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Problem 1-1

Consider a Copper penny that contains both positive and Negative charges, each of magnitude $1.83 \times 10^6 \text{ C}$. Suppose that these charges could be concentrated into two separate bundles, held 100m apart which attractive force would act on each bundle?

Data:- Copper penny Positive Charge, $q_1 = 1.83 \times 10^6 \text{ C}$
Copper penny Negative Charge, $q_2 = -1.83 \times 10^6 \text{ C}$
Separation b/w Charges, $r = 100 \text{ m}$

Required:- $F = ??$

Formulae-
$$F = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r^2} \right) = K \frac{q_1 q_2}{r^2}$$

Solution:-

Using Coulomb's law formula,

Coulomb's Constant $\frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$

Putting values in formula,

$$F = \frac{(8.99 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2)(1.83 \times 10^6 \text{ C})(-1.83 \times 10^6 \text{ C})}{(100 \text{ m})^2}$$

$$F = -3.01 \times 10^{18} \text{ N}$$

Result:- The attractive force that acts on each bundle is $F = -3.01 \times 10^{18} \text{ N}$

Problem 1-2

The average distance r between the electron and the Proton in atom is 7.4×10^{-11} m. what is the magnitude of the average electrostatic force that acts between these two particles?

Data:- Charge on electron, $q_e = 1.60 \times 10^{-19}$ C
 Charge on Proton, $q_p = 1.60 \times 10^{-19}$ C
 Distance, $r = 7.4 \times 10^{-11}$ m

Required:- $F = ??$

Formula:-
$$F = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r^2} \right) = K \frac{q_1 q_2}{r^2}$$

Solution:-

→ Coulomb's Constant $1/4\pi\epsilon_0 = 8.99 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$

Putting values in formula,

$$F = \frac{(8.99 \times 10^9)(1.60 \times 10^{-19})(1.60 \times 10^{-19})}{(7.4 \times 10^{-11} \text{ m})^2}$$

$$F = 4.20 \times 10^{-8} \text{ N}$$

Result:-

The Electrostatic force acts b/w to particles.

$$\boxed{F = 4.20 \times 10^{-8} \text{ N}}$$

Problem 1-3

The nucleus of an atom has a radius of about 6×10^{-15} m and contains 26 protons. What repulsive electrostatic force act b/w two protons in such a nucleus that are separated by a distance of one radius?

Data:- Separation $r = 6 \times 10^{-15}$ m
Charg on proton, $q_p = 1.60 \times 10^{-19}$ C

Required:- Repulsive Force = ??

Formula:-
$$F = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r^2} \right) = k \frac{q_1 q_2}{r^2}$$

Solution:-

Coulomb's Constant $1/4\pi\epsilon_0 = 8.99 \times 10^9 \text{ N.m}^2/\text{C}^2$

Putting values in formula,

$$F = \frac{(8.99 \times 10^9 \text{ N.m}^2/\text{C}^2) (1.60 \times 10^{-19} \text{ C}) (1.60 \times 10^{-19} \text{ C})}{(6 \times 10^{-15} \text{ m})^2}$$

$$F = 6.39 \text{ N}$$

Result:-

⇒ The Repulsive Force b/w Protons

$$\boxed{F = 6.39 \text{ N}}$$

Problem 1-4

Figure shows three charged particles, held in place by forces not shown. What electrostatic force, owing to the other charges, act on q_1 ? (Find the value of F_{12} & F_{13})?
Take $q_1 = 4.2 \mu\text{C}$, $q_2 = 8.4 \mu\text{C}$, $q_3 = 3.4 \mu\text{C}$, $r_{12} = 19 \text{ cm}$, $r_{13} = 19 \text{ cm}$.

Data available in Problem question.

Required... Electrostatic Force (F_{12} & F_{13}) = ??

Formula:
$$F = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r^2} \right)$$

Solution: Coulomb's Constant $1/4\pi\epsilon_0 = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2$

Putting value in Formula,

$$F_{12} = \frac{(8.99 \times 10^9 \text{ Nm}^2/\text{C}^2)(4.2 \times 10^{-6} \text{ C})(8.4 \times 10^{-6} \text{ C})}{(0.19 \text{ m})^2}$$

$$F_{12} = 8.78 \text{ N}$$

The charges q_1 and q_2 have opposite signs so that the force b/w them is attractive. Hence F_{12} points to the right shown in figure.

We also have F_{13} ,

$$F_{13} = \frac{(8.99 \times 10^9 \text{ Nm}^2/\text{C}^2)(4.2 \times 10^{-6} \text{ C})(3.4 \times 10^{-6} \text{ C})}{(0.19 \text{ m})^2}$$

$$F_{13} = 3.55 \text{ N}$$

Result: Electrostatic force is acting from other charges.

$$F_{12} = 8.78 \text{ N}$$

$$F_{13} = 3.55 \text{ N}$$

Problem 1-5

What must be the distance b/w point charge $q_1 = 96.7 \mu\text{C}$ and $q_2 = 87.7 \mu\text{C}$ in order that the attractive electrical force between them has a magnitude of 7.98 N ?

Data: Point charge $q_1 = 96.7 \mu\text{C} = 96.7 \times 10^{-6} \text{ C}$

Point charge $q_2 = 87.7 \mu\text{C} = 87.7 \times 10^{-6} \text{ C}$

Attractive Electrical Force $F = 7.98 \text{ N}$

Coulomb's Constant $1/4\pi\epsilon_0 = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2$

Required: Distance b/w Point charges, $r = ??$

Formula: $F = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r^2} \right) = K \frac{q_1 q_2}{r^2}$

Solution: - Rearranging Formula and we get,

$$r^2 = \frac{K q_1 q_2}{F}$$

$$r = \sqrt{\frac{K q_1 q_2}{F}} \quad (i)$$

Putting values in formula

$$r = \sqrt{\frac{(8.99 \times 10^9) (96.7 \times 10^{-6} \text{ C}) (87.7 \times 10^{-6} \text{ C})}{(7.98 \text{ N})}}$$

$$r = \sqrt{9.55} \Rightarrow 3.09$$

Result:

Distance between Point Charges is

$$r = 3.090 \text{ m}$$

$$r = 3.09 \text{ m}$$

Problem 1-6

A Point charge of $+7.12 \times 10^{-6} \text{ C}$ is 13.4 cm distant from a second point charge of $-2.48 \times 10^{-6} \text{ C}$. Calculate the magnitude of the force on each charge.

Data:- Point Charge $q_1 = +7.12 \times 10^{-6} \text{ C}$
 Point Charge $q_2 = -2.48 \times 10^{-6} \text{ C}$
 Separation, $r = 13.4 \text{ cm} = 13.4 \times 10^{-2} \text{ m}$
 Coulomb's Constant $1/4\pi\epsilon_0 = 8.99 \times 10^9 \text{ NM}^2/\text{C}^2$

Required:- $F = ??$

Formula:-
$$F = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r^2} \right) = k \frac{q_1 q_2}{r^2}$$

Solution:-

Putting values in formula,

$$F = \frac{(8.99 \times 10^9 \text{ NM}^2/\text{C}^2) (+7.12 \times 10^{-6}) (-2.48 \times 10^{-6})}{(13.4 \times 10^{-2} \text{ m})^2}$$

$$F = -8.840 \text{ N}$$

Result:- Magnitude of the force of each charge is

$$F = -8.840 \text{ N}$$

$$F = -8.840 \text{ N}$$

Problem 1-7

A Point charge of $+4.00 \times 10^{-6} \text{ C}$ is 13.0 cm distant from a Second ^{Point} charge of $6.50 \times 10^{-6} \text{ C}$. Calculate the magnitude of the force on each charge.

Data: Point charge $q_1 = +4.00 \times 10^{-6} \text{ C}$

Point charge $q_2 = 6.50 \times 10^{-6} \text{ C}$

Separation, $r = 13.0 = 13.0 \times 10^{-2} \text{ m}$

Coulomb's Constant $1/4\pi\epsilon_0 = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2$

Required:

$F = ??$

Formula: $F = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r^2} \right) = K \frac{q_1 q_2}{r^2}$

Solution: Putting values in formula,

$$F = \frac{(8.99 \times 10^9 \text{ Nm}^2/\text{C}^2) (+4.00 \times 10^{-6} \text{ C}) (6.50 \times 10^{-6} \text{ C})}{(13.0 \times 10^{-2} \text{ m})^2}$$

$$F = 13.83 \text{ N}$$

Result: Magnitude of the force of each charge is

$$F = 13.83 \text{ N}$$

Problem 1-8

What must be the distance b/w point charge $q_1 = 23.0 \mu\text{C}$ and $q_2 = 25.0 \mu\text{C}$ for the electrostatic force b/w them to have a magnitude of 7.50 N ?

Data: Point charge $q_1 = 23.0 \mu\text{C} = 23.0 \times 10^{-6} \text{ C}$

Point charge $q_2 = 25.0 \mu\text{C} = 25.0 \times 10^{-6} \text{ C}$

Electrostatic force $F = 7.50 \text{ N}$

Coulomb's Constant $\frac{1}{4\pi\epsilon_0} = K = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2$

Required: Distance b/w Point charges, $r = ??$

Formula:

$$F = \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r^2} \right) = K \frac{q_1 q_2}{r^2}$$

Rearranging

$$r^2 = \frac{K q_1 q_2}{F}$$

$$r = \sqrt{\frac{K q_1 q_2}{F}} \quad (1)$$

Solution: Putting values in formula.

$$r = \sqrt{\frac{(8.99 \times 10^9) (23.0 \times 10^{-6}) (25.0 \times 10^{-6})}{(7.50)}}$$

$$r = \sqrt{\frac{5.16925}{7.50}} \Rightarrow 0.830$$

Result: Distance b/w Point charge is

$$r = 0.830 \text{ m}$$