

# Half Adder:

Expression:

Sum

A \ B	0	1
0	0	1
1	1	0

Carry

A \ B	0	1
0	0	0
1	0	1

$$G1 = \bar{A}B \quad G2 = A\bar{B}$$

$$X = \bar{A}B + A\bar{B}$$

$$= A \oplus B$$

$$G1 = A \cdot B$$

$$X = AB$$

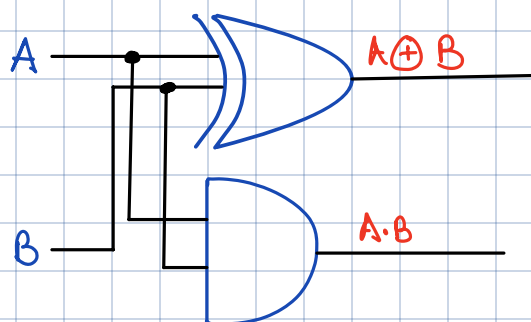
Truth table

A	B	Sum $A \oplus B$	Carry $A \cdot B$
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

$$\text{Sum: } A \oplus B$$

$$\text{Carry: } A \cdot B$$

Circuit:



Full adder

Expression:

$$\text{Sum: } A \oplus B \oplus C_{in}$$

$$\text{Carry: } A \cdot B + (A \oplus B) \cdot C_{in}$$

Truth table

Sum

AB \ C <sub>in</sub>	0	1
00	0	1
01	1	0
11	0	1
10	1	0

$$G1 = \bar{A}\bar{B}C_{in}$$

$$G2 = \bar{A}B\bar{C}_{in}$$

$$G3 = AB\bar{C}_{in}$$

$$G4 = A\bar{B}C_{in}$$

A	B	C <sub>in</sub>	$A \oplus B \oplus C_{in}$	$A \cdot B + (A \oplus B) \cdot C_{in}$
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

$$X = \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + AB\bar{C}_{in} + A\bar{B}C_{in}$$

$$= \bar{C}_{in}(\bar{A}B + A\bar{B}) + C_{in}(AB + \bar{A}\bar{B})$$

$$\text{Let } X = \overline{A}B + A\overline{B}$$

$$= \overline{C_{in}} X + C_{in} \overline{X}$$

$$= C_{in} \oplus X$$

$$= C_{in} \oplus (\overline{A} \oplus \overline{B})$$

Carry

AB \ C <sub>in</sub>	0	1
00	0	0
01	0	1
11	1	1
10	0	1

$$G1 = BC_{in}$$

$$G2 = AB$$

$$G3 = C_{in} A$$

$$X = AB + AC_{in} + BC_{in}$$

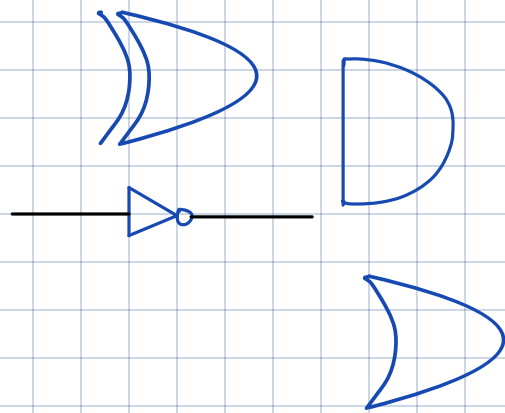
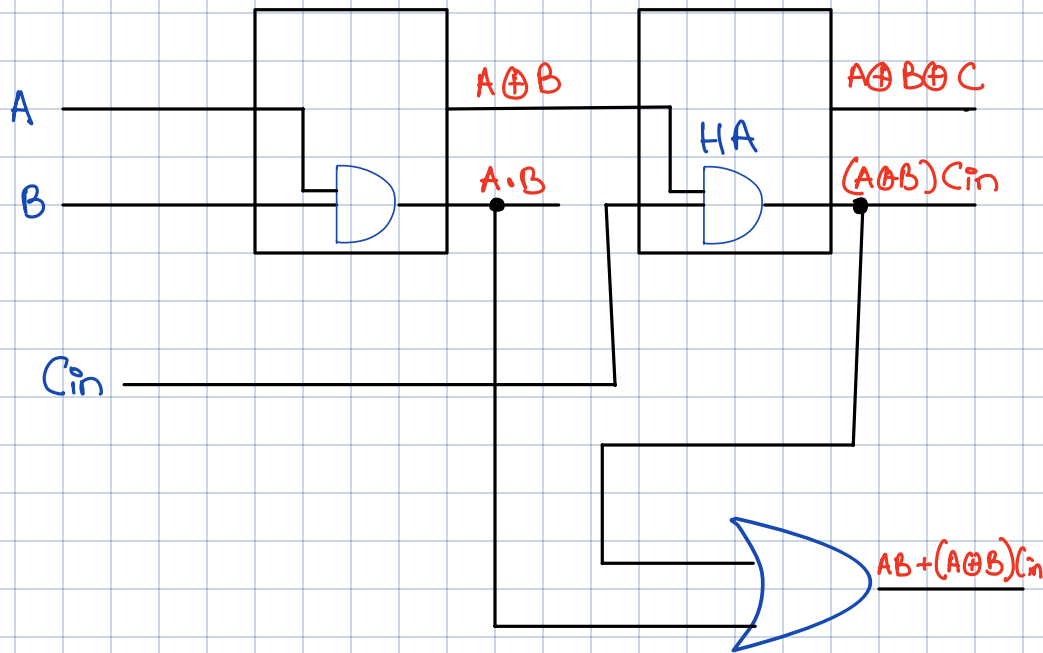
$$= AB + AC_{in}(B + \overline{B}) + BC_{in}(A + \overline{A})$$

$$= AB + ABC_{in} + \overline{A}BC_{in} + ABC_{in} + \overline{A}BC_{in}$$

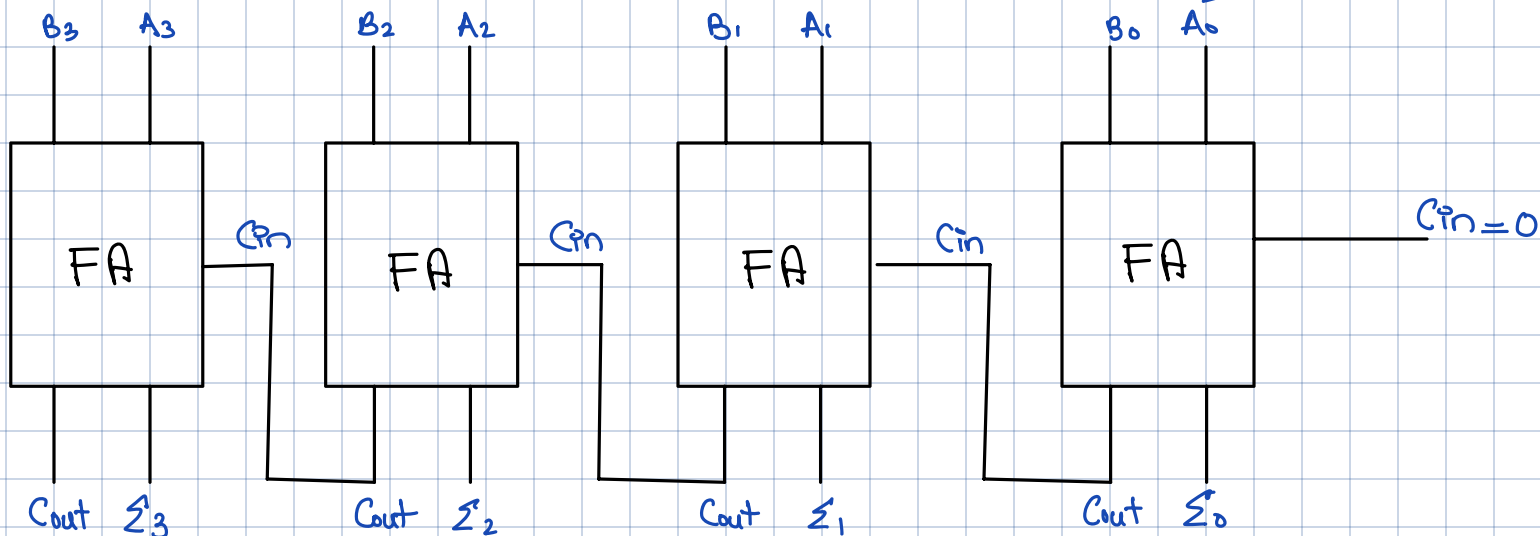
$$= AB + ABC_{in} + \overline{A}BC_{in} + \overline{A}BC_{in}$$

$$= AB(1 + C_{in}) + C_{in}(\overline{A}B + \overline{A}B)$$

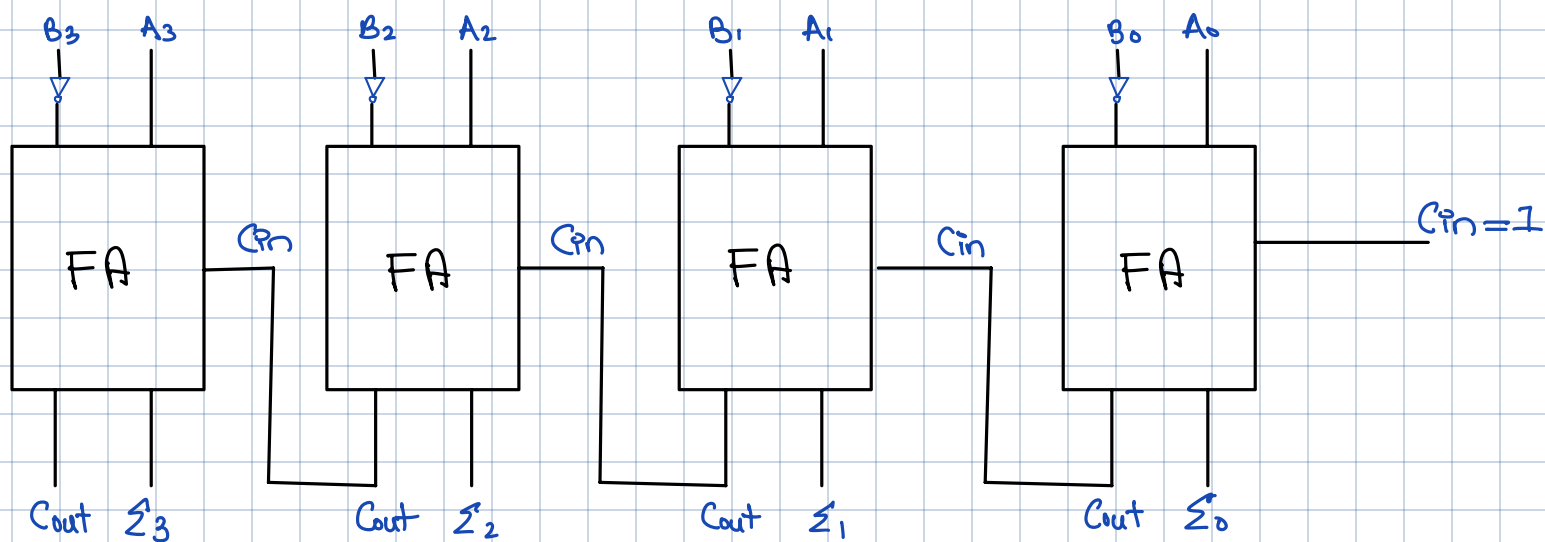
$$= AB + (A \oplus B)C_{in}$$



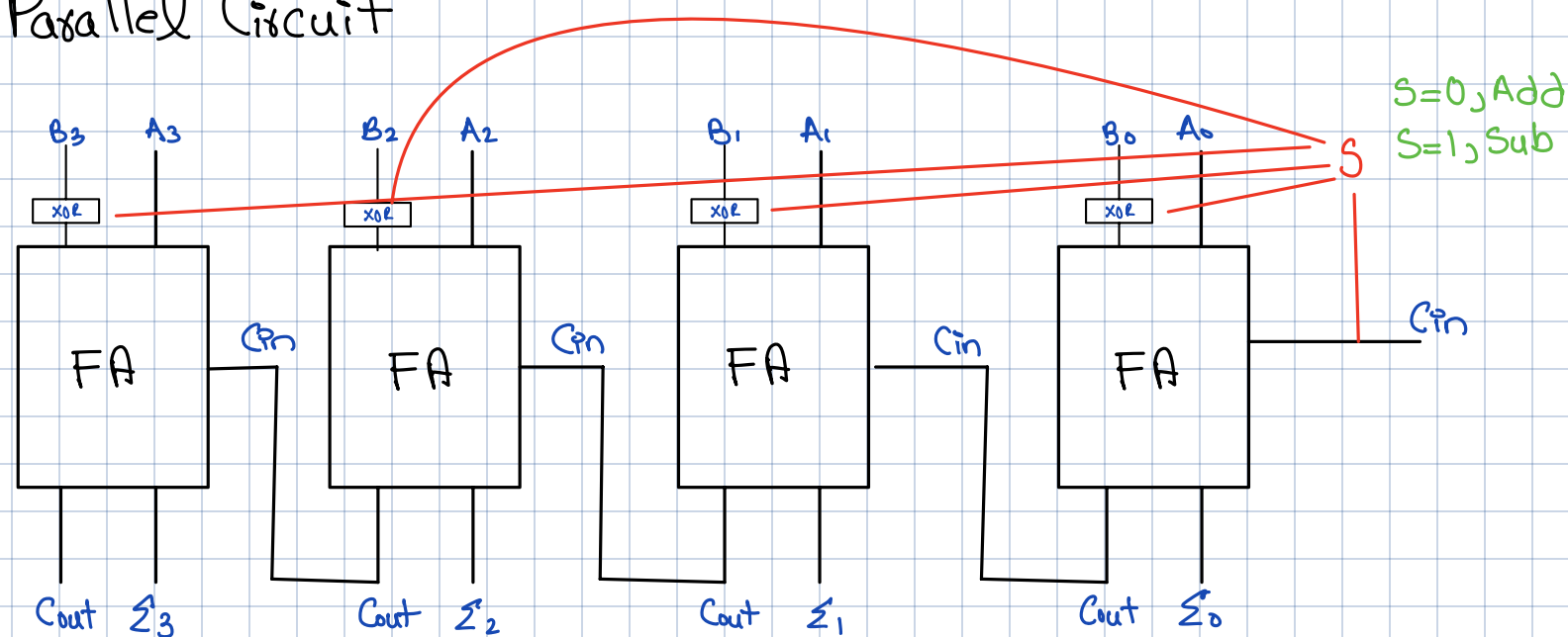
4 bit Adder



## 4-bit subtractor



## Parallel Circuit



Decodes -  $2 \times 4$

Expression:

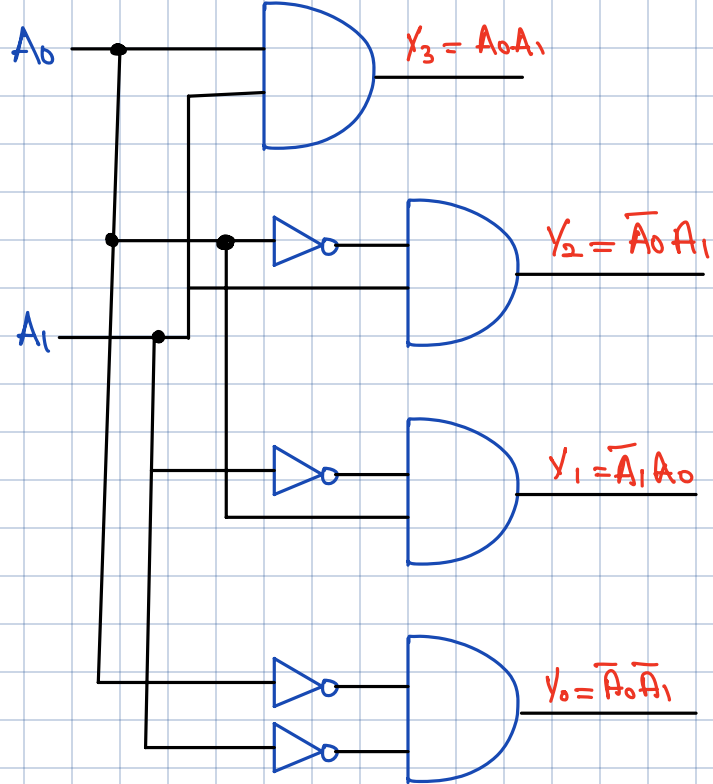
$$Y_0 = \overline{A_1} \overline{A_0} \quad Y_2 = A_1 \overline{A_0}$$

$$Y_1 = \overline{A_1} A_0 \quad Y_3 = A_1 A_0$$

Circuit:

### Truth table

$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	0	1
0	1	0	0	1	0
1	0	0	1	0	0
1	1	1	0	0	0



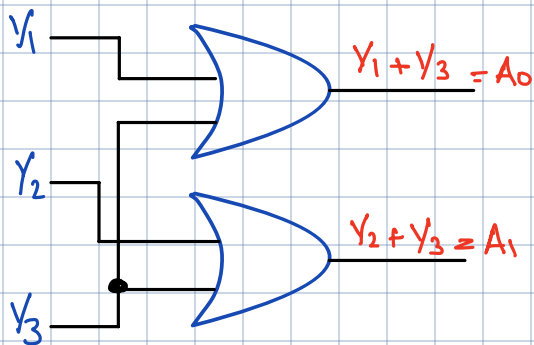
Encoder: - 4 x 2

Expression:

$$A_0 = Y_1 + Y_3$$

$$A_1 = Y_2 + Y_3$$

Circuit



Truth table

$Y_3$	$Y_2$	$Y_1$	$Y_0$	$A_1$	$A_0$
0	0	0	1	0	0
0	0	1	0	0	1
0	1	0	0	1	0
1	0	0	0	1	1

Truth table

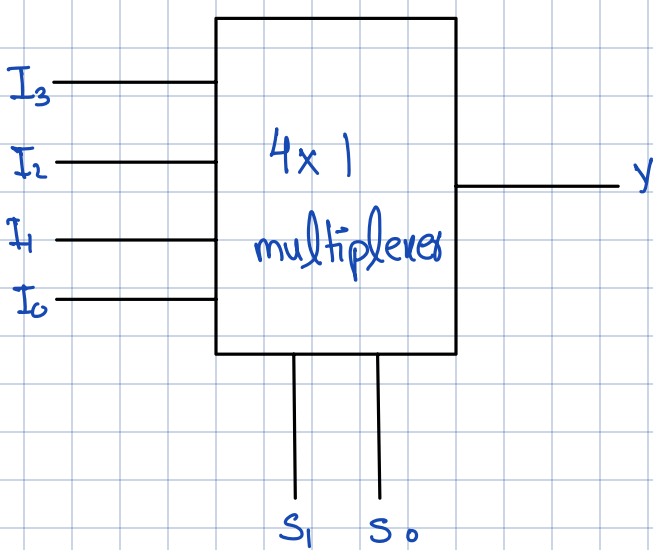
$I_3$	$I_2$	$I_1$	$I_0$	$S_1$	$S_0$	$Y$
			1	0	0	$I_0$
		1		0	1	$I_1$
	1			1	0	$I_2$
1				1	1	$I_3$

Multiplexer

Expression:

$$Y = \bar{S}_1\bar{S}_0I_0 + \bar{S}_1S_0I_1 + S_1\bar{S}_0I_2 + S_1S_0I_3$$

Circuit:



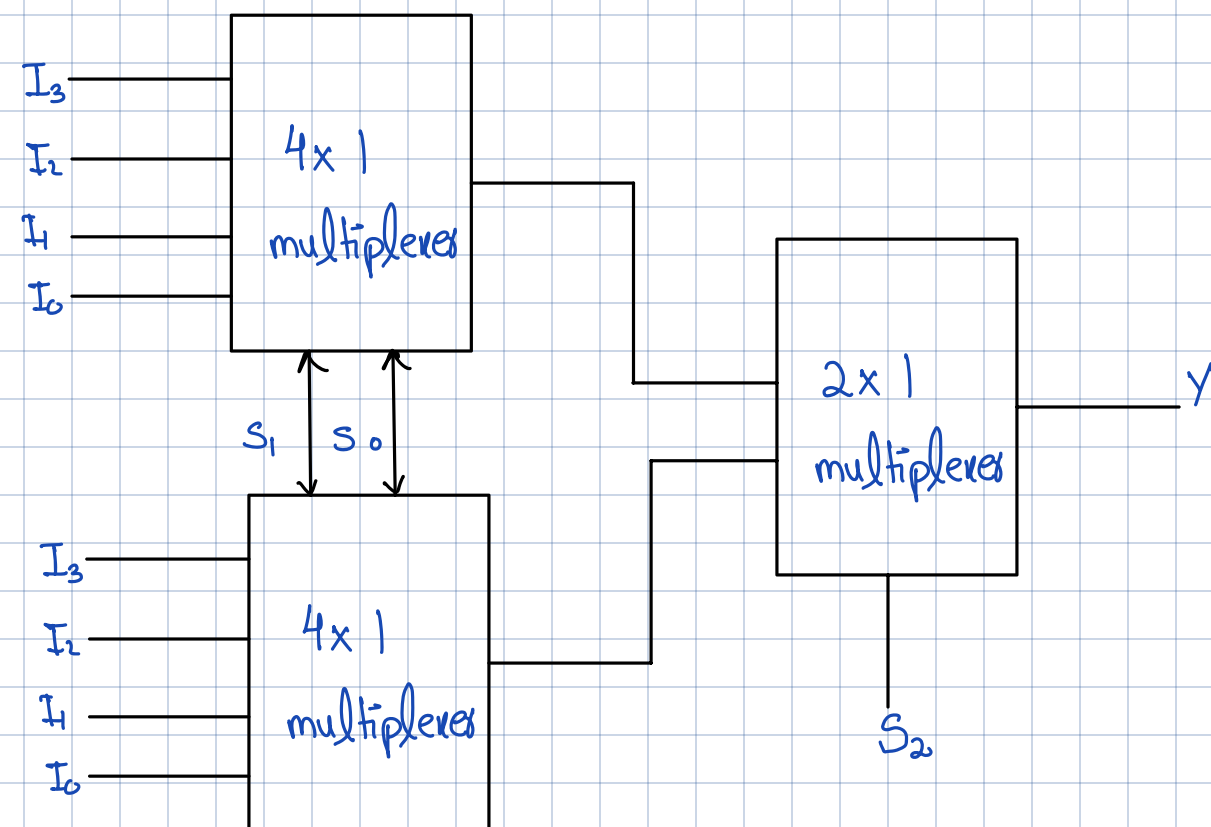
Truth table

Expression:

$$Y = \bar{S}_2 \bar{S}_1 \bar{S}_0 I_0 + \bar{S}_2 \bar{S}_1 S_0 I_1 + \bar{S}_2 S_1 \bar{S}_0 I_2 + \bar{S}_2 S_1 S_0 I_3 + S_2 \bar{S}_1 \bar{S}_0 I_4 + S_2 \bar{S}_1 S_0 I_5 + S_2 S_1 \bar{S}_0 I_6 + S_2 S_1 S_0 I_7$$

	$I_7$	$I_6$	$I_5$	$I_4$	$I_3$	$I_2$	$I_1$	$I_0$	$S_2$	$S_1$	$S_0$	$y$
								1	0	0	0	$I_0$
							1		0	0	1	$I_1$
						1			0	1	0	$I_2$
					1				0	1	1	$I_3$
				1					1	0	0	$I_4$
			1						1	0	1	$I_5$
		1							1	1	0	$I_6$
	1								1	1	1	$I_7$

Circuit.



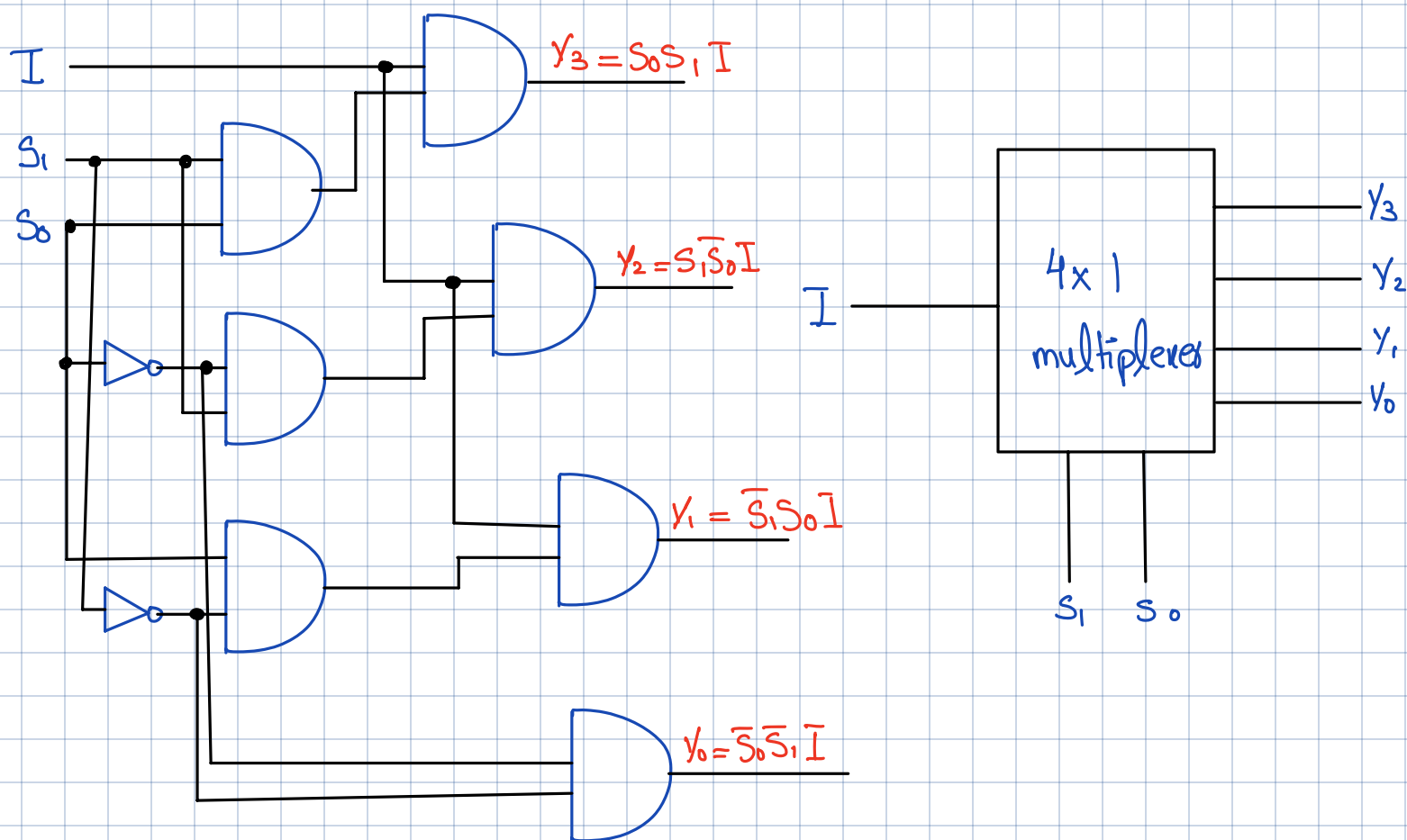
# De-Multiplexers

## Expression

$$Y_3 = S_1 S_0 I \quad Y_1 = \bar{S}_1 S_0 I$$

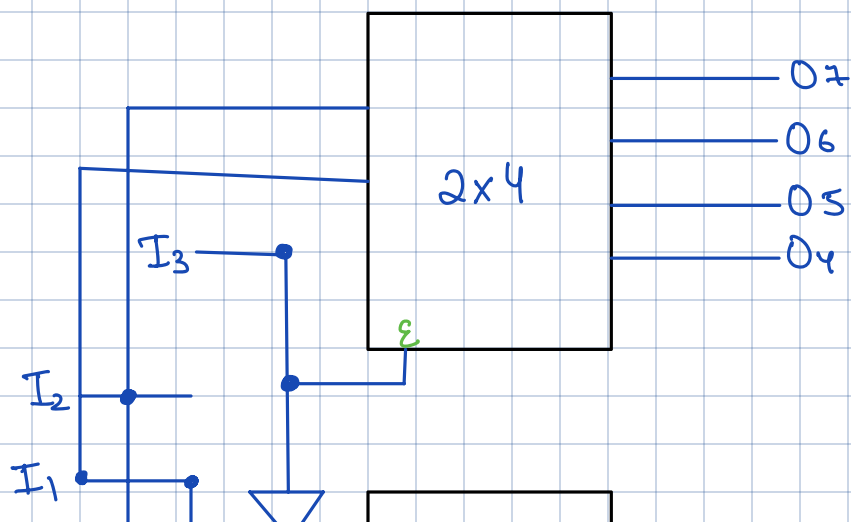
$$Y_2 = S_1 \bar{S}_0 I \quad Y_0 = \bar{S}_1 \bar{S}_0 I$$

## Circuit:



## Decoders:

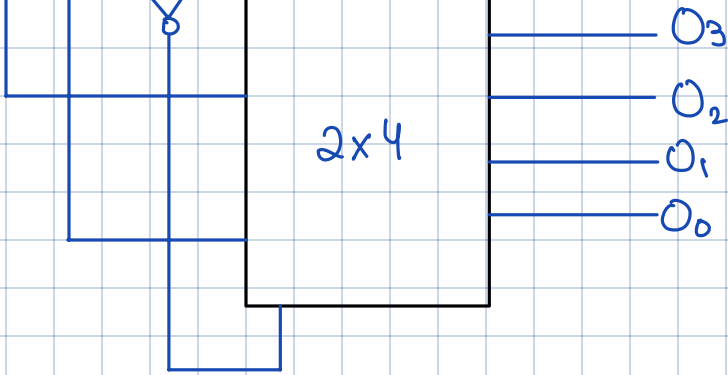
3x8 using 2x4



## Truth table

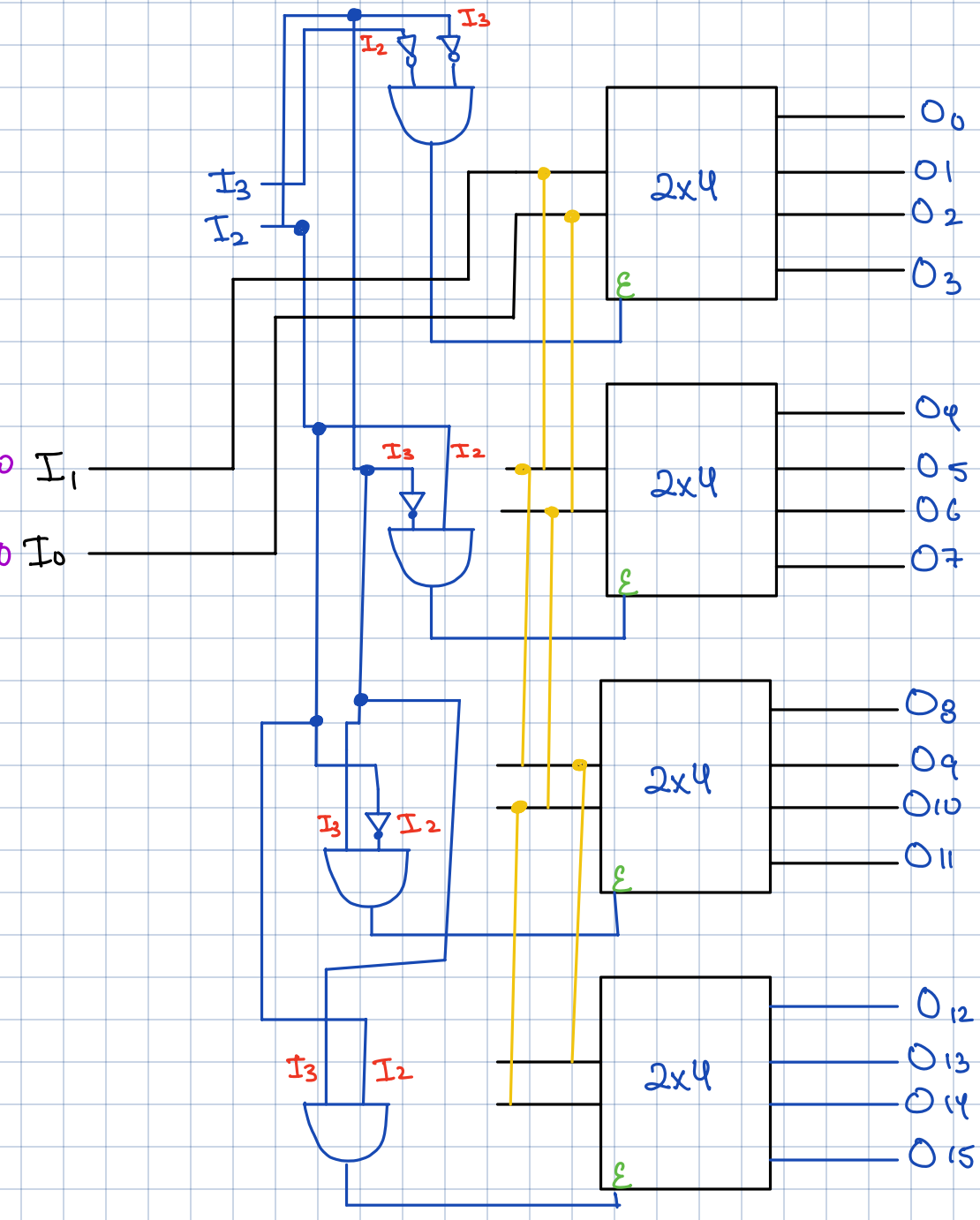
$I$	$S_1$	$S_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0				0
0	0	1			0	
0	1	0		0		
0	1	1	0			

$I_3$	$I_2$	$I_1$
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1

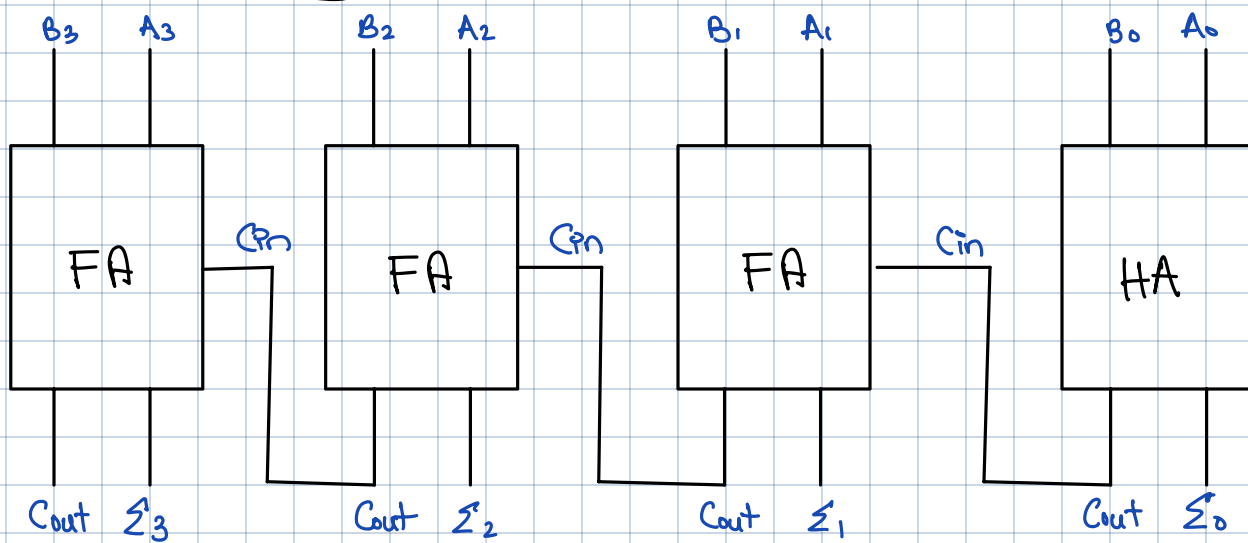


4x16 using 2x4

	$I_3$	$I_2$	$I_1$	$I_0$
0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
	0	1	0	1
	0	1	1	0
	0	1	1	1
	1	0	0	0
	1	0	0	1
	1	0	1	0
	1	0	1	1
	1	1	0	0
	1	1	0	1
	1	1	1	0
	1	1	1	1



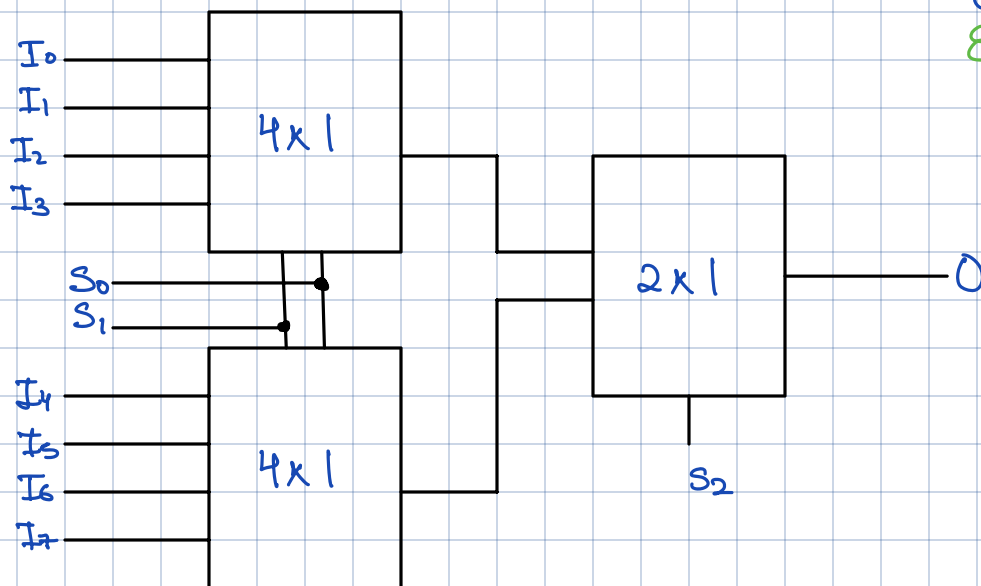
4 bit adder using half adder:



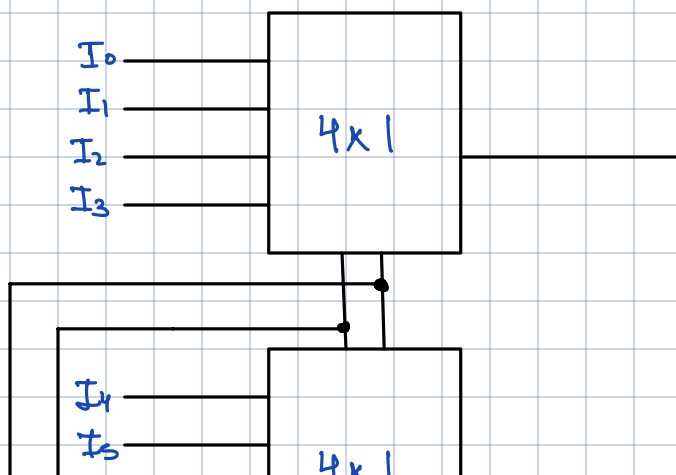
Multiplexers:

8x1 mux using 4x1

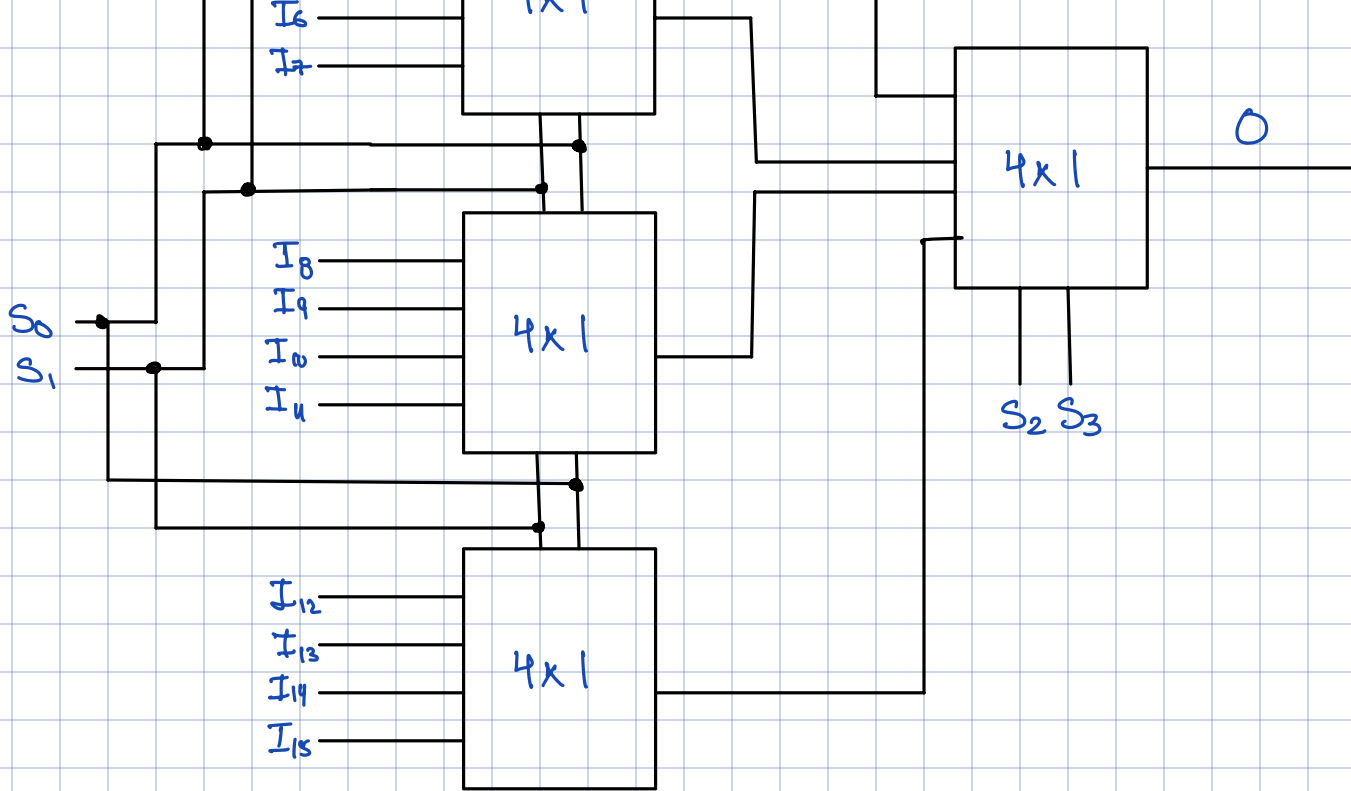
$$\begin{array}{r} 0011 \\ 0001 \\ \hline 0010 \\ \text{E}_2 \text{ E}_1 \text{ E}_0 \end{array}$$



16x1 mux using 4x1

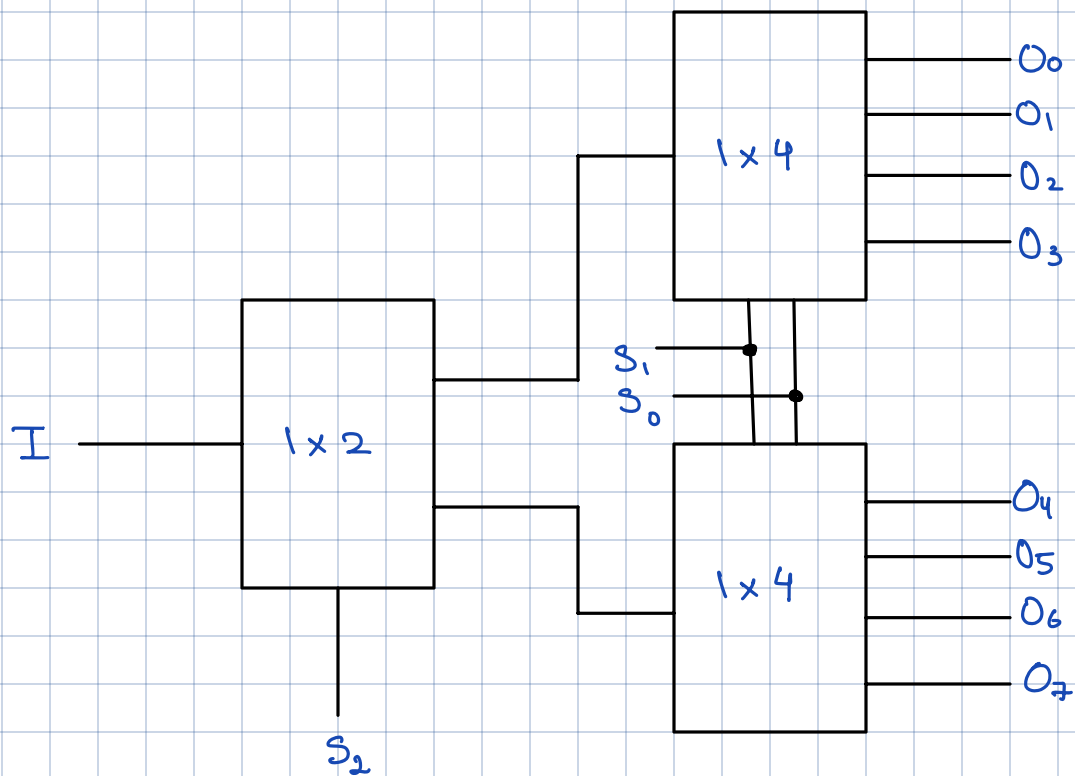




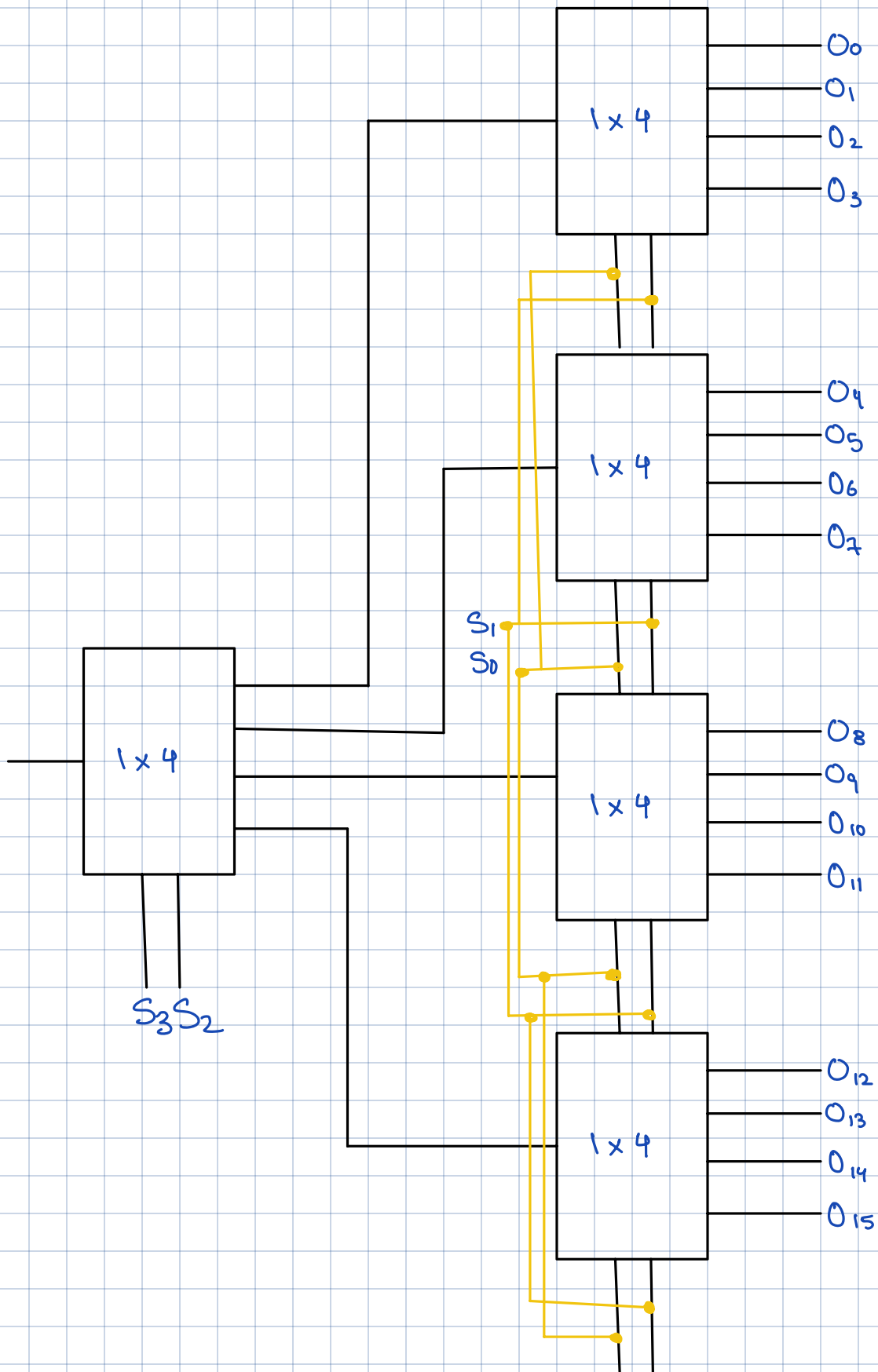


De-Multiplexers:

1x8 DeMux using 1x4



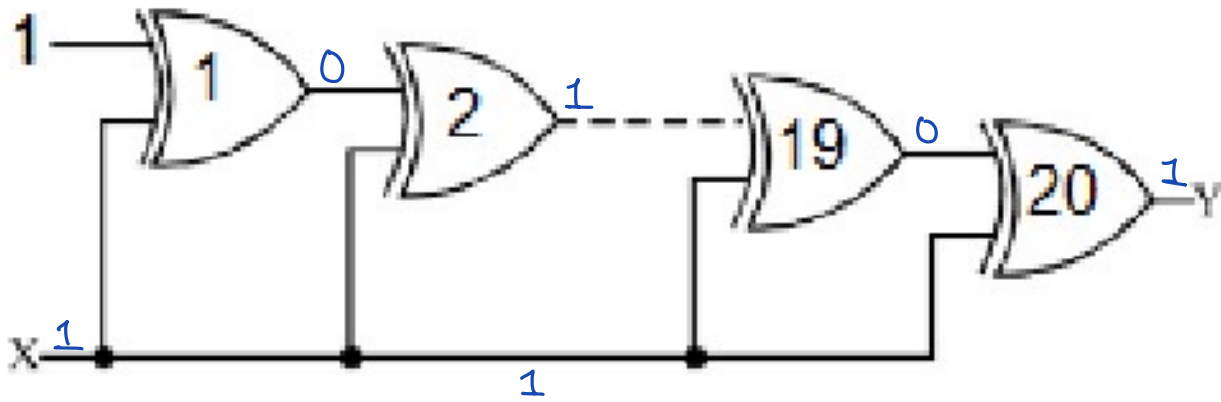
16x1 DeMux using 4x1 DeMux



Mid 2021

Section: 01

Q1.



X	Y
0	0
1	1

Q<sub>2</sub>.

ii)

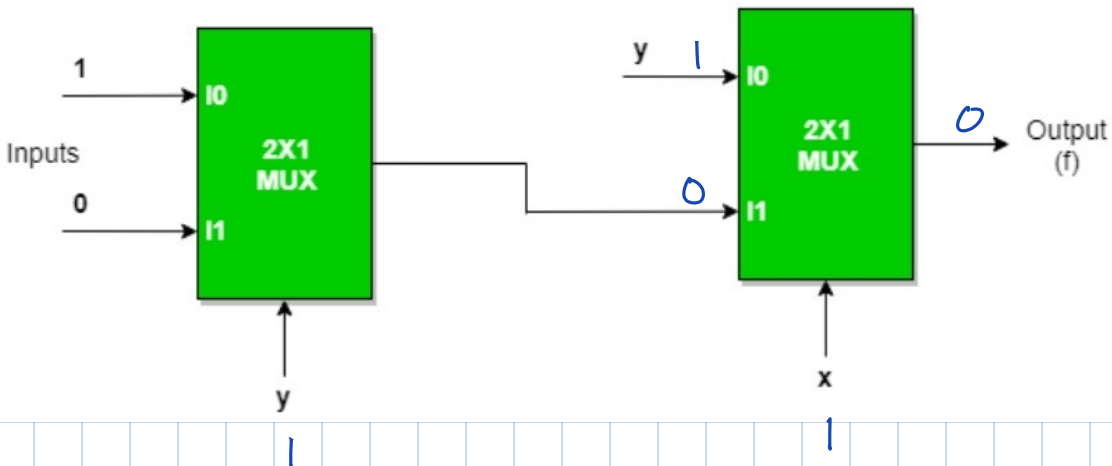
2	254	
2	127	0
2	63	1
2	31	1
2	15	1
2	7	1
2	3	1
2	1	1

i)

$$\begin{array}{r}
 01111110 \\
 + \quad \quad \quad 10000001 \\
 \hline
 100000010
 \end{array}$$

01111110

Q<sub>3</sub>.



x	y	f
0	0	0
0	1	1
1	0	1
1	1	0

x \ y	0	1
0	0	1
1	1	0

$$A1 = \overline{x}y$$

$$A2 = x\overline{y}$$

$$f = \overline{x}y + x\overline{y}$$

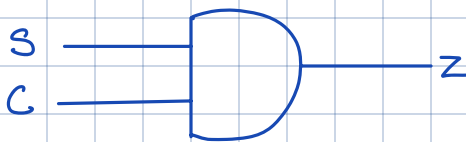
$$= x \oplus y$$

Q4.

S	C	Z
0	0	0
0	1	0
1	0	0
1	1	1

x \ y	0	1
0	0	0
1	0	1

$$Z = SC$$



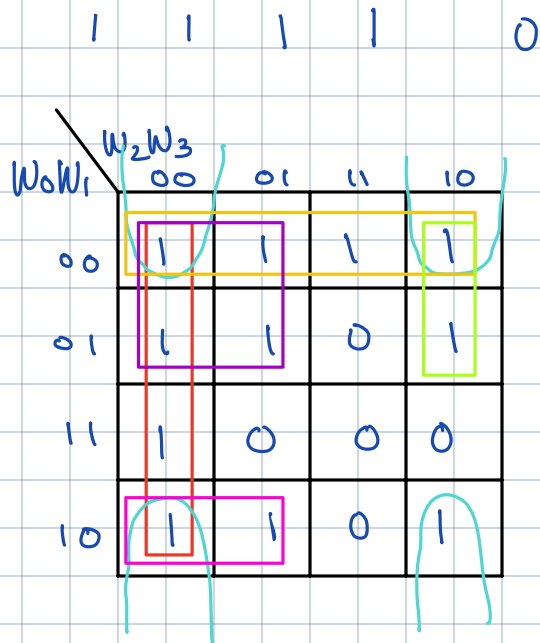
Section: 02

Q1.

No	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	A
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0

wheel break = 0  
wheel work = 1

Alarm work = 1  
Alarm Stop = 0



$$h5 = \overline{W_0} \overline{W_2}$$

$$h6 = \overline{W_0} W_2 \overline{W_3}$$

$$h7 = \overline{W_0} \overline{W_1}$$

$$h2 = \overline{W_2} \overline{W_3}$$

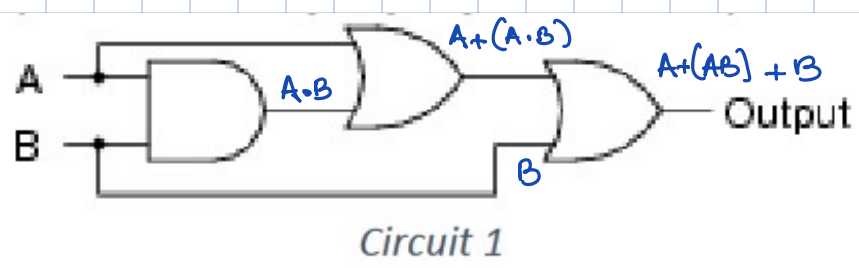
$$h3 = \overline{W_1} \overline{W_3}$$

$$h4 = \overline{W_1} W_0 \overline{W_2}$$

$$A = \overline{W_0} \overline{W_3} W_2 + \overline{W_0} W_2 + \overline{W_0} W_3 + \overline{W_2} \overline{W_3} + \overline{W_1} \overline{W_3} + W_0 \overline{W_1} \overline{W_2}$$

Q2.

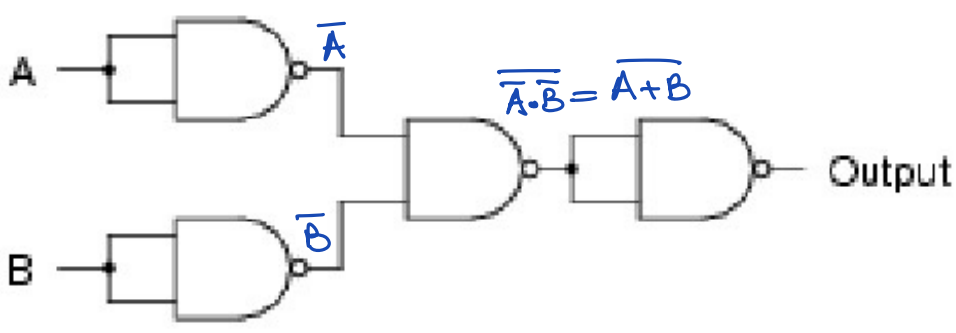
A.



$$A + AB + B$$

$$A(1 + B) + B$$

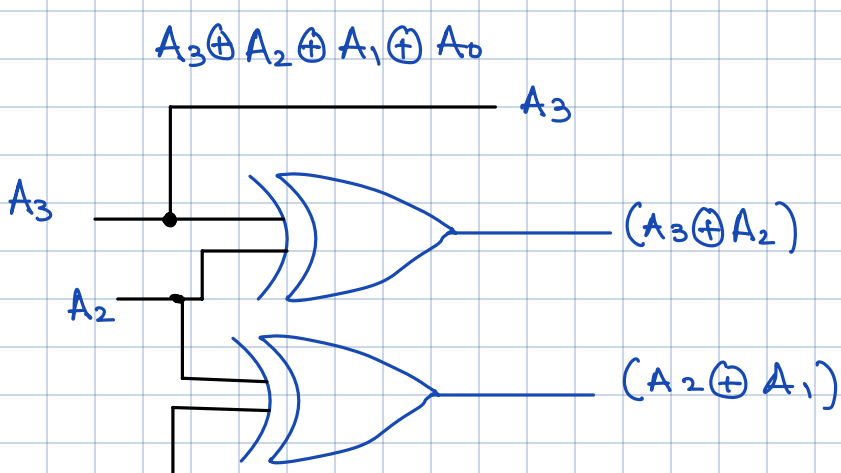
$$A + B$$

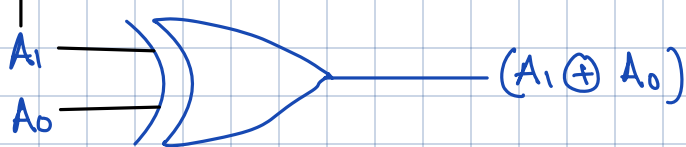


$$\overline{A + B} = \overline{A} \overline{B}$$

$$\overline{\overline{A} + \overline{B}} = \overline{\overline{A + B}}$$

B:





Q3.

	x	y	z	A	B	C	
0	0	0	0	0	0	1	1
1	0	0	1	0	1	0	2
2	0	1	0	0	1	1	3
3	0	1	1	1	0	0	4
4	1	0	0	0	1	1	3
5	1	0	1	1	0	0	4
6	1	1	0	1	0	1	5
7	1	1	1	1	1	0	6

For A:

xy \ z	0	1
00	0	0
01	0	1
11	1	1
10	0	1

$$A1 = yz$$

$$A2 = xz$$

$$A3 = xy$$

$$A = xy + yz + xz$$

For B:

xy \ z	0	1
00	0	1
01	1	0
11	0	1
10	1	0

$$A1 = \bar{x}\bar{y}z$$

$$A2 = \bar{x}y\bar{z}$$

$$A3 = xyz$$

$$A4 = x\bar{y}\bar{z}$$

$$B = \bar{x}\bar{y}z + \bar{x}y\bar{z} + xyz + x\bar{y}\bar{z}$$

For C:

xy \ z	0	1
00	1	0
01	1	0
11	1	0
10	1	0

$$A1 = \bar{z}$$

$$C = \bar{z}$$

Fall 2022

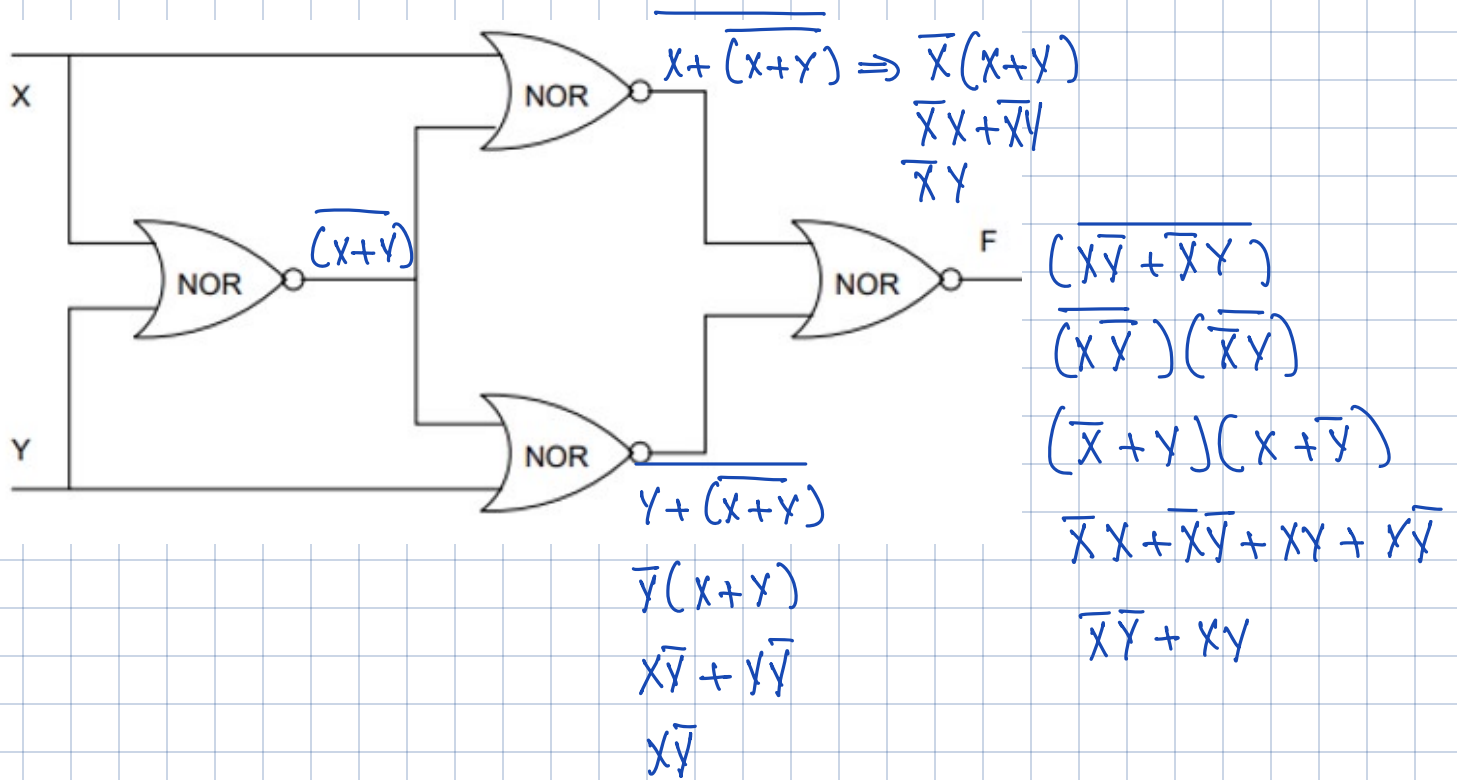
Section 01:

Q1.

$x_3$	$x_2$	$x_1$	$x_0$	ODD	EVEN	tev	-ev
0	0	0	0	0	1	1	0
0	0	0	1	1	0	1	0
0	0	1	0	0	1	1	0
0	0	1	1	1	0	1	0
0	1	0	0	0	1	1	0
0	1	0	1	1	0	1	0
0	1	1	0	0	1	1	0
0	1	1	1	1	0	1	0
1	0	0	0	0	1	0	1

1	0	1	1	1	0	0	1
1	0	0	0	0	1	0	1
1	0	0	1	1	0	0	1
1	1	1	0	0	1	0	1
1	1	1	1	1	0	0	1
1	1	0	0	0	1	0	1
1	1	0	1	1	0	0	1

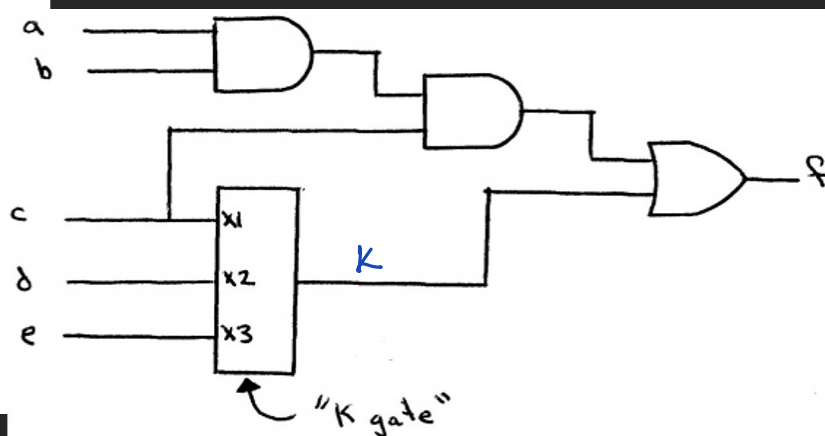
Q3.



Q5.

Truth table for the "K gate":

X1	X2	X3	K
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

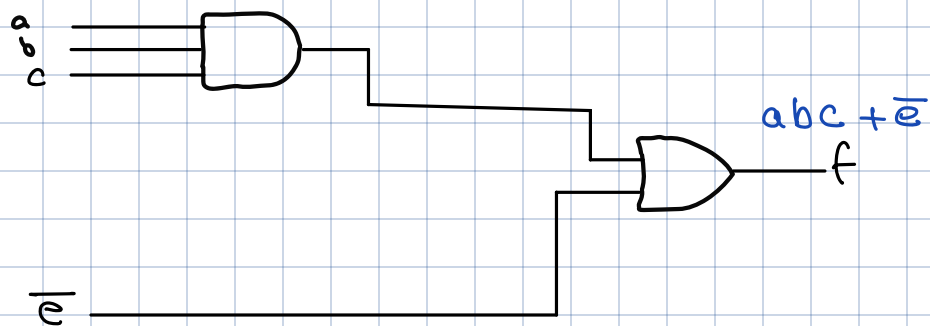


For K:

X1X2 \ X3	0	1
00	1	0
01	1	0
11	1	0
10	1	0

$$K3 = \overline{X_3}$$

$$K = \overline{X_3}$$



$a$	$b$	$c$	$\bar{e}$	$abc + \bar{e}$
0	0	0	1	1
0	0	0	0	0
0	0	1	1	1
0	0	1	0	0
0	1	0	1	1
0	1	0	0	0
0	1	1	1	1
0	1	1	0	0
1	0	0	1	1
1	0	0	0	0
1	0	1	1	1
1	0	1	0	0
1	1	0	1	1
1	1	0	0	0
1	1	1	1	1
1	1	1	0	1

$ab \backslash ce$	00	01	11	10
00	1	0	0	1
01	1	0	0	1
11	1	0	1	1
10	1	0	0	1

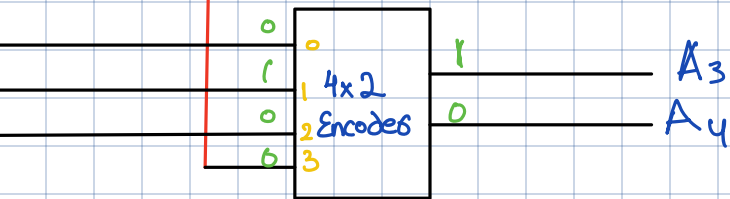
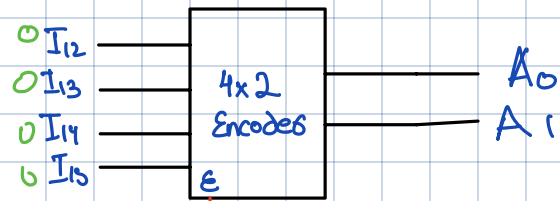
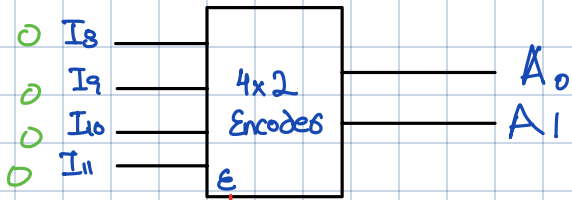
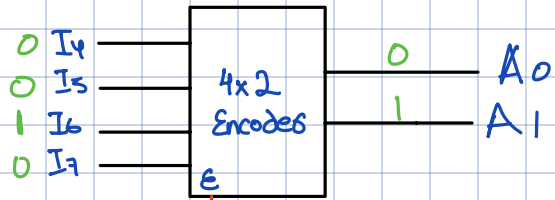
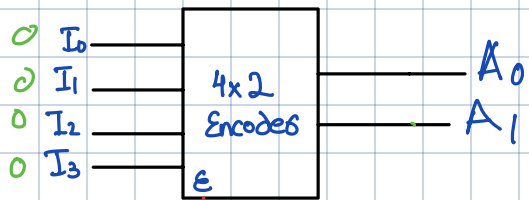
$$K1 = \bar{e}$$

$$K2 = abc$$

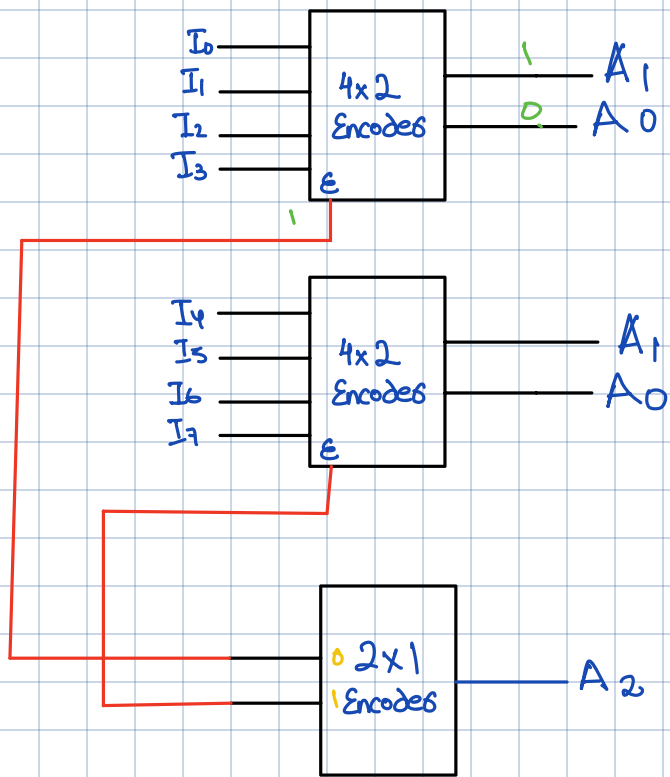
$$abc + \bar{e}$$

16 x 4 Encoders using 4 x 2 encoders





8x3 encoder using 4x2 encoder



$A_2$	$A_1$	$A_0$
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1