

Customer Churn Prediction using Quotation Data

Master Thesis

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1 Introduction

Predicting churners in order to retain customers has become one of the most important issues for companies in the field of CRM. In the ideal case, companies want to detect potential churners before they leave by estimating probabilities for a churn in the next period of time. To tackle this issue, more and more advanced Machine-Learning-Algorithms are used guaranteeing solid accuracy in their out-of-sample predictions.

Fortunately for most of the companies, churn rates from one period to another are very small. However in classification models predicting a rare event can become challenging. In this so called "Imballanced Classes" issue certain arrangements to the underlying training data or the selected objective function need be made. Without these arrangements and with highly imballanced classes, a poor algorithm will simply never predict the outcome of the minority class. In a dataset with 1000 customers containing 5 churners for example, this loss-minimizing algorithm would have an in-sample accuracy of 99.5%.

In order to avoid the high amount of "False-Negative"-classifications there are many methods ranging from upsampling the minority class or downsampling the majority class to more advanced techniques like custom loss functions. In this work we present and compare the different methods while applying them to the underlying problem.

We also want to emphasize the importance of using quotation data for predicting customer churn. A company can track (potential) customer behavior on their distribution channels. Nowadays, in most cases the products or services are offered online on websites, which makes it easy to track website visitor data. In the context of dealing with customer churn this data can be matched to the customers already having a product or contract of this company. We show that first the number of visits of a current customer in the last period and second the average of the seen price during the visits have a high importance when predicting the probability of that customer leaving in the next period.

In order to evaluate the importance and relationship of not only the quotation features but also the other explanatory variables with the to-be-explained variable there is typically a trade-off during model selection. The trade-off lies between the model complexity and the model interpretability. Deep neural networks or boosted trees belong to the complex models which are famous for their comparatively high accuracy in almost all domains, espacially in computer vision and natural language processing. Understanding and interpreting the model is less important in these areas.

However in the course of this work and in many other areas understanding understanding how explanatory features interact with the outcome of the model becomes desirable. The most transparent models in terms of interpretability are linear or logistic models. There the magnitude and sign of the corresponding coefficients (after being testet for significance) illustrate the changes of the outcome for a change in the specific explanatory variable. These models however lack in terms of accuracy when being compared to the complex ones, because they do not allow for non-linearities and interactions in the explanatory features. Extensions, like general additive models (GAMs) [8] or GAMs al-

lowing for pairwise interactions (GA²Ms) [13] incorporate non-linearities.

In this work we focus on comparing the predictive accuracy and interpretability of black-box and white-box models. For the black-box model we fit gradient-boosted trees [5] as they outperform other models in most applications with tabular data. Partial dependency plots [4], Shapley values [14] and LIME [16] are novel approaches designed to make these black-box models interpretable. Additionally we present the accuracy and interpretability of "Explainable Boosting Machines" (EBM) developed by Microsoft researchers Lou et al. [15] which are based on a GA²Ms model and are therefore interpretable in the form of their shape functions. EBMs aim to combine the high accuracy of complex models on the one hand and the interpretability of general additive models on the other hand.

2 Data and Methodology

2.1 Understanding the Problem

For this work we use customer data from a big insurance company in Germany. Due to data protection the data is anonymized which does not affect the model accuracy and interpretability in any form. We focus on the product of automobile liability insurance, which is by law a mandatory service every car owner must hold in Germany.

Typically car owners close a deal with an insurance company which can be terminated by the end of each year. In rare cases both sides agree on a contract with a due date during the year. If the contract does not get terminated it is automatically extended for another year. Besides the option to terminate the contract at the due date there is also an option to terminate it earlier in a few special cases. These cases mainly involve the exceptional right of termination given to a customer after a car accident or a vehicle change. To sum up, here are the two cases in which a churn can (but not must) occur before the contract due date:

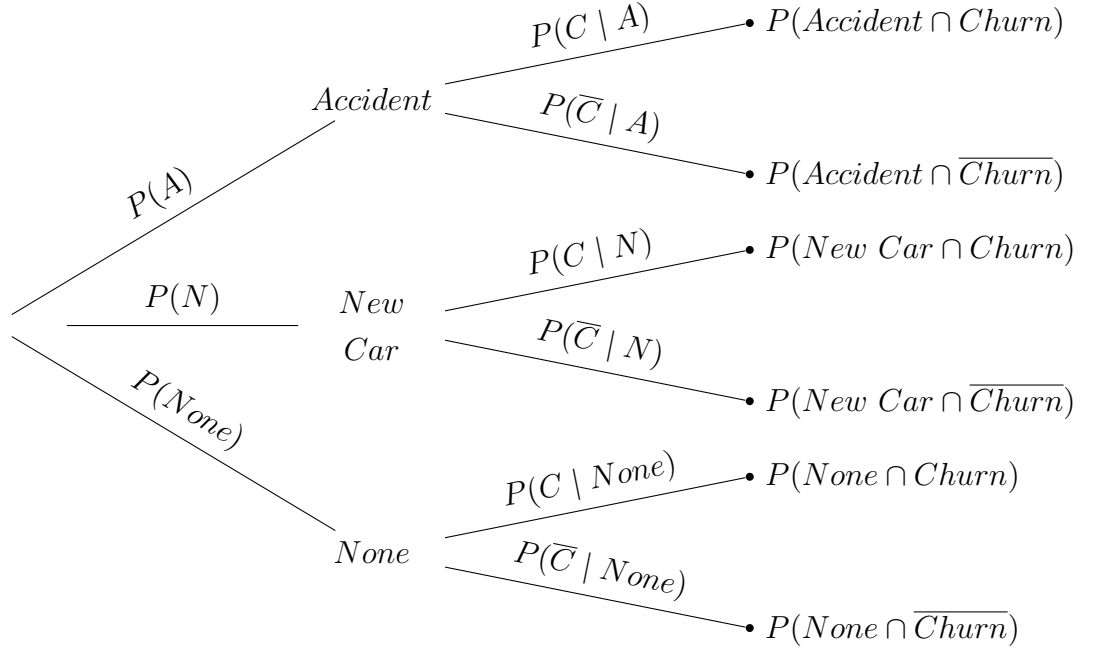
Event A: Contractor is involved in an Accident.

Event N: Contractor buys a new Car.

The problem of modelling customer churn needs to be separated into the probability of a customer leaving before his contract due date and churns happening at the due date. The reason is that the optimal modelling approach and explanatory variables have differences. One example is the premium adjustment sent to the customers before their due date, which has a high contribution to the decision of the customers at the due date. Meanwhile, churns before the due date are dependent on the occurrence of the events *A* and *N*. In this work we focus on predicting churns occurring before the due date.

This tree diagram illustrates how the probability of a churn before the due date can be

decomposed using the Events A (Accident), N (New Car) and C (Churn).



By assumption we set $P(C | None) = 0$ as the amount of terminated contracts during the year which are not being caused by a new car, an accident or a due date is very small and can be omitted. Therefore we leave these cases out of our data. What we are interested in predicting is the overall probability of a churn, which can be rewritten as:

$$\begin{aligned}
 P(C) &= P(A \cap C) + P(N \cap C) + P(D \cap C) \\
 &= P(A)P(C | A) + P(N)P(C | N) + P(D)P(C | D)
 \end{aligned}$$

One idea would be to model the three branches of A and N separately. The logic behind this is that different models and sets of explanatory variables have the best fit for the probabilities of the tree branches. Not only the the branches but also the unconditional and conditional probabilities of a single branch may vary in their best modelling approach. For predicting an accident a model of type (XY) is more suitable, whereas (YZ) would go better with modelling the probability of churn given an accident occurred. In the course of this work we begin with a general modelling approach trying to predict the probability $P(C)$. At a later stage we compare the accuracy outcomes of separately predicting the branch probabilities with the baseline approach.

The purpose is to build a model which can be used at any time t of the year to predict the probability of a costumer leaving the company in the next period of time $(t, t + s]$ and not at his due date. It can be argued that in order to provide a model with maximized utility for production one would want to keep s small. For example a company would highly benefit from a model, which can predict the churn-probability of the next week. However we see that having a small s decreases the accuracy of our models, creating a trade-off situation between model accuracy and the benefits of a small s . With a smaller period the classes of the data become more imballanced, creating a higher challange of feeding the model enough information about churners. Furthermore, a small s decreases

the scope of action for a company to retain potential customers leaving.

2.2 Data

Most customer churn prediction models have been using only one timestamp to train a model. We want to emphasize the usage of multiple timestamps and show that it significantly improves prediction accuracy. The improvement is a result of an increased training set size and the ability of the model to especially learn more about the rare class. Furthermore, the model becomes more generalizable in time which is crucial if this model is applied in production (see: [7]). Explain more using graphics.

Part of this work is the evaluation if the churn probability of customers is time invariant. Therefore we statistically test the equality of monthly mean churn rates. We see that there is a seasonality in the churn rate which underlines the importance of including different timestamps in the training data for the model to learn the monthly differences. These different timestamps are simply appended to the data as additional rows creating a panel dataset. The month of these timestamps are therefore added as an explanatory feature.

To build the models we use historical data of the insurance company. More specifically we pick T timestamps with $t = 1, \dots, T$ in the past and collect all the active contracts to these timestamps. One row corresponds to one active contract at t . So if one hypothetical contract is active in all T periods it appears as T separate rows in our data. To each row we merge the status of that contract in $t + s$, which represents the target variable. Furthermore, we join the number of requests corresponding to that contract in the period $[t - m, t]$. For the period length m we include multiple features with different m 's. The optimal length(s) for predicting C is either picked by the dimension reduction technique or the model itself.

- (Graphical Illustration)
- (Description of the ETL Process)
- (Description of the most important features)

3 Modelling Approach

3.1 Literature Review

Introduction in to the next subsections. Say sth like "there is a wide range of literature on classification techniques and specifically on customer churn prediction. Baseline: Logistic Regression. They propose following advanced techniques. In chapter 3.x we are going to focus on X, Y and Z" Also include introductory words for the next subsections.

3.2 Preprocessing

Put the ETL process here? Including multiple time stamps explanation here instead of Chapter 2?

Feature Selection

A full collection of the explanatory features in our data can be found in the appendix. As we have many features and some of them are highly correlated, preprocessing this dataset is essential. The goal is to retain only the minimal optimal subset of features. In many cases, due to multicollinearity in models with many features, dimension reduction techniques can even improve the accuracy of models.

In the current literature of machine learning there are many approaches for feature selection, ranging from manual selection to fully automated selection procedures. We use the "Maximum Relevance Minimum Redundancy" (MRMR) - approach designed by Ubers machine-learning researchers Zhao et al. [21]. The authors focus on designing an algorithm which detects the best subset of features instead of the subset of best features. The latter is often used in applications of machine learning, where a model is trained and features are selected a posteriori based on certain feature importance scores for that model. This however does not eliminate redundant features, which in reality do not improve the model performance due to being already represented in correlated other input features. Using the best subset of features also helps us to identify the optimal length of the request window m . As we want to examine the impact of quotation data for predicting customer churn, we include multiple number-of-request features with different values for m in our unfiltered selection of features F . These are obviously expected to be highly correlated, which additionally delivers a possibility to monitor the effectiveness of the MRMR.

MRMR works iteratively, so at each iteration a new best feature is identified and added to the list of selected features. Once a feature is selected it cannot ever be unselected in the next iterations. One drawback of this approach is that the number of iterations and therefore the number of selected features has to be predefined. We extend it however in a way that we iterate through the entire feature set F and cache the resulting sets and scores of each iteration. So the resulting iterative process starts with an empty selected S and full unselected U set and ends with a full S and an empty U . This lets us define the optimal number of iterations retroactively.

The algorithm MRMR got his name from the fact, that at each iteration j a new feature is selected into S that has the maximum relevance with respect to the target variable scaled by the redundancy with respect to the features that are already in S . Therefore at each iteration and for each of the remaining features of U the following score is computed:

Table 1: Relationship Metric based on Scale

	nominal	dichotomous	continuous
nominal	Cramers-V-Correlation		
dichotomous	Cramers-V-Correlation	Cramers-V-Correlation	
continuous	Eta-Correlation	Point-Biserial-Correlation	Bravais-Pearson-Correlation

$$score_i(feature_{i \in U}) = \frac{relevance(feature_{i \in U}, C)}{redundancy(feature_{i \in U}, features \in S)} \quad (1)$$

The sets U and S get updated each iteration by transferring the feature with the highest score from U to S . In their paper, Zhao et al. present multiple metrics for both relevance and redundancy. We focus on one approach which yielded the best result in their paper and slightly adapt it to our problem, as we have categorical features in our data.

At each iteration the relevance of the remaining features in U has to be computed with a new model with only these remaining features. We use gradient boosted trees and its package "lightgbm" (LGBM) in python in each iteration to score the new relevance of each remaining feature. LGBM can handle categorical features on the one hand and has a build in method for calculating feature importance on the other hand. There, feature importance is computed as the number of times that specific feature is selected for a split. So this feature importance is assigned to the corresponding features as the relevance score. How gradient boosted trees work is explained in chapter 3.4.

For redundancy an average over certain standardized metrics for the relationship between the to be evaluated feature and the features already in S needs to be computed. These metrics depend on the scales of measurement for the features. Zhao et al. only cover the case of continuous features and their relationship. We extend the redundancy score to categorical and dichotomous features. Thereby we need to pay attention to the fact, that the scores need to stay comparable for the different scales. Therefore the chosen metrics are all standardized to values between 0 and 1, where 0 indicates no and 1 the strongest possible relationship. The different scale-pairs and their relationship metrics can be summarized by table 1 (see [10]):

Redundancy is then calculated by the mean of the relationship scores as follows:

$$Redundancy(feature_{i \in U}, features \in S) = \frac{1}{n(S)} \sum_{s=1}^{n(S)} relationship(i, s) \quad (2)$$

The slightly modified MRMR-approach we use can therefore be illustrated by this simplified pseudo-code:

- The results of MRMR for our dataset are as follows: Show using graphics of average score of each iteration. Argue with an elbow criterium?

Algorithm 1 MRMR-Algorithm

```
corrmatrix  $\leftarrow$  corr(X)  
S  $\leftarrow$  []  
U  $\leftarrow$  [X.columns]  
cachedict  $\leftarrow$  {}  
for j in range len(X.columns) do  
    relvector  $\leftarrow$  LGBMscorer(U)  
    redvector  $\leftarrow$  mean(corrmatrix [U] [S])  
    scorevector  $\leftarrow$  relvector/redvector  
    bestfeat  $\leftarrow$  max(scorevector).name  
    bestscore  $\leftarrow$  max(scorevector)  
    S.append(bestfeat)  
    U.drop(bestfeat)  
    cachedict.append(j, bestfeat, bestscore)  
end for
```

3.3 Handling Class Imbalance

Studying the rarity of an event in the context of machine learning has become an important challenge in the recent two decades. Rare events, such as a customer churning in the next period, are much harder to identify and learn for most of the models. HaiYing Wang et al. [19] study the convergence rate and distributional properties of a Maximum-Likelihood estimator for the parameters of a logistic regression while predicting rare events. Their finding is that the convergence rate of the MLE is equal to the inverse of the number of examples in the minority class rather than the overall size of the training data set. So the accuracy of the estimates for the parameters is limited to the available information on the minority class, even if the size of the dataset is massive.

Therefore some methods have been developed to decrease the problematic of imbalanced classes. In this chapter we present different methods which can be applied to the training set, before feeding it to the model. Also, we present different objective loss functions which also aim in solving the problematic. To handle and evaluate the outcomes of predicting rare events also the appropriate models and model evaluation metrics must be chosen. This is discussed in the next two subsections however.

(i) Downsampling

The first basic sampling method is named downsampling. It randomly eliminates examples from the majority class in order to artificially decrease the imbalance between the two classes. The downside of this approach is that it possibly eliminates useful examples for the model to maintain a high accuracy in predicting the majority class [20]. HaiYing Wang et al. also study the convergence rate and distributional properties when applying

downsampling. According to their findings the asymptotic distribution of the resulting parameters may be identical to the MLE's using the full data set. Under this condition there is no loss in terms of efficiency (minimum possible variance of an unbiased estimator divided by its actual variance).

(ii) Upsampling

The second basic sampling method is the upsampling approach. This method simply duplicates examples from the minority class until the classes are more balanced. While duplicating examples though, the chances of overfitting to these duplicates becomes a more probable threat. Also, no new data is being generated in order to let the model learn more valuable features about the minority class [20]. Additionally, the computational performance of this approach can get rather poor, especially with large datasets and highly imbalanced classes. While evaluating the asymptotics of the MLE's with upsampling, HaiYing Wang et al find out that it also decreases the efficiency. A probable higher asymptotic variance of the estimators is the reason for that.

(iii) SMOTE

The more advanced SMOTE-approach (Synthetic Minority Oversampling Technique) [3] also creates more artificial examples of the minority class. Instead of simply duplicating some rows SMOTE creates new nearest neighbors in terms of feature values for the minority class examples. While constructing the feature values of the new example ($N + 1$) (where N is the size of the unsampled dataset) as a new nearest neighbor for example i of the minority class one has to differentiate between continuous and nominal features. The k -nearest neighbors for the minority class are typically constructed with the Euclidean Distance for continuous features and the Value Distance Metric for nominal features (TODO: maybe include other distance measures here? Mahalanobis Distance to calculate out correlation?).

A. Continuous features:

- 1) Construct difference between corresponding feature value of example i and one of its k nearest neighbors.
- 2) Multiply this difference with a random value drawn from a uniform distribution between 0 and 1.
- 3) Construct the feature value of the new example by adding the multiplied difference to the feature value of example i .

B. Nominal features:

- 1) Choose the feature value which is the majority vote between the feature value i and its k nearest neighbors.

2) Assign this value to the corresponding feature of the new example.

With this approach it is ensured that the model learns more about the neighborhood regions of the minority class. It decreases the probability, that the model overfits to the duplicates created in upsampling.

(iv) Cost-Sensitive Classifiers

One drawback of the presented sampling methods is that the sample distribution is being changed. A different starting point is to change the objective loss function which is minimized during the model fitting. Thereby the sample size and the distribution stay the same. In the modified cost function we want to penalize false-negative classifications with a higher weight. Reason behind this is to ensure that the event of interest, represented by the minority class, is predicted correctly [18].

The challenge of this approach is to find the appropriate penalty parameters. It is hard to measure the cost of misclassifying an insurance-customer regarding churn-probabilities. The fact that these costs can come from multiple sources which are not easily definable is one part of the reasoning. Therefore we focus on two types of modified loss functions. One conventional method is to assign simple parameter weights w_0 and w_1 to the loss function. By default one might use the inverse of the class frequency as the associated weights. These parameters however can also be optimized during grid search. We call this method the "Simple Weighted Loss Function". The derivation is part of the next subchapter.

The second approach is called "Focal Loss Function" and was originally designed by FAIR (Facebook Artificial Intelligence Research) for an object detection purpose [11]. As it also aims to penalize false-negative classifications it is widely used for predicting rare events. Again, the exact structure is shown in the next subchapter and the parameters can be tuned with grid search.

3.4 Machine Learning Models and Interpretability

(i) Logistic Regression

The logistic regression is used as a benchmark model for all classification problems. It has high advantages in terms of computational complexity and interpretability, but fails in capturing complex relationships and interactions. As in most cases it has the lowest accuracy of all classifiers we use it as a baseline model in order to evaluate the advantages of additional complexity in the models, as in GBT and EBM. Thereby we focus on model performance on unseen data and model interpretability.

Logistic regression applies a sigmoid function to the a linear model in order to get output values (probabilities) between 0 and 1 as in a Bernoulli distribution. We use the following

conventional notation throughout this work:

$$\widehat{C}_{t+s} = P(C_{t+s} = 1 | X_t) = f(g(X_t)) = \frac{e^{g(X_t)}}{1 + e^{g(X_t)}} \quad (3)$$

Note that from now on we use a vectorized notation. So \hat{C} represents a vector of probabilities, where the i 'th element ($i = 1, \dots, N$) corresponds to the probability of a churn in time $t + s$ of the same at t active contract. This probability vector is constructed by a model conditional on a feature matrix X at time t . Again, each row of X represents a different contract and column j is the feature j ($j = 1, \dots, M$) of that contract. Therefore $f(\cdot)$ is the sigmoid function used on function $g(\cdot)$, where in logistic regression $g(\cdot)$ is a linear model. For GBM and EBM this function is allowed to be more complex.

$$g(X_t) = \beta X_t + \epsilon_t \quad (4)$$

Maximum Likelihood is then used to estimate the vector of parameters β of the model. It maximizes the joint probability that the status of the training data contracts are drawn from the Bernoulli distribution stated in (3). For the final model in production, when estimating probabilities for a churn in the next period, t is of course equal across all contracts in X . But as already stated, for training the model we use multiple timestamps of the historized data. Therefore the index t is left out for the input matrix X and output vector C while estimating model parameters, avoiding a misleading notation. Still, the status of contract i is determined after s units of time for all contracts. The likelihood function to be maximized is described as follows:

$$\mathcal{L}(C; X, \beta) = \prod_{i=1}^N P(C^{(i)} = 1 | X^{(i)})^{I(C^{(i)}=1)} \left(1 - P(C^{(i)} = 1 | X^{(i)})\right)^{1-I(C^{(i)}=1)} \quad (5)$$

To describe this term as a loss function it is characterized by the negative logarithm of (5), which can be minimized with respect to β using Gradient Descent, Newton Raphson (Zitieren!) or other optimization methods.

$$\begin{aligned} l(C; X, \beta) &= - \sum_{i=1}^N C^{(i)} \log(P(C^{(i)} = 1 | X^{(i)})) + (1 - C^{(i)}) \log(1 - P(C^{(i)} = 1 | X^{(i)})) \\ &= - \sum_{i=1}^N C^{(i)} \log(\widehat{C}^{(i)}) + (1 - C^{(i)}) \log(1 - \widehat{C}^{(i)}) \end{aligned} \quad (6)$$

In our case we have a lot of features in the raw matrix X . Consequently it makes sense to add a penalty term to the loss function to avoid overfitting to the training data.

While minimizing this loss function during training, this additional penalty term either shrinks some parameters of β towards zero (L2 regularization), or sets some to exact 0 (L1 regularization). However, we can also reduce the dimension of features prior to fitting the model, as already explained with the MRMR-approach.

Additionally, as already mentioned in (3.3), one technique to handle imbalanced classes is to use cost-sensitive classifiers. We can implement this by setting additional penalty weights to our loss function. The resulting objective "Simple Weighted Loss Function" is described as:

1: Simple Weighted Loss Function

$$L(C, \widehat{C}) = - \sum_{i=1}^N w_1 C^{(i)} \log(\widehat{C}^{(i)}) + w_0 (1 - C^{(i)}) \log(1 - \widehat{C}^{(i)}) + \lambda h(\beta) \quad (7)$$

Here, the penalty term $h(\cdot)$ can either be an L1 or L2 regularization on β . The additional parameters of λ , w_0 and w_1 are hyperparameters which can be tuned during grid search. Following (whose?) approach, w_1 and w_0 can also be set by default to the inverse of their corresponding class frequencies in the training data.

The objective "Focal Loss Function" is set up like this:

2: Focal Loss Function

$$L(C, \widehat{C}) = - \sum_{i=1}^N \alpha (1 - \widehat{C}^{(i)})^\gamma C^{(i)} \log(\widehat{C}^{(i)}) + (1 - \alpha) \widehat{C}^{(i)^\gamma} (1 - C^{(i)}) \log(1 - \widehat{C}^{(i)}) + \lambda h(\beta) \quad (8)$$

Again, λ , α and γ are hyperparameters, which can be optimized during grid search. We use and compare both 7 and 8 for our classifiers to get the best out-of-sample performance.

After having found the optimal set of parameters it is time to define the classification cutoff τ for predicting a churn. The logistic regression model outputs a probability which is between 0 and 1. The rule of thumb is to set $\tau = 0.5$, such that probabilities larger than 0.5 are predicted as churns and the rest as non-churns.

- Interpretability of Logistic Regression runterschreiben

(ii) Tree-based Classifier

Single Classification Tree

Classification trees have a different approach on building a prediction model for $\widehat{C}_{t+s} = P(C_{t+s} = 1 \mid X_t)$. Unlike logistic regression, they allow for non-linearities and interactions.

Classification trees search for the optimal sequential binary sample splits in order to minimize an objective loss function. So at each node of the tree the optimal feature j and its optimal split point r need to be found. The search at each node can be summarized as follows:

$$\begin{aligned} S_1(j, r) &= \{X \mid X^j \geq r\}, S_2(j, r) = \{X \mid X^j < r\} \\ \{j, r\} &\in \arg \min_{j, r} \sum_{i: X^{(i)} \in S_1(j, r)} l(C^{(i)}; X^{(i)}, \widehat{p}^k) + \sum_{i: X^{(i)} \in S_2(j, r)} l(C^{(i)}; X^{(i)}, \widehat{p}^k) \end{aligned} \quad (9)$$

The loss function for region S_k is calculated using the resulting region prediction \widehat{p}^k (applied to all observations which are assigned to this region after the splits $i : X^{(i)} \in S_k$), which are simply the shares of churns in S_k . The typical loss functions are based on evaluating the purity of the resulting regions. In the ideal case, one would like to find the splits in X which always correctly assign contracts of the two classes into two different regions. In this case, \widehat{p}^k would always be either 1 or 0. In order to approach this case one either uses the Gini-index or the Cross-entropy for region S_k :

$$\text{Gini-index:} \quad 2\widehat{p}^k(1 - \widehat{p}^k)$$

$$\text{Cross-entropy:} \quad -\widehat{p}^k \log(\widehat{p}^k) - (1 - \widehat{p}^k) \log(1 - \widehat{p}^k)$$

The splits at each node are performed until certain criteria for the loss functions or other hyperparameters are met. Hyperparameters of a single tree are summarized in table 2. To get the prediction $\widehat{C}^{(i)}$, one assigns \widehat{p}^k as the region prediction of the corresponding end node of observation i to that value.

Boosted Trees for Classification

In most applications the predictions of a single classification tree have high variance due to overfitting to the training data. The accuracy in the prediction on unseen data will therefore be rather poor compared to the accuracy during training. Random forests [2] are designed to reduce the variance of the predictions, by averaging over predictions of multiple independent trees. This phenomenon is called "Wisdom of the Crowds" and is underlined by the fact that the average of multiple estimators for the same parameter will have the same bias but a smaller variance (how much depends on N and the correlation (which is 0 if we assume that the base learners are independent) of the estimators) than a single estimator.

The current literature (cite!!!) however agrees on the fact that Boosted Tree Algorithms outperform Random Forests, and therefore also a single tree. Therefore we focus on the core methodology and hyperparameters of boosted trees in the following.

The idea of boosted trees for classification is to have a sequence of dependent base learners (trees), which improve in terms of accuracy where it is most needed. Thereby, the base learners $\hat{g}_b(X)$ ($b = 1, \dots, B$) are constructed in a shallow shape, avoiding an overfitted

single learner. Additionally the $\hat{g}_b(X)$ are now regression trees, which output values in $(-\infty, \infty)$. So for the optimal split at the nodes of each tree the squared error reduction of the log-odds? (besser erklären, bzw statt classification trees einfach regression trees einführen?) are now being compared. To get an interpretable result we again have to apply the sigmoid function $f(\cdot)$ to get a probability in $[0, 1]$. The resulting loss of each tree is then fitted by the preceeding trees. So the procedure can be summarized by this pseudo code:

Algorithm 2 Boosted-Trees-Algorithm

```

 $\hat{G}(X) \leftarrow 0$ 
 $L \leftarrow \sum_{i=1}^N l(C^{(i)}, f(\hat{G}(X^{(i)})))$ 
for  $b$  in range(1, B) do
    Fit tree  $\hat{g}_b(X)$  which minimizes  $L = \sum_{i=1}^N l\left(C^{(i)}, f\left(\hat{G}(X^{(i)}) + \hat{g}_b(X^{(i)})\right)\right)$ 
     $\hat{G}(X) \leftarrow \hat{G}(X) + \lambda \hat{g}_b(X)$ 
end for
 $\hat{C} = \hat{f}(X) = f(\sum_{b=1}^B \lambda \hat{g}_b(X))$ 

```

- Gradient boosted bagged trees noch?

The hyperparameter λ is called learning rate and set to a small number to learn slowly and to avoid overfitting. It should not be confused with the λ of regularization (change notation in regularization?). Also notice, that the loss function defined here is the objective loss function used for gradient boosting and is defined differently than the loss function, when constructing a single tree. We use the same two objective loss functions for Gradient Boosting derived in (7) and (8) and perform hyperparameter optimization to get the best set of hyperparameters belonging to these loss functions. As already stated, this allows us to handle the class imbalance. We leave out the regularization term $h(\cdot)$ in GBT.

To apply the log-loss function in (7) or (8) we need to derive the gradient as well as the hessian of this function. Herewith the lightgbm-package [5] aims to improve time-cost as is it takes the second order Taylor Expansion to compute the optimal loss minimizing $\hat{f}_b(X)$ in each iteration $b = 1, \dots, B$. These are calculated in the appendix.

The main cost with boosted trees is learning the single trees, and the most time-consuming part in that is to find the best split-points. Therefore we make use of the histogram-based approach of the lightgbm-package in our prediction model which aims to tackle this issue. The so called histogram-based approach is designed to bin the features which creates high efficiency gains during searching for the optimal splits, especially for continuous variables. Another important aspect to note about lightgbm's implementation of boosted trees is the fact that the base trees grow leaf-wise instead of depth-wise. As proposed by Friedman et al., the idea is to extend nodes in first-best order. Thereby, the best node is the one which maximally reduces the sum of the tree loss function in the resulting regions. This

Table 2: Hyperparameters for lgbm

	Hyperparameter	Description	Grid Search Values
Boosting	learning rate	Boosting learning rate λ	Shrinking learning rate
	n_estimators	Number of boosted Trees B	
	objective	Objective or objective loss function	Custom loss function
	subsample	Subsample ratio of training data used	
	subsample_freq	Frequency of usage of subsample	
	reg_alpha	L1 regularization term on weights	
	reg_lambda	L2 regularization term on weights	
Single Tree	num_leaves	Maximum number of tree leaves	
	subsample_for_bin	Number of samples for constructing bin	
	min_split_gain	Minimum loss reduction for split	
	min_child_samples	Minimum number of data in new region	
	colsample_bytree	Subsample ratio of columns for tree	

enables the possibility that a first-best split is found at a node in level $r + 1$ eventhough in level r only one of two nodes are split. (Show graphically?)

If we let the trees grow without tree structure restrictions to full trees, both the leaf-wise and depth-wise approach result in the same trees. As all gradient boosters rely on shallow trees, the combination of hyperparameters such as the maximum number of leaves, the minimum loss reduction required for a further split the first-best split approach result in a better (cite!) shallow tree structure.

– Explain regalpha and reglambda in boosted trees

There are a lot of hyperparameters which allow to tune the learning structure. They can be split into the hyperparameters for single tree structure and hyperparameters for the learning process. In Table 2 is an overview of the hyperparameters we focus on and the corresponding values we use for grid search.

(iii) Explainable Boosting Classifiers

Explainable boosting machines (EBM) were developed by researchers at Microsoft [15] and aim to have high accuracy as most complex models, while maintaining an easy interpretable approach. It is maintained by the functional form which is similar to the standard GAM-Model, developed originally in 1987 by Hastie et al. [8]:

$$g(X_t) = \beta_0 + \sum_{j=1}^M k_j(X_t^j) + \epsilon_t \quad (10)$$

Thereby M is the number of features and $k_j(\cdot)$ is the so called shape function for feature j . In standard GAM-models $k_j(\cdot)$ is approximated by scatterplot smoothers (Wenn noch Zeit und Platz ist, Running mean oder running lines smoother erklären, aber eigentlich für diese Arbeit unwichtig.). In EBM the approximation for $k_j(\cdot)$ is allowed to be calculated by a complex modern learner such as a decision tree or a random forest.

As the name of the method already reveals, gradient boosting is applied to improve the preceeding trees in direction of the gradient of the loss function. The main difference to the standard gradient boosting classifier is that no longer one tree fits all features $\hat{g}_b(X) = \hat{g}_b(X^1, \dots, X^M)$ in each iteration $b = 1, \dots, B$. Instead in each iteration, the algorithm cycles through all features to improve the single shape function $k_j(\cdot)$, where it is most needed. By cycling through the features one at a time and maintaining a low learning rate the feature order does not matter and the potential problem of multicollinearity is reduced.

Unfortunetaly there is still a huge gap between standard GAM-models and full complexity models in terms of predictive accuracy, even if we allow for non-linearities in $k_j(\cdot)$. Full complexity models, such as gradient boosted trees and deep neural nets, have the advantage of allowing for an arbitrary number of interactions between features. To allow for pairwise interactions, EBM's make use of the idea of GA²M-models developed by Lou et al. [13]. The resulting shape functions $k_{m,n}(X^m, X^n)$, (where $m \neq n$ and $m, n \in \{1, \dots, M\}$) are still interpretable with a heatmap on the two dimensional X^m, X^n -plane. Also, results from Lou et al. not only show that GA2M-models have a high improvement in accuracy over GAM-models, but also compete with high complexity-models in most applications. There are a number of approaches to detect the best set of feature interactions for our model as in [9], [6], [12], [17]. These methods however are either computationally inefficient or almost even infeasible with high-dimensional data. Therefore we use the "FAST" approach presented by Lou et al. [13], which are also available in the EBM-package.

FAST's structure is based on a greedy forward stagewise selection strategy. It can be compared to the MRMR in a way that it starts with an empty set of selected pairs and an unselected set containing all possible feature pairs. In each iteration all possible unselected pairs are used separately to fit the current objective loss function resulting from the additive model including only the already selected pairs. The pair with the highest loss improvement is selected in that iteration. The iteration stops, when the objective loss function stops improving for any other inclusion of a pair.

If we assume that we have M features in our data the amount of possible pairwise interactions equals $\binom{M}{2} = \frac{M(M-1)}{2}$. As a result, calculating the set of interaction functions and fitting all possible new models in each iteration is very time consuming for large M . FAST therefore builds the interaction functions more efficiently by defining optimized quadrants in the space of the two features and taking the mean values of each quadrant.

Table 3: Confusion Matrix

	$\hat{C} = 0$	$\hat{C} = 1$
$C = 0$	# True Negatives (TN)	# False Positives (FP)
$C = 1$	# False Negatives (FN)	# True Positives (TP)

Please refer to [13] for more insights on this procedure.

- Our modelling approach with EBM will be as follows: 1. FAST to collect the right number of interactions 2. MRMR to select the right features 3. Gradient Boosting the resulting GA2M

Parameter and hyperparameter search for the models

We will split our dataset (stratified split) into a training (99%), validation (1%) and test set (1%). All parameters of the models will be constructed using a 3-fold cross-validation on the training set to ensure generalizable training scores and the selection of the best generalizable model. Additionally, the best hyperparameters of each model captured with a randomized implementation of grid-search. The validation set is used for both GBT and EBM to have an early-stopping-criterion evaluated on an out-of-sample data during training.

- Results of grid-search hier?

3.5 Model Evaluation Metrics

To get an unbiased estimate of the generalized performance of our model, it has to be tested on unseen data, which was not part of the training process. In order to espacially ensure time generalizability of our models, we use unseen data (test set) of an additional different timestamp to generate evaluations.

For the evaluation of classification models there is a huge variety of metrics. As already stated, selecting the correct metric is crucial. Let us first define the possible outcomes of our model with the confusion matrix:

Using accuracy $(TN + TP / N)$ will lead to unreliable estimates of the performance with rare events. The accuracy will be high indicating a good fit, even if the churners are not frequently detected. Therefore it makes sense to either use the precision $(TP / TP + FP)$ or the recall $(TP / TP + FN)$ metrics. A combination of both measures is provided by the F1-score which is the harmonic mean of both metrics and therefore still defined between 0 and 1 [20]:

$$F1 = \frac{2 * precision * recall}{precision + recall} \quad (11)$$

Another widely used metric is the area under the receiver-operating-characteristic-curve (AUROC). The ROC-curve represents the tradeoff between the false-positive-rate ($FPR = FP/FP + TN$) on the X-axis and recall on the y-axis of a classifier using different cutoff values τ .

The ROC always starts at the lower left-hand corner ($FPR = 0$, $Recall = 0$) for $\tau = 1$, and ends at the upper right-hand corner ($FPR = 1$, $Recall = 1$) for $\tau = 0$. The other values of the curve are defined by alternating τ in values between 0 and 1. An area under the curve of 1 is the best score and 0.5 is the worst, representing the classifier-results of a simple coin-flipping algorithm.

This measure also has its downsides with very small positive classes, as the FPR is highly dependend on the number of negatives. The FPR will only improve by a small amount if a there is a substantial decrease in FP's as the number of TN's will be very high for most τ 's.

For a small number of positive examples it makes more sense to look at the area under the precision-recall-curve (AUPRC) [1]. There the curve also plots values for the recall on the X-axis and precision on the y-axis for different τ 's. It now starts at the upper left corner ($Recall = 0$, $Precision = 1$) for $\tau = 1$ (als * hinzufügen, dass für TP und FP gegen 0, Precision gegen 1) and ends in the lower right corner ($Recall = 1$, $Precision = 0$) for $\tau = 0$ (als * hinzufügen, dass precision gegen 0 geht, da wir sehr viele FP's haben. Die Kurve wird niemals genau unten rechts enden.).

It is plotted as follows as an example:

Now when it comes to interpreting the metric, it is not as easy as the AUROC. The baseline now is not a simple coin-flip, but instead defined by the ratio of churners ($\#C/N$) in the data. Every AUPRC score above that baseline is an improvement from predicting customers as Churners randomly using a Bernoulli-distribution for each ($C^{(i)} \sim B(\frac{\#P}{N})$).

For calculating the AUROC or the AUPRC there are multiple methods. All of them rely on estimates, as the true function of the curve can only be approximated using a finite number of cutoff values τ . (Mehr darauf eingehen).

3.6 Interpreting the Models

One of the main tasks of this work is to interpret the structure of our models. More precisely, we want to know how each feature interacts with the probability of a churn. Espacially the usage of quotation data turns out to have high predicitive power, but we want to check if the assumed interaction is true and how the shape of the interaction in our models really looks like. This question is also answered for other features which turn

out to have high predictive importance in our model.

In prediction models in general, one has to make a decision between two questions the modelling approach needs to answer. The first question is what is predicted and the second is why is it predicted. In application where missclassifications have low consequences or/and the why question does not deliver any benefit the interpretability may be neglected. Therefore e.g. in movie recommender systems (low missclassification costs) or in object detection applications (why is not important) very complex models are used to ensure that the What question is answered correctly.

For many applications however answering the what question correctly is not enough. Especially econometricians accept a drop in predictive accuracy for a better answer to the why question. That is why in econometric applications the modelling approach relies on simple models such as linear or logistic regression. Thereby, the focus is on testing necessary assumptions and the significance of parameters which make the interpretability of such model reliable.

The modelling approach of this work tries to answer both questions as much as possible. Therefore we do not rely on complex black-box models which only aim to have high predictive accuracy but at the same time are not solely interested on statistical significance of parameters for reliable inference. Therefore we use modern techniques which maximize the utility of jointly answering both questions. As our two models GBT and EBM have different approaches in terms of interpretability we split the interpretation of the models in two parts. Thereby we compare and check if the findings are in line with each other.

Explaining Gradient Boosted Trees

For a complex model such as gradient boosted trees the model structure struggles to explain itself. Therefore the current literature relies on simple explanation models, which are defined as interpretable approximations of the original model. We shortly summarize and apply two mostly used methods SHAP (Shapley Additive explanation cite) and LIME (cite).

SHAP

LIME

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