

**Misol.** Chiziqli tenglamalar sistemasini Kramer formulalari yordamida yeching:

$$\begin{cases} 3x_1 - 2x_2 + 4x_3 = 21 \\ 3x_1 + 4x_2 - 2x_3 = 9 \\ 2x_1 - x_2 - x_3 = 10 \end{cases}$$

**Yechim:** Sistemani Kramer formulalari yordamida yechamiz.

$$D = \begin{vmatrix} 3 & -2 & 4 \\ 3 & 4 & -2 \\ 2 & -1 & -1 \end{vmatrix} = 3 \cdot \begin{vmatrix} 4 & -2 \\ -1 & -1 \end{vmatrix} + 2 \cdot \begin{vmatrix} 3 & -2 \\ 2 & -1 \end{vmatrix} + 4 \cdot \begin{vmatrix} 3 & 4 \\ 2 & -1 \end{vmatrix} =$$

$$= 3 \cdot (-4 - 2) + 2 \cdot (-3 + 4) + 4 \cdot (-3 - 8) = -18 + 2 - 44 = -60 \neq 0, \text{ demak, tizim yagona yechimga ega.}$$

$$D_1 = \begin{vmatrix} 21 & -2 & 4 \\ 9 & 4 & -2 \\ 10 & -1 & -1 \end{vmatrix} = 21 \cdot \begin{vmatrix} 4 & -2 \\ -1 & -1 \end{vmatrix} + 2 \cdot \begin{vmatrix} 9 & -2 \\ 10 & -1 \end{vmatrix} + 4 \cdot \begin{vmatrix} 9 & 4 \\ 10 & -1 \end{vmatrix} =$$

$$= 21 \cdot (-4 - 2) + 2 \cdot (-9 + 20) + 4 \cdot (-9 - 40) = -126 + 22 - 196 = -300$$

$$x_1 = \frac{D_1}{D} = \frac{-300}{-60} = 5$$

$$D_2 = \begin{vmatrix} 3 & 21 & 4 \\ 3 & 9 & -2 \\ 2 & 10 & -1 \end{vmatrix} = 3 \cdot \begin{vmatrix} 9 & -2 \\ 10 & -1 \end{vmatrix} - 21 \cdot \begin{vmatrix} 3 & -2 \\ 2 & -1 \end{vmatrix} + 4 \cdot \begin{vmatrix} 3 & 9 \\ 2 & 10 \end{vmatrix} =$$

$$= 3 \cdot (-9 + 20) - 21 \cdot (-3 + 4) + 4 \cdot (30 - 18) = 33 - 21 + 48 = 60$$

$$x_2 = \frac{D_2}{D} = \frac{60}{-60} = -1$$

$$D_3 = \begin{vmatrix} 3 & -2 & 21 \\ 3 & 4 & 9 \\ 2 & -1 & 10 \end{vmatrix} = 3 \cdot \begin{vmatrix} 4 & 9 \\ -1 & 10 \end{vmatrix} - 3 \cdot \begin{vmatrix} -2 & 21 \\ -1 & 10 \end{vmatrix} + 2 \cdot \begin{vmatrix} -2 & 21 \\ 4 & 9 \end{vmatrix} =$$

$$= 3 \cdot (40 + 9) - 3 \cdot (-20 + 21) + 2 \cdot (-18 - 84) = 147 - 3 - 284 = -60$$

$$x_3 = \frac{D_3}{D} = \frac{-60}{-60} = 1$$

**Javob:**  $x_1 = 5, x_2 = -1, x_3 = 1$ .

**Misollar.** Chiziqli tenglamalar sistemasini Kramer formulalari yordamida yeching.

1. 
$$\begin{cases} 2x - y + z = 4 \\ x + 3y - z = 7 \\ 3x - y + 4z = 12 \end{cases}$$
2. 
$$\begin{cases} 2x + 3y - 4z = 3 \\ 3x - 4y + 2z = -5 \\ 2x + 7y - 5z = 13 \end{cases}$$
3. 
$$\begin{cases} 2x - 7y + 5z = 9 \\ x + 5y - 5z = -2 \\ 4x - 2y + 7z = 24 \end{cases}$$
4. 
$$\begin{cases} 2x + 3y - z = 0 \\ x - 2y + 4z = 9 \\ y + z = 2 \end{cases}$$
5. 
$$\begin{cases} x + 3y + 4z = 17 \\ 2x - 3y + 5z = 16 \\ 3x + 4y - z = 7 \end{cases}$$
6. 
$$\begin{cases} 2x + 2y - 4z = 6 \\ x + 3y - 5z = 6 \\ 3x - 2y + 6z = 6 \end{cases}$$
7. 
$$\begin{cases} 3x + 4y + 5z = 22 \\ x - 3y - 6z = -9 \\ 2x + 4y - 4z = 10 \end{cases}$$
8. 
$$\begin{cases} 2x_1 - x_2 + 2x_3 = 3 \\ x_1 + x_2 + 2x_3 = -4 \\ 4x_1 + x_2 + 4x_3 = -3 \end{cases}$$
9. 
$$\begin{cases} 2x - y - z = 14 \\ 3x + 4y - 2z = 11 \\ 3x - 2y + 4z = 11 \end{cases}$$
10. 
$$\begin{cases} 3x - y + z = 12 \\ x + 2y + 4z = 6 \\ 5x + y + 2z = 3 \end{cases}$$
11. 
$$\begin{cases} 2x - y + 3z = -4 \\ x + 3y - z = 11 \\ x - 2y + 2z = -7 \end{cases}$$
12. 
$$\begin{cases} 2x + y + 3z = 7 \\ 2x + 3y + z = 1 \\ 3x + 2y + z = 6 \end{cases}$$

$$13. \begin{cases} 3x - 2y + 4z = 12 \\ 3x + 4y - 2z = 6 \\ 2x - y - z = -9 \end{cases}$$

$$14. \begin{cases} 2x - y + 2z = 3 \\ x + y + 2z = -4 \\ 4x + y + 4z = -3 \end{cases}$$

$$\begin{cases} 3x + 2y + 4z = 31 \\ 5x + y + 2z = 29 \\ 3x - y - z = 10 \end{cases}$$