



بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ

In the name of Allah, the Most Merciful, the Most Kind

Date: 22-10-2021

BCS 103

Digital Logic & Computer Architecture

Lecture 21 and 22

IN THE LAST LECTURE

We have discussed

- **Sum of Product (minterm)**
- **Product of Sum (Maxterm)**
- **Karnaugh Map (2-variables)**

TODAY

We will discuss about

- **Karnaugh Map (3 variables)**

Karnaugh Maps

- 2 variables Karnaugh map

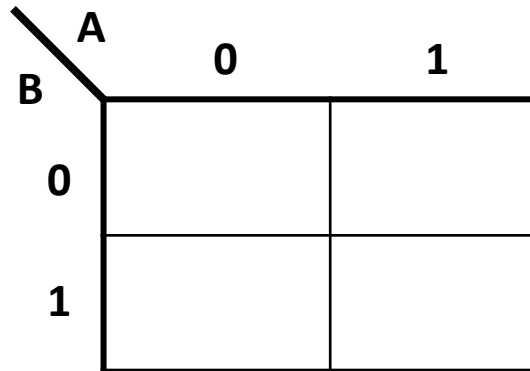
Q: Simplify the following expressions

1. $AB' + AB + A'B'$

2. $A'B' + A'B$

3. $A'B + AB$

4. $A'B' + A'B + AB' + AB$



- 2 variables Karnaugh map

$$AB' + AB + A'B'$$

		B	
		0	1
A	0		
	1		

		A	
		0	1
B	0		
	1		

- 2 variables Karnaugh map

$$A'B' + A'B$$

		B	
		0	1
A	0		
	1		

		A	
		0	1
B	0		
	1		

- 2 variables Karnaugh map

$$A'B + AB$$

		B	
		0	1
A	0		
	1		

		A	
		0	1
B	0		
	1		

- 2 variables Karnaugh map

$$A'B' + A'B + AB' + AB$$

		B	
		0	1
A	0		
	1		

		A	
		0	1
B	0		
	1		

Karnaugh Maps

- 3 variables Karnaugh map

BC	A	
	0	1
00		
01		
11		
10		

C	AB			
	00	01	11	10
0				
1				

A	BC			
	00	01	11	10
0				
1				

Three-Variable K-Maps

$$f = \sum(0,4) = \overline{B} \overline{C}$$

		BC			
		00	01	11	10
A	0	1	0	0	0
	1	1	0	0	0

$$f = \sum(4,5) = A \overline{B}$$

		BC			
		00	01	11	10
A	0	0	0	0	0
	1	1	1	0	0

$$f = \sum(0,1,4,5) = \overline{B}$$

		BC			
		00	01	11	10
A	0	1	1	0	0
	1	1	1	0	0

$$f = \sum(0,1,2,3) = \overline{A}$$

		BC			
		00	01	11	10
A	0	1	1	1	1
	1	0	0	0	0

$$f = \sum(0,4) = \overline{A} C$$

		BC			
		00	01	11	10
A	0	0	1	1	0
	1	0	0	0	0

$$f = \sum(4,6) = A \overline{C}$$

		BC			
		00	01	11	10
A	0	0	0	0	0
	1	1	0	0	1

$$f = \sum(0,2) = \overline{A} \overline{C}$$

		BC			
		00	01	11	10
A	0	1	0	0	1
	1	0	0	0	0

$$f = \sum(0,2,4,6) = \overline{C}$$

		BC			
		00	01	11	10
A	0	1	0	0	1
	1	1	0	0	1

Three-Variable K-Maps

A \ BC	BC			
	00	01	11	10
0		1		
1	1		1	1

A \ BC	BC			
	00	01	11	10
0	1		1	1
1	1			1

A \ BC	BC			
	00	01	11	10
0			1	1
1	1	1		

A \ BC	BC			
	00	01	11	10
0			1	
1	1		1	1

A \ BC	BC			
	00	01	11	10
0		1	1	1
1		1	1	

A \ BC	BC			
	00	01	11	10
0				
1				

Three-Variable K-Maps

$$AB'C + A'B'C + ABC + AB + AC + BC$$

Three-Variable K-Maps

$$A'B'C' + A'B' + AB'C + A'B + AC' + AB'C'$$

Thanks