
Software Engineering

(CSE 355)

Lecture 9

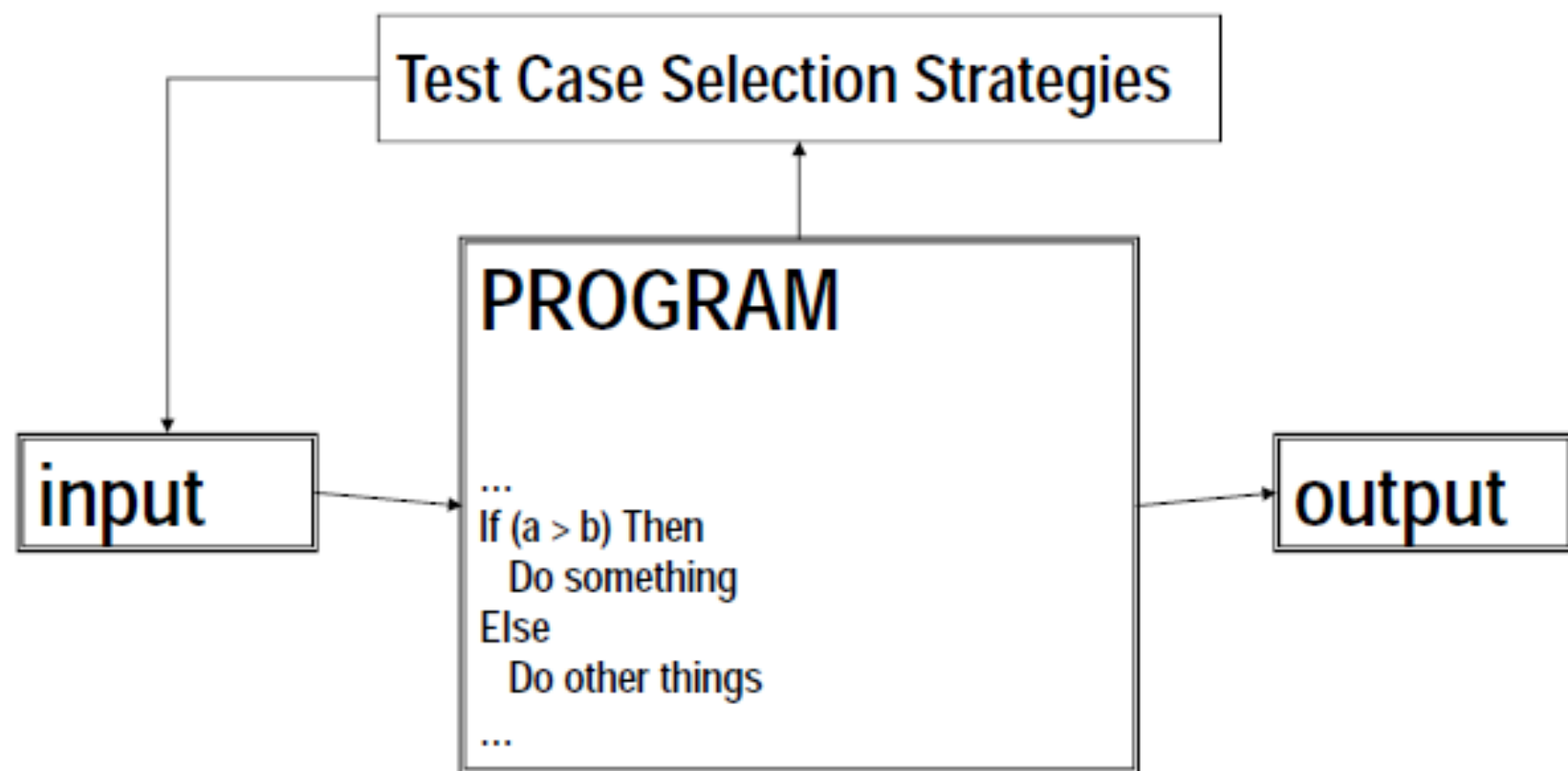
(White Box Testing)

White Box Testing

White Box Testing: Introduction

- Test Engineers have access to the source code.
 - Typical at the Unit Test level as the programmers have knowledge of the internal logic of code.
 - Tests are based on coverage of:
 - Code statements;
 - Branches;
 - Paths;
 - Conditions.
 - Most of the testing techniques are based on *Control Flow Graph* (denoted as CFG) of a code fragment.
-

White Box Testing – A common view



Control Flow Graph: Introduction

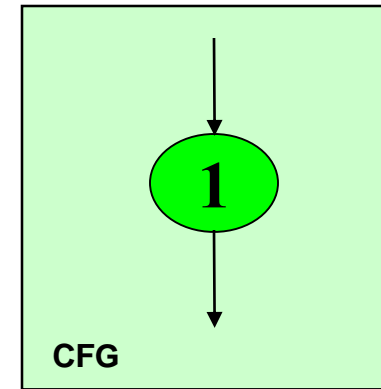
- An abstract representation of a structured program/function/method.
 - Consists of two major components:
 - **Node:**
 - Represents a stretch of sequential code statements with no branches.
 - **Directed Edge** (also called *arc*):
 - Represents a branch, alternative path in execution.
 - Path:
 - A collection of *Nodes* linked with *Directed Edges*.
-

Simple Examples

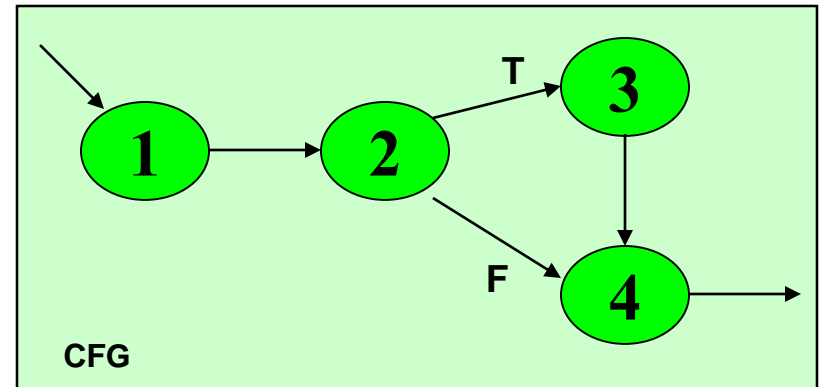
```
int a;  
float b;  
printf("Hello World");  
scanf("%d", &a);
```

```
Statement1;  
Statement2;  
Statement3;  
Statement4;
```

Can be
represented as
one node as there
is no branch.



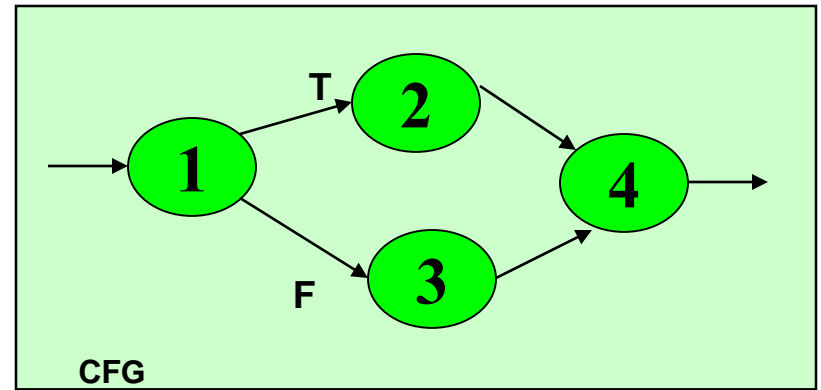
```
Statement1;  
Statement2; 1  
  
if X < 10 then 2  
    Statement3; 3  
  
Statement4; 4
```



More Examples

```
if X > 0 then  
    Statement1;  
else  
    Statement2;
```

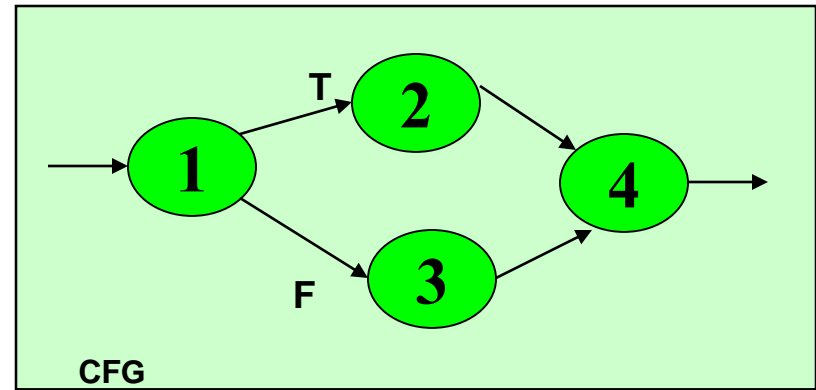
1
2
3



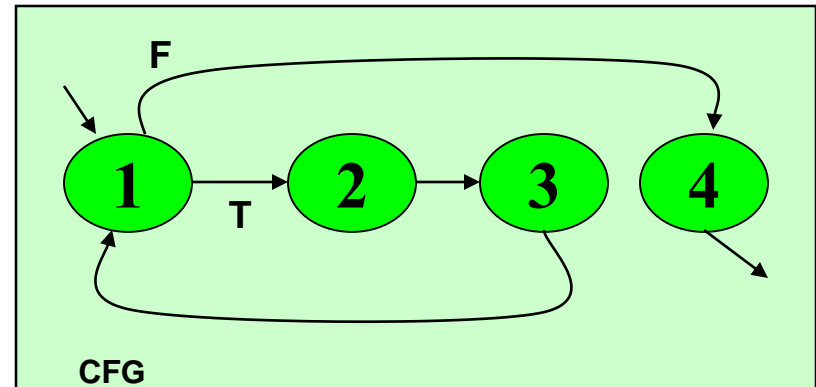
More Examples

```
if X > 0 then  
    Statement1;  
else  
    Statement2;
```

1
2
3



```
while X < 10 {  
    Statement1;  
    X++; }  
1  
2  
3
```

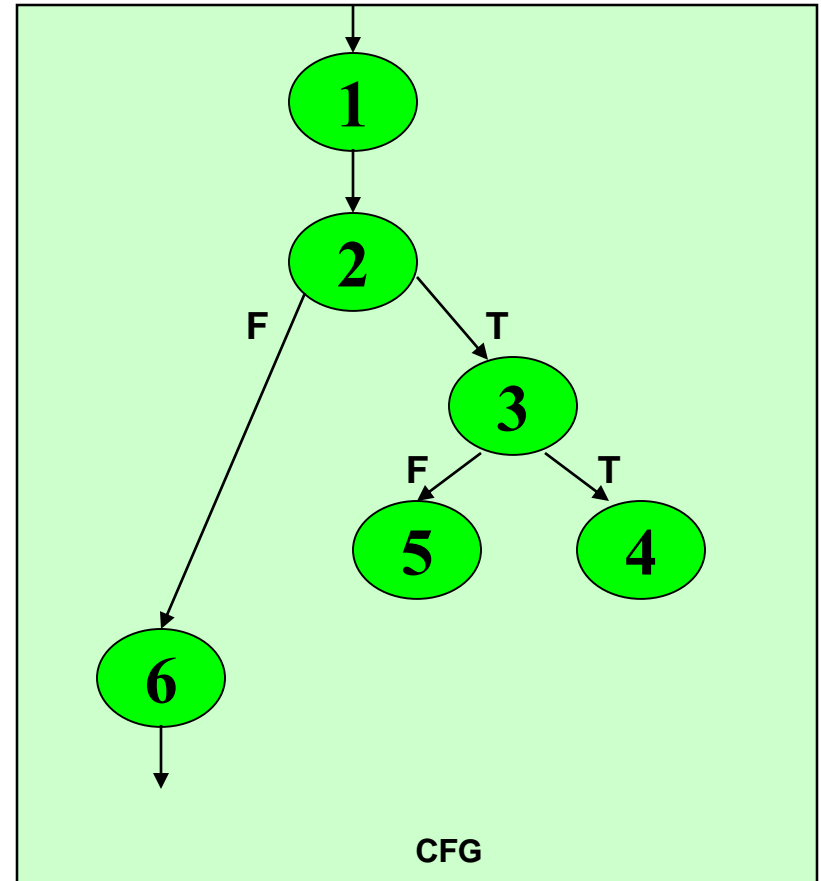
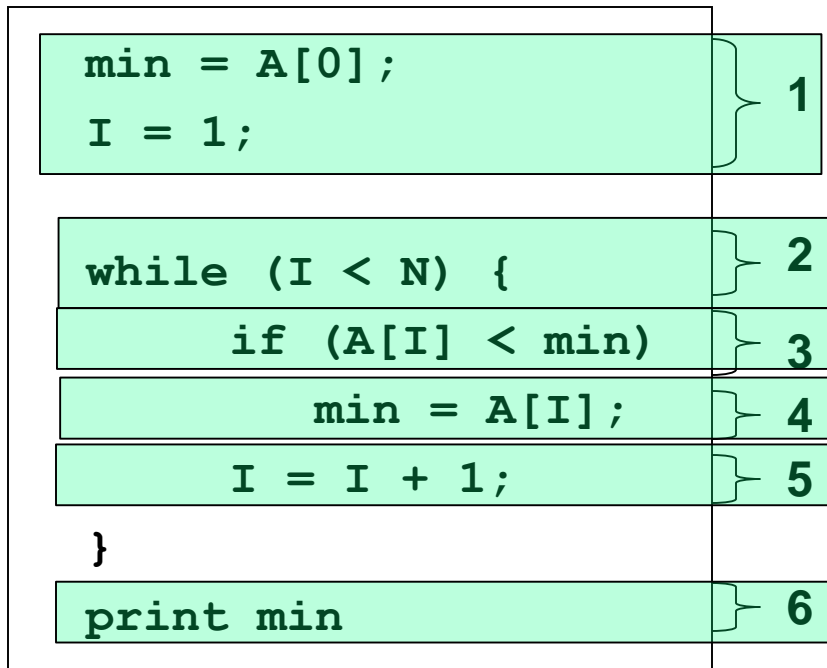


Question: Why is there a node 4 in both CFGs?

Notation Guide for CFG

- A CFG should have:
 - 1 entry arc (known as a directed edge, too).
 - 1 exit arc.
- All nodes should have:
 - At least 1 entry arc.
 - At least 1 exit arc.
- **A Logical Node** that does not represent any actual statements can be added as a joining point for several incoming edges.
 - Represents a logical closure.
 - Example:
 - Node 4 in the `if-then-else` example from previous slide.

Example: Minimum Element

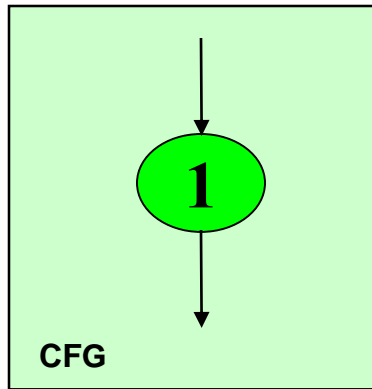


Note: The CFG is **INCOMPLETE**. Try to complete it

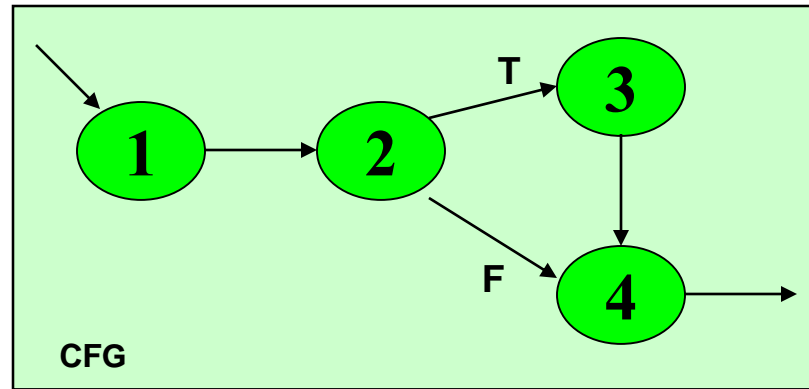
Number of Paths through CFG

- Given a program, how do we exercise all statements and branches at least once?
- Translating the program into a CFG, an equivalent question is:
 - Given a CFG, how do we cover all arcs and nodes at least once?
- Since a path is a trail of nodes linked by arcs, this is similar to ask:
 - Given a CFG, what is the set of paths that can cover all arcs and nodes?

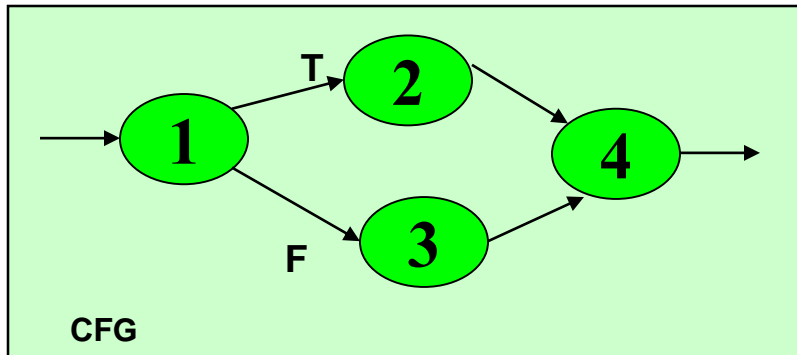
Example



- Only **one** path is needed:
 - [1]



- **Two** paths are needed:
 - [1 - 2 - 4]
 - [1 - 2 - 3 - 4]



- **Two** paths are needed:
 - [1 - 2 - 4]
 - [1 - 3 - 4]

White Box Testing: Path Based

- A generalized technique to find out the number of paths needed (known as *cyclomatic complexity*) to cover all arcs and nodes in CFG.
- Steps:
 1. Draw the CFG for the code fragment.
 2. Compute the *cyclomatic complexity number* **C**, for the CFG.
 3. Find at most **C** paths that cover the nodes and arcs in a CFG, also known as **Basic Paths Set**;
 4. Design test cases to force execution along paths in the **Basic Paths Set**.

Path Based Testing: Step 1

```
min = A[0];
```

```
I = 1;
```

```
while (I < N) {
```

```
    if (A[I] < min)
```

```
        min = A[I];
```

```
    I = I + 1;
```

```
}
```

```
print min
```

1

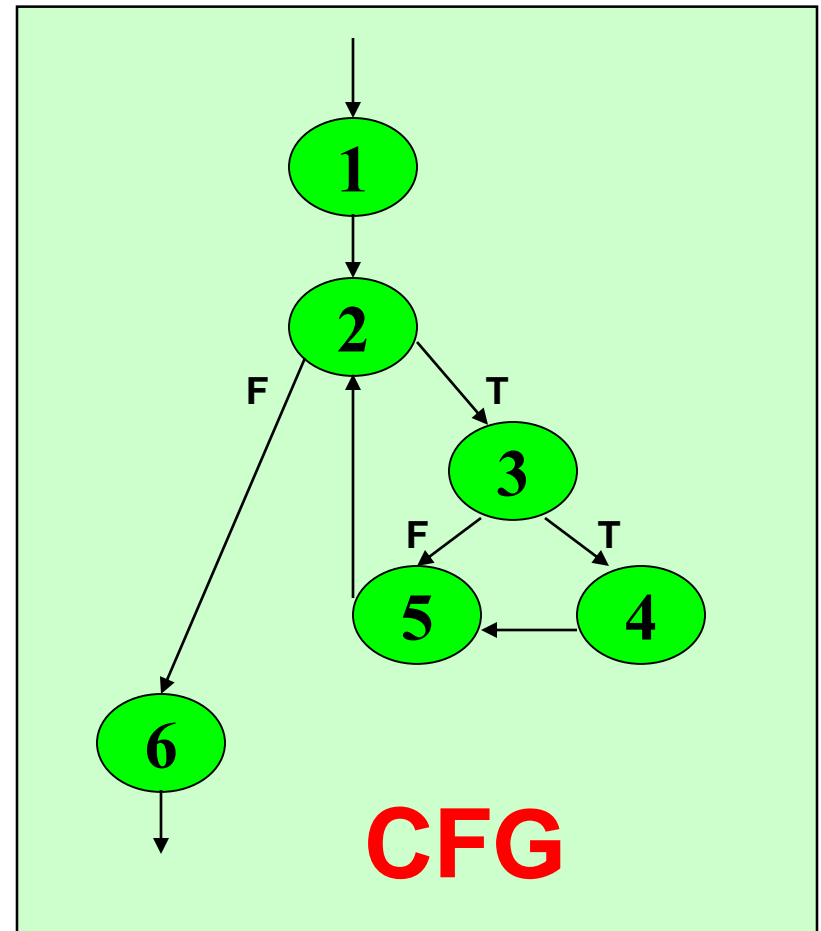
2

3

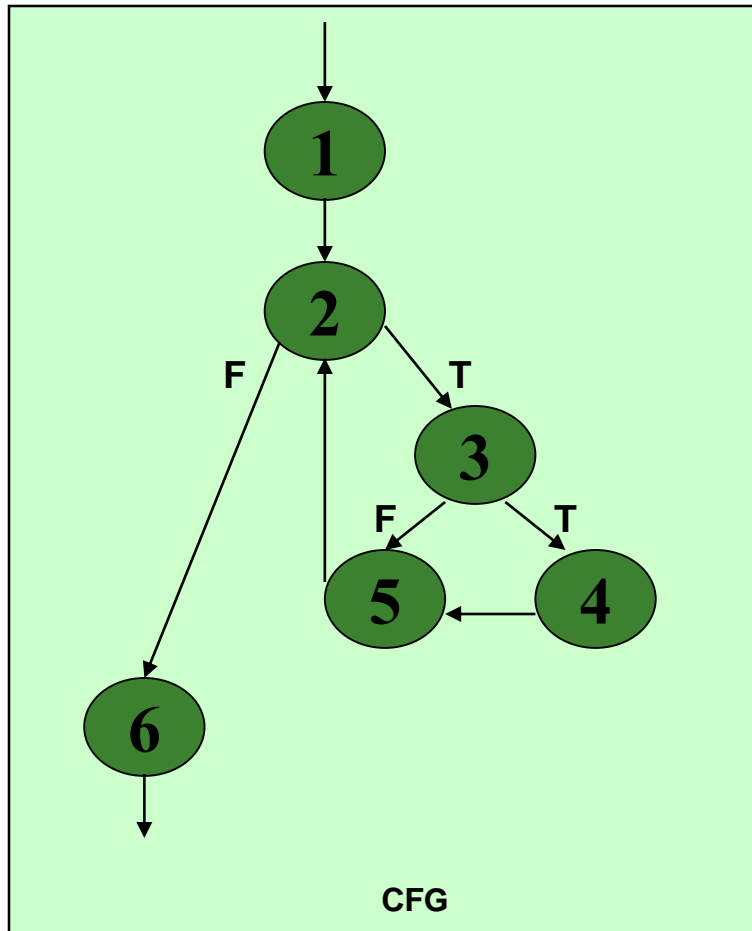
4

5

6

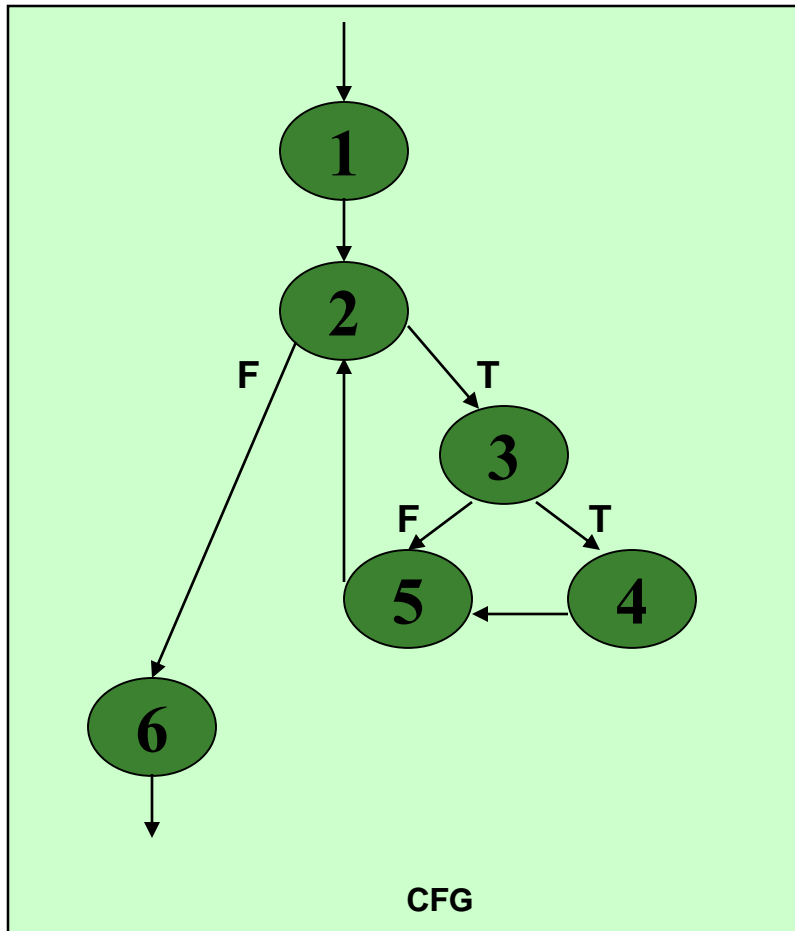


Path Base Testing: Step 2



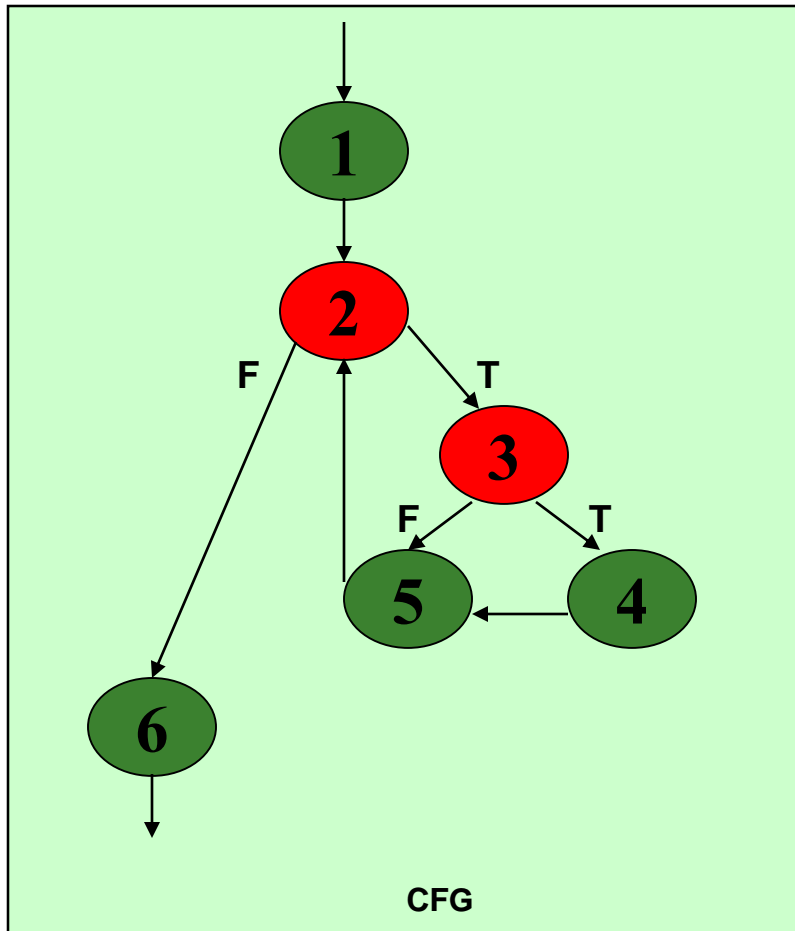
- Cyclomatic complexity =
 - The number of 'regions' in the graph; OR
 - The number of predicates + 1.

Path Base Testing: Step 2



- **Region:** Enclosed area in the CFG.
 - Do not forget the outermost region.
- In this example:
 - 3 Regions (see the circles with different colors).
 - Cyclomatic Complexity = 3
- Alternative way in next slide.

Path Base Testing: Step 2



■ Predicates:

- Nodes with multiple exit arcs.
- Corresponds to branch/conditional statement in program.

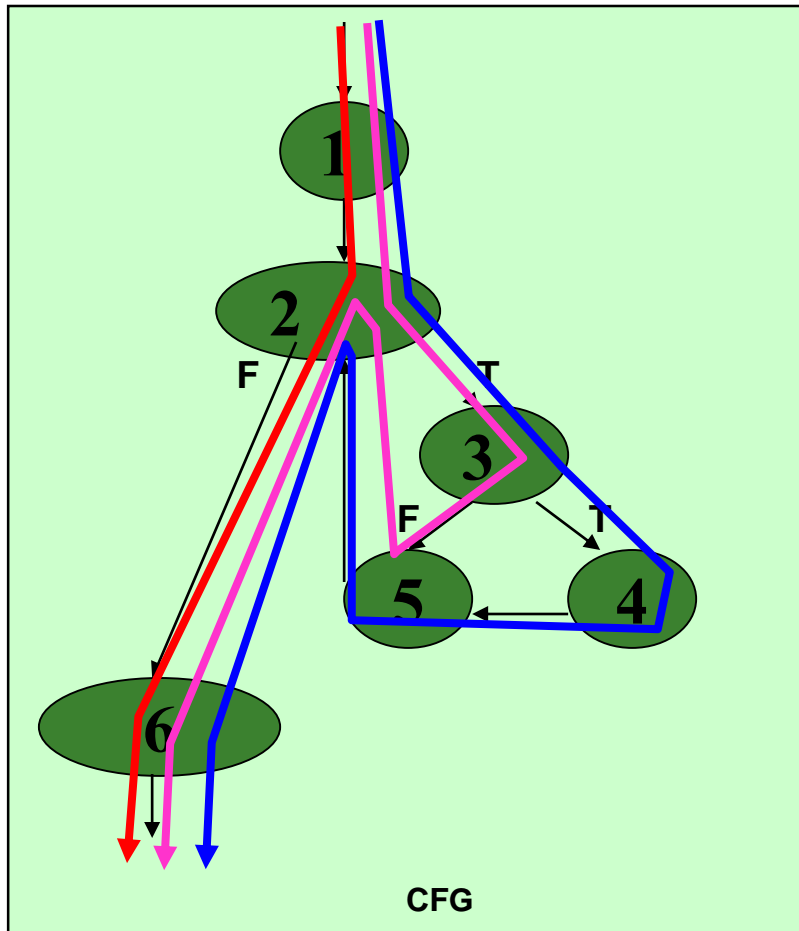
■ In this example:

- Predicates = 2
 - (Node 2 and 3)
- Cyclomatic Complexity
 $= 2 + 1$
 $= 3$

Path Base Testing: Step 3

- Independent path:
 - An **executable** or **realizable path** through the graph from the start node to the end node that has not been traversed before.
 - **Must** move along **at least one arc** that has not been yet traversed (an unvisited arc).
 - The objective is to cover all statements in a program by independent paths.
- The number of independent paths to discover \leq cyclomatic complexity number.
- Decide the Basis Path Set:
 - It is the maximal set of *independent paths* in the flow graph.
 - **NOT** a unique set.

Path Base Testing: Step 3



```
min = A[0]; } 1
I = 1;
while (I < N) { } 2
    if (A[I] < min) } 3
        min = A[I]; } 4
        I = I + 1; } 5
    }
print min } 6
```

- Cyclomatic complexity = 3.
- Need at most 3 independent paths to cover the CFG.
- In this example:
 - [1 - 2 - 6]
 - [1 - 2 - 3 - 5 - 2 - 6]
 - [1 - 2 - 3 - 4 - 5 - 2 - 6]

Path Base Testing: Step 4

- Prepare a test case for each independent path.
- In this example:
 - Path: [1 – 2 – 6]
 - Test Case: $A = \{ 5, \dots \}$, $N = 1$
 - Expected Output: 5
 - Path: [1 – 2 – 3 – 5 – 2 – 6]
 - Test Case: $A = \{ 5, 9, \dots \}$, $N = 2$
 - Expected Output: 5
 - Path: [1 – 2 – 3 – 4 – 5 – 2 – 6]
 - Test Case: $A = \{ 8, 6, \dots \}$, $N = 2$
 - Expected Output: 6
- These tests will result a complete decision and statement coverage of the code.

Try to verify that the test cases actually force execution along a desired path.

Another Example

```
int average (int[ ] value, int min, int max, int N) {
    int i, totalValid, sum, mean;
    i = totalValid = sum = 0;
    while ( i < N && value[i] != -999 ) {
        if (value[i] >= min && value[i] <= max) {
            totalValid += 1; sum += value[i];
        }
        i += 1;
    }
    if (totalValid > 0)
        mean = sum / totalValid;
    else
        mean = -999;
    return mean;
}
```

Step 1: Draw CFG

```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean;  
    i = totalValid = sum = 0; } ①  
    while ( i < N && value[i] != -999 ) {  
        ②    if (value[i] ④ >= min && value[i] ③ <= max) ⑤ {  
            totalValid += 1; sum += value[i]; ⑥  
        }  
        i += 1; ⑦  
    }  
    if (totalValid > 0) ⑧  
        mean = sum / totalValid; ⑨  
    else  
        mean = -999; ⑩  
    return mean; ⑪  
}
```

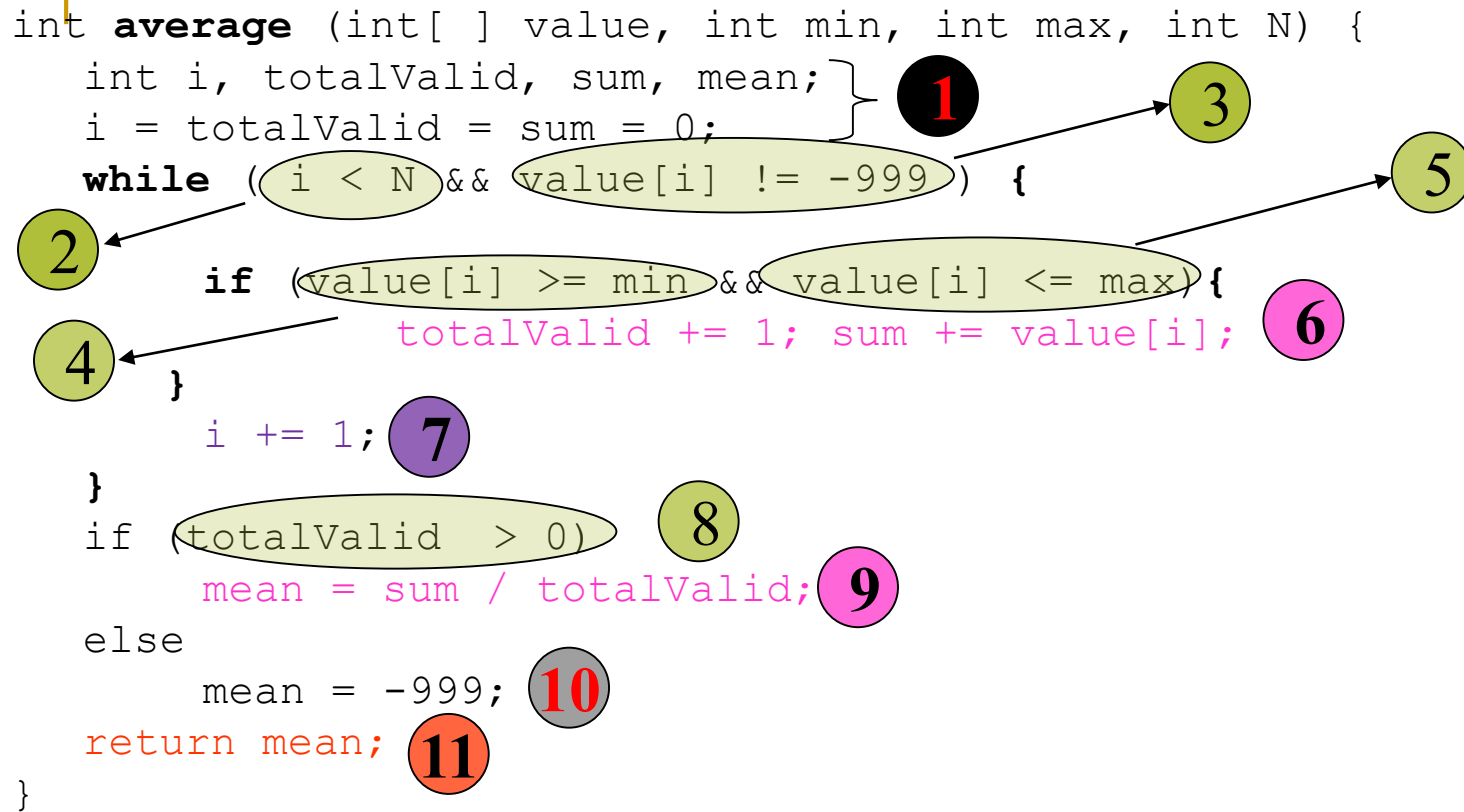
Step 1: Draw CFG

```
int average (int[] value, int min, int max, int N) {  
    int i, totalValid, sum, mean;  
    i = totalValid = sum = 0;  
    while ( i < N && value[i] != -999 ) {  
        if (value[i] >= min && value[i] <= max) {  
            totalValid += 1; sum += value[i];  
        }  
        i += 1;  
    }  
    if (totalValid > 0) {  
        mean = sum / totalValid;  
    }  
    else {  
        mean = -999;  
    }  
    return mean;  
}
```

Step 1: Draw CFG

```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean;  
    i = totalValid = sum = 0;  
    while ( i < N && value[i] != -999 ) {  
  
        if (value[i] >= min && value[i] <= max){  
            totalValid += 1; sum += value[i];  
        }  
        i += 1;  
    }  
    if (totalValid > 0)  
        mean = sum / totalValid;  
    else  
        mean = -999;  
    return mean;  
}
```


Step 1: Draw CFG



```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean; } 1  
    i = totalValid = sum = 0;  
    while (i < N && value[i] != -999) {  
        2 if (value[i] >= min && value[i] <= max) {  
            4 totalValid += 1; sum += value[i]; 6  
        }  
        i += 1; 7  
    }  
    if (totalValid > 0) 8  
        mean = sum / totalValid; 9  
    else  
        mean = -999; 10  
    return mean; 11  
}
```

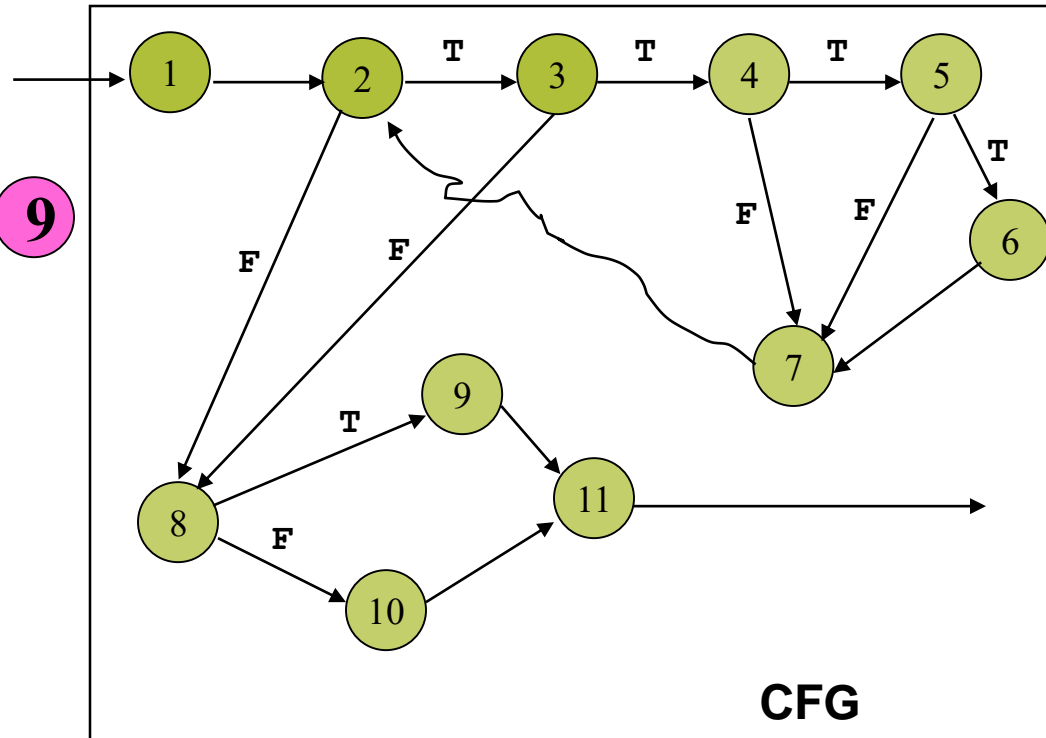
The diagram illustrates the control flow of the `average` function. It features 11 numbered nodes connected by arrows:

- Node 1** (black circle) is at the end of the first closing brace of the function signature.
- Node 2** (green circle) is at the start of the `if` statement inside the `while` loop.
- Node 3** (green circle) is at the end of the `while` loop's condition.
- Node 4** (green circle) is at the start of the `totalValid += 1; sum += value[i];` line.
- Node 5** (green circle) is at the end of the `while` loop's body.
- Node 6** (pink circle) is at the end of the `totalValid += 1; sum += value[i];` line.
- Node 7** (purple circle) is at the end of the `i += 1;` line.
- Node 8** (green circle) is at the end of the `if (totalValid > 0)` condition.
- Node 9** (pink circle) is at the end of the `mean = sum / totalValid;` line.
- Node 10** (grey circle) is at the end of the `mean = -999;` line.
- Node 11** (orange circle) is at the end of the `return mean;` line.

Arrows indicate the flow: 1 to 3, 3 to 5, 5 to 7, 7 to 8, 8 to 9, 9 to 10, 10 to 11, 11 to the final closing brace. Additionally, there are arrows from 2 to 4 and from 4 to 6, representing the flow within the `if` block. There is also an arrow from 1 to 2.

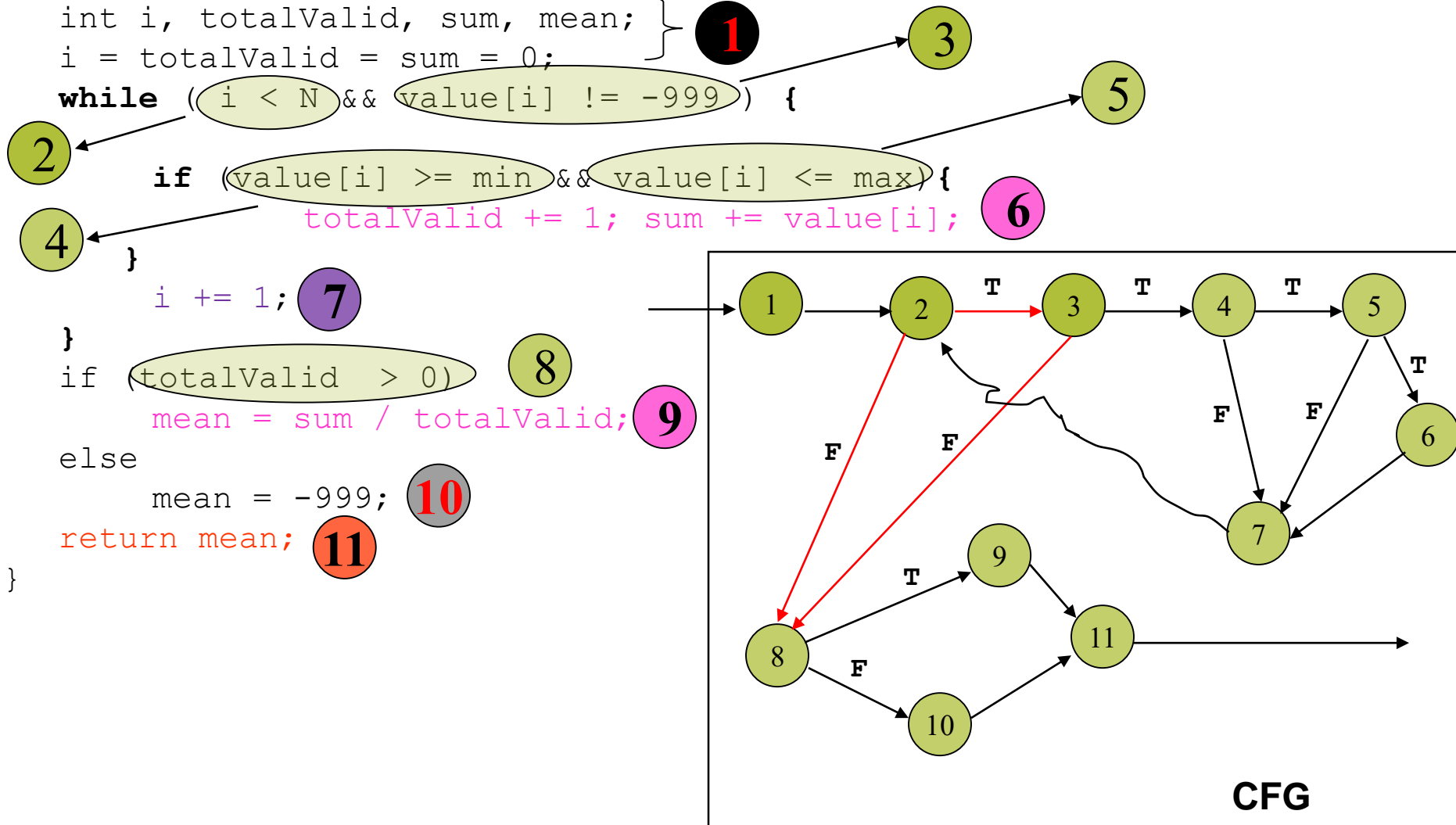
Step 1: Draw CFG

```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean; } 1  
    i = totalValid = sum = 0;  
    while ( i < N && value[i] != -999 ) {  
        if ( value[i] >= min && value[i] <= max ) {  
            totalValid += 1; sum += value[i]; 6  
        }  
        i += 1; 7  
    }  
    if ( totalValid > 0 ) 8  
        mean = sum / totalValid; 9  
    else  
        mean = -999; 10  
    return mean; 11  
}
```



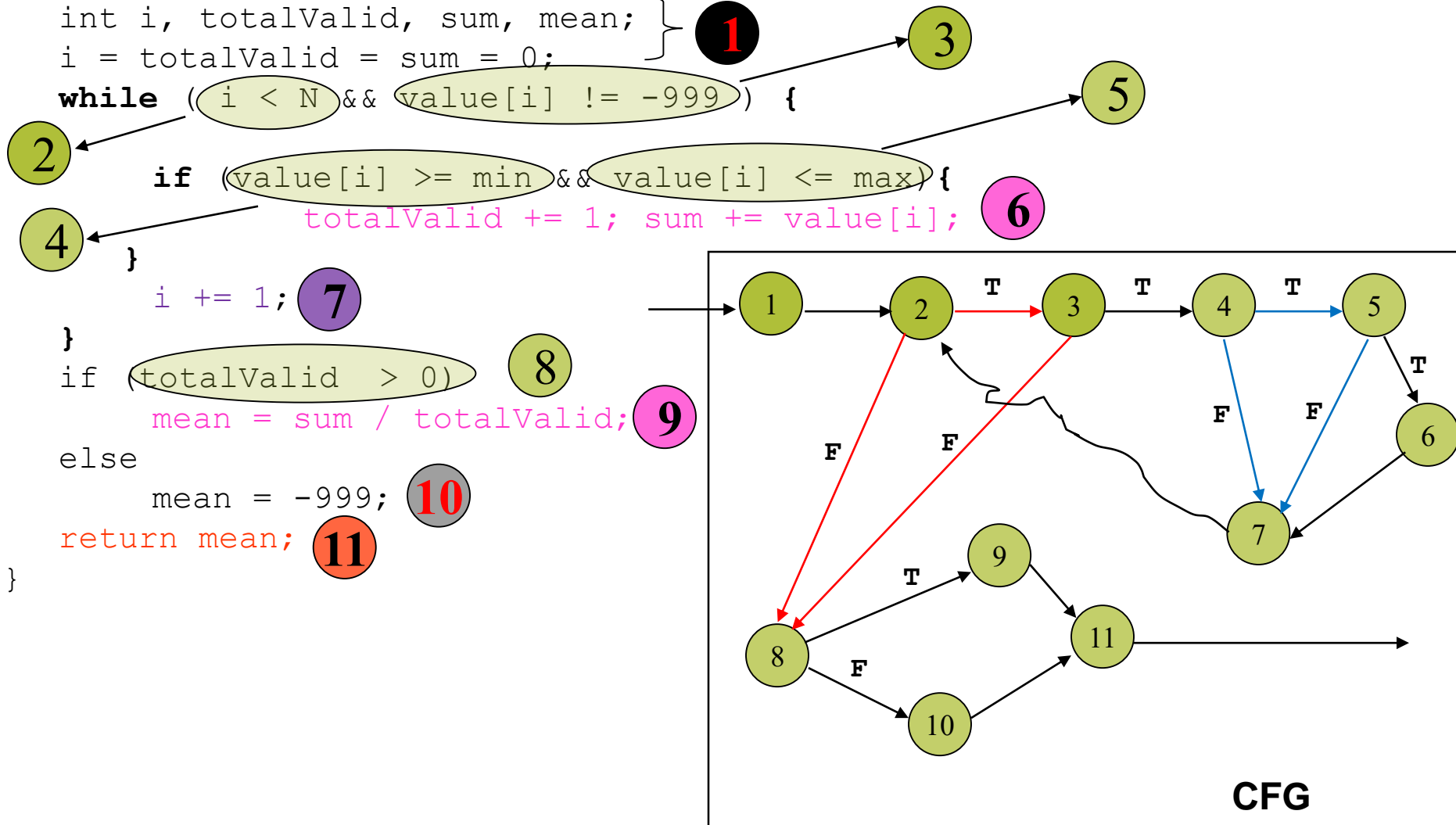
Step 1: Draw CFG

```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean;  
    i = totalValid = sum = 0;  
    while ( i < N && value[i] != -999 ) {  
        if ( value[i] >= min && value[i] <= max ) {  
            totalValid += 1; sum += value[i];  
        }  
        i += 1;  
    }  
    if ( totalValid > 0 )  
        mean = sum / totalValid;  
    else  
        mean = -999;  
    return mean;  
}
```



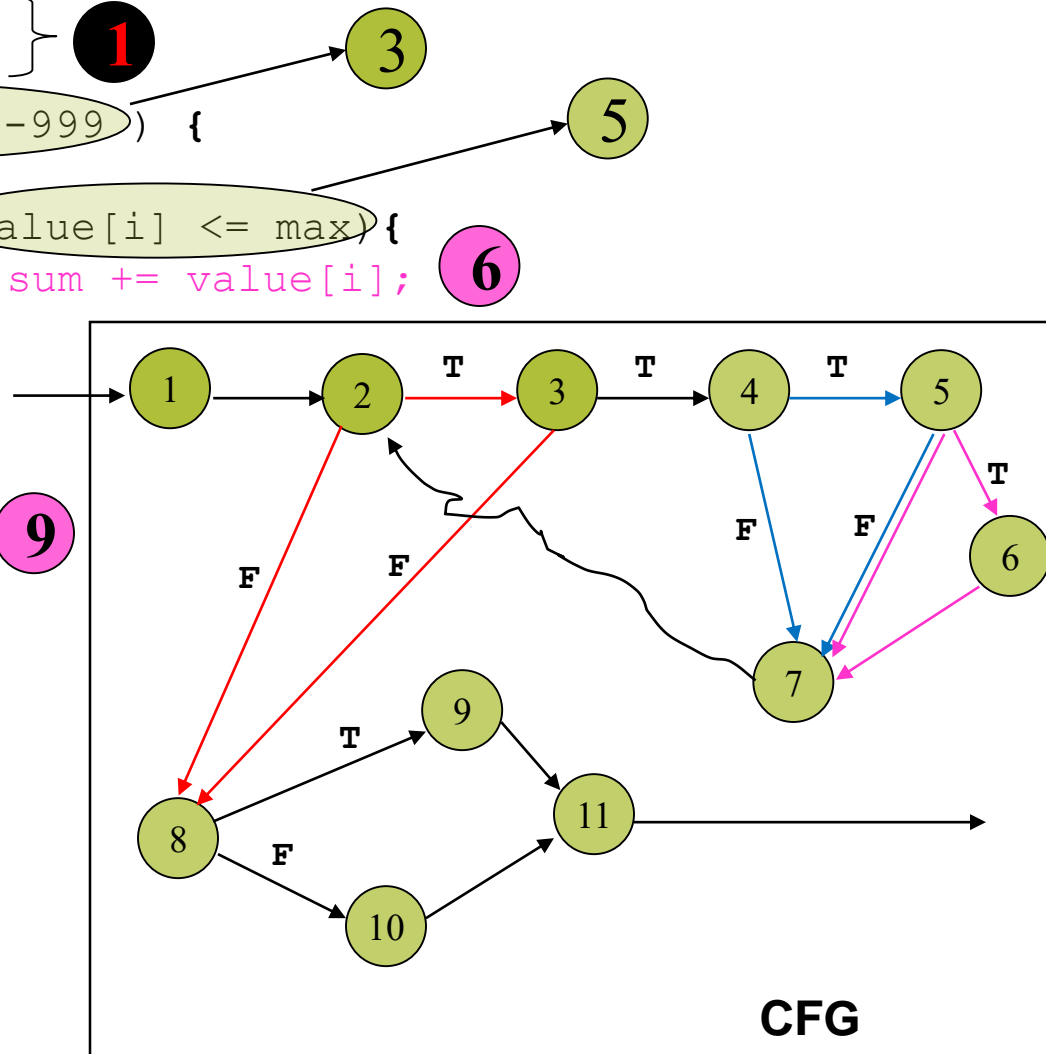
Step 1: Draw CFG

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int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean;  
    i = totalValid = sum = 0;  
    while ( i < N && value[i] != -999 ) {  
        if ( value[i] >= min && value[i] <= max ) {  
            totalValid += 1; sum += value[i];  
        }  
        i += 1;  
    }  
    if ( totalValid > 0 )  
        mean = sum / totalValid;  
    else  
        mean = -999;  
    return mean;  
}
```



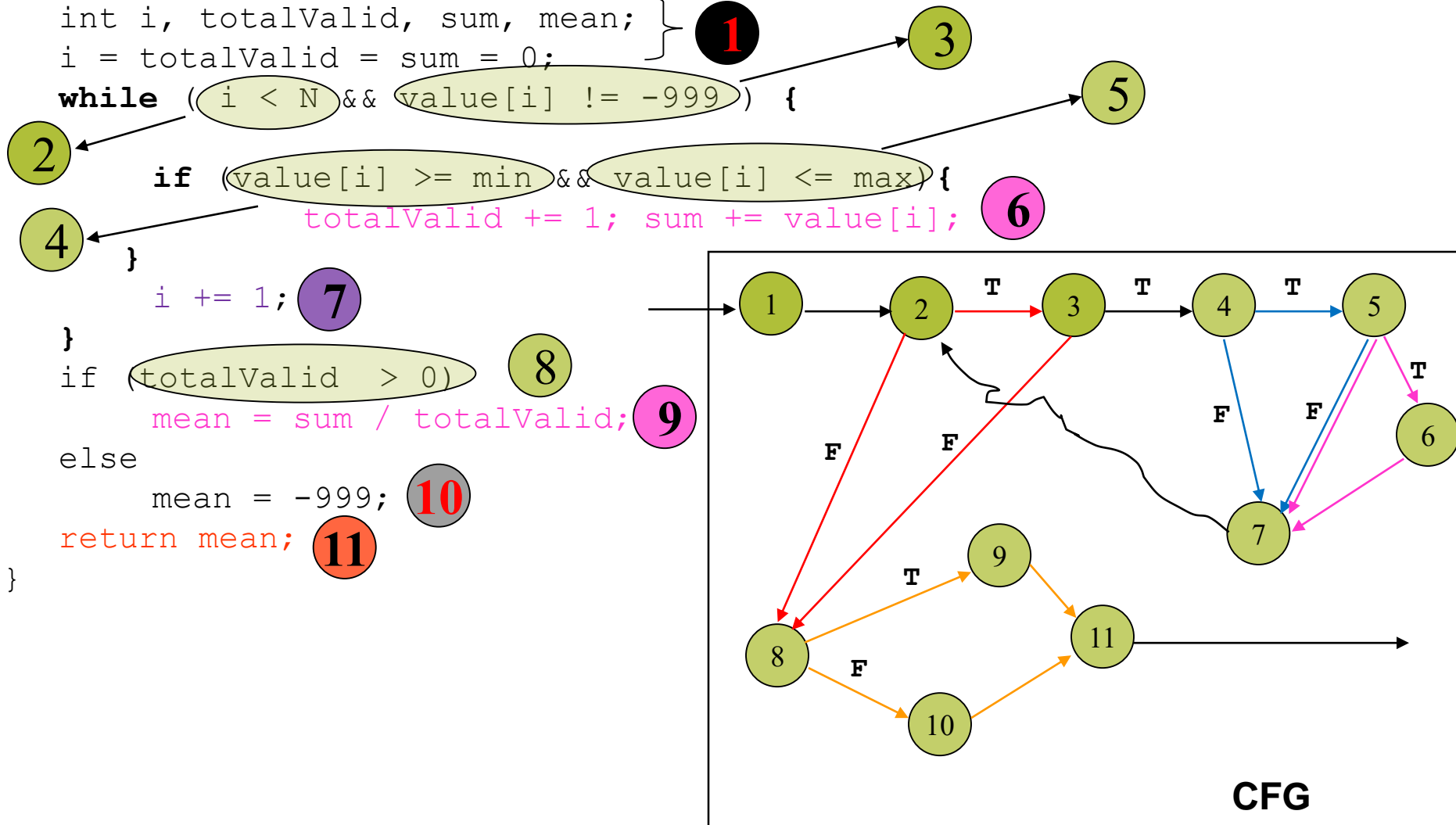
Step 1: Draw CFG

```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean;  
    i = totalValid = sum = 0;  
    while (i < N && value[i] != -999) {  
        if (value[i] >= min && value[i] <= max) {  
            totalValid += 1; sum += value[i];  
        }  
        i += 1;  
    }  
    if (totalValid > 0) {  
        mean = sum / totalValid;  
    }  
    else {  
        mean = -999;  
    }  
    return mean;  
}
```



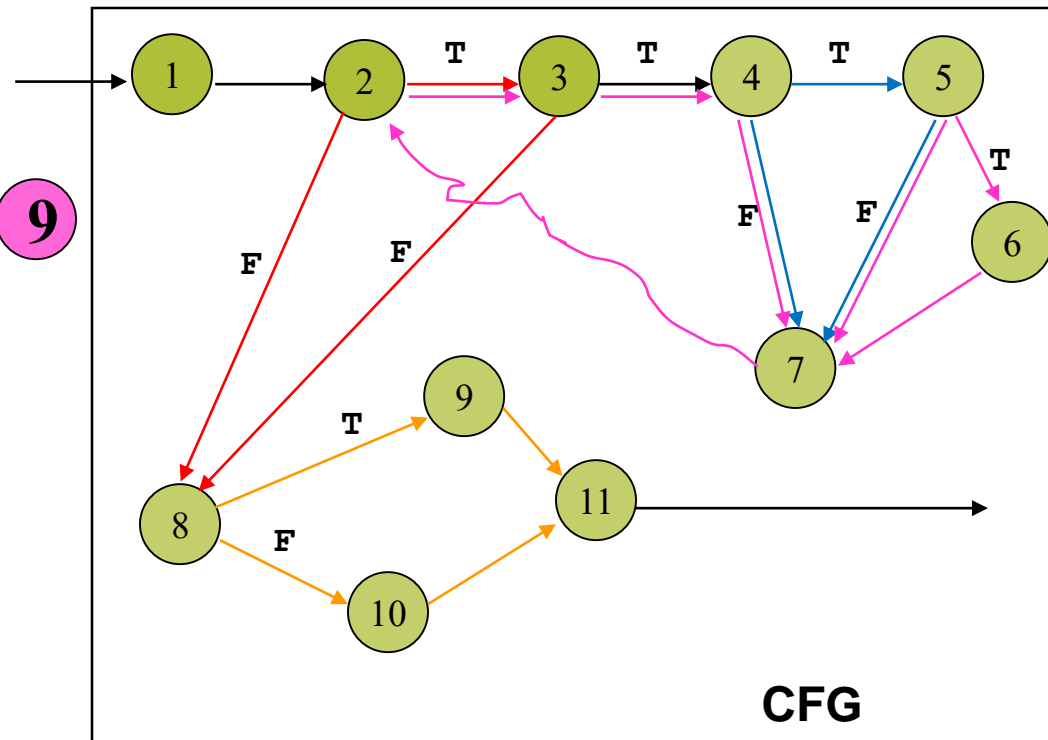
Step 1: Draw CFG

```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean;  
    i = totalValid = sum = 0;  
    while ( i < N && value[i] != -999 ) {  
        if ( value[i] >= min && value[i] <= max ) {  
            totalValid += 1; sum += value[i];  
        }  
        i += 1;  
    }  
    if ( totalValid > 0 )  
        mean = sum / totalValid;  
    else  
        mean = -999;  
    return mean;  
}
```



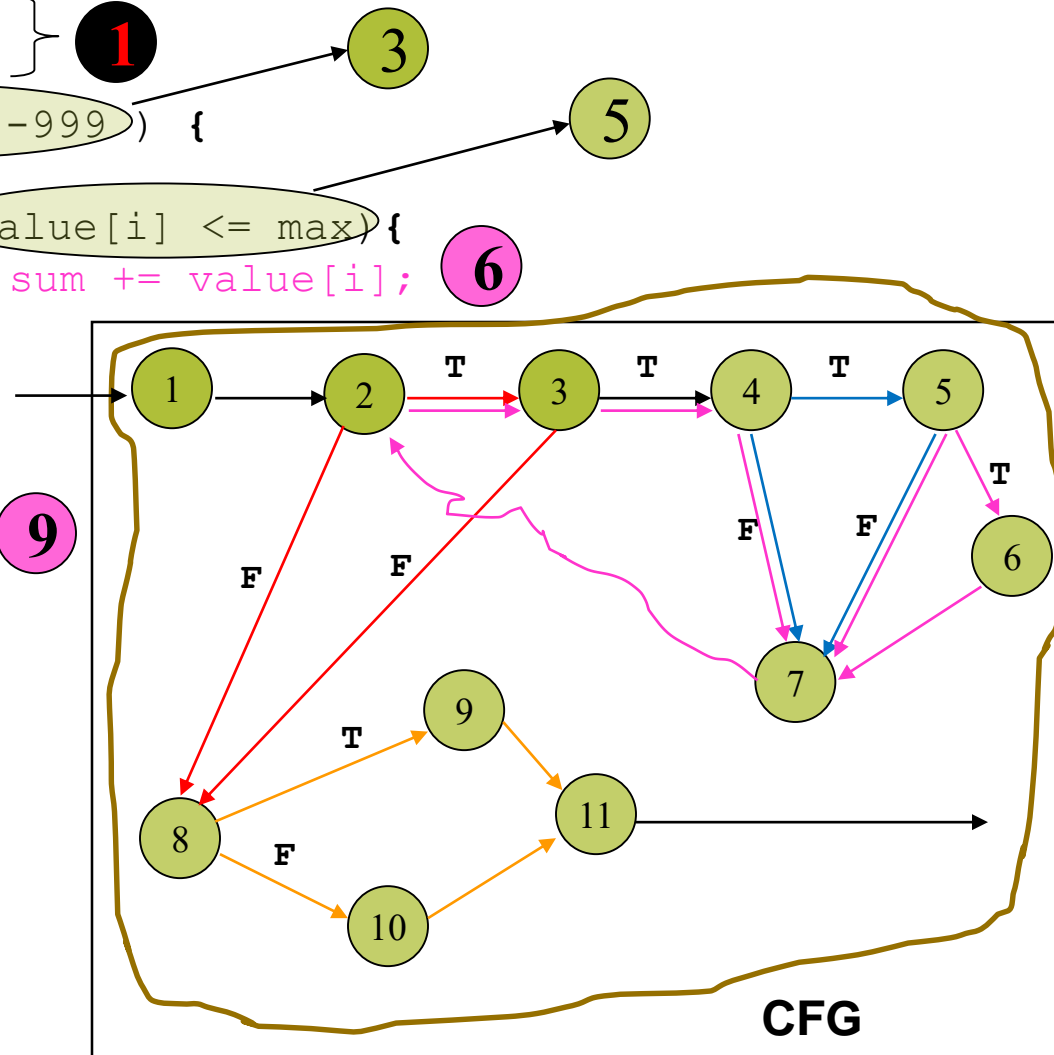
Step 1: Draw CFG

```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean; } 1  
    i = totalValid = sum = 0;  
    while ( i < N && value[i] != -999 ) {  
        if ( value[i] >= min && value[i] <= max ) {  
            totalValid += 1; sum += value[i]; 6  
        }  
        i += 1; 7  
    }  
    if ( totalValid > 0 ) 8  
        mean = sum / totalValid; 9  
    else  
        mean = -999; 10  
    return mean; 11  
}
```

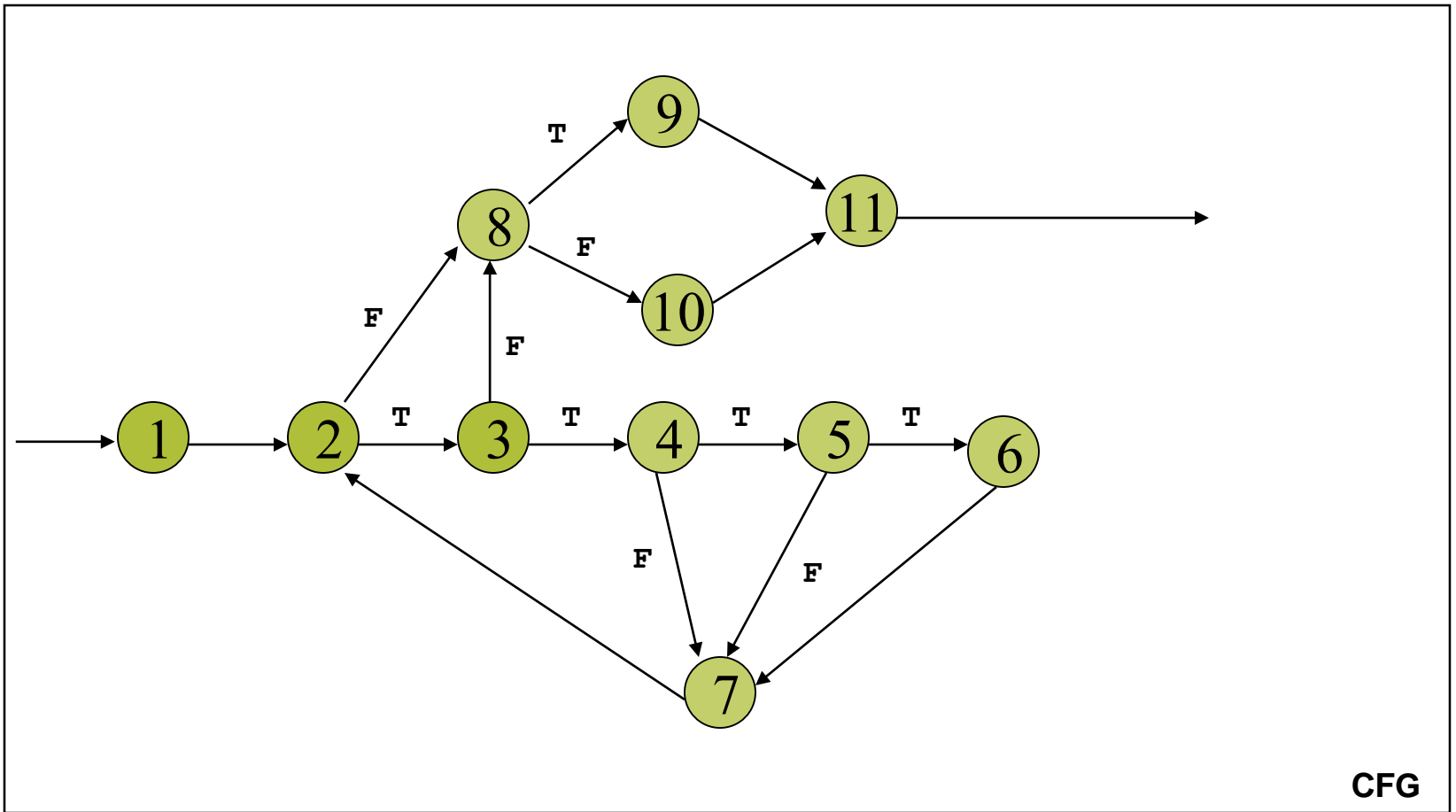


Step 1: Draw CFG

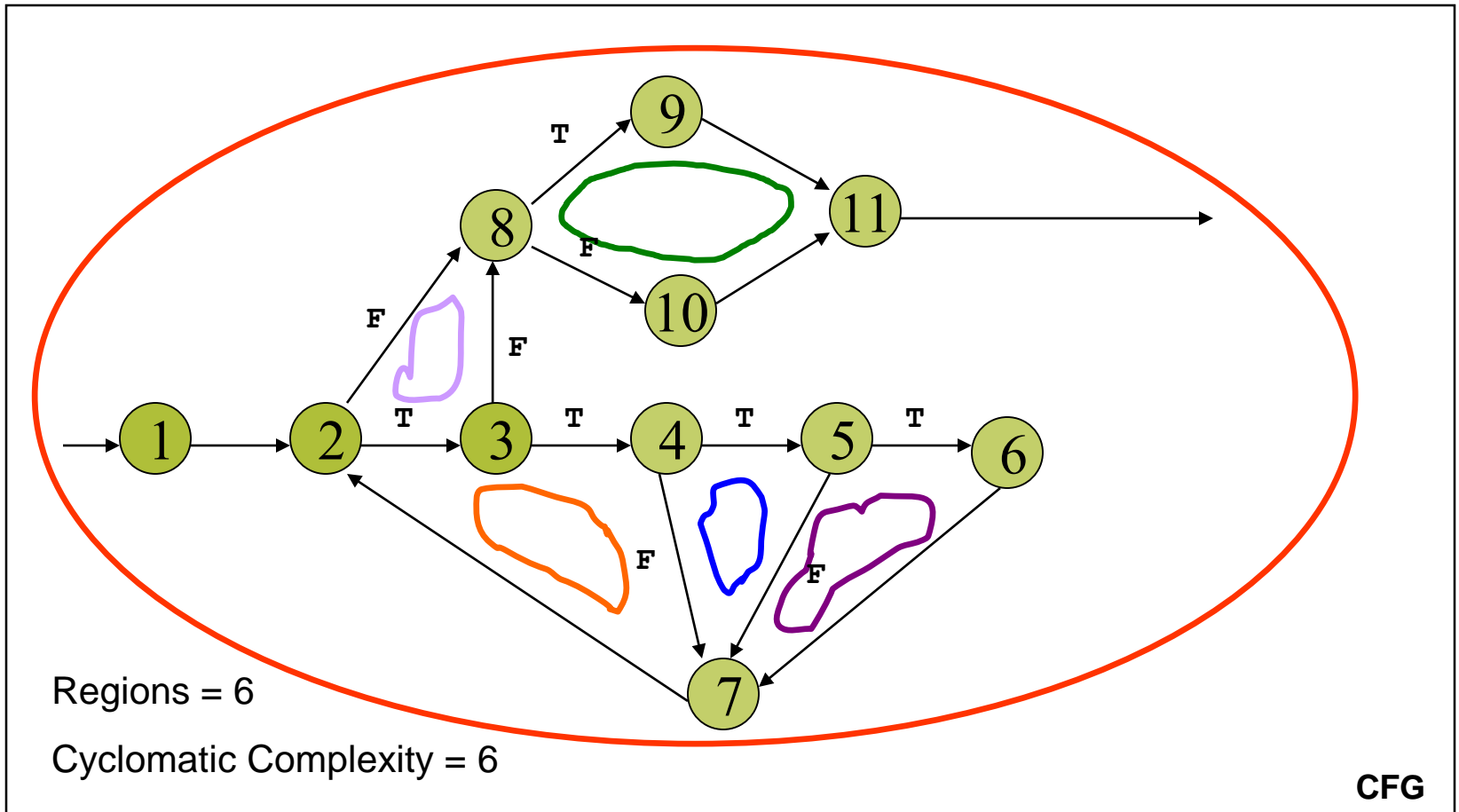
```
int average (int[ ] value, int min, int max, int N) {  
    int i, totalValid, sum, mean; } 1  
    i = totalValid = sum = 0;  
    while ( i < N && value[i] != -999 ) {  
        if ( value[i] >= min && value[i] <= max ) {  
            totalValid += 1; sum += value[i]; 6  
        }  
        i += 1; 7  
    }  
    if ( totalValid > 0 ) 8  
        mean = sum / totalValid; 9  
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    return mean; 11  
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```



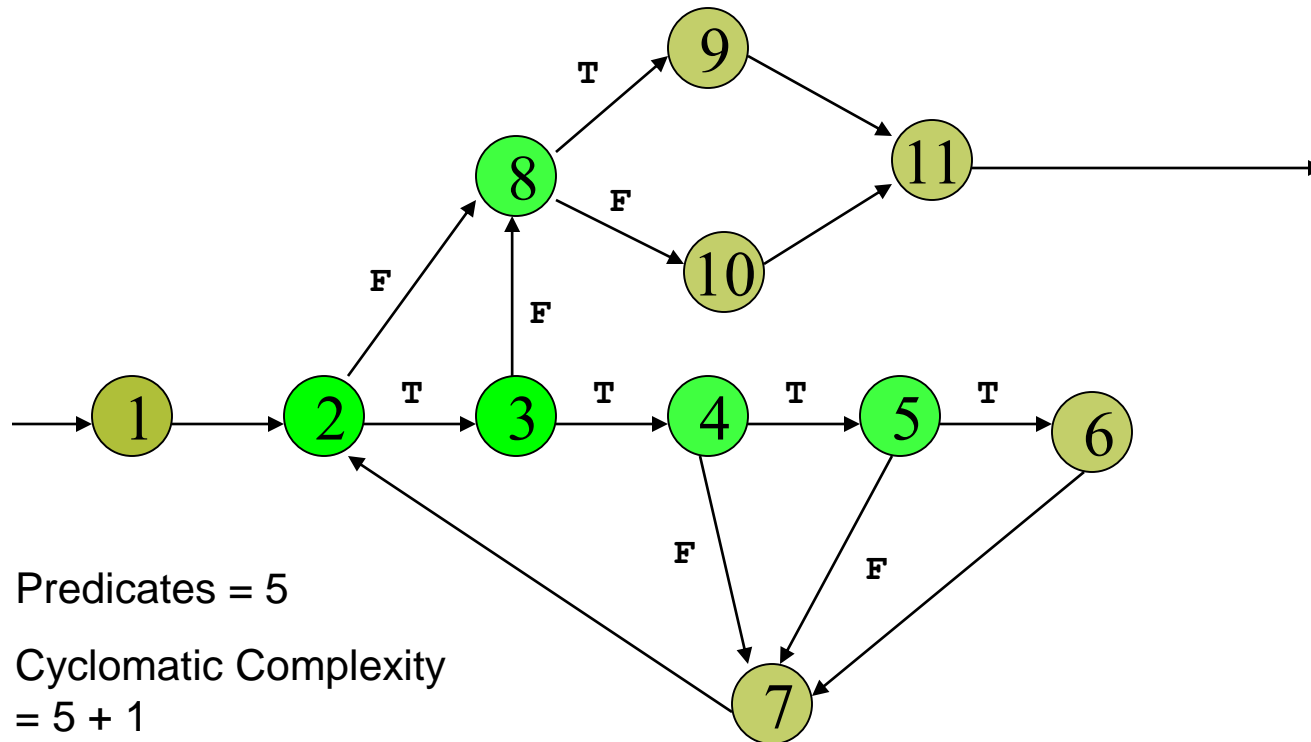
Step 1: Draw CFG



Step 2: Find Cyclomatic Complexity



Step 2: Find Cyclomatic Complexity



Predicates = 5

Cyclomatic Complexity

= 5 + 1

= 6

CFG

Step 3: Find Basic Path Set

- Find at most 6 independent paths.
- Usually, simpler path == easier to find a test case.
- However, some of the simpler paths are not possible (not realizable):
 - Example: [1 – 2 – 8 – 9 – 11].
 - Not Realizable (i.e., impossible in execution).
 - Verify this by tracing the code.
- Basic Path Set:
 - [1 – 2 – 8 – 10 – 11].
 - [1 – 2 – 3 – 8 – 10 – 11].
 - [1 – 2 – 3 – 4 – 7 – 2 – 8 – 10 – 11].
 - [1 – 2 – 3 – 4 – 5 – 7 – 2 – 8 – 10 – 11].
 - [1 – (2 – 3 – 4 – 5 – 6 – 7) – 2 – 8 – 9 – 11].
- In the last case, (...) represents possible repetition.

Step 4: Derive Test Cases

■ Path:

- [1 – 2 – 8 – 10 – 11]

■ Test Case:

- value = {...} irrelevant.

- N = 0

- min, max irrelevant.

■ Expected Output:

- average = -999

```
... i = 0; ①
while (i < N && ②
       value[i] != -999) {
    .....
}
if (totalValid > 0) ⑧
    .....
else
    mean = -999; ⑩
return mean; ⑪
```

Step 4: Derive Test Cases

■ Path:

- [1 – 2 – 3 – 8 – 10 – 11]

■ Test Case:

- value = {-999}

- N = 1

- min, max irrelevant

■ Expected Output:

- average = -999

```
... i = 0; ①
while (i < N && ②
       value[i] != -999) ③
    .....
}
if (totalValid > 0) ⑧
    .....
else ⑩
    mean = -999;
return mean; ⑪
```

Step 4: Derive Test Cases

- Path:
 - [1 – 2 – 3 – 4 – 7 – 2 – 8 – 10 – 11]
 - Test Case:
 - A single value in the `value[]` array which is smaller than *min*.
 - `value = { 25 }, N = 1, min = 30, max irrelevant.`
 - Expected Output:
 - `average = -999`
-
- Path:
 - [1 – 2 – 3 – 4 – 5 – 7 – 2 – 8 – 10 – 11]
 - Test Case:
 - A single value in the `value[]` array which is larger than *max*.
 - `value = { 99 }, N = 1, max = 90, min irrelevant.`
 - Expected Output:
 - `average = -999`
-

Step 4: Derive Test Cases

- Path:
 - [1 – 2 – 3 – 4 – 5 – 6 – 7 – 2 – 8 – 9 – 11]
- Test Case:
 - A single valid value in the `value[]` array.
 - `value = { 25 }, N = 1, min = 0, max = 100`
- Expected Output:
 - `average = 25`

OR

- Path:
 - [1 – 2 – 3 – 4 – 5 – 6 – 7 – 2 – 3 – 4 – 5 – 6 – 7 – 2 – 8 – 9 – 11]
 - Test Case:
 - Multiple valid values in the `value[]` array.
 - `value = { 25, 75 }, N = 2, min = 0, max = 100`
 - Expected Output:
 - `average = 50`
-

Summary: Path Base White Box Testing

- A simple test that:
 - Cover all statements.
 - Exercise all decisions (conditions).
- The cyclomatic complexity is an **upperbound** of the independent paths needed to cover the CFG.
 - If more paths are needed, then either cyclomatic complexity is wrong, or the paths chosen are incorrect.
- Although picking a complicated path that covers more than one unvisited edge is possible all times, it is not encouraged:
 - May be hard to design the test case.

Summary

■ Test Case Design

□ White Box

- Control Flow Graph
- Cyclomatic Complexity
- Basic Path Testing

□ Black Box

- Equivalence Classes
 - Boundary Value Analysis
-