

$$e^x = 1 + x + \frac{x^2}{2!} + \dots + \frac{x^n}{n!} + o(x^n) = \sum_{k=0}^n \frac{x^k}{k!} + o(x^n)$$

$$a^x = 1 + \frac{\ln a}{1!} x + \frac{\ln^2 a}{2!} x^2 + \dots + \frac{\ln^n a}{n!} x^n + o(x^n) = \sum_{k=0}^n \frac{x^k \ln^k a}{k!} + o(x^n)$$

$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots + (-1)^{n+1} \frac{x^{2n-1}}{(2n-1)!} + o(x^{2n-1}) = \sum_{k=1}^n \frac{(-1)^{k+1} x^{2k-1}}{(2k-1)!} + o(x^{2n-1})$$

$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots + (-1)^n \frac{x^{2n}}{(2n)!} + o(x^{2n}) = \sum_{k=0}^n \frac{(-1)^k x^{2k}}{(2k)!} + o(x^{2n})$$

$$(1+x)^\alpha = 1 + \alpha x + \frac{\alpha(\alpha-1)x^2}{2!} + \dots + \frac{\alpha(\alpha-1)\dots(\alpha-(n-1))x^n}{n!} + o(x^n) = 1 + \sum_{k=1}^n \frac{\alpha(\alpha-1)\dots(\alpha-(k-1))x^k}{k!} + o(x^n)$$

$$\frac{1}{1-x} = 1 + x + x^2 + \dots + (-1)^n x^n + o(x^n) = \sum_{k=0}^n x^k + o(x^n)$$

$$\frac{1}{1+x} = 1 - x + x^2 - \dots + (-1)^n x^n + o(x^n) = \sum_{k=0}^n (-1)^k x^k + o(x^n)$$

$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \dots + \frac{(-1)^{n-1} x^n}{n} + o(x^n) = \sum_{k=1}^n \frac{(-1)^{k+1} x^k}{k} + o(x^n)$$

$$\operatorname{arctg} x = x - \frac{x^3}{3} + \frac{x^5}{5} - \dots + (-1)^n \frac{x^{2n+1}}{2n+1} + o(x^{2n+1}) = \sum_{k=1}^n \frac{(-1)^{k+1} x^{2k-1}}{2k-1} + o(x^{2n+1})$$

$$\arcsin x = x + \frac{x^3}{6} + \frac{3x^5}{40} + \dots + \frac{(2n)! x^{2n+1}}{2^{2n} (n!)^2 (2n+1)} + o(x^{2n+1}) = \sum_{k=0}^n \frac{(2k)! x^{2k+1}}{2^{2k} (k!)^2 (2k+1)} + o(x^{2n+1})$$