

Date: May 19, 2025

Math Section 3.3

Practice Test

Name:

Class of:

Teacher:

Homeroom:

Solutions

- 1. Which option is equivalent to $\log_{16} 2$?
 - A. $\frac{\log_2 16}{\log_{16} 2}$
 - $B. \ \frac{\ln 16}{\ln 2}$
 - $C. \ \frac{4\log 2}{\log 16}$
 - $D. \ \frac{\log_7 2}{\log_7 16}$

Solution.

$$\log_{16} 2 = \frac{\ln 2}{\ln 16} = \frac{\ln 2}{\ln (2^4)} = \frac{\ln 2}{4 \ln 2} = \frac{1}{4}.$$

Change of base with any common base k gives $\log_{16} 2 = \frac{\log_k 2}{\log_k 16}$. Only choice D has that exact structure.

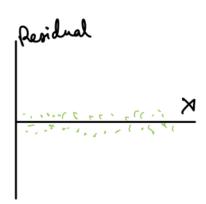
 \mathbf{D}

- 2. Mara's 6-year-old car is currently valued at \$18500. If the car depreciated at a continuous rate of 9% per year, which equation correctly represents the value C of the car when it was new?
 - A. $C = 18500(1 0.09)^6$
 - B. $C = 18500 \left(1 + \frac{0.09}{12}\right)^{72}$
 - C. $C = 18500 e^{0.54}$
 - D. $C = 18500 e^{-0.54}$

Solution. Continuous decay formula:

$$P_{\text{now}} = Ce^{-rt} \implies C = P_{\text{now}}e^{rt} = 18500 e^{0.09 \cdot 6} = 18500 e^{0.54}.$$

3. Linear regressions were constructed for four data sets, and the residual plots are shown below. Which residual plot indicates that an exponential function would be a better model for the relationship between the two variables?

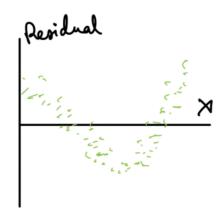


Residual

В.

D.

A.



С.

Solution. Residual Plot C displays a clear U-shape: positive residuals at low and high x, negative in the middle. Such systematic curvature means a straight line is missing multiplicative structure—typical of underlying exponential data. Plots A, B, D show no such pattern.

 \mathbf{C}

4. Solve
$$\frac{1}{2}(5^{3x-2}) = 40$$
.

A.
$$x = \log_5(\frac{8}{5}) + \frac{2}{3}$$

B.
$$x = \frac{\log_5 80 + 2}{3}$$

C.
$$x = \frac{2 - \log_5 80}{3}$$

D.
$$x = \frac{\log_2 80 - 2}{3}$$

Solution.

$$\frac{1}{2} 5^{3x-2} = 40 \implies 5^{3x-2} = 80 \implies 3x - 2 = \log_5 80 \implies x = \frac{\log_5 80 + 2}{3}.$$

5. Elena deposits \$15,000 into a savings account that compounds monthly at an annual rate of 3%.

Which function matches this scenario and provides the <u>correct</u> amount of time Elena must wait for her deposit to reach at least \$25 000?

A.
$$A(t) = 15,000 \left(1 + \frac{0.03}{12}\right)^{12t}$$
 — predicts **19** years

B.
$$A(t) = 15,000 \left(1 + \frac{0.03}{12}\right)^{12t}$$
 — predicts **18** years

C.
$$A(t) = 15,000 \left(1 + \frac{3}{12}\right)^{12t}$$
 — predicts **19** years

D.
$$A(t) = 15,000 \left(1 + \frac{3}{12}\right)^{12t}$$
 — predicts **18** years

Solution. Proper monthly-compounding model:

$$A(t) = 15\,000 \left(1 + \frac{0.03}{12}\right)^{12t}.$$

Set $A = 25\,000$:

$$\left(1 + \frac{0.03}{12}\right)^{12t} = \frac{25\,000}{15\,000} = 1.666\overline{6} \implies t = \frac{\ln(5/3)}{12\ln(1 + 0.0025)} \approx 18.8 \text{ yr}.$$

Rounded up, Elena must wait 19 years. Choice A alone uses the correct formula and states 19 years.

