# Symplectic Geometry and Toric Varieties



#### Abdullah Ahmed

Syed Babar Ali School of Science and Engineering Lahore University of Management Sciences Mathematics Department

> A semesterly report submitted in partial fulfilment of the requirements for a Bachelor's Thesis in Mathematics

Due on: 15 January 2024
Currently in progress, will be updated from time to time starting 15
December

#### Abstract

In this expository work, I have currently explored the fundamentals of Symplectic Geometry, and also unraveled their local behaviour through symplectic equivalences given by Darboux-Moser-Weinstein Theory. Moreover, I have also talked about the role of closely related Contact Structures and associated Reeb vector fields. Finally, I end it by discussing the natural connections between Symplectic and Complex Geometry, with notions of Dolbeault Cohomolgy and even psuedo-holomorphic curves being touched upon. It may be noted that as of now, there has not been much exploration into the second part of this thesis: Toric Varieties/Manifolds. This is because I wanted to cover all of the fundamentals of Symplectic Geometry in depth, even if some were relatively unrelated to the study of Toric Manifolds. This will enable me to explore other directions within this exciting field in the future. That said, as far as this thesis is concerned, I will now be moving on to study Hamiltonian actions and moment maps, until eventually breaking upon the grand correspondence between Delzant Polytopes and Toric Varieties.

## Contents

1	Symplectic Structure		
	1.1	Symplectic Vector Spaces	3
	1.2	Symplectic Manifolds	4
	1.3	Lagrangian Submanifolds	5

# Chapter 1

Symplectic Structure

1.1 Symplectic Vector Spaces

## 1.2 Symplectic Manifolds

### 1.3 Lagrangian Submanifolds