When the dependent variable is categorical, then logistic regression is one of the most appropriate regression model. Logistic regression is a binary classifier, but multiple classification is possible using one vs. all model. If a data set D = (x,y) : $x \in X$, $y \in Y$ where X is the independent variables and Y is the set of category. The hypothesis function h $\theta(x)$ is given below which is a sigmoid function

$$h_{\theta}(\mathbf{x}) = \frac{1}{1 + e^{-\theta^T X}}$$

Using this hypothesis function a curved line is drawn which is used to classify the data. To derive the coefficients a cost function $J(\theta)$ is used. The value of $J(\theta)$ is shown in following equation,

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^{m} [y_i \log h_{\theta}(\mathbf{x}_i) + (1-y_i)\log(1 - h_{\theta}(\mathbf{x}_i))]$$

Figure 1: Basic Logistic Regression

After minimizing the cost function, the values of the coefficients are derived. The following equation is used to update the values of θ ,

$$\theta_{\rm j} = \theta_{\rm j}$$
- $\frac{1}{m} \sum_{i=1}^{m} (h_{\rm j}(x_{\rm i}) - y_{\rm i}) x_{\rm ij}$

Logistic Regression