelism, so we need a way to create parallel tasks:

```
fork :: Par () -> Par ()
```

The semantics of fork are entirely conventional: the computation passed as the argument to fork (the "child") is executed concurrently with the current computation (the "parent"). In general, fork allows a tree of computations to be expressed; for the purposes of the rest of this paper we will call the nodes of this tree "threads".

Of course, fork on its own isn't very useful; we need a way to communicate results from the child of fork to the parent. For our communication abtraction we use IVars (also called I-structures):

data IVar a -- instance Eq

new :: Par (IVar a)
get :: IVar a -> Par a

put :: NFData a => IVar a -> a -> Par ()

²The current version is available at http://hackage.haskell.org/package/monad-par

An IVar is a write-once mutable reference cell, supporting two operations: put and get. The put operation assigns a value to the IVar, and may only be executed once per IVar (subsequent puts are an error). The get operation waits until the IVar has been assigned a value, and then returns the value.

One unusual aspect of our interface is the NFData ("normal-form data") context on put: our put operation is fully-strict in the value it places in the IVar, and the NFData context is a prerequisite for full-strictness. This aspect of the design is not forced; indeed our library also includes another version of put, put_, that is only head-strict. However, making the fully-strict version the default eliminates a common pitfall, namely putting a lazy computation into an IVar, and thereby deferring the work until the expression is extracted with get and its value subsequently demanded. By forcing values communicated via IVars to be fully evaluated, the programmer gains a clear picture of which work happens on which thread.

3.1 Derived combinators

A common pattern is for a thread to fork several children and then collect their results; indeed, in many parallel programs this is the only parallel pattern required. We can implement this pattern straightforwardly using the primitives. First, we construct an abstraction for a single child computation that returns a result:

```
spawn :: NFData a => Par a -> Par (IVar a)
spawn p = do
   i <- new
   fork (do x <- p; put i x)
   return i</pre>
```

The IVar in this context is commonly called a *future*, because it represents the value of a computation that will be completed at some later point in time.

Generalising spawn to a list is trivial: the monadic combinator mapM does the trick. However, a more useful pattern is to combine a spawn with a map: for each element of a list, create a child process to compute the application of a given function to that element. Furthermore, we usually want to wait for all the children to complete and return a list of the results. This pattern is embodied in the combinator parMapM, defined as follows:

```
parMapM :: NFData b => (a -> Par b) -> [a] -> Par [b]
parMapM f as = do
  ibs <- mapM (spawn . f) as
  mapM get ibs</pre>
```

The parMapM given above works on lists, but it can be trivially extended to work on any Traversable structure.

In principle, spawn subsumes fork, new, and put. Furthermore, spawn ensures that each IVar it creates is only ever put into once, so using spawn instead of separate fork and put gives a static guarantee that a multiple-put exception cannot occur at runtime. Static guarantees are good, so one may reasonably ask whether spawn should replace fork, new and put in the API. In practice we have found it to be convenient to have access to fork, new and put as these sometimes allow a computation to be expressed more straightforwardly; we shall see an example of this in Section 4. Programmers who wish to statically rule out a multiple-put exception can elect to restrict themselves to spawn.

3.2 Dataflow

The programming interface we described above yields a dataflow model, in which each fork creates a new computation node in the dataflow graph, and each IVar gives rise to edges from the producer to each of the consumers. Figure 1 shows pictorially a particular example of a network.

3.3 Safety

The interface given above does not prevent the programmer from returning an IVar from runPar and then passing it to other instances of runPar; the behaviour of the programming model is undefined under these circumstances. The semantics we give later will rule out such cases, but the API given above and our implementation of it do not. There is a well-known solution to this problem using parametricity [11], wherein a type variable parameter s is added both to the monad type and the variables (IVars, in our case):

```
newtype Par s a
runPar :: (forall s . Par s a) -> a
data IVar s a
new :: Par s (IVar s a)
get :: IVar s a -> Par s a
put :: IVar s a -> Par s ()
```

The type of this alternate version of runPar statically prevents any IVars from being returned by the Par computation. If the programmer were to try to do this, then the type variable a would be unified with a type involving s, and thus s would escape the forall quantifier, so the typechecker would complain. However, there is a tradeoff with this design: the extra type parameter per-

vades client code and can be somewhat inconvenient. We are currently investigating the tradeoff and expect at the least to provide this version of the Par monad as an alternative.

4. Examples

In the following sections we illustrate some realistic uses for the Par monad.

4.1 A parallel type inferencer

An example that naturally fits the dataflow model is program analysis, in which information is typically propagated from definition sites to usage sites in a program. For the sake of concreteness, we pick a particular example: inferring types for a set of non-recursive bindings. Type inference gives rise to a dataflow graph; each binding is a node in the graph with inputs corresponding to the free variables of the binding, and a single output represents the derived type for the binding. For example, the following set of bindings

```
f = ...
g = ... f ...
h = ... f ...
j = ... g ... h ...
```

can be represented by the dataflow graph in Figure 1. We assume the following definitions:

```
type Env = Map Var (IVar Type)
infer :: Env -> (Var,Expr) -> Par ()
```

where Expr is the type of expressions, Type is the type of types,

and Map is a type constructor for finite maps (such as that provided by the Data.Map module in Haskell). The function infer infers the type for a binding, and calls put to augment the environment mapping for the bound variable with its inferred type.

We can then define a parallel type inferencer as follows:

```
parInfer :: [(Var,Expr)] -> [(Var,Type)]
parInfer bindings = runPar $ do
  let binders = map fst bindings
  ivars <- replicateM (length binders) new
  let env = Map.fromList (zip binders ivars)
  mapM_ (fork . infer env) bindings
  types <- mapM_ get ivars
  return (zip binders types)</pre>
```

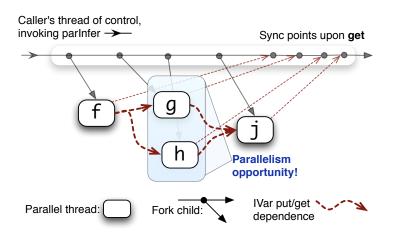


Figure 1. A dataflow graph, dynamically constructed by an invocation of the parInfer function. Threads synchronize upon requests for an IVar's value. IVars are not shown explicitly above, but a red arrow indicates that a thread gets an IVar which was put by another thread.

The first three lines of the do expression build up the environment of type Env for passing to infer, in which each variable is mapped to a newly created IVar. The fourth line forks a call to infer to run the type inferencer for each binding. The next line waits for all the results using mapM_ get, and the last line returns the results.

This implementation extracts the maximum parallelism inherent in the dependency structure of the given set of bindings, with very little effort on the part of the programmer. There is no explicit dependency analysis; the Par monad is doing all the work to resolve the dependencies. The same trick can be pulled using lazy evaluation of course, and indeed we could achieve the same parallel structure using lazy evaluation together with Strategies, but the advantage of the Par monad version is that the structure is programmed explicitly and the runtime behaviour is not tied to one particular evaluation strategy (or compiler).

This example illustrates the motivation for several aspects of the design:

- The dataflow graph generated is entirely *dynamic*; there is no way that we could statically predict the structure of the graph, because it depends only on the input program. (We highlight this point because some dataflow programming models only allow *static* dataflow graphs to be constructed.)
- We considered earlier whether it would make sense to replace new and put by spawn (Section 3.1). This example demonstrates two reasons why that would be inconvenient:
 - Consider extending the type inferencer to support Haskell's
 pattern bindings in which each equation binds multiple variables; then it is extremely convenient for infer to simply
 call put once for each variable bound by a particular equation.
 - If we had spawn only and no new, then then consider how to write parInfer. The output of spawn would be required in order to construct the Env which is passed back into the call to spawn itself. Hence we would need recursion, either in the form of a fixPar operator or recursive do notation.

4.2 A divide and conquer skeleton

Algorithmic skeletons are a technique for achieving modularity in parallel programming [8]. The idea is that the parallel algorithm is expressed as the composition of a parallel *skeleton* with the sequential algorithm (suitably factorised into pieces that can be executed in parallel). In the Par monad, as with other functional parallel programming models, skeletons are readily expressed as higher-order functions. We saw an example of a simple skeleton above: parMap, otherwise known as the master-worker skeleton. A skeleton corresponding to divide-and-conquer algorithms can be defined as follows:

this is a general divide-and-conquer of arbitrary (even variable) degree. The caller supplies functions that respectively determine whether the current problem is indivisible, split the problem into a list of sub-problems, join the results from sub-problems into a

single result, and solve a particular problem instance.

4.3 Stream Processing Pipelines

IVars can be used as communication channels between threads, enabling producer-consumer parallelism. This is possible because while an IVar carries only a single value during its lifetime, that value may in turn contain other IVars. Thus, a linked list using IVars as tail pointers can serve as a stream datatype:

```
data IList a = Null | Cons a (IVar (IList a))
type Stream a = IVar (IList a)
```

Actors, or *kernels*, that process streams are nothing more than Par threads that perform gets and puts. Our current Par distribution includes a library of higher-order stream operators built in this way. As an example, the following function applies a stateful kernel to the elements of a stream, updating the state after each element processed and writing results to an output stream:

Notice that the above kernel will execute continuously as long

as data is available, keeping that kernel on a single processor, where its working set is in-cache. Our experiments show this is effective: kernels typically execute on a single core for long periods.

The authors tried to make a similar construction using Strategies, and found it to be surprisingly difficult. Due to space constraints we are unable to describe the problem in detail, but in summary it is this: previously published techniques for pipeline Strategies [20] no longer work because they fall victim to requirement (c) from Section 2, the constraint that was added to avoid space leaks with the original formulation of Strategies [14]. It is possible to use element-wise parallelism instead, but that does not take advantage of the locality within a kernel. Ultimately we were not

```
\begin{array}{ccc} x,y & \in & \mathit{Variable} \\ i & \in & \mathit{IVar} \end{array}
             V ::= x \mid i \mid \ x \rightarrow M
Values
                       return M \mid M \gg N
                          runPar M
                          fork M
                          new
                          put i M
                          get i
                          done M
Terms \quad M, N \quad ::= \quad V \mid M N \mid \cdots
P \mid Q parallel composition
```

Figure 2. The syntax of values and terms

$$P \mid Q \equiv Q \mid P$$

$$P \mid (Q \mid R) \equiv (P \mid Q) \mid R$$

$$\nu x.\nu y.P \equiv \nu y.\nu x.P$$

$$\nu x.(P \mid Q) \equiv (\nu x.P) \mid Q, \qquad x \notin fn(Q)$$

$$\frac{P \rightarrow Q}{P \mid R \rightarrow Q \mid R} \qquad \frac{P \rightarrow Q}{\nu x.P \rightarrow \nu x.Q}$$

$$\frac{P \equiv P' \quad P' \rightarrow Q' \quad Q' \equiv Q}{P \rightarrow Q}$$

Figure 3. Structural congruence, and structural transitions.

able to achieve as much speedup with Strategies as we were with the Par monad on this example³.

5. Operational Semantics

In this section we add precision to our informal description of the programming model with a formal operational semantics. The operational semantics will allow non-determinism in the reduction order, modeling a truly parallel implementation, but we will argue (in Section 5.2) that the result of any given application of runPar is deterministic.

5.1 The semantics

Figure 2 gives the syntax of values and terms in our language. The only unusual form here is done M, which is an internal tool we shall use in the semantics for runPar; it is not a term form available

to the programmer.

 $\nu i.(\langle \rangle_i \mid \mathcal{E}[\mathsf{get}\ i]^*) \rightarrow$

The main semantics for the language is a big-step operational semantics written

$$M \Downarrow V$$

 $M \not\equiv V \quad M \Downarrow V$

The reader is invited to try; sample code can be found at: https://github.com/simonmar/monad-par/blob/master/examples/stream/disjoint_working_sets_pipeline.hs.

 $(M >>= \backslash x.\mathtt{done}\ x) \to^* \mathtt{done}\ N,\ N \Downarrow V$

(GCDeadlock)

Figure 4. Transition Rules

meaning that term M reduces to value V in zero or more steps. It is entirely conventional, so we omit all its rules except one, namely (RunPar) in Figure 4. We will discuss (RunPar) shortly, but the important point for now is that it in turn depends on a small-step operational semantics for the Par monad, written

$$P \rightarrow Q$$

Here P and Q are *states*, whose syntax is given in Figure 2. A state is a bag of terms M (its active "threads"), and IVars i that are either full, $\langle M \rangle_i$, or empty, $\langle \rangle_i$. In a state, the $\nu i.P$ serves (as is conventional) to restrict the scope of i in P. The notation $P_0 \to^* P_i$ is shorthand for the sequence $P_0 \to \ldots \to P_i$ where $i \ge 0$.

States obey a structural equivalence relation \equiv given by Figure 3, which specifies that parallel composition is associative and commutative, and scope restriction may be widened or narrowed provided no names fall out of scope. The three rules at the bottom of Figure 3 declare that transitions may take place on any sub-state, and on states modulo equivalence. So the \rightarrow relation is inherently non-deterministic.

The transitions of \rightarrow are given in in Figure 4 using an *evaluation* context \mathcal{E} :

$$\mathcal{E} ::= [\cdot] \mid \mathcal{E} >>= M$$

Hence the term that determines a transition will be found by looking to the left of >>=. Rule (Eval) allows the big-step reduction

semantics $M \Downarrow V$ to reduce the term in an evaluation context if it is not already a value.

Rule (Bind) is the standard monadic bind semantics.

Rule (Fork) creates a new thread.

Rules (New), (Get), and (PutEmpty) give the semantics for operations on IVars, and are straightforward: new creates a new empty IVar whose name does not clash with another IVar in scope, get returns the value of a full IVar, and put creates a full IVar from an empty IVar. Note that there is no transition for put when the IVar is already full: in the implementation we would signal an error to the programmer, but in the semantics we model the error condition by having no transition. Also note that the semantics here does not model the hyperstrict behaviour of the programmer-level put; indeed there are various options for the strictness of put, and the choice has no effect on the rest of the semantics or its determinism property, so we ignore it here.

Several rules that allow parts of the state to be *garbage collected* when they are no longer relevant to the execution. Rule (GCReturn) allows a completed thread to be garbage collected. Rule (GCFull) allows a full IVar to be garbage collected provided the IVar is not referenced anywhere else in the state. The equivalences for ν in Figure 3 allow us to push the ν down until it encloses only the dead IVar.

Rule (GCDeadlock) allows an empty IVar and a set of zero or more deadlocked threads to be garbage collected: the syntax $\mathcal{E}[\mathtt{get}\ i]^*$ means zero or more threads of the given form. Since there can be no other threads that refer to i, none of the gets can ever make progress. Hence the entire set of deadlocked threads together with the empty IVar can be removed from the state.

The final rule, (RunPar), gives the semantics of runPar and connects the Par reduction semantics \rightarrow with the functional reduction semantics \Downarrow . Informally it can be stated thus: if the argument M to runPar runs in the Par semantics yielding a result N, and N reduces to V, then runPar M is said to reduce to V. In order to express this, we need a distinguished term form to indicate that the "main thread" has completed: this is the reason for the form done M. The programmer is never expected to write done M directly, it is only used as a tool in the semantics. We will use a similar trick in the implementation of runPar itself (Section 6.2).

5.2 Determinism

An informal argument for determinism follows. We require that if $\operatorname{runPar} M \Downarrow N$ and $\operatorname{runPar} M \Downarrow N'$, then N = N', and furthermore that if $\operatorname{runPar} M \Downarrow N$ then there is no sequence of transitions starting from $\operatorname{runPar} M$ that reaches a state in which no reduction is possible. Informally, $\operatorname{runPar} M$ should either pro-

duce the same value consistently, or produce no value consistently (which is semantically equivalent to \perp).

First, observe that the system contains no transitions that take a full IVar to an empty IVar, or that change the contents of a full IVar. A non-deterministic result can only arise due to a race condition: two different orderings of reductions that lead to a different result. To observe non-determinism, there must be multiple reduction sequences leading to applications of the rule (PutEmpty) for the same IVar with different values. There is nothing in the semantics that prevents this from happening, but our determinism argument rests on the (RunPar) rule, which requires that the state at the end of the reduction consists of only done M for some M. That is, the rest of the state has completed or deadlocked and been garbage collected by rules (GCReturn), (GCFull), and (GCDeadlock). In the case where there is a choice between multiple puts, one of them will not be able to complete and will remain in the state, and thus the runPar transition will never be applicable.

The reader interested in a full proof of determinism should refer to Budimlic et al. [4], which contains a proof of determinism for Featherweight CnC, a language which is essentially equivalent to Par.

6. Implementation

As in Claessen [7], the implementation is in two parts: computations in the monad produce a lazy stream of operations, or *trace*, and a *scheduler* consumes the traces of the set of runnable threads, switching between them according to a scheduling policy.

In this section we first describe the implementation of the Par monad, and then give two scheduler implementations: first a sequential scheduler (Section 6.2), and then a true parallel scheduler using work-stealing (Section 6.3).

The separation between the Par monad and the scheduler is not a fundamental requirement of the technique, indeed we could combine the Par monad with the scheduler for a more efficient implementation. However, this modular presentation is much easier to understand, and separating the details of the scheduler from the Par monad allows us to describe two independent scheduler implementations without repeating the implementation of Par. Indeed, in our real implementation we retain this separation so as to facilitate the provision of multiple scheduling policies, or user-defined schedulers. Specialising the Par monad with respect to a particular scheduler is entirely possible and mechanical; we describe how to do this in Section 6.4.1.

6.1 Implementation of the Par monad

Computations in the Par monad produce a Trace:

Our fork and get operations require that we be able to suspend a computation and resume it later. The standard technique for implementing suspension and resumption is to use continuationpassing, which is exactly what we do in the form of a continuationpassing monad. The continuation result is fixed to be of type Trace, but otherwise the monad is completely standard:

```
newtype Par a = Par {
```

```
unPar :: (a -> Trace) -> Trace
}
instance Monad Par where
  return a = Par $ \c -> c a
  m >>= k = Par $
  \c -> unPar m (\a -> unPar (k a) c)
```

The basic operations in Par simply return the appropriate Trace values. Firstly, fork:

```
fork :: Par () -> Par ()
fork p = Par $
    \c -> Fork (unPar p (\_ -> Done)) (c ())
```

recall that Fork has two arguments of type Trace, these represent the traces for child and the parent respectively. The child is the Trace constructed by applying the argument p to the continuation (_ -> Done), while the parent Trace results from applying the continuation c to () - the unit value because fork returns Par ().

The IVar operations all return Trace values in a straightforward way:

```
new :: Par (IVar a)
new = Par $ New

get :: IVar a -> Par a
get v = Par $ \c -> Get v c

put :: NFData a => IVar a -> a -> Par ()
put v a = deepseq a (Par $ \c -> Put v a (c ()))
```

Note that put fully evaluates the argument a using deepseq before returning the Put trace.

6.2 A sequential scheduler

This sequential scheduler is implemented in the IO monad, but using only deterministic operations (runPar uses unsafePerformIO). By using IO here we will be able to smoothly extend the implementation to support true parallelism in Section 6.3.

Here are some of the main types in the scheduler:

```
sched :: SchedState -> Trace -> IO ()
type SchedState = [Trace]
newtype IVar a = IVar (IORef (IVarContents a))
data IVarContents a = Full a | Blocked [a -> Trace]
```

The scheduler is an IO function that takes some state of type SchedState, and the current thread of type Trace: The state of the scheduler, SchedState, is its work pool, represented by a list of threads ready to run. A IVar is represented by an IORef, which contains either a value (Full a), or a list of blocked threads waiting for the value (Blocked [a -> Trace]).

We need a small auxiliary function, reschedule, to choose the next thread to run from the pool and invoke the scheduler proper:

```
reschedule :: SchedState -> IO ()
reschedule [] = return ()
reschedule (t:ts) = sched ts t
```

We also use the following auxiliary function to modify the contents of an IORef:

```
modifyIORef :: IORef a \rightarrow (a \rightarrow (a,b)) \rightarrow IO b
```

Next, we describe each case of sched separately. First, the case for Fork:

```
sched state (Fork child parent) =
  sched (child:state) parent
```

We simply push the child thread on the stack of runnable threads, and continue with the parent. Note that we treat the runnable threads like a stack rather than a queue. If we were implementing concurrency, then fairness would be a consideration and a different data structure might be more appropriate. However, here the

scheduling policy is relevant only for performance, and so in the sequential scheduler we use a stack for simplicity. We return to the question of scheduling policies in Section 6.4.

When a thread has completed, its trace ends with Done; in that case, we look for more work to do with reschedule:

```
sched state Done = reschedule state
```

Next we deal with creating new IVars:

```
sched state (New f) = do
  r <- newIORef (Blocked [])
  sched state (f (IVar r))</pre>
```

The case for Get checks the current contents of the IVar. If it is Full, then we continue by applying the continuation in the Get constructor to the value in the IVar. If the IVar is empty, we block the current thread by adding its continuation to the list already stored in the IVar and pick the next thread to run with reschedule:

```
sched state (Get (IVar v) c) = do
  e <- readIORef v
  case e of
  Full a -> sched state (c a)
  Blocked cs -> do
    writeIORef v (Blocked (c:cs))
  reschedule state
```

The case for Put also checks the current state of the IVar. If it is Full, then this is a repeated put, so the result is an error. Otherwise, we store the value a in the IVar as Full a, and unblock

any blocked threads by applying them to a, and putting them in the work pool.

Finally, the implementation of runPar is below. Arranging for the return value of the main thread to be communicated out is a little tricky: the scheduler has no return value itself, and to give it one would require parameterising all our types with the return type (including Par and IVar). Instead, we create an IVar for the purpose of collecting the return value, and compose the main Par action, x, with a put operation to store the return value. (This is similar to the technique we used to define the semantics of runPar earlier.) When the scheduler returns, we extract the return value by reading the IVar's IORef.

6.3 A parallel work-stealing scheduler

We now modify the sequential scheduler described in the previous section to support true parallel execution, with a work-stealing scheduling policy. Any scheduling policy can be implemented, of course; the work-stealing algorithm happens to perform relatively well on a wide range of parallel programs, but the optimal scheduling policy may well depend on the algorithm to be parallelised [19]. Since our scheduler implementation is entirely in Haskell and is relatively simple, different schedulers can be readily implemented by the programmer, and over time we expect to build up a library of scheduling algorithms.

As described earlier, the Par monad is independent of the choice of scheduler. Specifically the definition of Trace, the definition of Par and its Monad instance, and the implementations of fork, get, put and new all remain the same as in Section 6.1.

Our parallel scheduler works as follows:

- One Haskell thread is created per processor core. We call these the worker threads.
- Each thread runs its own instance of the scheduler, and each
 has a local work pool of runnable Traces. When the local work
 pool runs dry, a scheduler attempts to steal items from the work
 pools of other worker threads.
- When a worker thread cannot find any work to do it becomes *idle*. The set of idle processors is represented as a list of MVars, such that calling putMVar on one of these MVars will wake up an idle worker thread. When a worker thread creates a new work item, it wakes up one idle worker thread.
- When all work pools are empty, the computation is complete and runPar can return.

For efficiency we use an IORef to represent shared state, and atomicModifyIORef to perform atomic operations on it. The atomicModifyIORef operation has the same signature as modifyIORef that we used earlier:

```
atomicModifyIORef :: IORef a -> (a -> (a,b)) -> IO b
```

the difference is that the update is performed atomically; the contents of the IORef are replaced by a lazy thunk representing the result.

When we require not only atomicity but also *blocking*, we use MVars. Alternatively, we could have used STM for all of the shared state, although that would add some overhead to the implementation.

The scheduler state SchedState is no longer just a work pool, but a record with four fields:

containing, in order:

- no: the thread number
- workpool: the local work pool, stored in an IORef so that other worker threads may steal from it
- idle: an IORef shared by all threads, containing the list of currently idle worker threads, each represented by an MVar Bool

(The Bool indicates whether the computation is complete or not: if a thread is woken up with putMVar m False then it should continue to look for more work, otherwise it should stop.)

scheds: the list of SchedStates corresponding to all schedulers (this is used by the current scheduler to find other workpools to steal from).

The reschedule function has the same signature as before, but is different in two ways: first, we must use atomicModifyIORef to remove an item from the work pool, and second if the work pool is empty the scheduler attempts to *steal* from other work pools. Stealing is implemented by a function steal that we shall describe shortly.

We add a new auxilliary function pushWork that is used for adding a new item to the local work pool. It also checks the list of idle worker threads; if there are any, then one is woken up.⁴ Note that here the value returned from atomicModifyIORef has type IO (); we bind this to r and then execute it in the IO monad.

```
pushWork :: SchedState -> Trace -> IO ()
pushWork SchedState { workpool, idle } t = do
  atomicModifyIORef workpool $ \ts -> (t:ts, ())
  idles <- readIORef idle
  when (not (null idles)) $ do
   r <- atomicModifyIORef idle $ \is ->
      case is of
      [] -> ([], return ())
      (i:is) -> (is, putMVar i False))
   r -- r has type IO ()
```

The scheduler itself has the same signature as before:

```
sched :: SchedState -> Trace -> IO ()
```

Fork and Done are straightforward:

```
sched state (Fork child parent) = do
  pushWork state child
```

```
sched state parent
```

sched state Done = reschedule state

The implementation of New is unchanged. Get is different only in that an atomicModifyIORef is needed to operate on the contents of the IVar:

⁴ Note that we first read the list of idle threads using a non-atomic readIORef and only use atomicModifyIORef if the list is found to be non-empty. This avoids performing an atomic operation in the common case that all schedulers are working.

Put requires atomicModifyIORef to operate on the IVar, and calls pushWork to wake up any blocked gets, but otherwise is straightforward:

```
sched state (Put (IVar v) a t) = do
  cs <- atomicModifyIORef v $ \e -> case e of
          Full _ -> error "multiple put"
          Blocked cs -> (Full a, cs)
  mapM_ (pushWork state . ($ a)) cs
  sched state t
```

The steal function implements work-stealing. It loops through the list of SchedStates (omitting the current one, which is known to have an empty work pool). For each sibling worker, we attempt to remove an item from its work pool using atomicModifyIORef. If successful, we can call sched to continue executing the stolen work item. If we get to the end of the list without stealing anything, we create a new MVar, add it to the idle list, and block in takeMVar, waiting to be woken up. The result of the takeMVar is a

Bool value indicating whether we should stop, or continue to look for more work to do. If the list of idle workers already contains numCapabilities-1 elements (where numCapabilities is the number of processors), then we know that all the work queues are empty, and we wake up all the idle workers passing True to indicate that they should exit.

Note that there is a race condition in steal. We do not atomically look at *all* the scheduler queues simultaneously, so it is possible that the search reaches the end of the list without finding any work and the worker becomes idle, meanwhile another worker has added items to its work pool. The result is lost parallelism (but not deadlock), since there would be an idle worker and a non-empty work queue. However, typically work items are being created regularly, so the next work item to be pushed will result in the idle worker being woken up again, hence we believe that there will be little lost parallelism in practice. So far we have not observed the problem in our benchmarks, but if it did become an issue then there are a number of ways to fix it, for example using STM.

Finally, the runPar operation is a small elaboration of the previous sequential version. We create one SchedState for each core (the number of which is given by numCapabilities). Then, we create one thread per core with forkOnIO; this GHC primitive creates a thread which is tied to a particular core and may not be migrated by the runtime system's automatic load-balancing mechanisms. One of these threads runs the "main thread" (that is, the Par computation passed to runPar); this should normally be chosen to be the current CPU, since it is likely to be cache-hot. In the implementation below, we simply refer to it as main_cpu and omit the details. The non-main threads simply call reschedule, and hence will immediately start looking for work to do. An MVar is used to pass the final result from the main thread back to runPar, which blocks in takeMVar until the result is available before returning it.

```
runPar :: Par a -> a
runPar x = unsafePerformIO $ do
    let n = numCapabilities
```

```
workpools <- replicateM n $ newIORef []
is <- newIORef []
let scheds =
       [ SchedState \{ no = x, \}
                      workpool = wp,
                       idle = is.
                      scheds=scheds }
       | (x,wp) < -zip [0..] workpools ]
m <- newEmptyMVar
forM_ (zip [0..] states) $ \(cpu, state) ->
  forkOnIO cpu $
      if (cpu /= main_cpu)
         then reschedule state
         else do
              rref <- newIORef Empty
              sched state $
                 runPar (x >>= put_ (IVar rref))
                         (const Done)
              r <- readIORef rref
              putMVar m r
r <- takeMVar m
case r of
 Full a -> return a
  -> error "no result"
```

6.3.1 Correctness

If some subterm evaluates to \bot during execution of runPar, then the value of the whole runPar should be \bot . The sequential scheduler implements this, but the parallel scheduler given above does not. In practice, however, it will make little difference: if one of the

workers encounters a \bot , then the likely result is a deadlock, because the thread that the worker was executing will probably have outstanding puts. Since deadlock is semantically equivalent to \bot , the result in this case is equivalent. Nevertheless, modifying the implementation to respect the semantics is not difficult, and we plan to modify our real implementation to do this in due course.

6.4 Optimising the scheduler

The implementation given above was used in generating the benchmark measurements presented in the next section, and gives entirely acceptable results for many benchmarks. However, when pushed to the limit, particularly with very fine-grained parallelism, there are overheads in this implementation that become apparent (measurements of the overhead are given in Section 7.2).

There are several ways in which we can reduce the overhead, as outlined in the following sections.

6.4.1 Deforesting Trace

As we remarked earlier, the Trace datatype is a useful device for separating the scheduler from the Par monad implementation, but it is not a fundamental requirement of the implementation. We can eliminate the intermediate Trace data structure entirely mechanically, and thereby specialise the Par monad to a particular scheduler, as follows. First we define

```
type Trace = SchedState -> IO ()
```

and then replace each constructor in Trace with a function of the same type, whose implementation is the appropriate case in sched. For example, instead of the Fork constructor, we define

```
traceFork :: Trace -> Trace -> Trace
traceFork child parent = ...
```

and then replace instances of Fork with traceFork. Finally, we replace any calls of the form sched state t with t state.

We have experimented with this optimisation but at present it fails to achieve any significant benefit due to known deficiencies in GHC's optimiser. When the issues with the optimiser are resolved, we anticipate that eliminating the Trace data structure in this way will improve the performance of Par significantly.

6.4.2 Alternative scheduling policies

Choice of scheduling policy may have an asymptotic effect on space usage [19], and so ideally we would like to be able to select the scheduling policy per-algorithm and at runtime. Some of the scheduling options we have in mind are:

- scheduling the child rather than the parent of fork first. This is as simple as switching the arguments to Fork.
- oldest-first or random work-stealing. This requires changing the
 data structure used to represent the work queue from a list to
 something else, such as Data. Sequence. Another option is to
 use lock-free work-stealing deques, which are implemented in
 the GHC runtime system for par, but not currently available
 at the Haskell level. We hope to expose this functionality to
 Haskell and hence make it possible to use lock-free workstealing deques in our Par monad scheduler.

While our primary implementation supports scheduling the parent in fork and newest-first work-stealing only, we have an experimental version that also supports child-first scheduling of fork and

random work stealing, selectable at compile-time⁵ and we hope to be able to allow runtime-selectable schedulers in the future.

6.4.3 Optimising nested runPars

Each call to runPar creates a new gang of Haskell threads and schedulers. This is a rather large overhead, and so the current implementation of runPar is only suitable for large-scale parallelism. If multiple runPars are active simultaneously, their threads will compete with each other for the processors, and pathological scheduling may occur. We believe it should be possible to have multiple

⁵ Indeed, toggling those options can reduce the running time of parfib by 40% from what is reported in Section 7.2.

runPar instances share a single scheduler instance via some global shared state, and we plan to investigate this in future work.

7. Performance

In this section we analyse the performance of the Par monad in two ways: firstly we measure the raw overhead imposed by the Par monad, and secondly we consider the scaling properties of a selection of existing parallel benchmarks when using both the Par monad and the Strategies abstraction.

7.1 Experimental setup

We benchmarked on a machine containing 4 Intel Xeon E7450 processors running at 2.4GHz. Each processor has 6 cores, for a total of 24 cores. The OS was Windows Server 2008, and we used a development version of GHC (7.1.20110301).

GHC by default uses a 2-generation stop-the-world parallel garbage collector. We configured the runtime to use a fixed nursery size of 1MB (which we have measured as close to optimal for this hardware). We also used a fixed overall heap size chosen for each benchmark to be about three times the maximum heap residency required by the program. The purpose here is to level the playing field: by using a fixed heap size we eliminate the possibility that one version is gaining an advantage by using a larger memory footprint in order to reduce the overhead of GC. A larger heap size also helps avoid artifacts due to the timing of old-generation GCs.

The Par implementation used is exactly the work-stealing implementation as described in Section 6.

7.2 Overhead

To assess the overhead of the Par monad relative to the low-level par/pseq operations used in the Strategies library, we used the parfib microbenchmark. The implementations are as follows, with par/pseq on the left and the Par monad version on the right:

We measured the time taken to evaluate parfib 34 on a single processor with each version, and the total memory allocated by each program. The results were as follows:

version	time (slowdown)	memory allocated
par/pseq	0.29s	0.17GB
Par monad	$6.15s(21\times)$	6.19GB

So the overhead of the Par monad is at least a factor of 21 over par/pseq. This is unarguably high, but there is ample opportunity for improvement: we examined the code generated by GHC for the Par monad version and observed several opportunities for optimisation that are not yet being performed by GHC's optimiser. Hence there is reason to believe that by paying attention to GHC's optimiser and by optimising the Par monad itself (Section 6.4) we should be able to reduce the overhead considerably.

Neither version of the parfib benchmark above parallelises well in practice, because the granularity is much too fine. As with

many divide-and-conquer algorithms, it is necessary to define a cut-off point below which the normal sequential version of the

⁶ the Par library works on older versions too, but we added an extra primitive in GHC 7.1 that allows a thread to determine which processor it is running on, which allows runPar to make a better choice about how to place the main thread, which in turn improves performance slightly. algorithm is used. Given a suitable cut-off point for parfib, the overhead of the Par monad becomes irrelevant (as indeed it is in most of our actual benchmarks). Running parfib 43 with a cut-off at 24, both implementations achieve a speedup of 21× on 24 cores and almost identical running times.

7.3 Scaling

To measure scaling performance we used a selection of benchmarks from two sources. The following benchmarks were taken from the Intel CnC Haskell⁷ distribution, and converted into two versions, one using Strategies and one using the Par monad:

- blackscholes: An implementation of the Black-Scholes algorithm for modeling financial contracts. This program is a straightforward use of parMap in both Strategies and Par versions.
- nbody: calculate the forces due to gravity between a collection of bodies in 3-dimensional space.

The following benchmarks were obtained from the nofib benchmark suite and converted to use the Par monad:

mandel: a mandelbrot set renderer.

- matmult: matrix multiplication (unoptimised; using a list-of-lists representation for the matrices).
- minimax: a program to find the best move in a game of 4×4 noughts-and-crosses, using alpha-beta searching of the game tree to a depth of 6 moves. The game tree is evaluated in parallel.
- queens: calculate the number of solutions to the N-queens problem for 14 queens on a 14x14 board. Parallelism is via divide-and-conquer.
- sumeuler: compute the sum of the value of Euler's function applied to each integer up to a given bound.

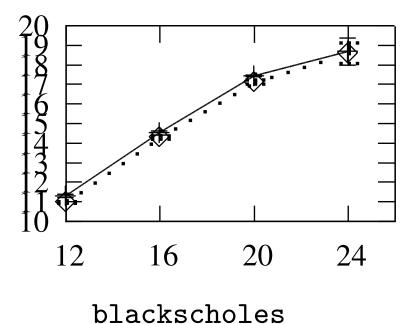
We measure the wall-clock running time of the whole program, which in some cases includes a sequential component where the program constructs its input data (matmult in particular has to construct the input matrices); the sequential component obviously limits the possible speedup.

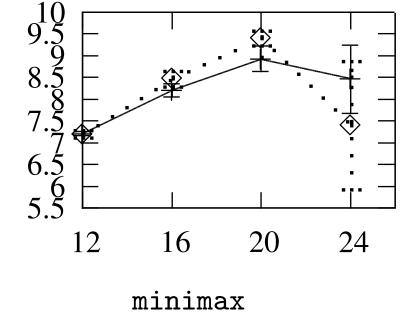
Figure 5 shows the scaling results up to 24 cores for each benchmark, comparing the Strategies version with the Par monad version. To make a direct comparison, we normalised both sets of results to the same baseline, namely the Strategies program compiled for sequential execution. We have omitted the results below 12 cores, which are largely uninteresting. Error bars are shown at one standard deviation; in most case the deviation is too small to be visible, except in one case — the 24-core result for minimax shows high variability. We believe this is an artifact of the high rate of GC performed by this benchmark together with the requirement that each GC perform a full synchronisation across all cores.

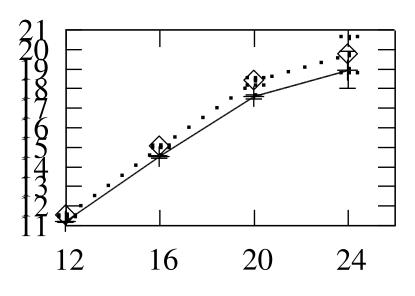
The results are surprisingly similar, and show a high degree of parallelism being achieved by both Strategies and Par. At 24 cores, two programs perform slightly better with Par: mandel and minimax, whereas one program is slightly worse: queens.

While the graphs only measure scaling, the absolute performance is also almost identical: the Strategies versions are on average 1% faster at 1 core, 2% slower at 12 cores and 2% slower at 24 cores. Hence we conclude that for typical parallel programs, the choice between Par and Strategies makes little difference to scaling or overall performance.

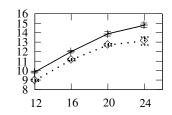
 $^{^{7}\,\}mathtt{http://hackage.haskell.org/package/haskell-cnc}$

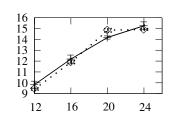






sumeuler





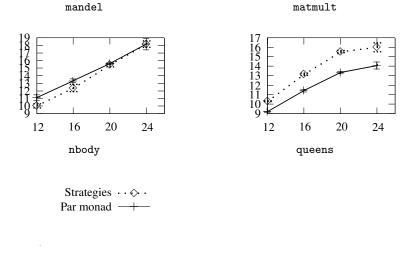


Figure 5. Speedup results on 24 cores (Y axis is speedup, X axis is number of OS threads)

8. Related Work

Key

Many parallel programming systems include a fork/join construct for dividing control flow, for example: Habanero Java [5] and Cilk [3]. These work well for divide-and-conquer algorithms and other problems where dataflow closely matches control flow.

Some of these models also integrate synchronous data structures as primitives, structuring the parallel scheduler around them.

pH [16], described in Section 1, is one example, including both IVars and MVars. Further, the Concurrent ML model provides synchronous point-to-point communication and has recently been paralellised [17]. Manticore [9] is a parallel variant of ML that supports both the CML programming model and a selection of parallel constructs including explicit futures.

Some systems based on Synchronous Data Flow [12] such as StreamIt [10], retain determinism but are significantly less expressive than the Par monad, being limited to first-order kernel functions and communication channels. Kahn process networks [12] are more general that Synchronous Dataflow, but to our knowledge there are no practical parallel programming systems currently available based on this abstraction. One that is closely related, however, is the Intel Concurrent Collections (CnC) model [4]. CnC provides a superset of the Par monad's functionality, including an extension of IVars that store a collection of key-value pairs. But CnC is a more complex model than Par and its implementations are focused on statically known networks rather than dynamic (forking) computations.

Finally, the dataflow model of computation induced by the Par monad and its IVars is very similar to that of the Skywriting language [15], although the context (distributed-memory cloud computing) is quite different. Indeed, with coarser grains of computation we conjecture that our monadic formalism constitutes an excellent domain-specific language for large-scale parallel programming, something we hope to try in the future.

A sceptical reader might reasonably ask whether the Par monad merely solves a problem that is unique to Haskell, namely laziness. After all, many of the difficulties identified in Section 2 relate to reasoning about strictness, a problem that simply does not arise

in a call-by-value language. True enough – but the strict-vs-lazy debate is a larger question than we address here; what we show in this paper is how to integrate selective control over evaluation order into a lazy language, without throwing the baby out with the bathwater. Moreover the Par monad lifts the implementation of the parallel fabric to the library level where it is vastly more malleable; a direct benefit of this is the ability to easily change the scheduling policy. This would be useful in any language, strict or lazy.

8.1 Comparison with par and Strategies

In Section 2 we outlined some difficulties with using the par operator and Strategies, and claimed that our new interface would avoid the problems; here we return to assess that claim, and also offer some comments on the other differences between the Par monad and Strategies.

Is the Par monad any easier to use than par?

• Each fork creates exactly one parallel task, and the dependencies between the tasks are explicitly represented by IVars. Parallel structure programmed in the Par monad is well-defined: we gave an operational semantics in Section 5 in terms of the Par monad operations themselves.

• The programmer does not need to reason about laziness. In fact, we have deliberately made the put operation hyperstrict by default, to head off any confusion that might result from communicating lazy values through an IVar. Hence, if the program is written such that each parallel task only reads inputs from IVars and producing outputs to IVars, the programmer can reason about the cost of each parallel task and the overall parallelism that can be achieved.

Nevertheless, the Par monad does not prevent lazy computations from being shared between threads, and the reckless programmer might even be able to capture some (unreliable) parallelism using only fork and laziness. This is not likely to work well: the Par monad scheduler cannot detect a thread blocked on a lazy computation and schedule another thread instead. Sharing lazy computations between threads in the Par monad is therefore to be avoided, but unfortunately we lack a way to statically prevent it.

A key benefit of the Strategies approach is that it allows the algorithm to be separated from the parallel coordination, by having the algorithm produce a lazy data structure that is consumed by the Strategy. The Par monad does not provide this form of modularity. However, many algorithms do not lend themselves to being decomposed in this way even with Strategies, because it is often inconvenient to produce a lazy data structure as output. We believe that higher-order skeletons (Section 4.2) are a more generally effective way to provide modular parallelism.

Strategies supports *speculation* in a strictly stronger sense than Par. In Strategies, speculative parallelism can be eliminated by the garbage collector when it is found to be unreferenced, whereas in Par, all speculative parallelism must be eventually executed.

The scheduler for Strategies is built-in to the runtime system, whereas the Par monad scheduler is written in Haskell, which enables us to easily use different scheduling policies.

Strategies includes a parBuffer combinator that can be used to evaluate elements of a lazy list in parallel. There is nothing directly equivalent in Par: all the parallelism must be complete when runPar returns, so we cannot return a lazy list from runPar with elements evaluated in parallel⁸. It is possible to program something equivalent to parBuffer inside the Par monad, however.

Finally, Par and Strategies can be safely combined. The GHC runtime system will prioritise Par computations over Strategies, because sparks are only evaluated when there is no other work.

9. Conclusion

We have presented our new parallel programming model, and demonstrated that it improves on the existing parallel programming models for Haskell in certain key ways, while not sacrificing performance on existing parallel benchmarks. In due course we hope that it is possible to go further and show that the extra control offered by the Par monad allows parallel algorithms to be tuned more effectively; we encountered one case of this in the pipeline example of Section 4.3.

It would be premature to claim that par and Strategies are redundant; indeed Strategies has advantages outlined in the previous section. Still, the difficulties with par indicate that it may be more appropriate as a mechanism for *automatic* parallelisation, than as a programmer-level tool.

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 $^{^8}$ although we believe this may be possible with modifications to ${\tt runPar}$

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